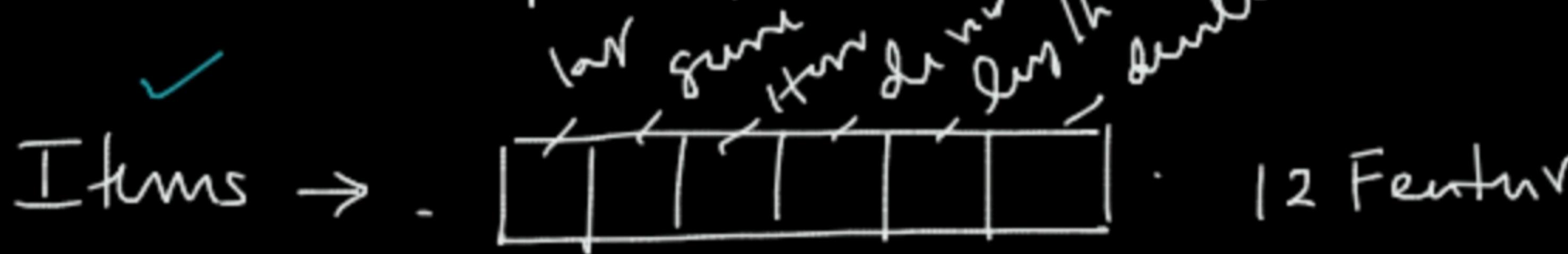
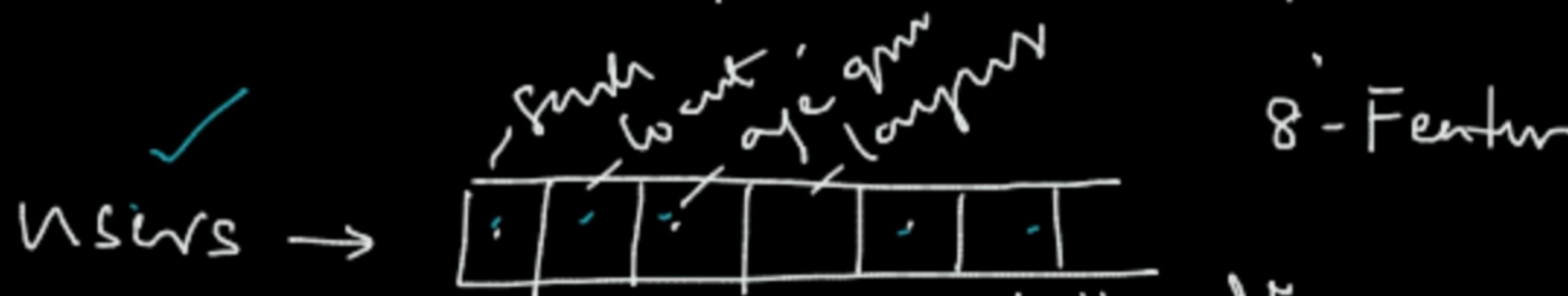


