ALY6015 – Intermediate Analytics – Week 1 – R Assignment

Regression Diagnostics with R

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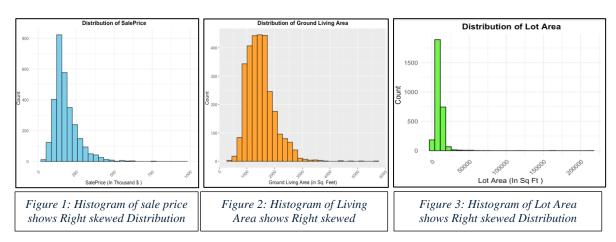
Introduction

This report performs exploratory data analysis (EDA) and regression analysis on the Ames Housing dataset to identify variables influencing sale price. The dataset contains 2,930 observations and 82 variables, sourced from the Ames Assessor's Office, which provides detailed housing attributes, including both structural and locational characteristics that impact residential property prices.

Data Analysis

Step-1: Data Cleaning and EDA

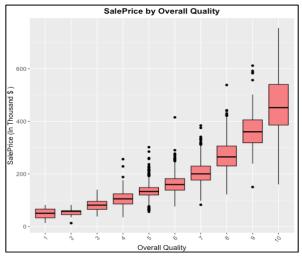
The first step involved pre-processing, including standardizing column names, categorizing data where necessary, and addressing missing values to ensure data quality for accurate analysis. Given the right-skewed distributions in Figures 1, 2, and 3, a log transformation was applied to normalize the values, reducing skewness and improving model predictability.

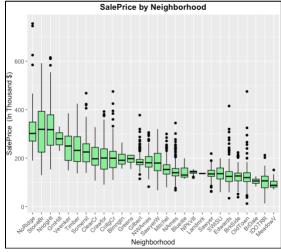


Figures 4 and 5 demonstrate that sale price varies significantly with both overall quality and neighborhood. This suggests that these factors play an essential role in determining home values.

Figure 4: Saleprice Positively varies by Overall Quality





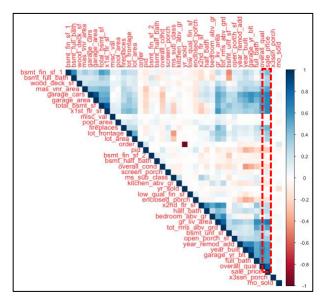


Further analysis is performed through correlation plots to investigate the relationships between sale price and other variables.

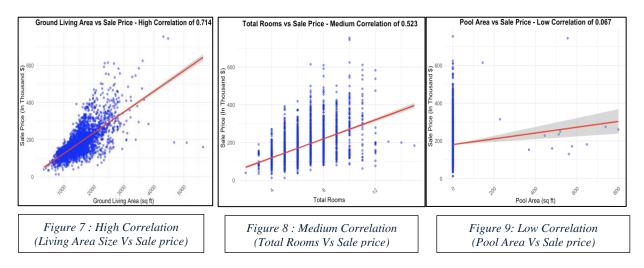
Step-3: Correlation Analysis With Corrplot() And Scatter Plot on Numerical Variables

Figure 6 presents the correlation between sale price and other numerical variables. The blue shading indicates positive correlations, while orange represents negative correlations, and white suggests no correlation. The intensity of the color indicates the strength of the correlation, with the red dotted line highlighting correlations with the sale price.

Figure 6: Correlation Plot Numerical Variables. Red-dashed line highlights our focus for sale_price column correlations



Figures 7, 8, and 9 illustrate the correlations between selected variables and sale price, with fitted regression lines. A strong positive correlation is observed between sale price and living area size (Figure 8), while a moderate correlation is noted between the number of rooms and sale price (Figure 9). Additionally, Figure 10 shows a negligible correlation between pool area and sale price.



Based on EDA and domain

knowledge, Several key variables were identified as potentially influential predictors of sale price. The key predictors of sale price include living area above grade (gr_liv_area), overall quality (overall_qual), garage area (garage_area), lot area (lot_area), total rooms above grade (tot_rms_abv_grd), and total basement area (total_bsmt_sf), with each contributing to price based on space, quality, utility, and potential for expansion.

