

## Collaborative

→ Similarity Based Algorithms -

- Featurize users & items
- Regression / classification

## user-user Similarity

## Item-Item Similarity

Users → 

✓	✓	✓		✓	✓	
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 8-Features

Items → 

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 12 Features

5 users      10 movies

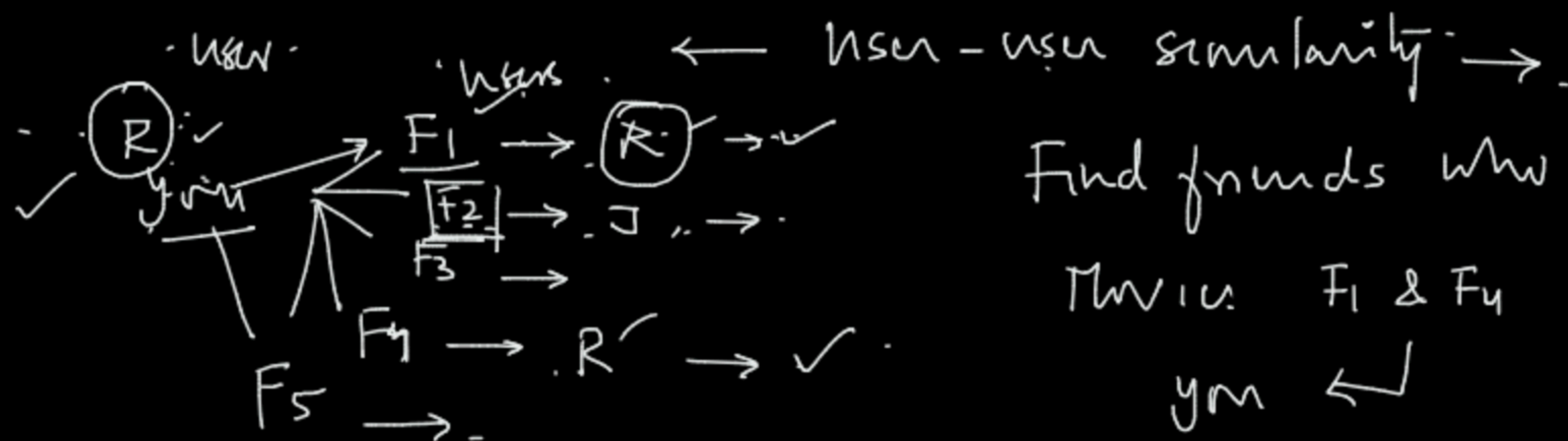
[illegible]

$$\boxed{M_{11}} \rightarrow \begin{array}{r} u_1 \underline{M_{11}} \\ u_2 \underline{M_{11}} \\ \hline u_3 \underline{M_{11}} \\ u_4 \underline{M_{11}} \\ \hline u_5 \underline{M_{11}} \end{array}$$

$W_6$   
 $=$   
 $u_6 M_1$   
 $u_6 M_2$   
 $u_6 M_{10}$

-	4.0 ✓
-	4.5 ✓





5 users →

↓ ✓ →

user = 100 ✓

Find users who have ratings similar to you  
 for items

1. Find users who are ill to user 100  
 (Based on ratings)

$u_{33}, u_{74}$

2. Find movies highly rated by  $u_{33}$  &  $u_{74}$

$\begin{matrix} \swarrow & \searrow \\ M_1 & M_7 \end{matrix} \quad \begin{matrix} \swarrow & \searrow \\ M_1 & M_{19} \end{matrix}$