# Recommender Systems

## Content Based

- Featureize users & items
- Regression / classification



5 users 10 movies

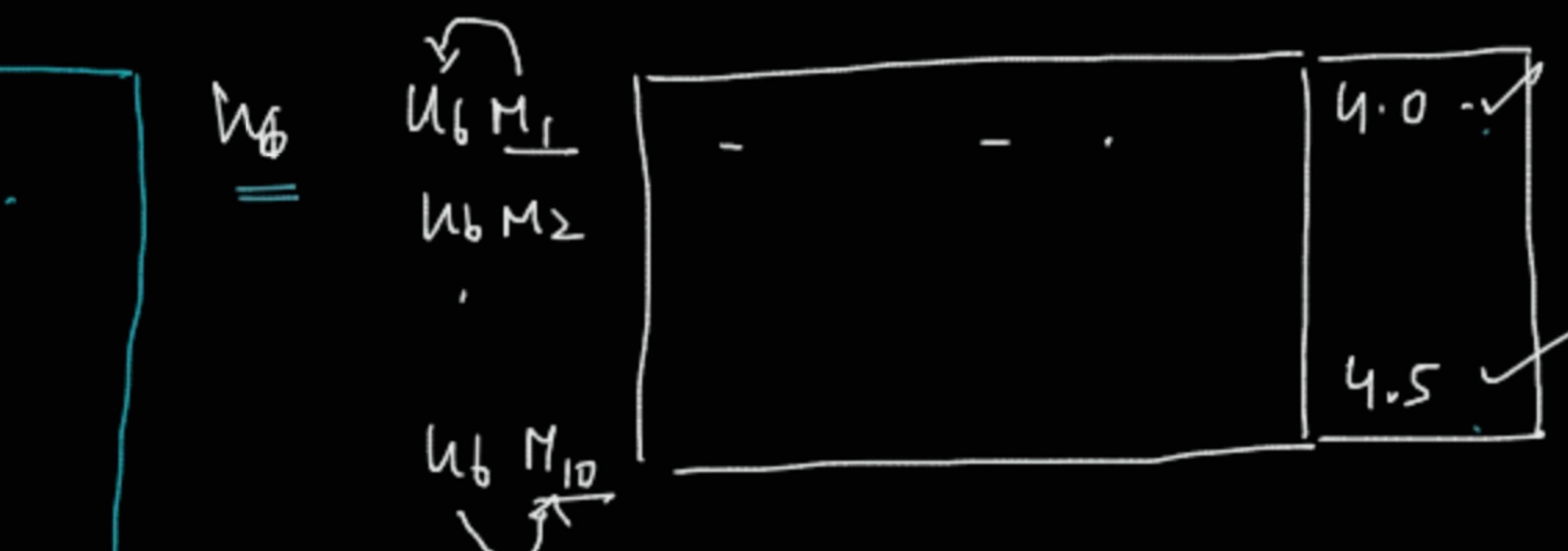
← Features →

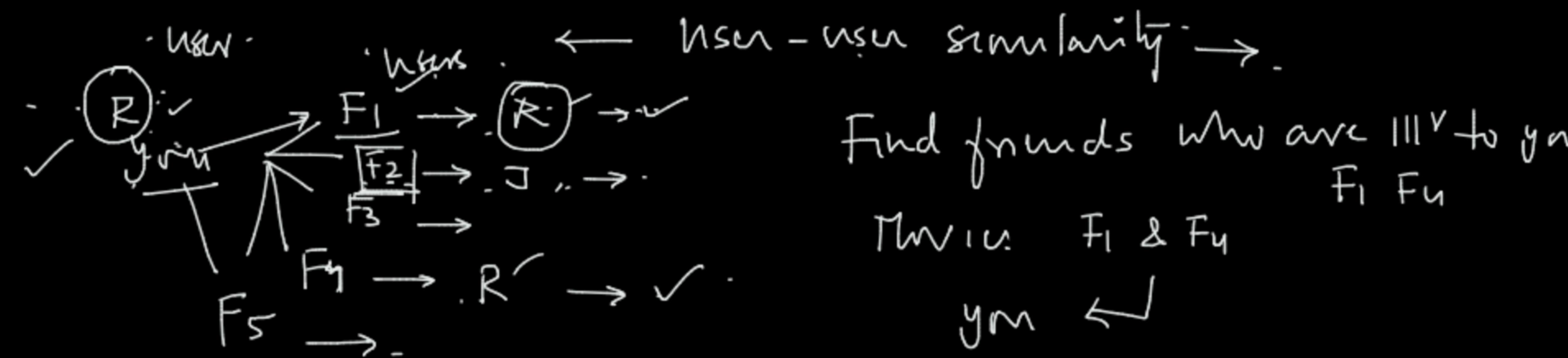
$u_1, M_1$	$u_1, M_2$	$u_1, M_3$	$u_2, M_1$	$u_2, M_2$	$u_3, M_1$	$u_3, M_2$	$u_4, M_1$	$u_4, M_2$	$u_5, M_1$	$u_5, M_2$	$u_5, M_3$	Rating
M 32 I En ...	- E thr - - - -	4.5	1									0
1 , , , ,	- - - - - - - -	2.0	0.									1
	- - - - - - - -	.	1									0
	- - - - - - - -	.	1									1
	- - - - - - - -	.	1									0.
	- - - - - - - -	3.5	.									1.5

## Collaborative

→ similarity Based Algorithms

User - User Item - Item  
Similarity Similarity





5 users  $\rightarrow$

$\downarrow \checkmark \rightarrow$

$\boxed{\text{user} = 100} \checkmark$

Find users who have ratings similar to you  
for items

1. Find users who are IIV to user 100  
(Based on ratings)

$u_{33}, u_{74}$

2. Find movies highly rated by  $u_{33}$  &  $u_{74}$

M1  $\swarrow$  M7  $\searrow$  M1 M19

3. Recommend M1 M7 M19 to user 100

← Item-Item Similarity →  
— Find items like to each other

Harry Potter → Magic related movies

user → item

1. Find items highly rated by user 100.

$M_1$   $M_2$

2. Find movies which are similar to  $M_1$  &  $M_2$  based on ratings

$M_5$   $M_7$   $M_{11}$   $M_{12}$

3. Recommend  $M_5, M_7, M_{11}, M_{12}$  to user 100

NSW - user similarity

$$X = \begin{bmatrix} u_1 & u_2 & u_3 & \dots & u_n \end{bmatrix} \begin{bmatrix} I_1 & I_2 & I_3 & \dots & I_m \end{bmatrix}^\top$$