Together, these variables provide a comprehensive view of the property's size, quality, and functionality, all of which are key determinants of its market value.

Step-4: Linear Model with No Feature Engineering

Figure 10 shows the summary of data of Linear Model Fitted without Feature Engineering

Figure 10: Summary of Linear Model Fitted without Feature Engineering

```
> summary(model1)
Call:
lm(formula = sale_price ~ gr_liv_area + overall_qual + garage_area
    lot_area + tot_rms_abv_grd + total_bsmt_sf + x1st_flr_sf,
Min 1Q Median 3Q Max
-551528 -19293 -470 16698 272143
Coefficients:
                     Estimate Std. Error t value Pr(>|t|)
                   -1.043e+05 4.053e+03 -25.742 < 2e-16 ***
(Intercept)
                    4.813e+01 2.839e+00 16.957 < 2e-16 ***
gr_liv_area
overall_qual
                    2.586e+04 6.966e+02 37.132 < 2e-16 ***
garage_area
lot_area
                    5.483e+01 4.121e+00 13.306 < 2e-16 ***
6.389e-01 9.432e-02 6.773 1.52e-11 ***
tot_rms_abv_grd -2.182e+03 7.547e+02 -2.891 0.00386 ** total_bsmt_sf 2.360e+01 2.783e+00 8.481 < 2e-16 ***
                                              8.481 < 2e-16 ***
                 1.045e+01 3.236e+00 3.230 0.00125 **
x1st_flr_sf
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Residual standard error: 37120 on 2922 degrees of freedom
Multiple R-squared: 0.7846, Adjusted R-squared: 0.78
                                     Adjusted R-squared: 0.7841
F-statistic: 1520 on 7 and 2922 DF, p-value: < 2.2e-16
```

Equation obtained:

```
sale_price = -104,300+48.13* gr_liv_area + 25,860*overall_qual + 54.83*garage_area + 0.639*lot_area - 2,182*tot_rms_abv_grd + 23.60* total_bsmt_sf + 10.45* x1st_flr_sf

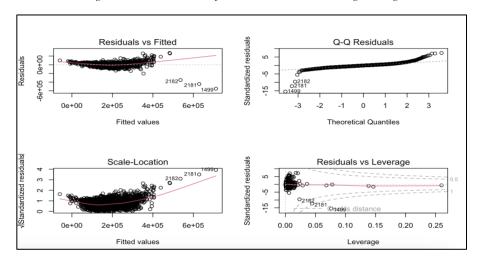
Adjusted R-Square: 0.7841 = 78.41% accuracy
```

Interpretation:

Figure 10 provides the summary of the linear model fitted without feature engineering. The equation obtained indicates that the intercept (-104,300) represents the estimated sale price when all predictors are zero. The coefficients represent the change in sale price for a one-unit increase in each variable. Notably, living area (gr_liv_area) and overall quality (overall_qual) have the highest impact on sale price, while other variables influence the price to a lesser extent. The adjusted R-squared of 0.7841 suggests that the model explains 78.41% of the variance in the sale price.

Step-5: Residual Plot Analysis

Figure 12: Residual Plot of Model without Feature Engineering



Insights from Figure 12:

Figure 12 presents the residual plot for the model without feature engineering, revealing several key insights:

- 1. **The linear assumption is violated**, as indicated by the non-flat residual vs. fitted plot.
- 2. The **residuals appear to be normally distributed**, as the Q-Q plot shows the residuals aligning with a straight line.
- 3. The **homoscedasticity test fails**, with the scale-location plot indicating non-constant variance.
- 4. **Multicollinearity exists**, as shown by outliers in the residuals vs. leverage plot.

Hence, the next step is to do scale, handle Multi Collinearity, Outliers to refine the model.

Step-6: Handle Homoscedasticity with Normalizing the variables

To address the skewness identified in the scale-location plot, log transformation was applied to continuous variables like sale_price and lot_area. This normalization helped mitigate the skewness and will improve model stability.

