## Problems on Numbers - Solved Examples(Set 2)

51. The difference of the squares of two consecutive even integers is always divisible by

A. 3 C. 4 B. 6 D. 7

**Hide Answer** 

<u>Discuss</u>

Notebook

answer with explanation

Answer: Option C

Explanation:

Let the consecutive even integers be n and (n + 2)

difference of the squares

$$=(n+2)^2-n^2$$

$$=(n^2+4n+4)-n^2$$

$$=4n+4$$

= 4(n + 1) which is always divisible by 4

52. Which one of the following numbers is completely divisible by 99?

A. 115909

B. 115919

C. 115939

D. 115929

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answer with explanation

Answer: Option D

Explanation:

If a number is divisible by two co-prime numbers, then the number is divisible by their product also.

If a number is divisible by more than two pairwise co-prime numbers, then the number is divisible by their product also. (<u>read more</u>)

If a number is divisible by another number, then it is also divisible by all the factors of that number. (<u>read more</u>)

We know that  $99 = 9 \times 11$  where 9 and 11 are co-prime numbers. Also, 9 and 11 are factors of 99. Hence,

- (1) If a number is divisible by 9 and 11, the number will be divisible by their product 99 also.
- (2) If a number is not divisible by 9 or 11, it is not divisible by 99

Using <u>divisibility rules</u>, we can find out whether a given number is divisible by another number without actually performing the division.

```
115929 is divisible by both 9 and 11
=> 115929 is divisible by 99
115939 is not divisible by 9
=> 115939 is not divisible by 99
115919 is not divisible by 9
=> 115919 is not divisible by 99
115909 is not divisible by 9
=> 115909 is not divisible by 99
Hence, 115929 is the answer
53. 612×612×612+321×321×321612×612-612×321+321×321=?
A. 933 B. 1000
C. 712 D. 843
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answer with explanation
Answer: Option A
Explanation:
a3+b3=(a+b)(a2-ab+b2)
(read more)
Given Equation is in the form (a3+b3)(a2-ab+b2)
where a=612 and b=321
(a3+b3)(a2-ab+b2)=(a+b)(a2-ab+b2)(a2-ab+b2)=(a+b)
Hence answer =(a+b)=612+321=933
54. How many terms are there in the G.P. 4, 8, 16, 32, ..., 1024?
```

B. 8

A. 9

```
C. 7
                                D. 6
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answer with explanation
Answer: Option A
Explanation:
n<sup>th</sup> term of a geometric progression (GP)tn=arn-1
where tn=n^{th} term, a=the first term, r=common ratio, n
= number of terms (read more)
a=4r=84=2tn=1024
tn=arn-1 \Rightarrow 1024=4 \times 2n-1 \Rightarrow 2n-1=10244=256=28 \Rightarrow 2n-1=28 \Rightarrow n-1=8 \Rightarrow n=8+1=9
55. 123×123+288×288+2×123×288=?
A. 168151 B. 178121
C. 168921 D. 162481
Hide Answer
              | Discuss
Notebook
answer with explanation
Answer: Option C
Explanation:
(a+b)2=a2+2ab+b2
read more...
123×123+288×288+2×123×288=(123+288)2=4112=168921
56. If a number is divided by 6, 3 is the remainder. What is the remainder if the the square of the
number is divided by 6?
```

B. 4

A. 5

C. 3 D. 2 **Hide Answer Discuss Notebook** answer with explanation Answer: Option C Explanation: if the number is divided by 6, 3 is the remainder Therefore, number =6k+3Square of the number =(6k+3)2=36k2+36k+9 [: (a+b)2=a2+2ab+b2] =36k2+36k+6+3=6(6k2+6k+1)+3 Hence, when the square of the number is divided by 6, we get 3 as remainder. 57. In a division, the remainder is 0 when a student mistook the divisor as 12 instead of 21 and obtained 35 as quotient. What is the correct quotient? A. 25 B. 20 C. 15 D. 10 **Hide Answer Discuss Notebook** answer with explanation Answer: Option B Explanation: Let x be the number  $x \div 12 = 35$ , remainder = 0  $=> x=35\times12$ correct quotient =x21=35×1221=5×123=5×4=20

