

Write pseudo code for prim's algorithm.

### Prim's Algorithm

The pseudocode for prim's algorithm shows how we create 2 sets of vertices  $U$  &  $V-U$ .  $U$  contains the list of vertices that have been visited &  $V-U$  the list of vertices that haven't. One by one, we move vertices from set  $V-U$  to Set  $U$  by connecting the least weight edge.

### Pseudo Code

$T = \emptyset$ ;

$U = \{1\}$ ;

while ( $U \neq V$ )

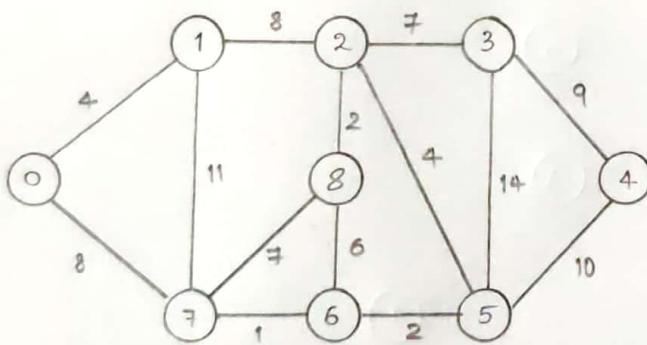
    let  $(u, v)$  be the lowest cost edge such that  $u \in U$  &  $v \in V-U$ ;

$T = T \cup \{(u, v)\}$

$U = U \cup \{v\}$

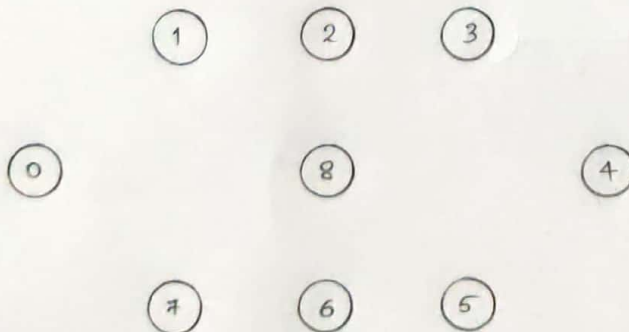
Use the algorithm to find minimum cost spanning tree for the graphs given below.

①



ans.

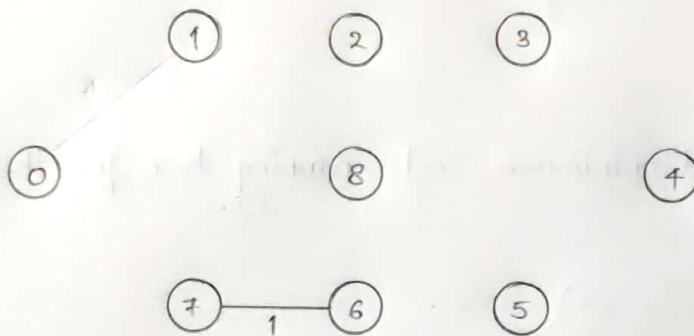
Step 1:-



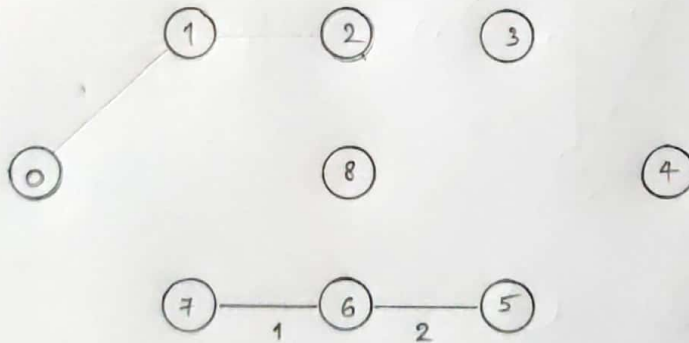
Step 2:-

	0	1	2	3	4	5	6	7	8
0	-	4	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$	8	$\infty$
1	4	-	8	$\infty$	$\infty$	$\infty$	$\infty$	11	$\infty$
2	$\infty$	8	-	7	$\infty$	4	$\infty$	$\infty$	2
3	$\infty$	$\infty$	7	-	9	14	$\infty$	$\infty$	$\infty$
4	$\infty$	$\infty$	$\infty$	9	-	10	$\infty$	$\infty$	$\infty$
5	$\infty$	$\infty$	4	14	10	-	2	$\infty$	$\infty$
6	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$	2	-	1	6
7	8	11	$\infty$	$\infty$	$\infty$	$\infty$	1	-	7
8	$\infty$	$\infty$	2	$\infty$	$\infty$	$\infty$	6	7	-