Step-7: Examine Outliers To Remove or Retain in the dataset

Figure 13: Outlier Test - Shows outliers with small p-values Figure 14: Outlier rows - Not removed as they contain Information > print(outlier_result) # Show the outlier rows with their values rstudent unadjusted p-value Bonferroni p > print(outlier_data[new_model_columns]) 1499 -16.128761 3.9671e-56 1.1624e-52 overall_qual tot_rms_abv_grd garage_area lot_area_normalized 6.0323e-32 2181 -12.585949 2.0588e-35 182 780 9.175335 5 2182 -9.736805 4.5317e-22 1.3278e-18 1554 1 4 487 9.587680 1768 7.464695 1.0957e-13 3.2103e-10 1499 10 12 1418 11.064871 1.0273e-12 1761 7.158503 3.0101e-09 2181 10 15 1154 10.578725 45 7.101896 1.5391e-12 4.5096e-09 2182 10 11 884 10.598982 434 6.005882 2.1381e-09 6.2646e-06 1183 9 9 864 10.109363 1064 5.980603 2.4931e-09 7.3049e-06 1556 6 250 9.047821 5.538845 3.3153e-08 9.7140e-05 433 373 6 544 9.384294 3.4097e-08

The outlier test results (Figure 13) reveal the presence of outliers in the dataset, with specific rows highlighted in Figure 14. These outliers stem from significant variations in garage area,

quality, and total room count in certain houses. Despite this, the inclusion of these values is relevant, as they offer insights into home sales trends across properties with both typical and high values for garage area and room count.

Step-8: Identify Multi Collinearity with VIF Test

Based on VIF Test in Figure -15, **gr_liv_area** and **x1st_flr_sf** are highly multicollinear variables with VIF of 4.37 and 3.41 respectively. Hence, these variables could be removed.

 Variance_Inflation_Factor

 gr_liv_area
 4.376503

 x1st_flr.sf
 3.418457

 total_bsmt_sf
 3.194123

 tot_rms_abv_grd
 2.995168

 overall_qual
 2.053302

 garage_area
 1.668443

 lot_area
 1.174085

Figure 15: VIF of Model of Model without Feature Engineering

Step-9: Build Model 2: After Feature Engineering:

After scaling, removing multicollinearity and examining outlier checks, new linear model was fitted to understand the variables influencing the normalized salesprice. The summary of model after feature engineering is shown in Figure-16.

Figure 16: Summary of Model After Feature Engineering

```
lm(formula = sale_price_normalized ~ overall_aual + tot_rms_abv_ard +
   garage_area + lot_area_normalized, data = housing)
             10 Median
                              30
-1.87675 -0.09760 0.01078 0.10994 0.76420
Coefficients:
                   Estimate Std. Error t value Pr(>|t|)
..ercept)
overall_qual
tot_rms
                                                <2e-16 ***
                 9.284e+00 6.700e-02 138.57
                  1.866e-01 3.149e-03 59.24
garage_area 3.631e-04 2.082e-05 17.44 lot_area_normalized 1.342e-01 7.650e-03 17.54
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' '1
Residual standard error: 0.1907 on 2925 degrees of freedom
Multiple R-squared: 0.7814,
                             Adjusted R-squared: 0.7811
F-statistic: 2613 on 4 and 2925 DF, p-value: < 2.2e-16
```

Equation obtained:

```
Sale Price (Normalized)=9.284+(0.1866\times overall\_qual)+(0.0323\times tot_rms\_abv\_grd)+(0.0003631\times garage\_area)+(0.1342\times lot\_area\_normalized)
Adjusted R-Square: 0.7811=78.11\%
```

Interpretation:

The equation reveals that overall quality has the strongest positive impact on sale price, followed by lot area, total rooms above grade, and garage area. These variables contribute to price based on size, quality, and functionality. The adjusted R-squared of 0.7811 indicates that the model

explains 78.11% of the variance in sale price, which is nearly identical to the previous model, but with only four significant predictors after feature engineering.