3. Recommend  $M_1 M_7 M_{19}$  to user 100



← Item-Item similarity →

— Find items  $l$ th to each other —

Harry Potter → Magic related movies  
↑

USER →  $l$ th

1. Find items highly rated by user  $l$ th.

$M_1$   $M_2$

2. Find movies which are similar to  $M_1$  &  $M_2$  based on ratings

$M_5$   $M_7$   $M_{11}$   $M_{12}$

3. Recommend  $M_5, M_7, M_{11}, M_{12}$  to user  $l$ th



user-user similarity

$$X = \begin{matrix} & \begin{matrix} I_1 & I_2 & \boxed{I_3} & \dots & I_m \end{matrix} \\ \begin{matrix} u_1 \\ u_2 \\ u_3 \\ \vdots \\ u_n \end{matrix} & \begin{bmatrix} R_{11} & R_{12} & R_{13} & \dots & R_{1m} \\ R_{21} & R_{22} & R_{23} & \dots & R_{2m} \\ - & - & \boxed{-} & \dots & - \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ R_{n1} & R_{n2} & R_{n3} & \dots & R_{nm} \end{bmatrix} \end{matrix} \quad \begin{matrix} \checkmark \\ \checkmark \end{matrix}$$

$n \times m$

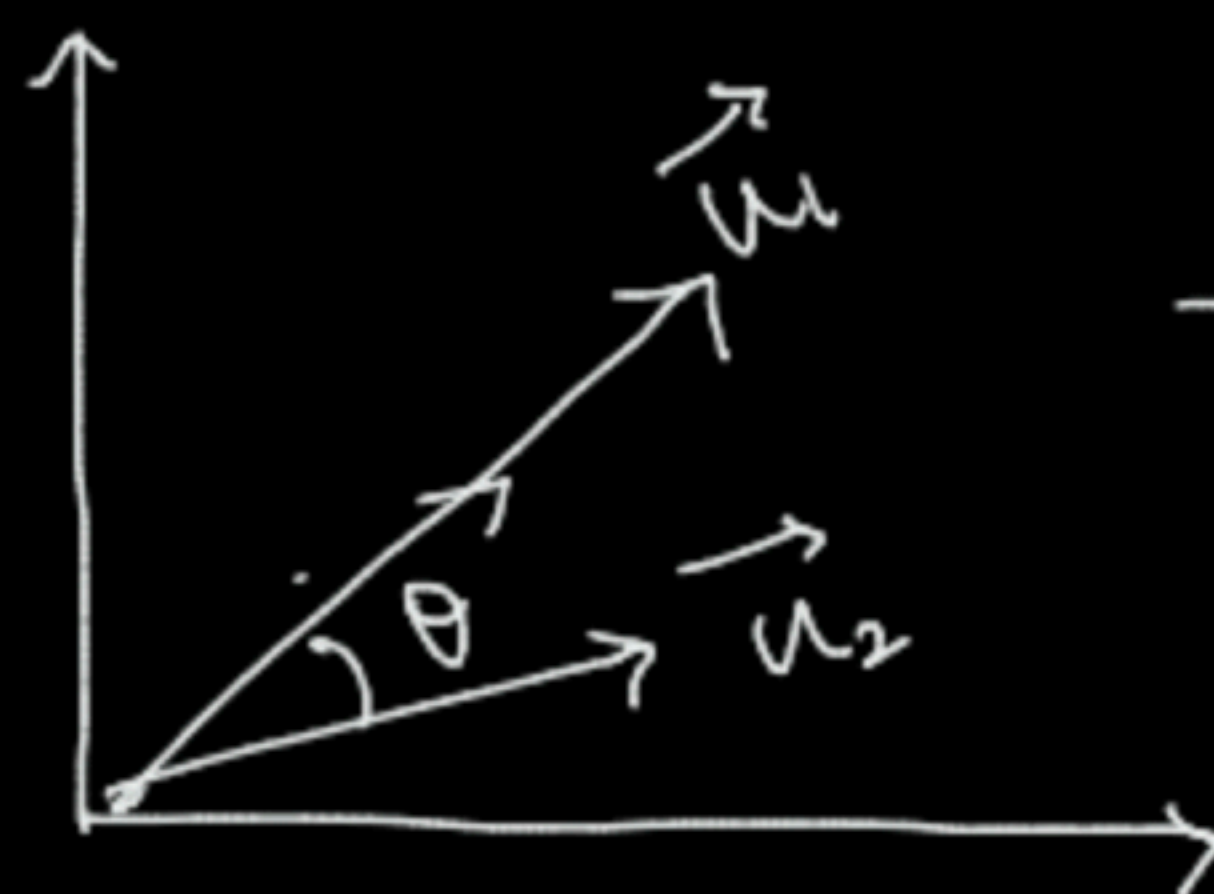
→ Sparse Matrix

→ Matrix Completion Problem

— Find column corresponding to the  
max rating given by user 3

$$\vec{u}_1 = \begin{bmatrix} R_{11} \\ R_{12} \\ R_{13} \\ \vdots \\ R_{1m} \end{bmatrix}$$

$$\vec{u}_2 = \begin{bmatrix} R_{21} \\ R_{22} \\ R_{23} \\ \vdots \\ R_{2m} \end{bmatrix}$$



→ cosine similarity -

$\theta = 0 ; 1 \rightarrow$  Exactly similar

$\theta \rightarrow \text{large} \rightarrow$  Very dissimilar



user similarity matrix.

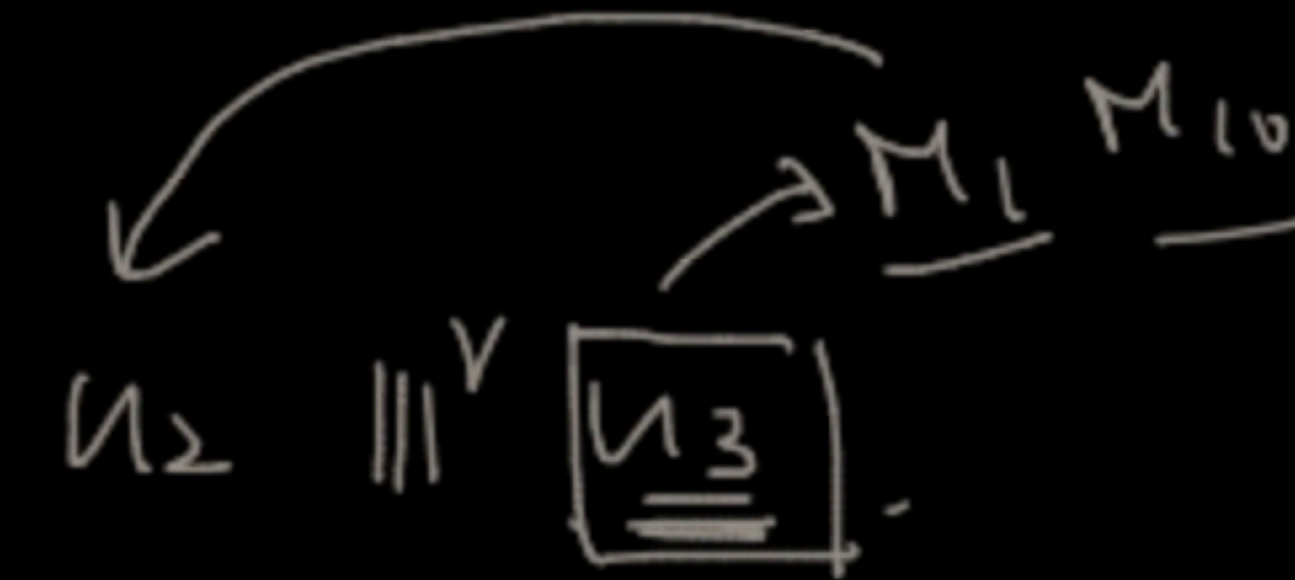
→

	$u_1$	$u_2$	$u_3$	$u_n$
$u_1$	1.0	0.87	0.15	0.34
$u_2$	0.87	1.0	0.94	0.37
$u_3$	0.15	0.94	1.0	0.73
$\vdots$				
$u_n$				0

←

→ max,

user 2.



Column Value corresponding to  
The highest similarity in the  
 $u_2$  row.

