

Design and Analysis of Algorithms (DAA) ①

Design and Analysis of Algorithms (DAA) ①②

Algorithm? A sequence of logically related instructions to solve a Computational problem

Computational problems

↳ I/P & o/p

✓
I/p: Array A, x

? Does $x \in A$

o/p: Yes/No

↘
I/p: Array A

? Sort A

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Any Algorithm must satisfy (Characteristics)

↳ I/P, o/p

↳ Finiteness! It must terminate after a finite amount of time (1s, 1hr, 1day, 1month)

↳ Definiteness! Each instruction must be unambiguous $\rightarrow \begin{bmatrix} x=5 & \checkmark \\ y=5 & \text{or } -4 \times \end{bmatrix}$

↳ Must involve 1 basic arithmetic instructions!

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①

→ MAX in an integer array

$i = 0$
 $max = A[i]$

For $i = 1$ to n

if $(A[i] > max)$

$max = A[i]$

Return max

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④-⑤

→ MAX in an integer array

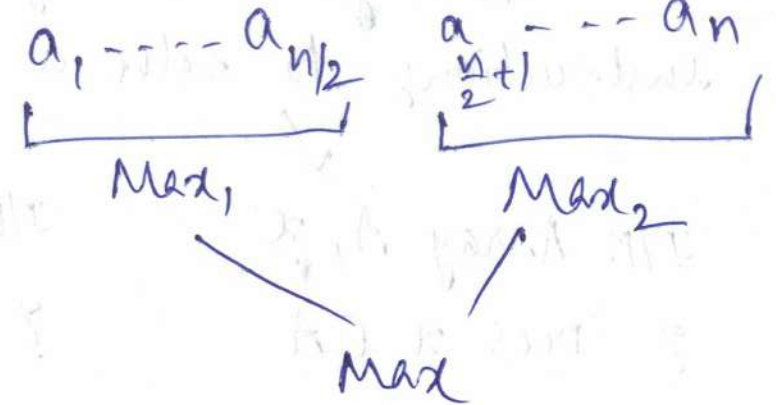
①

```
i = 0
max = A[i]
For i = 1 to n
    if (A[i] > max)
        max = A[i]
Return max
```

②

Sort A
Return A[n]

③



↳ Many approaches (Algorithms)

If the problem is Solvable (There exists an Algorithm)

↳ How many different algorithms are possible.

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⑥

CS



A set of Computational problems

✓
Solvable

(There exist an Algo)

!
unsolvable

(No Algo exist)

Design and Analysis of Algorithms (DAA)

⑥-⑦

CS



A set of Computational problems

Solvable

unsolvable

(There exist an Algo)

(No Algo exist)

↳ How many different
algorithms are possible

↳ How do we Compare Algo

↳ How to pick the best one
(Efficiency)

Design and Analysis of Algorithms (DAA)

⑥-⑦-⑧

CS



A set of Computational problems

Solvable

unsolvable

(There exist an Algo)

(No Algo exist)

↳ How many different
algorithms are possible

↳ How do we Compare Algo

↳ How to pick the best one
(Efficiency)

① Correctness [Is the strategy/Approach/Algorithm
designed performing the intended
task]

② How to measure the time spent / space occupied
(Time Complexity) / (Space Complexity)

③ Optimality A_1 is least $\begin{cases} A_1 - 10s \\ A_2 - 20s \\ A_3 - 30s \end{cases}$

Can we better A_1

Is there an algorithm whose time is $< 10s$

Suppose $A_4 (2s)$; Is A_4 best ever?

Ⓟ