## 1. COMPUTING BINOMIAL COEFFICIENT

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def binomial_coefficient(n, k):
  if k > n:
     return 0
  if k == 0 or k == n:
     return 1
  C = [[0 \text{ for } x \text{ in range}(k + 1)] \text{ for } x \text{ in range}(n + 1)]
  for i in range(n + 1):
     for j in range(min(i, k) + 1):
       if j == 0 or j == i:
          C[i][j] = 1
       else:
          C[i][j] = C[i-1][j-1] + C[i-1][j]
  return C[n][k]
n = 5
k = 2
print(f"Binomial Coefficient C({n},{k}) is {binomial_coefficient(n, k)}")
2. BELLMAN FORD
class Graph:
  def __init__(self, vertices):
     self.V = vertices
     self.graph = []
  def add_edge(self, u, v, w):
     self.graph.append([u, v, w])
  def bellman_ford(self, src):
     dist = [float("Inf")] * self.V
     dist[src] = 0
```

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for _ in range(self.V - 1):
       for u, v, w in self.graph:
         if dist[u] != float("Inf") and dist[u] + w < dist[v]:
           dist[v] = dist[u] + w
    for u, v, w in self.graph:
       if dist[u] != float("Inf") and dist[u] + w < dist[v]:
         print("Graph contains negative weight cycle")
         return
    self.print_solution(dist)
  def print_solution(self, dist):
    print("Vertex Distance from Source")
    for i in range(self.V):
       print(f"{i}\t\t{dist[i]}")
g = Graph(5)
g.add_edge(0, 1, -1)
g.add_edge(0, 2, 4)
g.add_edge(1, 2, 3)
g.add_edge(1, 3, 2)
g.add_edge(1, 4, 2)
g.add_edge(3, 2, 5)
g.add_edge(3, 1, 1)
g.add_edge(4, 3, -3)
g.bellman_ford(0)
3. WARSHAL FLOYD
def floyd_warshall(graph):
  dist = list(map(lambda i: list(map(lambda j: j, i)), graph))
```

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V = len(graph)
  for k in range(V):
    for i in range(V):
       for j in range(V):
         dist[i][j] = min(dist[i][j], dist[i][k] + dist[k][j])
  return dist
graph = [
  [0, 5, float("Inf"), 10],
  [float("Inf"), 0, 3, float("Inf")],
  [float("Inf"), float("Inf"), 0, 1],
  [float("Inf"), float("Inf"), float("Inf"), 0]
]
distance_matrix = floyd_warshall(graph)
print("Shortest distances between every pair of vertices:")
for row in distance_matrix:
  print(row)
4. MEET IN THE MIDDLE TECHNIQUE
def meet_in_the_middle(arr, S):
  n = len(arr)
  left = arr[:n//2]
  right = arr[n//2:]
  def subset_sums(arr):
    sums = []
    n = len(arr)
    for i in range(1 << n):
       sum = 0
       for j in range(n):
         if i & (1 << j):
```

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sum += arr[j]
      sums.append(sum)
    return sums
  left_sums = subset_sums(left)
  right_sums = subset_sums(right)
  right_sums.sort()
  for sum in left_sums:
    if binary_search(right_sums, S - sum):
      return True
  return False
def binary_search(arr, x):
  lo, hi = 0, len(arr) - 1
  while lo <= hi:
    mid = (lo + hi) // 2
    if arr[mid] == x:
      return True
    elif arr[mid] < x:
      lo = mid + 1
    else:
      hi = mid - 1
  return False
# Example usage
arr = [3, 34, 4, 12, 5, 2]
S = 9
if meet_in_the_middle(arr, S):
  print("Found a subset with the given sum")
else:
```

print("No subset with the given sum")