Step-10: Residual Plot After Feature Engineering

Figure 17 shows the residual plot for the model after feature engineering. The plots indicate that linearity, no multicollinearity, homoscedasticity, and outliers have been appropriately addressed, confirming the assumptions of a well-fitting linear regression model.

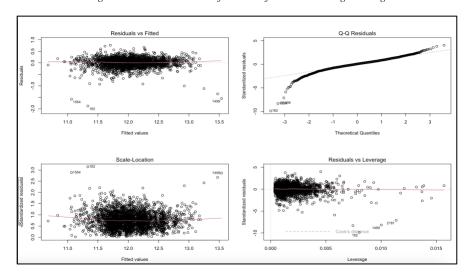


Figure 17: Residual Plot of Model After Feature Engineering

Step-11: Subset Regression with StepWise Regression

The stepwise regression model was used to identify the best set of predictor variables for **sale_price_normalized**. The results, displayed in **Figure 18**, indicate that each variable included in the final model contributes to reducing the **Akaike Information Criterion (AIC)**, which suggests that all variables have predictive value for the normalized sale price. The step model's best equation is as below:

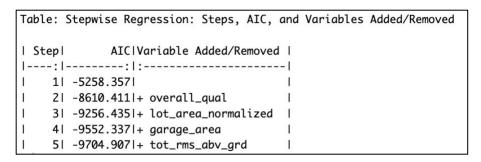


Figure 18: Stepwise Regression Results

Sale Price (Normalized)= $9.284+(0.1866\times overall_qual)+(0.0323\times tot_rms_abv_grd)+(0.0003631\times garage_area)+(0.1342\times lot_area_normalized)$ Adjusted R-Square: 0.7811=78.11%

Insights

- 1. Significant Predictors: The model indicates that overall quality, lot area, garage area, and total rooms above grade are all significant predictors of the sale price.
- **2. Model Fit**: With an **R-squared value of 0.7811**, the model explains approximately 78% of the variance in sale price, providing a good fit for predicting the normalized sale price.
- **3. AIC Reduction**: The stepwise approach, which selects predictors based on their contribution to minimizing AIC, has resulted in a set of variables that collectively contribute to the best model identified in Step-9 of this analysis.
- **4. Model Comparison:** The model with 7 variables and the model with 4 variables predict similarly, emphasizing the importance of identifying the most effective predictors.

Conclusion

The Stepwise Regression Model identifies key predictors—overall_qual, lot_area_normalized, garage_area, and tot_rms_abv_grd—with an adjusted R-squared of 0.7811, indicating a strong fit for predicting normalized sale prices as identified by model in Step-9. After performing feature engineering and addressing issues like multicollinearity and homoscedasticity, the revised model showed only slight improvement in fit, with fewer predictors but similar R-squared values. The stepwise model, being simpler and more interpretable, provides a clearer understanding of the most influential factors in determining sale prices, while both models underscore the importance of property quality, size, and functionality.

References:

- 1. Stack Overflow. (2018, April 5). *Using ggpairs on a large dataset with many variables*. Stack Overflow. https://stackoverflow.com/questions/48123611/using-ggpairs-on-a-large-dataset-with-many-variables
- 2. Stack Overflow. (2019, May 31). *R step function not writing out complete model in result report*. Stack Overflow. https://stackoverflow.com/questions/53531517/r-step-function-not-writing-out-complete-model-in-result-report

