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DEPT : B E COMPUTER SCIENCE AND ENGINEERING - A

Divide and Conquer

a. Number of Zeros in a Given Array

Aim: Given an array of 1s and 0s this has all 1s first followed by all 0s. Aim is to find the number of 0s. Write a program using Divide and Conquer to Count the number of zeroes in the given array.

Input Format

First Line Contains Integer m – Size of array

Next m lines Contains m numbers – Elements of an array Output Format

First Line Contains Integer – Number of zeroes present in the given array.

Algorithm:

```
function count(a, left, right) {
```

```
// base case: if left index exceeds right index if left is greater than right {
```

```
return 0
```

```
}
```

```
initialize mid as (left + right) / 2 // find the middle index
```

```

// check if the middle element is 1 if a[mid] is equal to 1 {

// check if the next element is 0 if a[mid + 1] is equal to 0 {

// count zeros from mid + 1 to right

initialize c as (right - (mid + 1)) + 1 return c

} else {

// search in the right half return count(a, mid + 1, right)

}

}

// check if both ends are 0

else if a[left] is equal to 0 and a[right] is equal to 0 { return right + 1 // return total count of elements

}

// search in the left half else {

return count(a, left, mid - 1)

}

}

function main() {

initialize n // number of elements read n from user

initialize arr array of size n // array to hold binary values

```

```
// read values into the arr array for i from 0 to n - 1 {
```

```
read arr[i] from user
```

```
}
```

```
initialize left as 0 // left index initialize right as n - 1 // ri
```

Program:

```
#include <stdio.h>
```

```
int count(int a[],int left,int right)
```

```
{
```

```
if(left>right)
```

```
{
```

```
return 0;
```

```
}
```

```
int mid=(left+right)/2; if(a[mid]==1)
```

```
{
```

```
if(a[mid+1]==0)
```

```
{
```

```
int c= (right-(mid+1))+1; return c;
```

```
}
```

```
else{
```

```
return count(a,mid+1,right);
```

```
}
```

```
}
```

```
else if(a[left]==0 && a[right]==0)
```

```
{  
  
return right+1;  
  
}
```

```
else
```

```
{  
  
return count(a,left,mid-1);  
  
}
```

```
}
```

```
int main()
```

```
{
```

```
int n; scanf("%d",&n); int arr[n];
```

```
for(int i=0;i<n;i++){ scanf("%d",&arr[i]);
```

```
}
```

```
int left=0; int right=n-1;
```

```
int result=count(arr,left,right); printf("%d",result);
```

```
}
```

Output:

	Input	Expected	Got	
✓	5 1 1 1 0 0	2	2	✓
✓	10 1 1 1 1 1 1 1 1 1 1 1	0	0	✓
✓	8 0 0 0 0 0 0 0 0 0	8	8	✓

a. Majority Element

Aim: Given an array `nums` of size `n`, return *the majority element*.

The majority element is the element that appears more than $\lfloor n / 2 \rfloor$ times. You may assume that the majority element always exists in the array.

Example 1:

Input: nums = [3,2,3]

Output: 3

Example 2:

Input: nums = [2,2,1,1,1,2,2]

Output: 2

Constraints:

$n == \text{nums.length}$

$1 \leq n \leq 5 * 10^4$

$-2^{31} \leq \text{nums}[i] \leq 2^{31} - 1$

Algorithm:

```
int divide(a, l, r, n) {
```

```
// base case: if left index equals right index if l is equal to r {
```

```
return a[l] // return the only element
```

```
}
```

```
initialize mid as (l + r) / 2 // find the middle index
```

```
// recursively divide the array
```

```
initialize min as divide(a, l, mid, n) // find min in left half initialize max as divide(a, mid + 1, r, n) // find max in right half
```

initialize leftc as 0 // counter for min occurrences initialize rightc as 0 // counter for max occurrences

// count occurrences of min and max in the entire array for i from 0 to n - 1 {

if a[i] is equal to min {

increment leftc by 1 // count occurrences of min

} else {

increment rightc by 1 // count occurrences of max

}

}

// check if min occurs more than n/2 times if leftc is greater than (n / 2) {

return min // return min if it is the majority element

} else {

return max // return max otherwise

}

}

int main() {

initialize n // number of elements read n from user

initialize a array of size n // array to hold input values

// read values into the array for j from 0 to n - 1 {


```
read a[j] from user
```

```
}
```

```
initialize l as 0 // left index initialize r as n - 1 // right index
```

```
// call the divide function initialize result as divide(a, l, r, n)
```

```
print result // output the final majority element
```

```
}
```