← Item-Item similarity →

✓

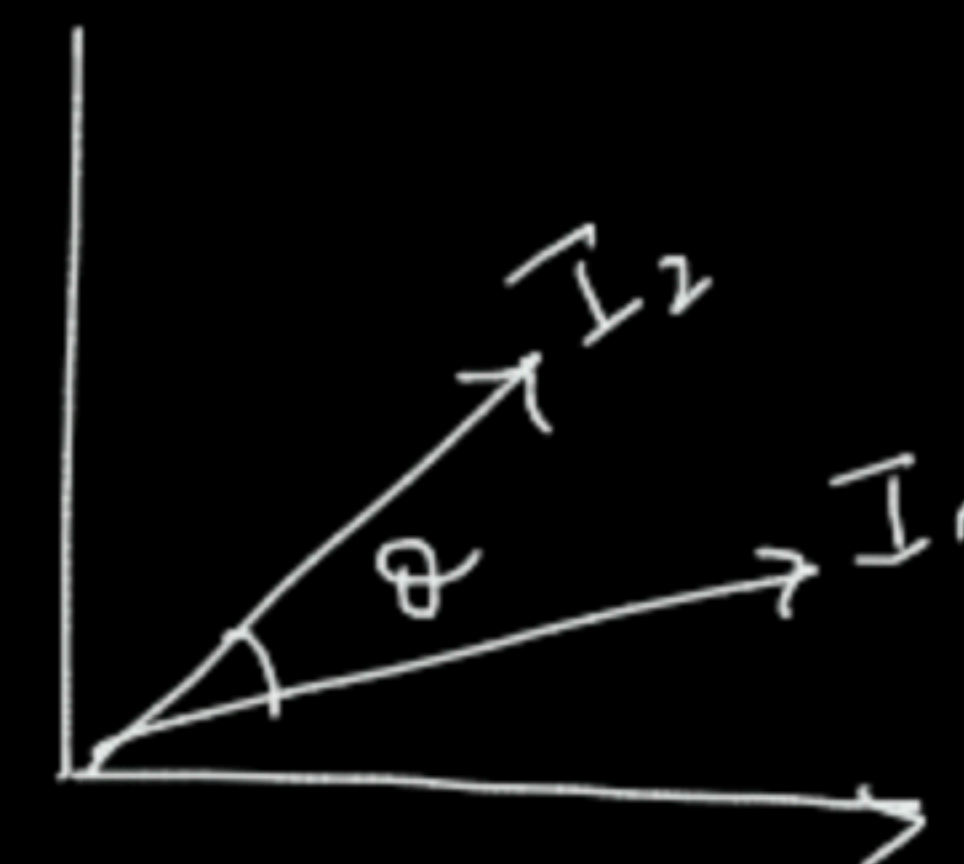
	$I_1$	$I_2$	$I_3$	...	$I_m$
$u_1$	$R_{11}$	$R_{12}$	$R_{13}$		$R_{1m}$
$u_2$	$R_{21}$	$R_{22}$	$R_{23}$	...	$R_{2m}$
$u_3$	$R_{31}$	$R_{32}$	$R_{33}$		$R_{3m}$
$\vdots$					
$u_n$	$R_{n1}$	$R_{n2}$	$R_{n3}$	...	$R_{nm}$

✓  $I_1 \rightarrow$

$$\begin{bmatrix} R_{11} \\ R_{21} \\ R_{31} \\ \vdots \\ R_{n1} \end{bmatrix}$$

$I_2 \rightarrow$

$$\begin{bmatrix} R_{12} \\ R_{22} \\ R_{32} \\ \vdots \\ R_{n2} \end{bmatrix}$$



1. Most popular movies

2. ...  
↳

✓

	$I_1$	$I_2$	$I_3$	$I_m$
$I_1$	1.0	0.2	0.9	
$I_2$	0.2	1.0	0.95	
$I_3$				
$\vdots$				
$I_m$				

1. Find items highly rated by user 2



1. user specific products → ✓ No search reqd - 5
2. products similar to searched → . - - - - 3
3. popular items - 2

10:45 am