Appendix A

R code

```
### ALY6015 - Week 1 - Regression Ananlysis
## Created By: Hari Priya Ramamoorthy
## Dataset Details: Ames Housing
## Aim of Analysis - Perform EDA and Regression Analysis on
Housing data to find the numeric variables that are influencing
sales price.
###### Load Packages
###
install.packages('GGally','tibble','knitr','tidyr','janitor','mo
ments','car','leaps')
library(GGally)
library(dplyr)
library(ggplot2)
library(tidyr)
library(tibble)
library(knitr)
library(corrplot)
library(janitor)
library(car)
library(moments)
library(leaps)
###### Load Packages
###
###### Data cleaning - Step-1,2
###
##Load Ameshousing Dataset
housing <- read.table(file.choose(), sep=",",header=TRUE,
stringsAsFactors = FALSE)
```

```
##Standardize column names with janitor package
housing<-janitor::clean names(housing)</pre>
names(housing)
create glimpse table <- function(df) {</pre>
 tibble(
    Column Name = names(df),
    Data Type = sapply(df, class),
    Example Value = sapply(df, function(x) if (length(x) > 0)
x[1] else NA)
 )
raw data glimpse<-create glimpse table(housing)</pre>
summary(housing)
str(housing)
### check missing values Check
missing values <- sapply(housing, function(x) sum(is.na(x)))
print(missing values[missing values > 0])
#Based on data dictionary, replace values for Columns where NA
means not present.
not present columns <- c('alley', 'garage finish',</pre>
'garage type', 'garage qual', 'garage cond',
'bsmt fin type 1', 'bsmt fin type 2', 'bsmt exposure', 'bsmt cond',
'bsmt qual',
                          'fireplace qu', 'pool qc','fence',
'misc feature')
# Replace NA values with 'Not Present' in the specified columns
housing[not present columns] <-</pre>
lapply(housing[not present columns], function(x)
ifelse(is.na(x), 'Not Present', x))
# for numerical columns let's replace NA values with Median
num missing cols <- sapply(housing, function(x) is.numeric(x) &&</pre>
any(is.na(x))
num missing cols <- names(num missing cols[num missing cols ==</pre>
TRUE1)
# Replace NA with the median in these numerical columns
housing[num missing cols] <- lapply(housing[num missing cols],
function(x) {
x[is.na(x)] \leftarrow median(x, na.rm = TRUE)
```

```
return(x)
})
### check missing values Again
missing values <- sapply(housing, function(x) sum(is.na(x)))
# Print the result
print(missing values[missing values > 0])
###### Data cleaning - Step-1,2
###### EDA Visualizations - Step3
###########
## Histogram on Sales Price Distribution - Right Skewed
ggplot(housing, aes(x = sale price/1000)) +
 geom histogram(bins = 30, fill = "skyblue", color = "black") +
 labs(title = "Distribution of SalePrice", x = "SalePrice (In
Thousand $ ) ", y = "Count") +
 theme minimal()+
 theme (
   plot.title = element text(hjust = 0.5, size = 14, face =
"bold"),
   axis.title.x = element text(size = 12),
   axis.title.y = element text(size = 12),
   axis.text.x = element text(size = 10, angle = 45, hjust =
1),
   axis.text.y = element text(size = 10)
 scale x continuous (limits = c(0,1000, 100))
## Histogram on Sales Price Distribution - Right Skewed
ggplot(housing, aes(x = lot area)) +
 geom histogram( fill = "green", color = "black") +
 labs(title = "Distribution of Lot Area", x = "Lot Area (In Sq
Ft ) ", y = "Count") +
 theme minimal()+
 theme (
   plot.title = element text(hjust = 0.5, size = 14, face =
"bold"),
   axis.title.x = element text(size = 12),
   axis.title.y = element text(size = 12),
   axis.text.x = element text(size = 10, angle = 45, hjust =
```

```
1),
    axis.text.y = element text(size = 10)
  )
# Histogram of Living Area
qqplot(housing, aes(x = qr liv area)) +
  geom histogram(bins = 30, fill = "orange", color = "black") +
  labs(title = "Distribution of Ground Living Area", x = "Ground
Living Area (in Sq. Feet)", y = "Count")+
  theme (
    plot.title = element text(hjust = 0.5, size = 14, face =