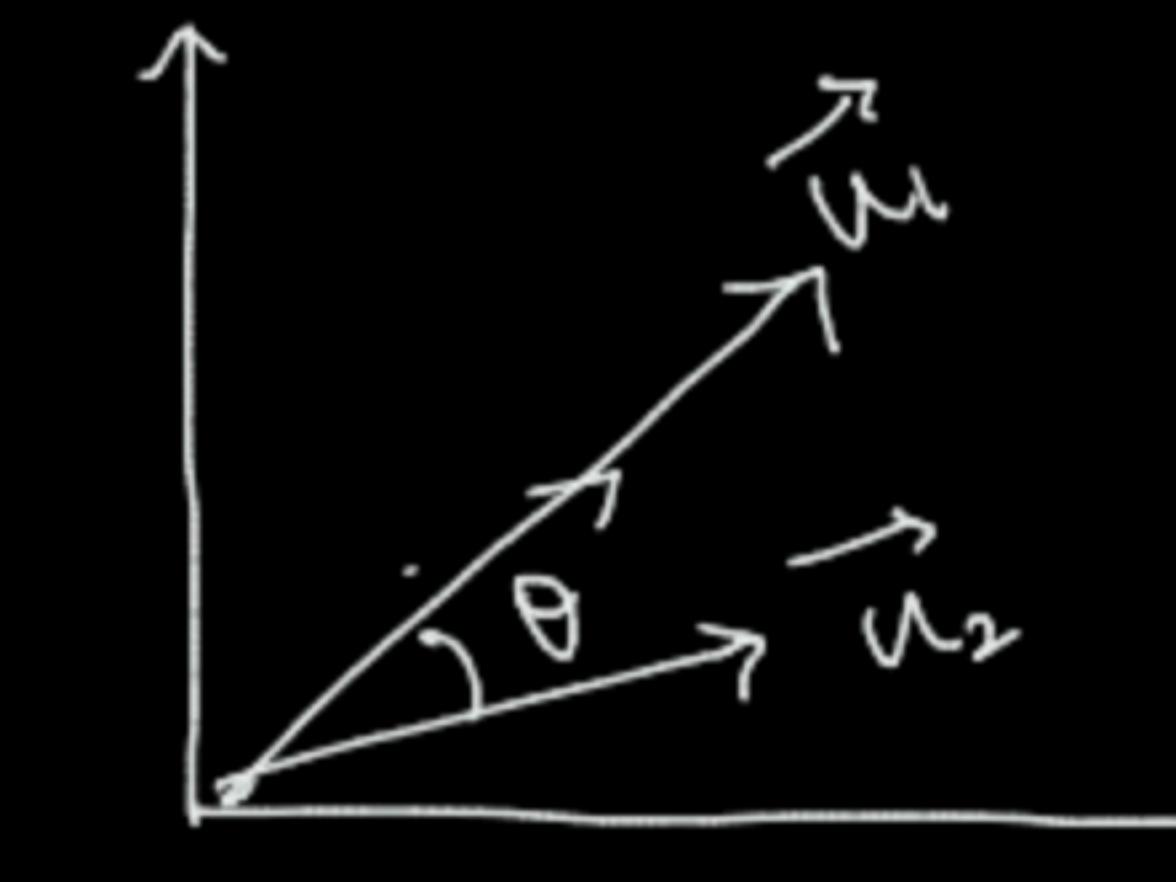
$100 \times 100$

→ Sparse Matrix

→ Matrix Completion Problem

— Find column corresponding to the max rating given by user 3

$$\begin{array}{l} \xrightarrow{\checkmark} \\ \xrightarrow{\checkmark} \end{array} \begin{array}{l} u_1 = \begin{bmatrix} R_{11} \\ R_{12} \\ R_{13} \\ \vdots \\ R_{1M} \end{bmatrix} \\ u_2 = \begin{bmatrix} R_{21} \\ R_{22} \\ R_{23} \\ \vdots \\ R_{2M} \end{bmatrix} \end{array}$$



→ cosine similarity

 $\theta = 0 ; 1 \rightarrow$  Exactly similar $\theta \rightarrow \text{large} \rightarrow$  Very dissimilar

User similarity matrix.

$$\rightarrow \underline{u_2} \left[ \begin{array}{ccccc} u_1 & u_2 & \boxed{u_3} & \cdots & u_n \\ \hline 1.0 & \boxed{0.87} & 0.15 & & \\ 0.87 & 1.0 & \boxed{0.94} & & \\ 0.15 & 0.94 & 1.0 & & \\ \vdots & & & \ddots & \\ u_n & & & & 0 \end{array} \right] \rightarrow \text{max.}$$

