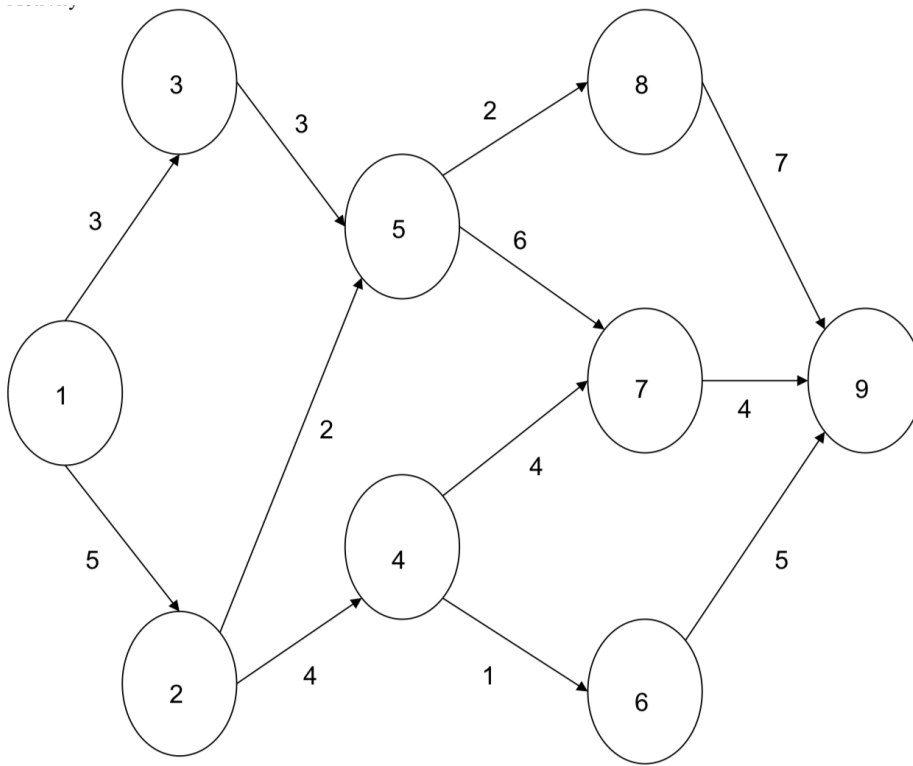


Assignment-5

Solution-1:

Given data



Decision Variables:

x₁₂ – activity from 1 to 2

x₁₃ – activity from 1 to 3

x₃₅ – activity from 3 to 5

x₂₄ – activity from 2 to 4

x₂₅ – activity from 2 to 5

x₄₆ - activity from 4 to 6

x₄₇ - activity from 4 to 7

x₅₇ – activity from 5 to 7

x₅₈ – activity from 5 to 8

x₆₉ - activity from 6 to 9

x₇₉ – activity from 7 to 9

x89 – activity from 8 to 9

Objective Function:

Maximum $z = 5x_{12} + 3x_{13} + 3x_{35} + 2x_{25} + 4x_{24} + 2x_{58} + 6x_{57} + 4x_{47} + x_{46} + 7x_{89} + 4x_{79} + 5x_{69}$.

Constraints:

Starting node

$$x_{13} + x_{12} = 1$$

Intermediate nodes

$$x_{12} - x_{25} - x_{24} = 0$$

$$x_{13} - x_{35} = 0$$

$$x_{24} - x_{47} - x_{46} = 0$$

$$x_{25} + x_{35} - x_{58} - x_{57} = 0$$

$$x_{46} - x_{69} = 0$$

$$x_{47} + x_{57} - x_{79} = 0$$

$$x_{58} - x_{89} = 0$$

Finish node

$$x_{89} + x_{79} + x_{69} = 1.$$

All decision variables are non-negativity (≥ 0).

Solution-2a:

a. Given data

	Stock							
	S1	S2	S3	H1	H2	H3	C1	C2
Price per share	\$40	\$50	\$80	\$60	\$45	\$60	\$30	\$25
Growth rate	0.05	0.10	0.03	0.04	0.07	0.15	0.22	0.25
Dividend	\$2.00	\$1.50	\$3.50	\$3.00	\$2.00	\$1.00	\$1.80	\$0.00

Fund to invest is 2.5million.

The client has stipulated that no more than 40 percent of the investment be allocated to any one of these three sectors.

To assure diversification, at least \$100,000 must be invested in each of the eight stocks.

Number of shares invested in any stock must be a multiple of 1000.

Pre-calculation:

Return = price * growth rate + dividend

$$S1=4$$

$$S2 = 6.5$$

$$S3 = 5.9$$

$$H1 = 5.4$$

$$H2 = 5.1$$

$$H3 = 10$$

$$C1 = 8.4$$

$$C2 = 6.25.$$

Decision Variables:

X_i = returns from firms

$i= 1,2,3,4,5,6,7,8=S1, S2, S3, H1, H2, H3, C1, C2$ respectively.

Objective Function:

Maximum: $4x_1 + 6.5x_2 + 5.9x_3 + 5.4x_4 + 5.15x_5 + 10x_6 + 8.4x_7 + 6.25x_8$

Constraints:

Investment 2.5 million

$$40x_1 + 50x_2 + 80x_3 + 60x_4 + 45x_5 + 60x_6 + 30x_7 + 25x_8 \leq 2500000;$$

Investment not more than 40%

$$40x_1 + 50x_2 + 80x_3 \leq 1000000;$$

$$60x_4 + 45x_5 + 60x_6 \leq 1000000;$$

$$30x_7 + 25x_8 \leq 1000000;$$

Invest at least

$$40x_1 \geq 100000$$

$$50x_2 \geq 100000$$

$$80x_3 \geq 100000$$

$$60x_4 \geq 100000$$

$$45x_5 \geq 100000$$

$$60x_6 \geq 100000$$

$$30x_7 \geq 100000$$

$$25x_8 \geq 100000$$

Solution2b:**Decision Variables:**

X_i = returns from firms

$i = 1, 2, 3, 4, 5, 6, 7, 8 = S1, S2, S3, H1, H2, H3, C1, C2$ respectively.

Objective Function:

Maximum $4x_1 + 6.5x_2 + 5.9x_3 + 5.4x_4 + 5.15x_5 + 10x_6 + 8.4x_7 + 6.25x_8$

Constraints:

Investment 2.5 million

$40x_1 + 50x_2 + 80x_3 + 60x_4 + 45x_5 + 60x_6 + 30x_7 + 25x_8 \leq 2500000$;

Investment not more than 40%

$40x_1 + 50x_2 + 80x_3 \leq 1000000$;

$60x_4 + 45x_5 + 60x_6 \leq 1000000$;

$30x_7 + 25x_8 \leq 1000000$;

Invest at least

$40x_1 \geq 100000$

$50x_2 \geq 100000$

$80x_3 \geq 100000$

$60x_4 \geq 100000$

$45x_5 \geq 100000$

$60x_6 \geq 100000$

$30x_7 \geq 100000$

$25x_8 \geq 100000$

$X_i = 1, 2, 3, 4, 5, 6, 7, 8 \geq 0$.

Percentage difference = $(\text{objective function}(b) - \text{objective function}(a)) / \text{objective function}(a) = 0.15\%$