58. 1531×132+1531×68=?

```
A. 306000 B. 306100
C. 306200 D. 306400
Hide Answer
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answer with explanation
Answer: Option C
Explanation:
a(b+c)=ab+ac
(distributive Law)
(read more)
1531×132+1531×68=1531(132+68)=1531×200=306200
59. 100010÷1028=?
A. 10
        B. 100
C. 1000 D. 10000
Hide Answer
            Discuss
Notebook
answer with explanation
Answer: Option B
Explanation:
(am)n=amn=(an)m
am.an=am+n
aman=am-n
read more...
1000101028=(103)101028=10301028=102=100
```

60. 2+22+222+2.22=?

B. 248

A. 246

```
C. 248.12 D. 248.22
Hide Answer
             Discuss
Notebook
answer with explanation
Answer: Option D
61. Which of the following numbers will completely divide (4915–1)?
A. 14 B. 46
C. 8 D. 50
Hide Answer
             Discuss
Notebook
answer with explanation
Answer: Option C
Explanation:
Solution 1
(xn-an)
is completely divisible by (x-a)
for every natural number n
read more...
(4915-1)=(4915-115)
which is divisible by (49 - 1) = 48
Since 8 is a factor of 48, (4915–1)
is also divisible by 8
Solution 2
(xn-an)
is completely divisible by (x+a)
when n is even
read more...
(4915-1)=[(72)15-1]=(730-1)=(730-130)
```

which is completely divisible by (7 + 1) = 8

62. How many even prime numbers are there less than 50? A. 1 B. 15 C. 2 D. 16 Hide Answer **Discuss Notebook** answer with explanation Answer: Option A Explanation: 2 is the only even prime number 63. How many prime numbers are there less than 50? A. 13 B. 14 C. 15 D. 16 **Hide Answer Discuss Notebook** answer with explanation Answer: Option C Explanation: 2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41, 43, 47 are the prime numbers less than 50 64. What is the difference between local value and face value of 7 in the numeral 657903? A. 6993 B. 69993 C. 7000 D. 7 **Hide Answer Discuss Notebook** answer with explanation Answer: Option A Explanation: (Local value of 7) - (Face value of 7) =(7000 - 7) = 699365. 108+109+110+...+202=? A. 14615 B. 14625

C. 14715 D. 14725

**Hide Answer** 

| <u>Discuss</u>

**Notebook** 

answer with explanation

Answer: Option D

Explanation:

# **Solution 1**

# Number of terms of an arithmetic progression

$$n=(l-a)d+1$$

where n = number of terms, a = first term, d = last term, d = common difference

# Sum of first n terms in an arithmetic progression

Sn=n2[2a+(n-1)d]=n2(a+l)

where a = the first term, d = common difference,

 $l=tn=n^{th} term =a+(n-1)d$ 

# (read more)

$$n=l-ad+1=202-1081+1=94+1=95$$
  $Sn=n2(a+l)=952(108+202)=95\times3102=95\times155=14725$ 

#### **Solution 2**

$$1+2+3+\cdots+n$$

$$=\sum_{n=n}^{\infty} n = n(n+1)2$$

# (Reference: Power Series)

$$=(1+2+3+\cdots+202)-(1+2+3+\cdots+107)$$

$$=(202\times2032)-(107\times1082)=(101\times203)-(107\times54)=20503-5778=14725$$

```
66. 23732×999=?
A. 23708268 B. 22608258
C. 22608268 D. 23708258
Hide Answer
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Notebook
answer with explanation
Answer: Option A
Explanation:
23732×999=23732(1000-1)=23732×1000-23732×1=23732000-23732=23708268
please go through speed maths methods to do calculations faster.
67. 123427201-?=568794
A. 123527207 B. 223521407
C. 123527407 D. 122858407
Hide Answer
            <u>Discuss</u>
Notebook
answer with explanation
Answer: Option D
Explanation:
Let 123427201-x=568794
x=123427201-568794=122858407
68. 2210×?=884
A. 23
 B. 25
C. 15
 D. 34
```