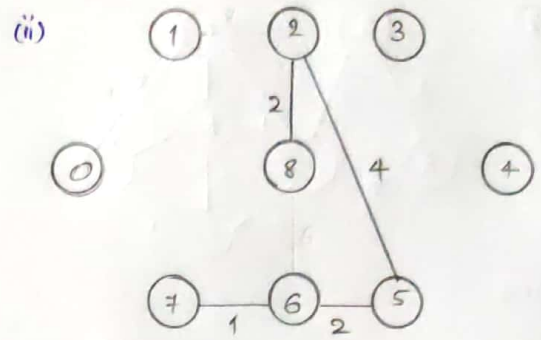
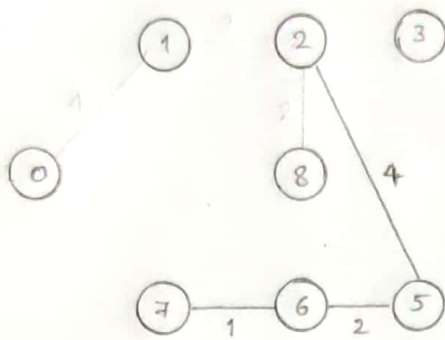
Step 3:-



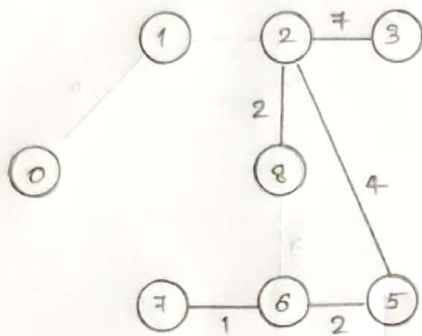
Step 4:-



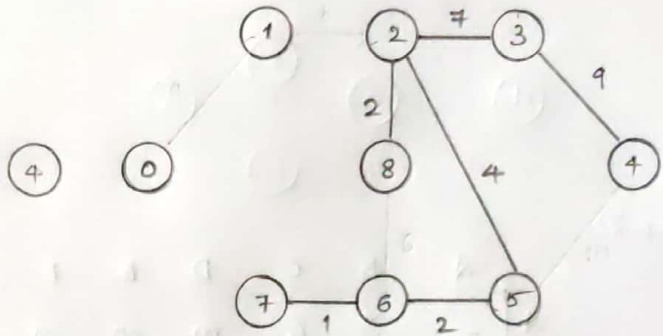
Step 5:- (i)



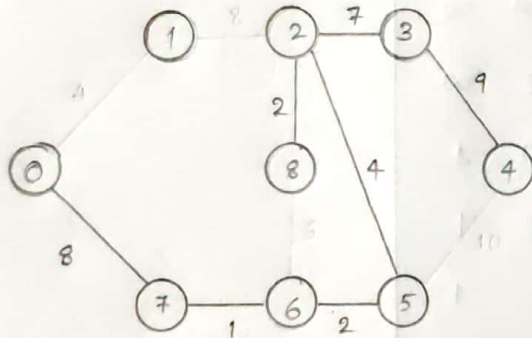
(iii)



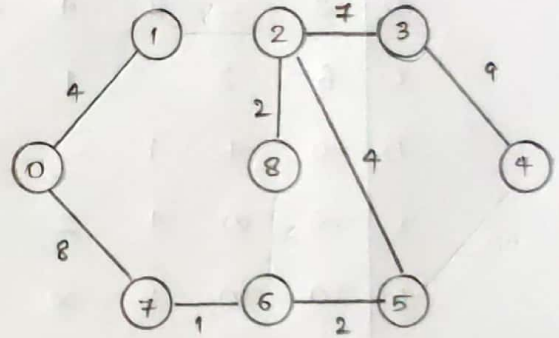
(iv)



(v)



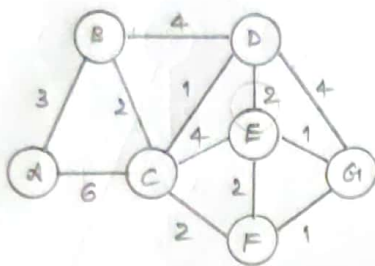
(vi)



No. of vertices - 1 = 9 - 1 = 8 edges have been obtained. So we stop.

