

1. DICE THROW PROBLEM

```
def dice_throw(n, m, X):  
    dp = [[0 for x in range(X + 1)] for y in range(n + 1)]  
    dp[0][0] = 1  
  
    for i in range(1, n + 1):  
        for j in range(1, X + 1):  
            dp[i][j] = 0  
            for k in range(1, m + 1):  
                if j - k >= 0:  
                    dp[i][j] += dp[i - 1][j - k]  
  
    return dp[n][X]  
  
n = 3 # number of dice  
m = 6 # number of faces  
X = 8 # desired sum  
print(f"Number of ways to get sum {X} with {n} dice: {dice_throw(n, m, X)}")
```

2. SUBSET SUM PROBLEM

```
def subset_sum(arr, S):  
    n = len(arr)  
    dp = [[False for x in range(S + 1)] for y in range(n + 1)]  
    for i in range(n + 1):  
        dp[i][0] = True  
  
    for i in range(1, n + 1):  
        for j in range(1, S + 1):  
            if j < arr[i - 1]:  
                dp[i][j] = dp[i - 1][j]  
            else:  
                dp[i][j] = dp[i - 1][j] or dp[i - 1][j - arr[i - 1]]
```

```
    return dp[n][S]
```

```
arr = [3, 34, 4, 12, 5, 2]
```

```
S = 9
```

```
if subset_sum(arr, S):
```

```
    print("Found a subset with the given sum")
```

```
else:
```

```
    print("No subset with the given sum")
```

3. ASSEMBLY LINE SCHEDULING

```
def assembly_line(a, t, e, x, n):
```

```
    T1 = [0] * n
```

```
    T2 = [0] * n
```

```
    T1[0] = e[0] + a[0][0]
```

```
    T2[0] = e[1] + a[1][0]
```

```
    for i in range(1, n):
```

```
        T1[i] = min(T1[i - 1] + a[0][i], T2[i - 1] + t[1][i] + a[0][i])
```

```
        T2[i] = min(T2[i - 1] + a[1][i], T1[i - 1] + t[0][i] + a[1][i])
```

```
    return min(T1[n - 1] + x[0], T2[n - 1] + x[1])
```

```
a = [[4, 5, 3, 2], [2, 10, 1, 4]] # assembly times
```

```
t = [[0, 7, 4, 5], [0, 9, 2, 8]] # transfer times
```

```
e = [10, 12] # entry times
```

```
x = [18, 7] # exit times
```

```
n = 4 # number of stations
```

```
print(f"Minimum time to assemble the product is: {assembly_line(a, t, e, x, n)}")
```

4. LONGEST PALINDROMIC SUBSEQUENCE

```
def longest_palindromic_subsequence(seq):
```

```
    n = len(seq)
```

```
dp = [[0 for x in range(n)] for y in range(n)]
```

```
for i in range(n):
```

```
    dp[i][i] = 1
```

```
for cl in range(2, n + 1):
```

```
    for i in range(n - cl + 1):
```

```
        j = i + cl - 1
```

```
        if seq[i] == seq[j] and cl == 2:
```

```
            dp[i][j] = 2
```

```
        elif seq[i] == seq[j]:
```

```
            dp[i][j] = dp[i + 1][j - 1] + 2
```

```
        else:
```

```
            dp[i][j] = max(dp[i][j - 1], dp[i + 1][j])
```

```
return dp[0][n - 1]
```

```
seq = "BBABCBCAB"
```

```
print(f"Length of the longest palindromic subsequence is: {longest_palindromic_subsequence(seq)}")
```