# Hide Answer | | Discuss Notebook answer with explanation Answer: Option B Explanation: Let 2210 ×x=884 x=8842210=4421105=3485=25

69. If P and Q are odd numbers, then which of the following is even?

$$A. P + Q$$

B. PQ

C. 
$$P + Q + 1$$

D. PQ + 2

**Hide Answer** 

<u>Discuss</u>

**Notebook** 

answer with explanation

Answer: Option A

Explanation:

The sum of two odd numbers is an even number. (read more)

Hence P + Q is an even number

or

Just take any two odd numbers, say 1 and 3

$$P + Q = 1 + 3 = 4 =$$
an even number  
 $P + Q + 1 = 1 + 3 + 1 = 5 =$ an odd number  
 $PQ = 1 \times 3 = 3 =$ an odd number  
 $PQ + 2 = (1 \times 3) + 2 = 5 =$ an odd number

Hence P + Q is the answer

70. Which of the following numbers will completely divide (319+320+321+322)?
A. 25 B. 16
C. 11 D. 12

```
Hide Answer
             Discuss
Notebook
answer with explanation
Answer: Option D
Explanation:
319+320+321+322=319(1+3+32+33)=319×40=318×3×4×10=318×12×10
which is divisible by 12
71. What is the largest 5 digit number exactly divisible by 94?
A. 99922
                             B. 99924
C. 99926
                             D. 99928
Hide Answer
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Notebook
answer with explanation
Answer: Option A
Explanation:
Largest 5 digit number = 99999
99999 \div 94 = 1063, remainder = 77
Hence largest 5 digit number exactly divisible by 94
= 99999 - 77 = 99922
72. What is the smallest 5 digit number exactly divisible by 94?
A. 10052
                              B. 10054
C. 10056
                              D. 10058
Hide Answer
             Discuss
<u>Notebook</u>
answer with explanation
Answer: Option D
Explanation:
Smallest 5 digit number = 10000
10000 \div 94 = 106, remainder = 36
```

94 - 36 = 58.

i.e., 58 should be added to 10000 to make it divisible by 94. Therefore, smallest 5 digit number exactly divisible by 94

$$= 10000 + 58 = 10058$$

73. 1234 - ? = 4234 - 3361

A. 351 B. 361

C. 371 D. 379

**Hide Answer** 

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**Notebook** 

answer with explanation

Answer: Option B

Explanation:

Let 1234-x=4234-3361

74. 
$$320 \div 2 \div 3 = ?$$

A. None of these B. 53.33

C. 160

D. 106

**Hide Answer** 

<u>Discuss</u>

**Notebook** 

answer with explanation

Answer: Option B

Explanation:

320÷2÷3=160÷3=53.33

or

320÷2÷3=320×12×13=1603=53.33

75. 476\*\*0 is divisible by both 3 and 11. What are the non-zero digits in the hundred's and ten's places respectively?

A. 8 and 5

B. 6 and 5

C. 8 and 2

D. 6 and 2

**Hide Answer** 

| Discuss

**Notebook** 

answer with explanation

Answer: Option A

Explanation:

# References

- 1. Divisibility by 3
- 2. Divisibility by 11

#### **Solution 1**

Just substitute the values in the missing places and apply divisibility rules.

