		Programming assignment 5: Optimization: Logistic regression
In	[1]:	<pre>import numpy as np import matplotlib.pyplot as plt %matplotlib inline</pre>
		<pre>from sklearn.datasets import load_breast_cancer from sklearn.model_selection import train_test_split from sklearn.metrics import accuracy_score, f1_score</pre>
		Your task
		In this notebook code skeleton for performing logistic regression with gradient descent is given. Your task is to complete the functions where required. You are only allowed to use built-in Python functions, as well as any numpy functions. No other libraries / imports are allowed.
		For numerical reasons, we actually minimize the following loss function $\mathcal{L}(\mathbf{w}) = \frac{1}{N} NLL(\mathbf{w}) + \frac{1}{2} \lambda \mathbf{w} _2^2$
		where $NLL(\mathbf{w})$ is the negative log-likelihood function, as defined in the lecture (Eq. 33)
		Exporting the results to PDF Once you complete the assignments, export the entire notebook as PDF and attach it to your homework solutions. The best way of doing that is
		way of doing that is 1. Run all the cells of the notebook. 2. Download the notebook in HTML (click File > Download as > .html)
		 Convert the HTML to PDF using e.g. https://www.sejda.com/html-to-pdf or wkhtmltopdf for Linux (tutorial) Concatenate your solutions for other tasks with the output of Step 3. On a Linux machine you can simply use pdfunite, there are similar tools for other platforms too. You can only upload a single PDF file to Moodle.
		This way is preferred to using <code>nbconvert</code> , since <code>nbconvert</code> clips lines that exceed page width and makes your code harder to grade.
		Load and preprocess the data In this assignment we will work with the UCI ML Breast Cancer Wisconsin (Diagnostic) dataset https://goo.gl/U2Uwz2 .
		Features are computed from a digitized image of a fine needle aspirate (FNA) of a breast mass. They describe characteristics of the cell nuclei present in the image. There are 212 malignant examples and 357 benign examples.
In	[2]:	<pre>X, y = load_breast_cancer(return_X_y=True) # Add a vector of ones to the data matrix to absorb the bias term</pre> <pre>X</pre>
		<pre>X = np.hstack([np.ones([X.shape[0], 1]), X]) # Set the random seed so that we have reproducible experiments np.random.seed(123)</pre>
		<pre># Split into train and test test_size = 0.3 X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=test_size)</pre>
		Task 1: Implement the sigmoid function
In	[3]:	<pre>def sigmoid(t): """ Applies the sigmoid function elementwise to the input data.</pre>
		Parameters t: array, arbitrary shape Input data.
		Returns t_sigmoid : array, arbitrary shape.
		Data after applying the sigmoid function. """ return 1/(1+np.exp(-t))
		Task 2: Implement the negative log likelihood As defined in Eq. 33
In	[4]:	<pre>def negative_log_likelihood(X, y, w): """ Negative Log Likelihood of the Logistic Regression.</pre>
		Parameters X: array, shape [N, D]
		<pre>(Augmented) feature matrix. y : array, shape [N] Classification targets. w : array, shape [D]</pre>
		Regression coefficients ($w[0]$ is the bias term). Returns
		<pre>nll : float The negative log likelihood. """ # TODO</pre>
		<pre>return -np.sum(np.add(np.multiply(y,np.log(sigmoid(np.dot(X,w))+1e-15)),</pre>
In	[5] :	Computing the loss function $\mathcal{L}(\mathbf{w})$ (nothing to do here) $\frac{\text{def compute_loss}(X, y, w, lmbda):}{\text{"""}}$
		Negative Log Likelihood of the Logistic Regression. Parameters
		<pre>X: array, shape [N, D] (Augmented) feature matrix. y: array, shape [N] Classification targets.</pre>
		<pre>w: array, shape [D] Regression coefficients (w[0] is the bias term). lmbda: float L2 regularization strength.</pre>
		Returns loss: float
		Loss of the regularized logistic regression model. """ # The bias term w[0] is not regularized by convention return negative_log_likelihood(X, y, w) / len(y) + lmbda * np.linalg.norm(w[1:])**2
		Task 3: Implement the gradient $ abla_{\mathbf{w}}\mathcal{L}(\mathbf{w})$
In	[6] :	Make sure that you compute the gradient of the loss function $\mathcal{L}(\mathbf{w})$ (not simply the NLL!) def get_gradient(X, y, w, mini_batch_indices, lmbda):
		""" Calculates the gradient (full or mini-batch) of the negative log likelilhood w.r.t. w. Parameters
		<pre> X: array, shape [N, D] (Augmented) feature matrix. y: array, shape [N]</pre>
		Classification targets. w: array, shape [D] Regression coefficients (w[0] is the bias term). mini_batch_indices: array, shape [mini_batch_size]
		The indices of the data points to be included in the (stochastic) calculation of the gradient. This includes the full batch gradient as well, if mini_batch_indices = np.arange(n_train). lmbda: float Regularization strentgh. lmbda = 0 means having no regularization.
