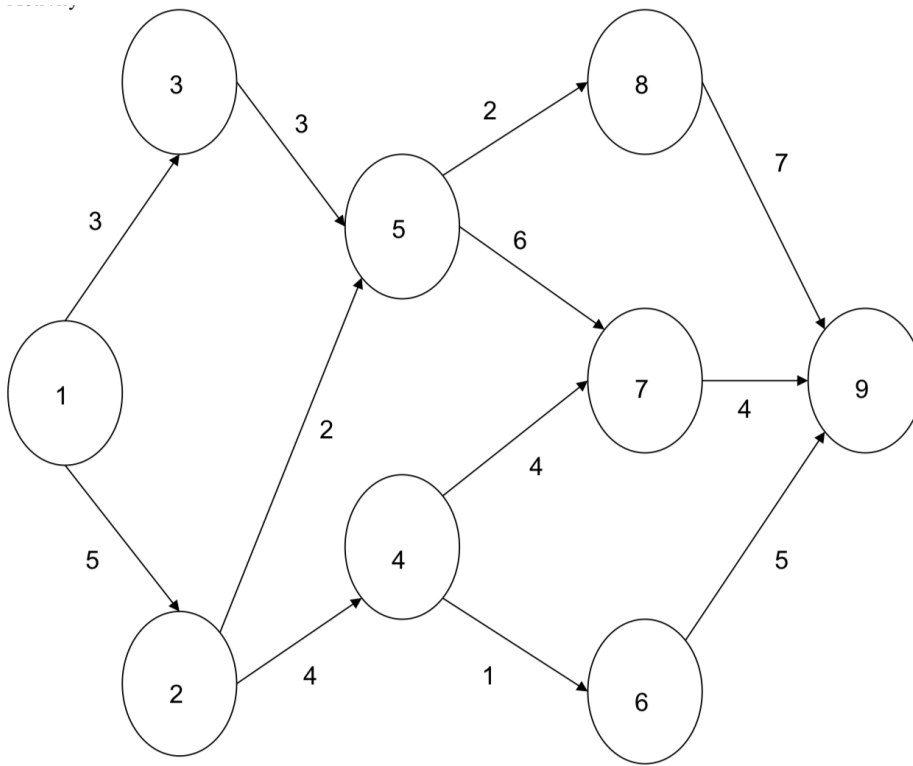


Assignment-5

Solution-1:

Given data



Decision Variables:

x₁₂ – activity from 1 to 2

x₁₃ – activity from 1 to 3

x₃₅ – activity from 3 to 5

x₂₄ – activity from 2 to 4

x₂₅ – activity from 2 to 5

x₄₆ – activity from 4 to 6

x₄₇ – activity from 4 to 7

x₅₇ – activity from 5 to 7

x₅₈ – activity from 5 to 8

x₆₉ – activity from 6 to 9

x₇₉ – activity from 7 to 9

x89 – activity from 8 to 9

Objective Function:

Maximum $z = 5x_{12} + 3x_{13} + 3x_{35} + 2x_{25} + 4x_{24} + 2x_{58} + 6x_{57} + 4x_{47} + x_{46} + 7x_{89} + 4x_{79} + 5x_{69}$.

Constraints:

Starting node

$$x_{13} + x_{12} = 1$$

Intermediate nodes

$$x_{12} - x_{25} - x_{24} = 0$$

$$x_{13} - x_{35} = 0$$

$$x_{24} - x_{47} - x_{46} = 0$$

$$x_{25} + x_{35} - x_{58} - x_{57} = 0$$

$$x_{46} - x_{69} = 0$$

$$x_{47} + x_{57} - x_{79} = 0$$

$$x_{58} - x_{89} = 0$$

Finish node

$$x_{89} + x_{79} + x_{69} = 1.$$

All decision variables are non-negativity (≥ 0).