if a=6 and b=2, number = 476620

$$4 + 7 + 6 + 6 + 2 + 0 = 25$$
 which is not divisible by 3

Hence 476620 is not divisible by 3

if a=8 and b=2, number = 476820

$$4 + 7 + 6 + 8 + 2 + 0 = 27$$
 which is divisible by 3

Hence 476820 is divisible by 3

$$4 + 6 + 2 = 12$$

$$7 + 8 + 0 = 15$$

$$15 - 12 = 3$$

Hence 476820 is not divisible by 11

if a=6 and b=5, number = 476650

$$4 + 7 + 6 + 6 + 5 + 0 = 28$$
 which is not divisible by 3

Hence 476650 is not divisible by 3

if a=8 and b=5, number = 476850

$$4 + 7 + 6 + 8 + 5 + 0 = 30$$
 which is divisible by 3

Hence 476850 is divisible by 3

$$4 + 6 + 5 = 15$$

$$7 + 8 + 0 = 15$$

$$15 - 15 = 0$$

Hence 476850 is divisible by 11

So a=8 and b=5 is the answer

#### **Solution 2**

Let the number be 476ab0

```
476ab0 is divisible by 3

=> 4 + 7 + 6 + a + b + 0 is divisible by 3

=> 17 + a + b is divisible by 3 ...(equation 1)

476ab0 is divisible by 11

=> (4+6+b)-(7+a+0) is 0 or divisible by 11

=> 3+(b-a) is 0 or divisible by 11 ...(equation 2)
```

Substitute the values of a and b with the values given in the choices and select the values which satisfies both equation 1 and 2.

```
if a=6 and b=2,

17 + a + b = 17 + 6 + 2 = 25 which is not divisible by 3.

Does not meet equation 1
```

if a=8 and b=2, 17 + a + b = 17 + 8 + 2 = 27 which is divisible by 3.

Meet equation 1

3+(b-a) = 3+(2-8) = -3 which is neither 0 nor divisible by 11

Does not meet equation 2

if a=6 and b=5, 17 + a + b = 17 + 6 + 5 = 28 which is not divisible by 3 Does not meet equation 1

if a=8 and b=5, 17 + a + b = 17 + 8 + 5 = 30 which is divisible by 3 Meet equation 1 3+(b-a) = 3+(5-8) = 0

Meet equation 2

Since these values satisfies both equation 1 and equation 2, this is the answer

76. On dividing 2272 as well as 875 by 3-digit number N, we get the same remainder. What is the sum of the digits of N?

A. 11 B. 10 C. 9 D. 8

**Hide Answer** 

| <u>Disc</u>uss

Notebook

answer with explanation

Answer: Option B

Explanation:

Let  $2272 \div N = a$ , remainder = r

$$=> 2272 = Na + r ...(1)$$

Let  $875 \div N = b$ , remainder = r

$$=> 875 = Nb + r ...(2)$$

(1)-(2)

$$\Rightarrow$$
 2272 - 875 = [Na + r] - [Nb + r]

$$=> 1397 = NA - Nb$$

$$=> 1397 = N(a - b) ...(3)$$

It means 1397 is divisible by N

But  $1397 = 11 \times 127$ 

(References: <u>factors of a number</u>, <u>prime factorization</u>)

You can see that 127 is the only 3 digit number which perfectly divides 1397

$$=> N = 127$$

Sum of the digits of N

$$= 1 + 2 + 7 = 10$$

77. What is the sum of first ten prime numbers?

A. 55

B. 101

C. 130

D. 129

**Hide Answer** 

<u>Discuss</u>

**Notebook** 

answer with explanation

Answer: Option D

Explanation:

(Reference : Prime Numbers)

Required Sum = 
$$2 + 3 + 5 + 7 + 11 + 13 + 17 + 19 + 23 + 29 = 129$$

78. Which f the following numbers is exactly divisible by 11?

A. 499774

B. 47554

## **Hide Answer**

| Discuss

**Notebook** 

answer with explanation

Answer: Option A

Explanation:

Reference: Divisibility by 11 Rule

#### Take 47554

$$4 + 5 + 4 = 13$$

$$7 + 5 = 12$$

$$13 - 12 = 1$$

1 is not divisible by 11

Hence 47554 is not divisible by 11

#### Take 466654

$$4 + 6 + 4 = 14$$

$$6 + 5 = 11$$

$$14 - 11 = 3$$

3 is not divisible by 11

Hence 466654 is not divisible by 11

# Take 4646652

$$4 + 4 + 6 + 2 = 16$$

$$6 + 6 + 5 = 17$$

$$17 - 16 = 1$$

1 is not divisible by 11

Hence 4646652 is not divisible by 11

#### Take 499774

$$4 + 9 + 7 = 20$$

$$9 + 7 + 4 = 20$$

$$20 - 20 = 0$$

We got the difference as 0.