"bold"),
    axis.title.x = element text(size = 12),
    axis.title.y = element text(size = 12),
    axis.text.x = element text(size = 10, angle = 45, hjust =
1),
    axis.text.y = element text(size = 10)
  )
# Boxplot comparing Saleprice variation by Overall Quality of
the house
qqplot(housing, aes(x =
reorder(factor(overall qual), desc(sale price/1000)), y =
sale price/1000)) +
  geom boxplot(fill = "lightcoral", color = "black") +
  labs(title = "SalePrice by Overall Quality", x = "Overall
Quality", y = "SalePrice (In Thousand $ )") +
    plot.title = element text(hjust = 0.5, size = 14, face =
"bold"),
    axis.title.x = element text(size = 12),
    axis.title.y = element text(size = 12),
   axis.text.x = element text(size = 10, angle = 45, hjust =
1),
    axis.text.y = element text(size = 10)
  )
# Box plot for SalePrice vs. Neighborhood
ggplot(housing, aes(x =
reorder(neighborhood, desc(sale price/1000)), y =
sale price/1000)) +
  geom_boxplot(fill = "lightgreen", color = "black") +
  theme (axis.text.x = element text (angle = 45, hjust = 1)) +
  labs(title = "SalePrice by Neighborhood", x = "Neighborhood",
y = "SalePrice (In Thousand $)")+
  theme(
```

```
plot.title = element text(hjust = 0.5, size = 14, face =
"bold"),
     axis.title.x = element text(size = 12),
     axis.title.y = element text(size = 12),
     axis.text.x = element text(size = 10, hjust = 1),
     axis.text.y = element text(size = 10)
   )
###### EDA - Step-3
############
####### Correlarion And Scatter Plot Analysis For Numeric
numeric vars <- sapply(housing, is.numeric)</pre>
corr matrix <- cor(housing[, numeric vars], use =</pre>
"complete.obs")
# Plot correlation matrix showing only the upper half
#### Insights from Plot
# High Correlation : gr liv area, overall quality; Low/No
Correlation: pool area, year ; Medium correlation-
tot rmsabv grd, full bath
corrplot(corr matrix, method = "color", order = "hclust", tl.cex
= 1.1, type = "upper")
title(main = "Correlation Heat Map")
# scatter plot-1 Between Highly Correlated Ground living Area vs
SalePrice
qqplot(housing, aes(x = qr liv area, y = sale price/1000)) +
 geom point(color = "blue", alpha = 0.5) +
 labs(title = "Ground Living Area vs Sale Price - High
Correlation of 0.714",
      x = "Ground Living Area (sq ft)",
      y = "Sale Price (In Thousand $)") +
 geom smooth(method = "lm", col = "red", size = 1) + # Linear
regression line
 theme minimal() +
 theme (
   plot.title = element text(hjust = 0.5, size = 14, face =
"bold"),
   axis.title.x = element text(size = 12),
   axis.title.y = element text(size = 12),
   axis.text.x = element text(size = 10, angle = 45, hjust =
1),
   axis.text.y = element text(size = 10)
```

```
# scatter plot-2 Between Least Correlated pool area vs SalePrice
ggplot(housing, aes(x = pool area, y = sale price/1000)) +
  geom point(color = "blue", alpha = 0.5) +
  labs(title = "Pool Area vs Sale Price - Low Correlation of
0.067",
       x = "Pool Area (sq ft)",
       y = "Sale Price (In Thousand $)") +
  theme minimal() +
  geom smooth(method = "lm", col = "red", size = 1) + # Linear
regression line
  theme (
    plot.title = element text(hjust = 0.5, size = 14, face =
"bold"),
    axis.title.x = element text(size = 12),
    axis.title.y = element text(size = 12),
    axis.text.x = element text(size = 10, angle = 45, hjust =
1),
    axis.text.y = element text(size = 10)
  )
ggplot(housing, aes(x = tot rms abv grd, y = sale price/1000)) +
  geom point(color = "blue", alpha = 0.5) +
  labs(title = "Total Rooms vs Sale Price - Medium Correlation
of 0.523",
       x = "Total Rooms ",
       y = "Sale Price (In Thousand $)") +
  theme minimal() +
  geom smooth(method = "lm", col = "red", size = 1) + # Linear
regression line
  theme (
    plot.title = element text(hjust = 0.5, size = 14, face =
"bold"),