User 2

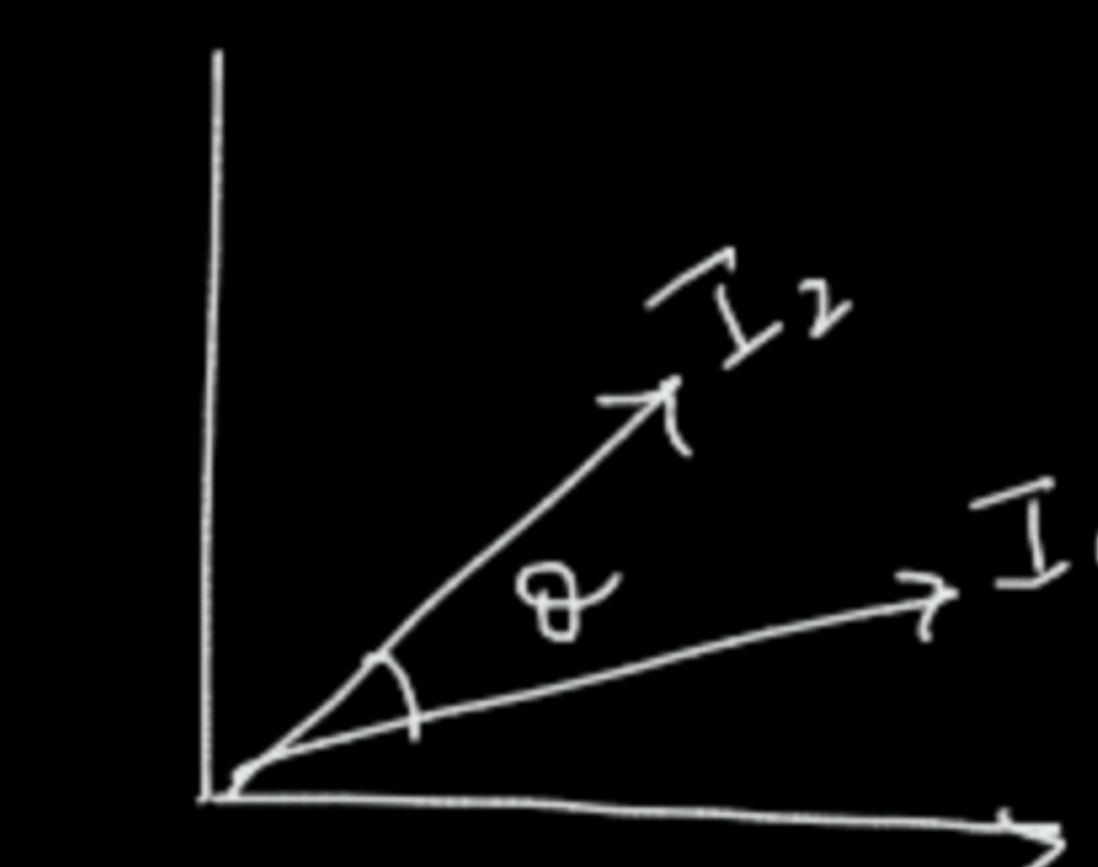
$$u_2 \parallel^V \boxed{u_3}.$$

$\xrightarrow{M_1} M_{10}$

Column Value corresponding to  
The highest similarity in the  
 $u_2$  row.

↙ Item-Item similarity →

✓

$$\rightarrow \begin{matrix} u_1 & \begin{bmatrix} I_1 & I_2 & I_3 & \dots & I_m \end{bmatrix} \\ u_2 & \begin{bmatrix} R_{11} & R_{12} & R_{13} & & R_{1m} \\ R_{21} & R_{22} & R_{23} & \dots & R_{2m} \\ R_{31} & R_{32} & R_{33} & & R_{3m} \\ \vdots & & & & \vdots \\ R_{n1} & R_{n2} & R_{n3} & \dots & R_{nm} \end{bmatrix} \\ \vdots & \end{matrix} \quad \rightarrow I_1 \rightarrow \begin{bmatrix} R_{11} \\ R_{21} \\ R_{31} \\ \vdots \\ R_{n1} \end{bmatrix} \quad \rightarrow I_2 = \begin{bmatrix} R_{i2} \\ R_{22} \\ R_{32} \\ \vdots \\ R_{n2} \end{bmatrix}$$


1. Most popular movies

2. ... ↴

$$\rightarrow \begin{matrix} I_1 & I_2 & I_3 & \dots & I_m \end{matrix} \quad \begin{bmatrix} 4.0 & 0.2 & 0.9 & \xrightarrow{0.95} & 0.12 \\ 0.2 & 1.0 & 0.95 & \xrightarrow{0.95} & \end{bmatrix} \rightarrow \text{User 2}$$

1. Find items highly rated by

1. user specific products  $\rightarrow \checkmark$  No search reqd - 1
  2. products similar to Searched  $\rightarrow$  - 2
  3. popular items  $\rightarrow$  - 3

10:45 am