Solution-2a:

a. Given data

| | Stock | | | | | | | |
|-----------------|--------|--------|--------|--------|--------|--------|--------|--------|
| | S1 | S2 | S3 | H1 | H2 | H3 | C1 | C2 |
| Price per share | \$40 | \$50 | \$80 | \$60 | \$45 | \$60 | \$30 | \$25 |
| Growth rate | 0.05 | 0.10 | 0.03 | 0.04 | 0.07 | 0.15 | 0.22 | 0.25 |
| Dividend | \$2.00 | \$1.50 | \$3.50 | \$3.00 | \$2.00 | \$1.00 | \$1.80 | \$0.00 |

Fund to invest is 2.5million.

The client has stipulated that no more than 40 percent of the investment be allocated to any one of these three sectors.

To assure diversification, at least \$100,000 must be invested in each of the eight stocks.

Number of shares invested in any stock must be a multiple of 1000.

Pre-calculation:

$$R = (D/P) + g$$

where

D=Dividend

P=Price

G=growth rate

R=Return

Accountingscholar.com online resource.

So, for S1 firm

$$S1 = 2/40 + 0.05 = 0.1$$

$$S2 = 0.130$$

$$S3 = 0.073$$

$$H1 = 0.09$$

$$H2 = 0.1145$$

$$H3 = 0.167$$

$$C1 = 0.280$$

$$C2 = 0.25.$$

Decision Variables:

X_i = returns from firms

$i = 1, 2, 3, 4, 5, 6, 7, 8 = S1, S2, S3, H1, H2, H3, C1, C2$ respectively.

Y_i = binary variables

1 = to buy stock

0 = not to buy stock.

Objective Function:

Maximum: $0.1 x_1 y_1 + 0.130 x_2 y_2 + 0.073 x_3 y_3 + 0.09 x_4 y_4 + 0.1145 x_5 y_5 + 0.167 x_6 y_6 + 0.280 x_7 y_7 + 0.25 x_8 y_8$.

Constraints:

Investment 2.5 million

$$40x_1y_1 + 50x_2y_2 + 80x_3y_3 + 60x_4y_4 + 45x_5y_5 + 60x_6y_6 + 30x_7y_7 + 25x_8y_8 \leq 2500000;$$

Investment not more than 40%

$$40x_1y_1 + 50x_2y_2 + 80x_3y_3 \leq 1000000;$$

$$60x_4y_4 + 45x_5y_5 + 60x_6y_6 \leq 1000000;$$

$$30x_7y_7 + 25x_8y_8 \leq 1000000;$$

Invest at least

$$40x_1y_1 \geq 100000$$

$$50x_2y_2 \geq 100000$$

$$80x_3y_3 \geq 100000$$

$$60x_4y_4 \geq 100000$$

$$45x_5y_5 \geq 100000$$

$$60x_6y_6 \geq 100000$$

$$30x_7y_7 \geq 100000$$

$$25x_8y_8 \geq 100000$$

Y_i = binary integers.

$i=1,2,3,4,5,6,7,8$.

Solution2b:

Decision Variables:

X_i = returns from firms

$i=1,2,3,4,5,6,7,8=S1, S2, S3, H1, H2, H3, C1, C2$ respectively.

Objective Function:

Maximum: $0.1 x_1 + 0.130 x_2 + 0.073 x_3 + 0.09 x_4 + 0.1145 x_5 + 0.167 x_6 + 0.280 x_7 + 0.25 x_8$.

Constraints:

Investment 2.5 million

$$40x_1 + 50x_2 + 80x_3 + 60x_4 + 45x_5 + 60x_6 + 30x_7 + 25x_8 \leq 2500000;$$

Investment not more than 40%

$$40x_1 + 50x_2 + 80x_3 \leq 1000000;$$

$$60x_4 + 45x_5 + 60x_6 \leq 1000000;$$

$$30x_7 + 25x_8 \leq 1000000;$$

Invest at least

$$40x_1 \geq 100000$$

$$50x_2 \geq 100000$$

$$80x_3 \geq 100000$$

$$60x_4 \geq 100000$$

$$45x_5 \geq 100000$$

$$60x_6 \geq 100000$$

$$30x_7 \geq 100000$$

$$25x_8 \geq 100000$$

$$x_i = 1, 2, 3, 4, 5, 6, 7, 8 \geq 0.$$