

# Turbulence Modelling

## Peddi Harishteja

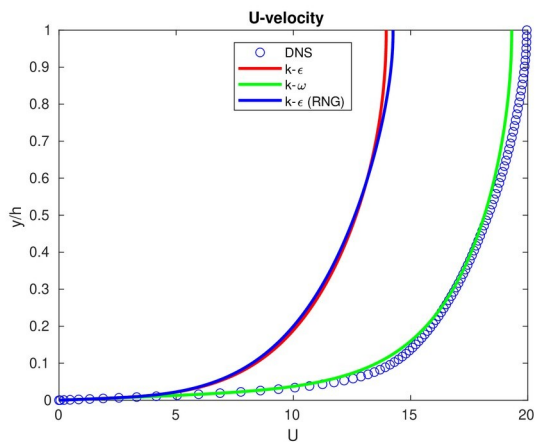
### 1. Boundary Conditions:

At wall, i.e., @y = 0,  $U=0$ ,  $k = 0$ ,  $\epsilon = 2\nu k/(y^2)$

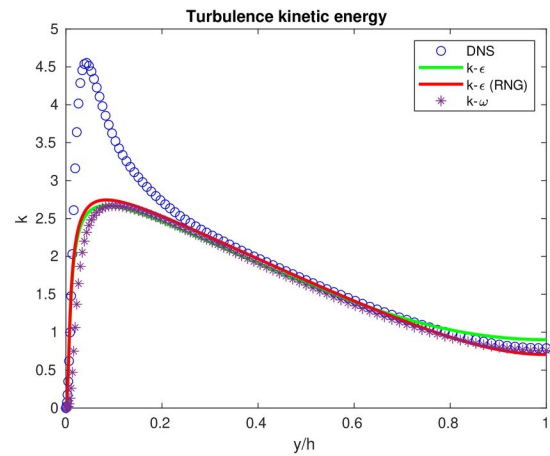
At centreline i.e., @y = 1, Symmetric boundary condition is applied for U,k and  $\epsilon$ .

### 2. Results:

#### A. Velocity:

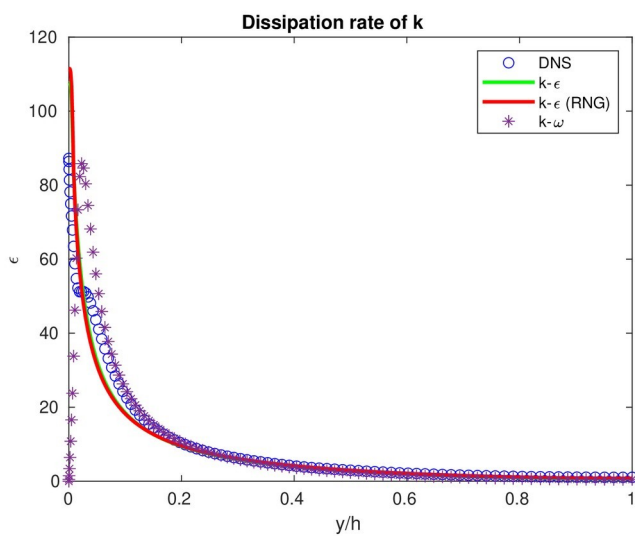


#### B. kinetic energy:

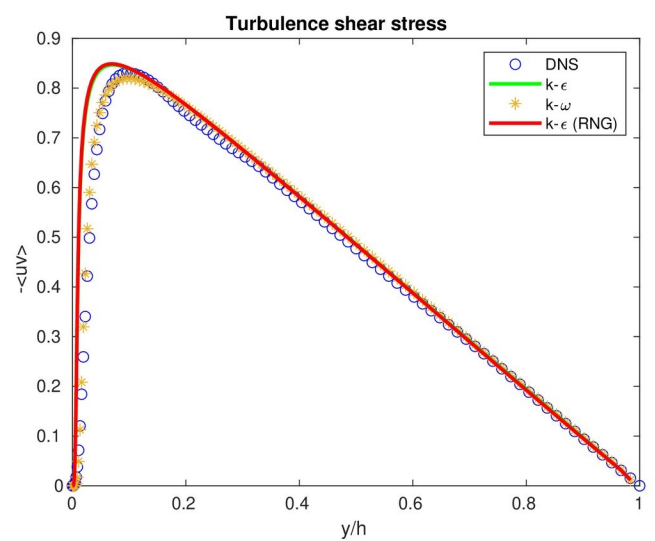


C.