    axis.title.x = element text(size = 12),
    axis.title.y = element text(size = 12),
    axis.text.x = element text(size = 10, angle = 45, hjust =
1),
    axis.text.y = element text(size = 10)
  )
# Scatter plot matrix for numeric variables with high, low,
medium correlation
# Reference: https://stackoverflow.com/questions/68638725/how-
to-address-overplotting-in-ggallyggpairs
```

```
ggpairs(housing[, c("sale price", "gr liv area",
"overall qual", "tot rms abv grd", "pool area", 'x1st flr sf')])
####### Correlarion And Scatter Plot Analysis For Numeric
###### LR model 1 - No Feature Engineering
#######
######## Select Highly correlated variables to model the sales
price
model columns <- c("gr liv area", "overall qual", "garage area",</pre>
'lot area', 'tot rms abv grd', 'total bsmt sf', 'x1st flr sf')
model1 <- lm(sale price ~ gr liv area + overall qual +</pre>
garage area + lot area + tot rms abv grd + total bsmt sf+
x1st flr sf, data=housing)
summary(model1)
### Residual Plot
par(mfrow=c(2,2))
plot (model1)
## Normalize continuous variables sale price lot area to remove
skewness,
housing$sale price normalized <- log(housing$sale price)
housing$lot area normalized =log(housing$lot area)
######## Multi-collinearity Check: correlation Matrix and VIF
Test , Outlier Check : car package #########
##### Insights from correlation Matrix and VIF Test
## 1. Remove gr liv area - correlated with Overall quality,1st
floor square feet
#corr matrix model data <- cor(housing[, model columns], use =</pre>
"complete.obs")
#corrplot(corr matrix model data, method = "color", order =
"hclust", tl.cex = 1.1, title = "Correlation Heatmap")
####### Identify Multi Collinearity with VIF Test
vif1<-data.frame("Variance Inflation Factor"=vif(model1))</pre>
######## Outlier Test on Model 2 ###################
outlier result <- outlierTest(model1)</pre>
print(outlier result)
# Let's get the indices of the outlier observations based on the
row numbers from the outlierTest result
```

```
outlier indices <- c(182, 1554, 1499, 2181, 2182, 1183, 1556,
373, 727)
# Extract the outliers from the dataset
outlier data <- housing[outlier indices, ]
# Show the outlier rows with their values
print(outlier data[model columns])
#### Insights 1. Outlier Present - Because of the room size and
garage, which has meaningful data, so no action taken
####### LR model 1 - No Feature Engineering
#######
###### LR model 2 - After Feature Engineering
#######
new model columns = c("overall qual", "tot rms abv grd",
"garage area", "lot area normalized")
model2 <- lm(sale price normalized ~ overall qual +</pre>
tot rms abv grd + garage area + lot area normalized ,
data=housing)
summary(model2)
### Residual Plot
par(mfrow=c(2,2))
plot(model2)
## Component +Residual Plot for each predictor
### Residual Plot
par(mfrow=c(1,1))
crPlots (model2)
###### LR model 2 - After Feature Engineering
#######
nullModel <- lm(sale price normalized ~ 1,data=housing )</pre>
```

```
fullModel <- lm(sale price normalized ~ overall qual +</pre>
tot rms abv grd + garage area + lot area normalized
, data=housing )
# step-wise regression in both directions
step model <-
step (nullModel, scope=list (lower=nullModel, upper=fullModel), direc
tion = "both")
# Extract the anova table from the stepwise model, which
contains the step information.
step info <- step model$anova</pre>
# Create a data frame to store step information for plotting
stepwise df <- data.frame(</pre>
 Step = 1:nrow(step info),
 AIC = step info$AIC,
 Variable = step info$Step
# Use kable to display the table in a report-friendly format
kable (stepwise df,
     caption = "Stepwise Regression: Steps, AIC, and Variables
Added/Removed",
     col.names = c("Step", "AIC", "Variable Added/Removed"),
     format = "markdown")
# Print the table for reporting
print(stepwise df)
summary(step model)
stepwise Regression
```