Hence 499774 is divisible by 11

79. What is the sum all even natural numbers between 1 and 101?

A. 5050

B. 2550

C. 5040

D. 2540

#### **Hide Answer**

**Discuss** 

Notebook

answer with explanation

Answer: Option B

Explanation:

Reference 1: Natural Numbers

Reference 2: Arithmetic Progression (AP) and Related Formulas

Required sum = 2 + 4 + 6 + ... + 100

This is an arithmetic progression with

$$a = 2$$

$$d = (4 - 2) = 2$$

$$n=(1-a)d+1=(100-2)2+1=982+1=49+1=50$$

$$2+4+6+\cdots+100=n2(a+1)=502(2+100)=502(102)=50\times51=2550$$

80. A boy multiplies 987 by a certain number and obtained 559981 as his answer. If in the answer both 9 are wrong, but the other digits are correct, then what will be the correct answer?

A. 556581

B. 555681

C. 555181

D. 553681

**Hide Answer** 

Discuss

**Notebook** 

answer with explanation

Answer: Option B

Explanation:

#### Solution 1

The answer is divisible by 987. So we can use hit and trial method to find out the number divisible by 987 from the given choices.

 $553681 \div 987$  gives a remainder not equal to 0

 $555181 \div 987$  gives a remainder not equal to 0

 $556581 \div 987$  gives a remainder not equal to 0

But 555681 ÷ 987 gives 0 as remainder. Hence this is the answer

#### Solution 2

If a number is divisible by two co-prime numbers, then the number is divisible by their product also.

If a number is divisible by more than two pairwise co-prime numbers, then the number is divisible by their product also. (<u>read more</u>)

If a number is divisible by another number, then it is also divisible by all the factors of that number. (<u>read more</u>)

The answer is divisible by 987.

 $987 = 3 \times 7 \times 47$  (prime factorization)

Here 3, 7 and 47 are pairwise co-prime numbers.

Also 3, 7 and 47 are factors of 987. Hence

- (1) If a number is divisible by 3, 7 and 47, the number will be divisible by their product 987 also.
- (2) If a number is not divisible by 3 or 7 or 47, it is not divisible by 987

Using <u>divisibility rules</u>, we can find out whether a given number is divisible by another number without actually performing the division.

556581 is divisible by 3

556581 is not divisible by 7

Hence 556581 is not divisible by 987

555181 is not divisible by 3

Hence 555181 is not divisible by 987

553681 is not divisible by 3

Hence 553681 is not divisible by 987

555681 is divisible by 3

555681 is divisible by 7

555681 is divisible by 47

Hence 555681 is divisible by 987

81. Which one of the following cannot be the square of a natural number?

A. 15186125824

B. 49873162329

C. 14936506225

D. 60625273287

**Hide Answer** 

| <u>Discuss</u>

Notebook

answer with explanation

Explanation:
Square of a natural number cannot end with 7. Hence 60625273287 is the answer
82. 7128+1252=1202+?  A. 6028 B. 1248 C. 2348 D. 7178  Hide Answer    Discuss Notebook answer with explanation  Answer: Option D  Explanation:
?=7128+1252-1202=7128+50=7178
, , , , , , , , , , , , , , , , , , ,
83. 3+32+33+···+38=?  A. 9820 B. 9240  C. 9840 D. 9220  Hide Answer    Discuss Notebook answer with explanation
Answer: Option C
Explanation:
Sum of first n terms in a geometric progression (GP)
$Sn = \left\{ \begin{array}{c c c c c c c c c c c c c c c c c c c $
where $a=$ the first term , $r=$ common ratio, $n=$ number of terms
(read more)
This is a Geometric Progression (GP) where $a = 3$ $r = 323=3$ $n = 8$

Answer: Option D

```
Sn=a(rn-1)r-1 =3(38-1)3-1 =3(6561-1)2 =3×65602=3×3280=9840
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```
84. 73411×9999=?
A. 724836589 B. 724036589
C. 734036589 D. 734036129
Hide Answer
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answer with explanation
```

