## Multiple Testing Project

## 2.2 P-value

## 1. Distribution of the p-value under the null

1.1 Show that for any  $\alpha$ ,  $c_{\alpha} = F_H^{-1}(1-\alpha)$ 

We know that  $\alpha = 1 - F_H(c_\alpha)$  from the definition of  $c_\alpha$ .

$$\alpha = 1 - F_H(c_\alpha)$$

$$\alpha - 1 = -F_H(c_\alpha)$$

$$-(\alpha - 1) = F_H(c_\alpha)$$

$$1 - \alpha = F_H(c_\alpha)$$

$$F_H^{-1}(1-\alpha) = c_\alpha$$

$$c_{\alpha} = F_H^{-1}(1 - \alpha)$$

Q.E.D.