## Schroedinger equation with Python 1: 1D Infinite Square-Well potential

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## I. INTRODUCTION

We obtain the numerical solutions for the eigen-energies and wavefunctions of the 1D infinite square-well potential. We solve the 1D Schroedinger equation (using finite-difference method [1]),

$$\frac{d^2\psi(x)}{dx^2} + 2m[E - V(x)]\psi(x) = 0, (1)$$

for the potential V(x),

$$V(x) = \begin{cases} 0 & 0 < x < L \\ \infty & otherwise \end{cases}$$
 (2)

To obtain the eigen-energies, we integrate the wavefunction upto x = L and look for energies such that  $\psi(x = L) = 0$ . The initial conditions for the finite-difference method are  $\psi(x = 0) = 0$  and  $\psi(x + h) = 1$ . From the finite-difference method, we have

$$\psi(x+2h) = -[1+2E \ dx^2]\psi(x) + 2\psi(x+h),\tag{3}$$

where h is the integration step. We use the atomic units in our calculations ( $m_e = 1, e = 1, \hbar = 1$ ). Figure 1 shows the roots of  $\psi(x = L)$  as a function of energy E and the eigen-energies are therefore the points where  $\psi(x = L) = 0$ . Note the obvious  $n^2$  behavior of the roots.

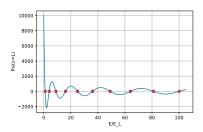


FIG. 1:  $\psi(x=L)$  as a function of energy. Note that our energy is scaled to  $E_L = \pi^2/2L^2$  which is the ground state energy of the 1D infinite square-well. The roots, i.e., eigen-energies (roots of  $\psi(x=L)=0$ ) are marked in red circles. We have set L=1

Figure 2 shows some of the wavefunctions for computed eigen-energies.

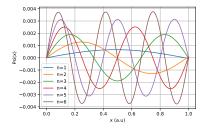


FIG. 2: First few wavefunctions of the 1D square-well potential