Answer: Option C

Explanation:

 $73411 \times 9999 = 73411(10000 - 1) = 734110000 - 73411 = 734036589$ 

85. 32+33+34+···+42=?
A. 397 B. 407
C. 417 D. 427
Hide Answer
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Notebook

answer with explanation

Answer: Option B

Explanation:

#### **Solution 1**

# Number of terms of an arithmetic progression

n=(l-a)d+1

where n= number of terms, a= the first term , l= last term, d= common difference

# Sum of first n terms in an arithmetic progression

$$Sn=n2[2a+(n-1)d]=n2(a+l)$$
  
where a = the first term, d= common difference,  
 $l=tn=n^{th}$  term =a+(n-1)d

# (read more)

$$n=(l-a)d+1=42-321+1=10+1=11$$

$$Sn=n2(a+1)=112(32+42)=11\times742=11\times37=407$$

#### **Solution 2**

$$1 {+} 2 {+} 3 {+} \cdots {+} n$$

$$=\sum n=n(n+1)2$$

(Reference: Power Series)

$$=(1+2+3+\cdots+42)-(1+2+3+\cdots+31)$$

$$=(42\times432)-(31\times322)=21\times43-31\times16=903-496=407$$

86. What is the digit in the unit place of the number represented by (795–358)

A. 4 B. 3

C. 2 D. 1

**Hide Answer** 

<u>Discuss</u>

<u>Notebook</u>

answer with explanation

Answer: Option A

Explanation:

Let's first find out the unit digit of 795

795=(74)23×73

Hence, unit digit of 795

= unit digit of  $(74)23 \times \text{unit digit of } 73 \dots (1)$ 

unit digit of (74)23

```
= unit digit of (7 \times 7 \times 7 \times 7)23
= unit digit of (9\times9)23 (\because 7\times7=49 and 9 is the unit digit of 49)
= unit digit of 123 (:: 9 \times 9 = 81 and 1 is the unit digit of 81)
= 1 ...(2)
unit digit of 73
= unit digit of (7 \times 7 \times 7)
= unit digit of (9 \times 7)(\because 7 \times 7 = 49 \text{ and } 9 \text{ is the unit digit of } 49)
= 3 ...(3)(\because 9 × 7 = 63 and 3 is the unit digit of 63)
from (1),(2) and (3),
unit digit of 795=1×3=3 ...(A)
Similarly we can find out unit digit of 358
358=(34)14×32
Hence, unit digit of 358
= unit digit of (34)14 \times unit digit of 32 ...(4)
unit digit of (34)14
= unit digit of (3\times3\times3\times3)14
= unit digit of (9\times9)14(:: 3\times3=9)
= unit digit of 114 (:: 9 \times 9 = 81 and 1 is the unit digit of 81)
= 1 ...(5)
unit digit of 32=9 ...(6)
Hence from (4),(5) and (6),
unit digit of 358=1×9=9 ...(B)
We have already found out that
unit digit of 795=3 (from A)
and unit digit of 358=9 (from B)
Hence, unit digit of (795–358)
= unit digit of 795 - unit digit of 358
= unit digit of [larger number of last digit 3 - smaller number of last digit 9](\because795>358)
= 4 (: 4 is the unit digit when a smaller number of last digit 9 is subtracted from a larger number of
last digit 3. example : 113 - 19 = 94)
87. What is the unit digit in the number represented by 365×659×771
```