		Returns dw: array, shape [D] Gradient w.r.t. w.
		<pre>x=np.zeros((len(mini_batch_indices),len(w))); Y=np.zeros((len(mini_batch_indices)));</pre>
		<pre>j=0; for i in mini_batch_indices: x[j,:]=X[i,:] Y[j]=y[i]; j=j+1;</pre>
		<pre>dw=(1/len(x))*(-np.dot(np.transpose(np.subtract(Y,sigmoid(np.dot(x,w)))),x)) +2*lmbda*w return dw</pre>
In	[7]:	Train the logistic regression model (nothing to do here)
		<pre>def logistic_regression(X, y, num_steps, learning_rate, mini_batch_size, lmbda, verbose): """ Performs logistic regression with (stochastic) gradient descent. Parameters</pre>
		<pre>Y: array, shape [N, D] (Augmented) feature matrix. y: array, shape [N]</pre>
		Classification targets. num_steps : int Number of steps of gradient descent to perform. learning rate: float
		The learning rate to use when updating the parameters w. mini_batch_size: int The number of examples in each mini-batch. If mini_batch_size=n_train we perform full batch gradient descent.
		<pre>lmbda: float Regularization strentgh. lmbda = 0 means having no regularization. verbose : bool Whether to print the loss during optimization.</pre>
		Returns w: array, shape [D]
		Optimal regression coefficients (w[0] is the bias term). trace: list Trace of the loss function after each step of gradient descent. """
		<pre>trace = [] # saves the value of loss every 50 iterations to be able to plot it later n_train = X.shape[0] # number of training instances</pre>
		<pre>w = np.zeros(X.shape[1]) # initialize the parameters to zeros # run gradient descent for a given number of steps for step in range(num_steps): parameters to zeros # run gradient descent for a given number of steps for step in range(num_steps): parameters to zeros</pre>
		<pre>permuted_idx = np.random.permutation(n_train) # shuffle the data # go over each mini-batch and update the paramters # if mini_batch_size = n_train we perform full batch GD and this loop runs only once</pre> <pre>Consider in recover (0 to the interior ministrate)</pre>
		<pre>for idx in range(0, n_train, mini_batch_size): # get the random indices to be included in the mini batch mini_batch_indices = permuted_idx[idx:idx+mini_batch_size] gradient = get_gradient(X, y, w, mini_batch_indices, lmbda)</pre>
		<pre># update the parameters w = w - learning_rate * gradient # calculate and save the current loss value every 50 iterations</pre>
		<pre>if step % 50 == 0: loss = compute_loss(X, y, w, lmbda) trace.append(loss) # print loss to monitor the progress</pre>
		<pre>if verbose: print('Step {0}, loss = {1:.4f}'.format(step, loss)) return w, trace</pre>
In	[8]:	Task 4: Implement the function to obtain the predictions def predict (X, w):
		Parameters X: array, shape [N_test, D]
		(Augmented) feature matrix. w : array, shape [D] Regression coefficients (w[0] is the bias term).
		Returns y_pred : array, shape [N_test] A binary array of predictions.
		<pre>""" return np.greater(sigmoid(np.dot(X,w)),0.5)</pre>
In	[9]:	<pre># Change this to True if you want to see loss values over iterations. verbose = False</pre>
In [[10]:	<pre>n_train = X_train.shape[0] w_full, trace_full = logistic_regression(X_train,</pre>
		<pre>num_steps=8000, learning_rate=1e-5, mini_batch_size=n_train, lmbda=0.1,</pre>
In [[11]:	<pre>n_train = X_train.shape[0] w_minibatch, trace_minibatch = logistic_regression(X_train,</pre>
		y_train, num_steps=8000, learning_rate=1e-5, mini_batch_size=50,
		Our reference solution produces, but don't worry if yours is not exactly the same.
		Full batch: accuracy: 0.9240, f1_score: 0.9384 Mini-batch: accuracy: 0.9415, f1_score: 0.9533
In [[12]:	<pre>y_pred_full = predict(X_test, w_full) y_pred_minibatch = predict(X_test, w_minibatch) print('Full batch: accuracy: {:.4f}, f1_score: {:.4f}'</pre>
		<pre>.format(accuracy_score(y_test, y_pred_full), f1_score(y_test, y_pred_full))) print('Mini-batch: accuracy: {:.4f}, f1_score: {:.4f}'</pre>
In [[13]:	Full batch: accuracy: 0.9240, f1_score: 0.9384 Mini-batch: accuracy: 0.9415, f1_score: 0.9533 plt.figure(figsize=[15, 10])
		<pre>plt.plot(trace_full, label='Full batch') plt.plot(trace_minibatch, label='Mini-batch') plt.xlabel('Iterations * 50') plt.ylabel('Loss \$\mathcal{L}(\mathbf{w})\$')</pre>
		<pre>plt.legend() plt.show()</pre> <pre>— Full batch</pre>
		— Full batch — Mini-batch
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		0.6 -
		0.4 -
		0 20 40 60 80 100 120 140 160 Iterations * 50