Program:

```
#include<stdio.h>
```

```
int divide(int a[],int l,int r,int n){ if(l==r)
```

```
{
```

```
return a[l];
```

```
}
```

```
int mid=(l+r)/2;
```

```
int min=divide(a,l,mid,n); int max=divide(a,mid+1,r,n); int leftc=0,rightc=0; for(int i=0;i<n;i++)
```

```
{
```

```
if(a[i]==min)
```

```
{
```

```
leftc++;
```

```
}
```

```
else
```

```

{
    rightc++;
}

}

if(leftc>(n/2))
{
    return min;

}

else
{
    return max;
}

}

int main(){ int n;

scanf("%d",&n); int a[n];

for(int j=0;j<n;j++){ scanf("%d",&a[j

]);

}

int l=0,r=n-1;

int result=divide(a,l,r,n); printf("%d",result);

}

```

Output:

	Input	Expected	Got	
✓	3	3	3	✓
	3 2 3			

a. Finding Floor Value

Aim: Given a sorted array and a value x , the floor of x is the largest element in array smaller than or equal to x . Write divide and conquer algorithm to find floor of x .

Input Format

First Line Contains Integer n – Size of array

Next n lines Contains n numbers – Elements of an array Last Line Contains Integer x – Value for x

Output Format

First Line Contains Integer – Floor value for x

Algorithm:

```
int large(arr, l, r, x){
```

```
// Base case: if the range is invalid if  $r < l$ 
```

```
return 0 // return 0 when there is no valid element
```

```
// Calculate the middle index  $mid = (l + r) / 2$ 
```

```
// Check if the middle element is equal to  $x$  if  $arr[mid]$  is equal to  $x$ 
```

```
return mid // return the index of  $x$  if found
```

```

// If the middle element is less than x else if arr[mid] < x

// Recursively search in the right half floorIndex = large(arr, mid + 1, r, x)


// Check if a valid floor index is found

if floorIndex is not equal to 0

return floorIndex // return the found index else

return mid // return mid as the largest element less than x


// If the middle element is greater than x, search in the left half else

return large(arr, l, mid - 1, x) // search in the left half


}

Int main()

initialize n // number of elements in the array read n from user


initialize arr of size n // array to hold input values


// Read values into the array for i from 0 to n - 1

read arr[i] from user


initialize l as 0 // left index initialize r as n - 1 // right index

```

initialize x // the value for which we want to find the largest element less than or equal to

x

read x from user

// Call the large function result = large(arr, l, r, x)

// Check the result if result is equal to 0

print x // if no valid element, print x else

print arr[result] // print the largest element less than or equal to x

Program:

```
#include<stdio.h>
```

```
int large(int arr[],int l,int r,int x){ if (r < l) {
```

```
    return 0;
```

```
}
```

```
    int mid=(l+r)/2; if (arr[mid]==x)
```

```
    {
```

```
        return mid;
```

```
    }
```

```
    else if (arr[mid]<x)
```

```
    {
```

```
        int floorIndex=large(arr,mid+1,r,x); if(floorIndex!=0)
```

```
    {
```

```
return floorIndex;

}

else

{

return floorIndex=mid;


}

}

else

{

return large(arr,l,mid-1,x);

}

}
```

```
int main(){ int n;

scanf("%d",&n); int arr[n];

for (int i=0;i<n;i++){ scanf("%d",&arr[i]);

}
```

```
int l=0; int

r=n-1; int x;

scanf("%d",&x); int

result=large(arr,l,r,x); if

(result == 0)

{
```

```
printf( "%d",x);  
  
}  
  
else  
  
{  
  
printf( "%d",arr[result]);  
  
}  
  
}
```

Output:

	Input	Expected	Got	
✓	6 1 2 8 10 12 19 5	2	2	✓
✓	5 10 22 85 108 129 100	85	85	✓
✓	7 3 5 7 9 11 13 15 10	9	9	✓

a. Two Elements Sum to X

Aim: Given a sorted array of integers say arr[] and a number x. Write a recursive program using divide and conquer strategy to check if there exist two elements in the array whose sum = x. If there exist such two elements then return the numbers, otherwise print as "No". Note: Write a Divide and Conquer Solution

Input Format

First Line Contains Integer n – Size of array

Next n lines Contains n numbers – Elements of an array Last Line Contains Integer x – Sum Value

Output Format

First Line Contains Integer – Element1

Second Line Contains Integer – Element2 (Element 1 and Elements 2 together sums to value "x")