A. 1 B. 2

```
C. 3 D. 4
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answer with explanation
Answer: Option D
Explanation:
Let's first find out the unit digit of 365
365=(34)16×3
Hence, unit digit of 365
= unit digit of [(34)16\times3]
= unit digit of [(3\times3\times3\times3)16\times3]
= unit digit of [(9\times9)16\times3] (:: 3×3=9)
= unit digit of [116\times3] (\because 9\times9=81 and 1 is the unit digit of 81)
= 1 \times 3
= 3 ...(A)
unit digit of 659=6 ...(B)(\because unit digit is 6 for all powers of 6)
771=(74)17×73
Hence, unit digit of 771
= unit digit of (74)17 \times unit digit of 73 ----(1)
unit digit of (74)17
= unit digit of (7 \times 7 \times 7 \times 7)17
= unit digit of (9\times9)17(: 7\times7=49 and 9 is the unit digit of 49)
= unit digit of 117(\because 9 \times 9 = 81 \text{ and } 1 \text{ is the unit digit of } 81)
= 1 ...(2)
unit digit of 73
= unit digit of (7 \times 7 \times 7)
= unit digit of (9\times7)(\because 7\times7 = 49 \text{ and } 9 \text{ is the unit digit of } 49)
= 3 ...(3)(: 9 × 7 = 63 and 3 is the unit digit of 63)
Hence from (1),(2) and (3),
unit digit of 771=1×3=3 ----(C)
We have already found out that
unit digit of 365=3 (from A)
unit digit of 659=6 (from B)
```

```
Hence, unit digit in the number represented by 365×659×771
= unit digit of (3\times6\times3)
= unit digit of (8\times3)
(: 3 × 6 = 18 and 8 is the unit digit of 18)
= 4 (\because 8 \times 3 = 24 \text{ and } 4 \text{ is the unit digit of } 24)
88. 112 \times 112 + 88 \times 88 = ?
A. 26218 B. 20328
C. 20288
             D. 24288
Hide Answer
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answer with explanation
Answer: Option C
Explanation:
(a+b)2=a2+2ab+b2(a-b)2=a2-2ab+b2(a+b)2+(a-b)2=2(a2+b2)
(read more)
112 \times 112 + 88 \times 88 = 1122 + 882 = (100 + 12)2 + (100 - 12)2 = 2(1002 + 122) = 2(10000 + 144) = 2 \times 10144 = 20288
89. 9312×9999=?
A. 93110688 B. 93010688
C. 93110678 D. 83110688
Hide Answer
              Discuss
Notebook
answer with explanation
Answer: Option A
Explanation:
9312×9999=9312(10000-1)=93120000-9312=93110688
```

unit digit of 771=3 (from C)

90. 112×112-88×88=?

```
A. 4600 B. 4700
C. 4800 D. 4900
Hide Answer
             <u>Discuss</u>
Notebook
answer with explanation
Answer: Option C
Explanation:
a2-b2=(a-b)(a+b)
(read more)
112×112-88×88=1122-882=(112-88)(112+88)=24×200=4800
91. 1234+123+12-?=1221
A. 148 B. 158
C. 168 D. 178
Hide Answer
             <u>Discuss</u>
Notebook
answer with explanation
Answer: Option A
Explanation:
?=1234+123+12-1221=148
92. A three-digit number 4a3 is added to another three-digit number 984 to give a four digit number
13b7, which is divisible by 11. What is the value of (a + b)?
A. 9
                                             B. 10
C. 11
                                             D. 12
Hide Answer
             Discuss
Notebook
answer with explanation
Answer: Option B
Explanation:
```

(Reference: Divisibility by 11 rule)

=> a + 8 = b ...(1)

13b7 is divisible by 11 => (1 + b) - (3 + 7) is 0 or divisible by 11

Assume that (b - 9) = 0=> b = 9

Substituting the value of b in (1),

$$a + 8 = b$$
  
 $a + 8 = 9$   
 $=> a = 9 - 8 = 1$ 

If 
$$a = 1$$
 and  $b = 9$ ,  
 $(a + b) = 1 + 9 = 10$ 

10 is there in the given choices. Hence this is the answer.

