

Huber Loss :

Huber loss is a ~~loss~~^{cost} function. whenever we want to learn about the outliers as well as ignore them then we can go to this function because it is a combination of Mean Square Error and Mean Absolute Error. So it balances and combines good properties of both MAE and MSE.

→ According to MSE, it penalizes the model for making large errors (outliers) by squaring them. So, Mean Squared Error is not robust to outliers.

→ But Mean Absolute Error is robust to outliers. But there we cannot learn about outliers.

So, Huber loss comes under in that situation.

$$\boxed{\text{Huber loss} = \text{MSE} + \text{MAE}}$$

The Loss function of Huber loss is

$$\text{Loss} = \begin{cases} \frac{1}{2} (\underbrace{y - \hat{y}}_{\text{Quadratic Equation}})^2, & \text{if } |y - \hat{y}| \leq \delta \\ \delta |y - \hat{y}| - \frac{1}{2} \delta^2, & \text{otherwise} \end{cases}$$

Predicted value \hat{y}
 Actual value y
 Hyperparameter δ
 Linear Equation

So, Huber loss is combination of Quadratic Equation and Linear Equation.

if $|y - \hat{y}| > \delta$ then we use $\delta|y - \hat{y}| - \frac{1}{2}\delta^2$
means if $|y - \hat{y}|$ is huge (outlier) then we use the about
linear equation, to calculate the cost of the residuals.

If $|y - \hat{y}| \leq \delta$ then we use Quadratic equation
 $\frac{1}{2}(y - \hat{y})^2$ to calculate the cost of the residuals.

Advantages:

- It is differentiable at zero.
- Outliers are handled properly due to linearity above δ .
- The hyper parameter, δ can be tuned to maximize model accuracy.

Disadvantages:

- The additional conditionals and comparisons make Huberloss computationally expensive for large datasets.
- In order to maximize model accuracy, δ (hyperparameter) needs to be optimized and it is an iterative process.
- It is differentiable only once.

RMSE [Root Mean Squared Error]:

RMSE is a square root of Mean Square Error

$$[MSE] = \sqrt{MSE}$$

$$RMSE = \sqrt{\frac{1}{n} \sum_{i=1}^n (y - \hat{y})^2} = \sqrt{MSE}$$

→ RMSE is also called the Root Mean Square Deviation.

→ It measures the average magnitude of the residuals/errors.

- It concerns with the deviation from the actual value.
- If $RMSE = 0$ means the model has a perfect fit.
- The lower the RMSE value, the better the model and its predictions.
- The higher the RMSE indicates that there is a large deviation from the residual to the ground truth.

So simply, RMSE is inversely proportional to the performance of the model.

$$RMSE \propto \frac{1}{\text{Performance of the model}}$$

- RMSE can be used with different features as it helps in figuring out if the feature is improving the model's prediction (or) not.

Advantages:

- RMSE is easy to understand.
- It serves as a heuristic for training models.
- RMSE does not penalize the errors as much as MSE due to the Square root.

Disadvantages:

- RMSE is sensitive to outliers.
- RMSE increases with an increase in size of the test sample.
- It increases in magnitude if the scale of the \nearrow error increases.