Algorithm:

```
int findPairWithSum(arr, left, right, x){

// Base case: if there are no more pairs to check if left >= right

print "No" // No pair found return


// Calculate the sum of the elements at the left and right indices sum = arr[left] + arr[right]


// Check if the sum is equal to x if sum is equal to x

print arr[left] // Print the first element of the pair print arr[right] // Print the second element of the pair return


// If the sum is less than x, move the left index up


if sum < x

findPairWithSum(arr, left + 1, right, x) // Recursive call with increased left index else findPairWithSum(arr, left,
right - 1, x) // Recursive call with decreased right index

}

function main()

initialize n // number of elements in the array read n from user


initialize arr of size n // array to hold input values


// Read values into the array for i from 0 to n - 1
```

read arr[i] from user

initialize x // the target sum value read x from user

// Call the findPairWithSum function findPairWithSum(arr, 0, n - 1, x)

Program:

```
#include <stdio.h>
```

```
void findPairWithSum(int arr[], int left, int right, int x) { if (left >= right) {
```

```
//No pair found
```

```
printf("No\n")
```

```
; return;
```

```
}
```

```
int sum = arr[left] + arr[right];
```

```
if (sum == x){
```

```
// If the pair is found printf("%d\n%d\n", arr[left], arr[right]); return;
```

```
}
```

```
if (sum < x){
```

```
    findPairWithSum(arr, left + 1, right, x);
```

```
}
```

```
else{
```

```
    findPairWithSum(arr, left, right - 1, x);
```

```
}
```

```
}
```

```
int main()
```

```
{ int n; scanf("%d",
```

```
&n); int arr[n];
```

```
for (int i = 0; i < n; i++) { scanf("%d", &arr[i]);
```

```
}
```

```
int x; scanf("%d", &x);
```

```
findPairWithSum(arr, 0, n - 1, x);
```

```
}
```

Output:

	Input	Expected	Got	
✓	4 2 4 8 10 14	4 10	4 10	✓
✓	5 2 4 6 8 10 100	No	No	✓

a. Implementation of Quick Sort

Aim: Write a Program to Implement the Quick Sort Algorithm

Input Format:

The first line contains the no of elements in the list-n The next n lines contain the elements.

Output:

Sorted list of elements

Algorithm:

```
int partition(a, left, right)
```

```
{
```

```
    pivot = right // Choose the last element as pivot i
```

```
    = left - 1 // Index of smaller element
```

```
for j from left to right - 1
```

```
{
```

```
if a[j] < a[pivot]
```

```
{
```

```
i++
```

```
// Swap a[i] and a[j] temp = a[i]
```

```
a[i] = a[j] a[j] = temp
```

```
}
```

```
}
```

```
// Swap a[i + 1] and a[right] temp = a[i + 1] a[i + 1] = a[right]
```

```
a[right] = temp
```

```
return (i + 1) // Return the partition index
```

```
}
```

```
function quick(a, left, right)
```

```
{
```

```
if left < right
```

```
{
```

```
p = partition(a, left, right) // Partition the array
```

```
quick(a, left, p - 1) // Recursively sort the left sub-array quick(a, p + 1, right) // Recursively sort the right
```

sub-array

}

}

int main()

{

initialize n // number of elements read n from user

initialize a of size n // array to hold input values for i from 0 to n - 1

{

read a[i] from user

}

quick(a, 0, n - 1) // Call the quicksort function

// Print the sorted array

for i from 0 to n - 1

{

print a[i]

}

}

Program:

```
#include <stdio.h>
```

```
int partition(int a[], int left, int right) { int pivot = right;
```

```
int i = left-1;
```

```
for (int j = left; j < right; j++) {
```

```
if (a[j] < a[pivot]) { i++;
```

```
int temp = a[i]; a[i] = a[j]; a[j] = temp;
```

```
}
```

```
}
```

```
int temp = a[i + 1]; a[i + 1] =
```

```
a[right]; a[right]
```

```
= temp; return (i
```

```
+ 1);
```

```
}
```

```
void quick(int a[], int left, int right)

{ if (left < right) {

int p = partition(a, left, right); quick(a, left, p - 1); quick(a, p + 1, right);

}

}
```

```
int main()

{ int n; scanf("%d", &n);

int a[n];

for (int i = 0; i < n; i++) { scanf("%d", &a[i]);

}
```

```
quick(a, 0, n - 1);
```

```
for (int i = 0; i < n; i++) { printf("%d ", a[i]);

}

}
```


Output:

	Input	Expected	Got	
✓	5 67 34 12 98 78	12 34 67 78 98	12 34 67 78 98	✓
✓	10 1 56 78 90 32 56 11 10 90 114	1 10 11 32 56 56 78 90 90 114	1 10 11 32 56 56 78 90 90 114	✓
✓	12 9 8 7 6 5 4 3 2 1 10 11 90	1 2 3 4 5 6 7 8 9 10 11 90	1 2 3 4 5 6 7 8 9 10 11 90	✓