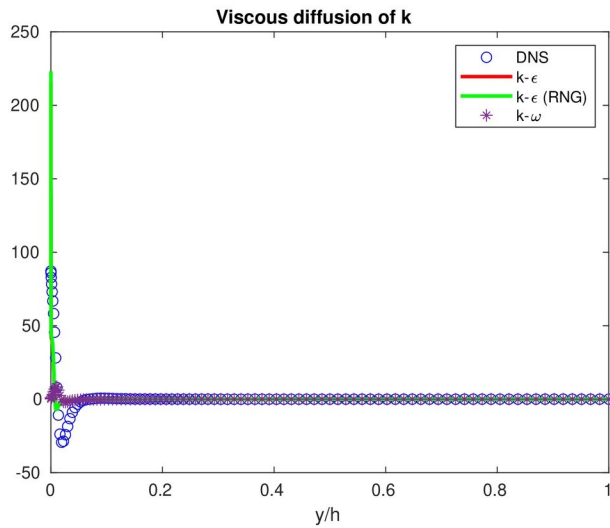
#### C. Dissipation( $\epsilon$ ):



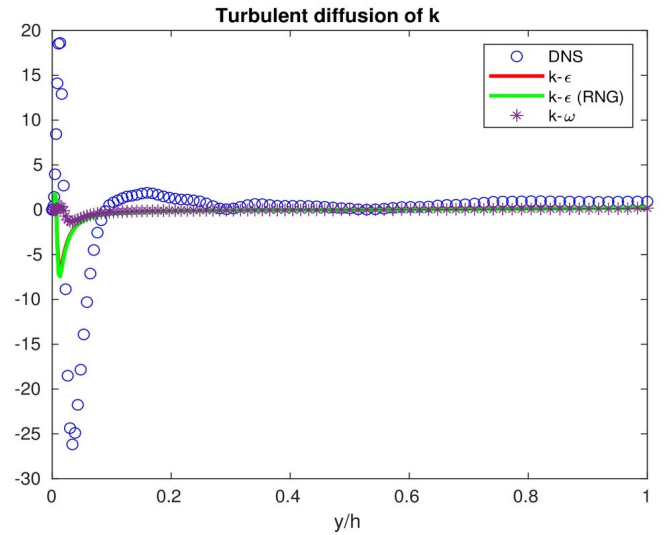
#### D. Turbulent Shear Stress:



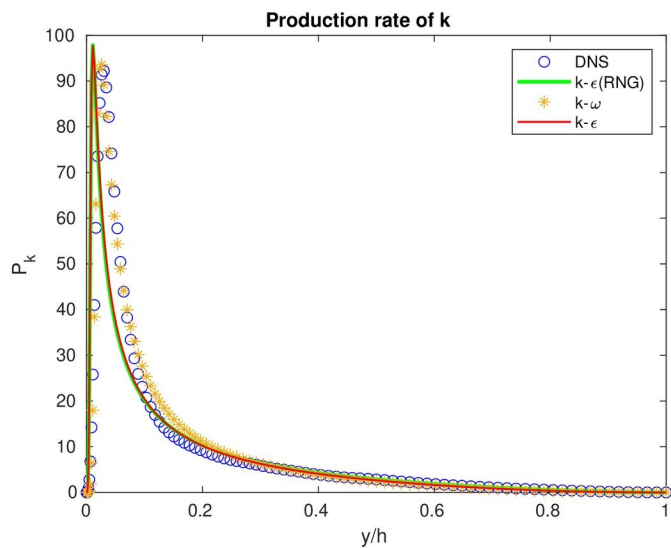
### E. viscous Diffusion of K:



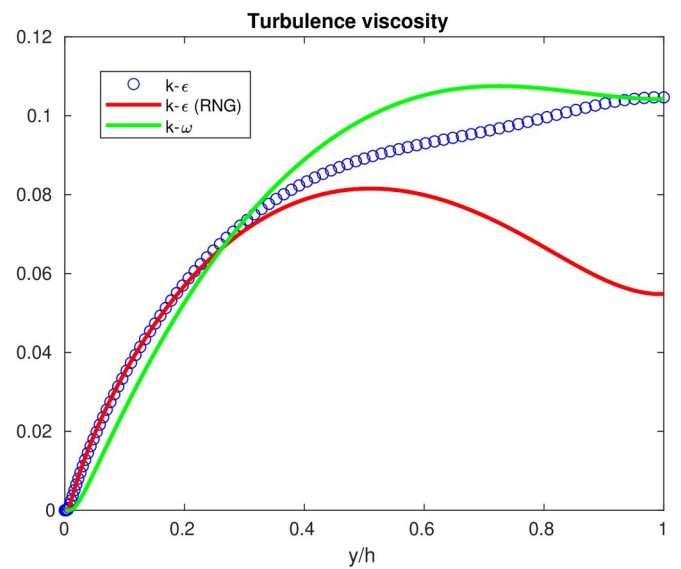
### F. Turbulent Diffusion of K



### G. Production rate of K:

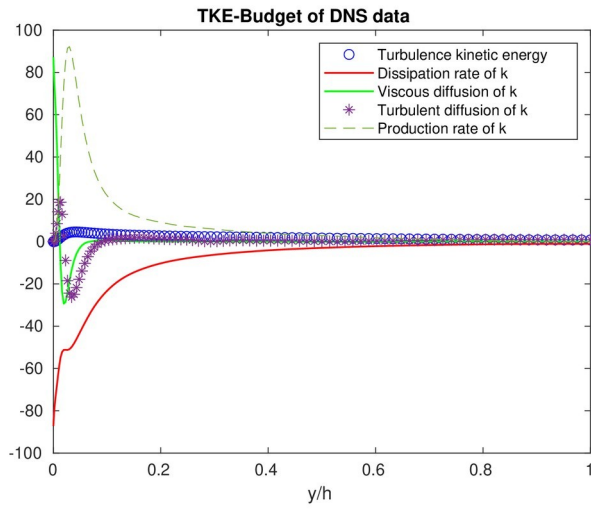


### H. Turbulent viscosity:

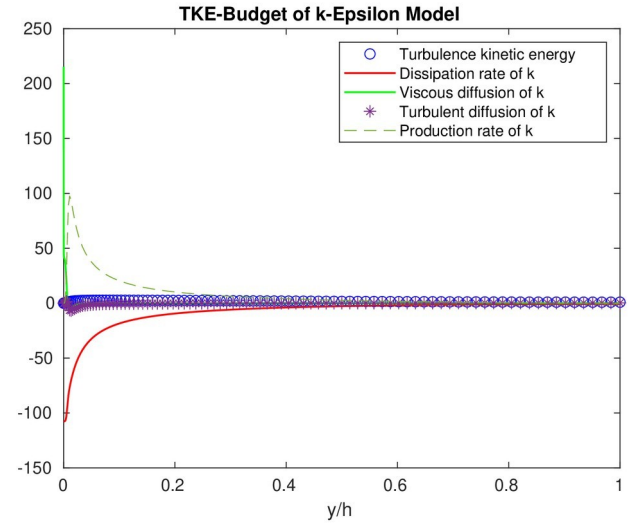


## TKE -Budget:

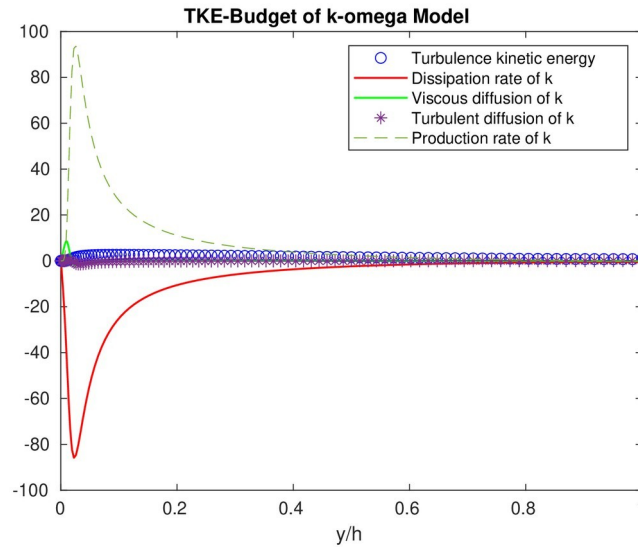
i) DNS



ii) k-epsilon



iii) k-omega



## Boundary Conditions:

- i) velocity=0 at the wall.
- ii) production rate=0 at the wall
- iii) Turbulence Kinetic Energy  $k=0$  at the wall
- iv) Eddy Viscosity  $\nu_t=0$  at the wall
- v) Calculate the wall-normal gradient of velocity using a finite difference method.
- vi)  $\epsilon = 2\nu k/(y^2)$  wall function for  $\epsilon$  for wall-normal distances within a certain range ( $y^+ \leq 3$ ).
- vii) At centreline i.e., @  $y = 1$ , Symmetric boundary condition is applied for  $U, k$  and  $\epsilon$ .

$$\tau_w = -\partial P / \partial x:$$

Given the momentum equation for fully developed flow:

$$0 = (-1/\rho) * (\partial P / \partial x) + \partial [(v + v_t) \partial U / \partial y] / \partial y$$

Integrating the equation from wall to channel centerline (from 0 to  $\delta$ ):

$$\int (-1/\rho) * (\partial P / \partial x) dy + \int \{ \partial [(v + v_t) \partial U / \partial y] / \partial y \} dy = 0$$

Now, we have:

$$(-1/\rho) * (\partial P / \partial x) \delta + [(v + v_t) \partial U / \partial y] \delta = 0 \text{ from } (0 \text{ to } \delta)$$

Given that  $v_t=0$  at the wall ( $y=0$ ) and  $\partial U / \partial y=0$  at the channel axis ( $y=\delta$ ):

$$(1/\rho) * (\partial P / \partial x) = -v [\partial U / \partial y]$$

Given  $\rho=1$  and  $\delta=1$

$$-(\partial P / \partial x) = \tau_w.$$