A. 44000 B. 42000

C. 38000 D. 40000

**Hide Answer** 

**Notebook** 

answer with explanation

Answer: Option D

Explanation:

$$(a-b)2=a2-2ab+b2$$

(read more)

```
C. 364 D. 560
Hide Answer
               <u>Discuss</u>
Notebook
answer with explanation
Answer: Option D
Explanation:
12+22+32+\cdots+n2
=\sum n2=n(n+1)(2n+1)6
(read more)
22+42+62+...+142
=(2\times1)2+(2\times2)2+(2\times3)2+\cdots+(2\times7)2
=(22\times12)+(22\times22)+(22\times32)+\cdots+(22\times72)
=22(12+22+32+\cdots+72) = 22[n(n+1)(2n+1)6] = 4[7(7+1)(2\times7+1)6] = 4\times7\times8\times156 = 4\times7\times8\times52 = 2\times7\times16
8 \times 5 = 56 \times 10 = 560
95. The sum of the two numbers is 11 and their product is 24. What is the sum of the reciprocals of
these numbers?
A. 712
 B. 1112
C. 1124
 D. 78
Hide Answer
               Discuss
Notebook
answer with explanation
Answer: Option C
Explanation:
Let the numbers be x
and y Then
x+y=11xy=24
```

A. 559 B. 363

```
Hence,
x+yxy=1124
\Rightarrow1y+1x=1124
96. What is the difference between the place values of two sevens in the numeral 54709479?
                                    B. 699990
A. 699930
C. 99990
                                    D. None of these
Hide Answer
              <u>Discuss</u>
Notebook
answer with explanation
Answer: Option A
Explanation:
Required Difference
= 700000 - 70 = 699930
97. Which of the following numbers completely divides (461+462+463+464)
A. 11 B. 10
C. 9 D. 7
Hide Answer
              Discuss
Notebook
answer with explanation
Answer: Option B
Explanation:
461+462+463+464=461(1+41+42+43)=461(1+4+16+64)=461\times85=461\times5\times17=460\times4\times5\times17=460\times10
20×17=460×10×2×17
Hence this is completely divisible by 10
98. A number when divided by 75 leaves 34 as remainder. What will be the remainder if the same
number is divided by 65?
                                               B. 1
A. 3
C. 6
                                               D. 9
Hide Answer
              Discuss
```

**Notebook** 

answer with explanation

Answer: Option D

Explanation:

Let the number be x

Let  $x \div 75 = p$  and remainder = 34

$$\Rightarrow$$
x=75p+34 $\Rightarrow$ x=(25p×3)+25+9 $\Rightarrow$ x=25(3p+1)+9

Hence, if the number is divided by 25, we will get 9 as remainder

99. The number 7490xy is divisible by 90. Find out (x+y)

A. 4 B. 5

C. 6 D. 7

**Hide Answer** 

Discuss

**Notebook** 

answer with explanation

Answer: Option D

Explanation:

If a number is divisible by two co-prime numbers, then the number is divisible by their product also.(<u>read more</u>)

A number is divisible by 10 if the last digit is 0. (read more)

A number is divisible by 9 if the sum of its digits is divisible by 9.(read more)

10×9=90 where 10 and 9 are co-prime numbers. Hence, if 7490xy

is divisible by 9 and 10, it will also be divisible by 90

Suppose 7490xy is divisible by 10. We know that a number is divisible by 10 if the last digit is 0. Hence y=0

Thus we have the number 7490x0. If this is divisible by 9, 7+4+9+0+x+0 is divisible by 9

 $\Rightarrow$  20+x is divisible by 9 (where x is a digit)

=> x=7

Hence, (x+y)=(7+0)=7

100. What is the smallest 3 digit prime number?

A. 107 C. 102 B. 100D. 101

**Hide Answer** 

<u>Discuss</u>

**Notebook** 

answer with explanation

Answer: Option D

Explanation:

- 1. Prime Numbers
- 2. Divisibility Rules

102 is divisible by 2

=> 102 is not a prime number

100 is divisible by 2

=> 100 is not a prime number.

 $\sqrt{101} < 11$ 

101 is not divisible by the prime numbers 2, 3, 5, 7

Hence 101 is a prime number.

Since 100 is not a prime number, 101 is the smallest 3 digit prime number.

√107<11

107 is also not divisible by the prime numbers 2,3,5,7

Hence 107 is also a prime number.

But the smallest 3 digit prime number is 101