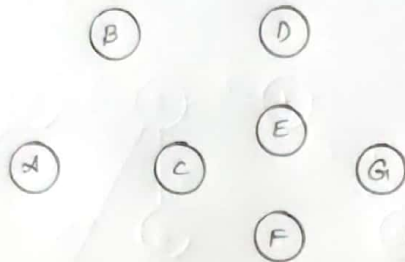
$$\begin{aligned} \text{Minimum weight} &= 4 + 8 + 2 + 4 + 1 + 2 + 7 + 9 \\ &= \underline{\underline{37}} \end{aligned}$$

②



ans

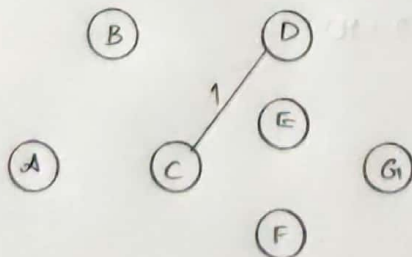
Step 1:-



Step 2:-

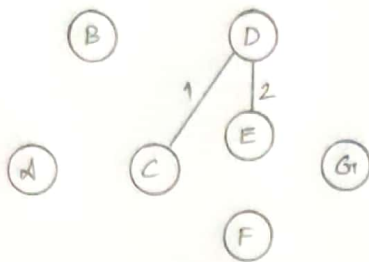
	A	B	C	D	E	F	G
A	-	3	6	$\infty$	$\infty$	$\infty$	$\infty$
B	3	-	2	4	$\infty$	$\infty$	$\infty$
C	6	2	-	1	4	2	$\infty$
D	$\infty$	4	1	-	2	$\infty$	4
E	$\infty$	$\infty$	4	2	-	2	1
F	$\infty$	$\infty$	2	$\infty$	2	-	1
G	$\infty$	$\infty$	$\infty$	4	1	1	-

Step 3:-

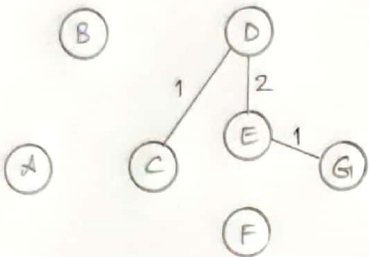




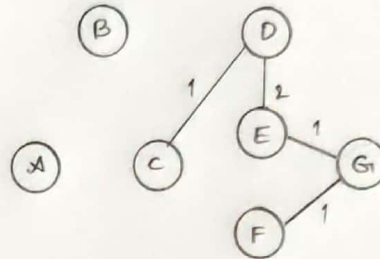
Step 4:-



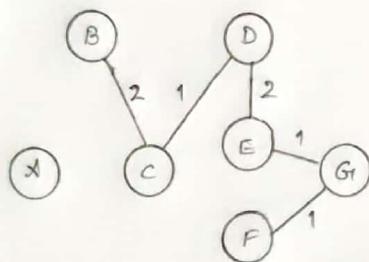
Step 5:- (i)



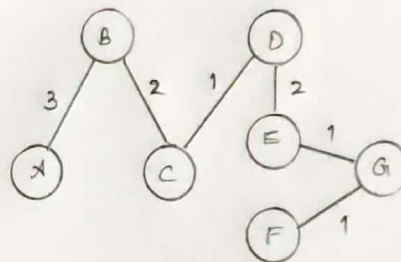
(ii)



(iii)



(iv)



No. of vertices - 1 =  $7 - 1 = 6$  edges have been obtained. So we stop.  
 Minimum weight =  $3 + 2 + 1 + 2 + 1 + 1$   
 $= \underline{\underline{10}}$