

### Backup Question 1:

Calculate the following parameters for Al (FCC,  $a=4.05$ ):

The number of atoms per unit cell.

The nearest neighbor distance.

The atomic radius  $r$ .

The surface density.

The volume density of atoms in the crystal.

The packing factor of the crystal.

Solution 1:

1. Number of Atoms per Unit Cell:

$$\text{Number of atoms per unit cell} = 8 \cdot \frac{1}{8} + 6 \cdot \frac{1}{2} = 1 + 3 = 4$$

2. Nearest Neighbour Distance:

In an FCC structure, the nearest neighbours are located along the face diagonals. The face diagonal can be calculated as:

The nearest neighbor distance  $d_{nn}$  is half of the face diagonal:

$$\text{Nearest Neighbour Distance, } d_{nn} = 2.86 \text{ \AA}$$

3. Atomic Radius,  $r$ :

$$r = d_{nn}/2 = 2.86/2 \text{ \AA} = 1.43 \text{ \AA}$$

4. Surface Density on the (100) Plane:

$$\text{Number of atoms per surface} = 1 + 4 \cdot \frac{1}{4} = 2$$

$$\text{Area} = a^2 = 4.05^2 = 16.4 \text{ \AA}^2$$

$$\text{Surface Density} = \text{Number of atoms on the plane} / \text{Area of the plane} = 2/16.4 = 0.122 \text{ atoms/\AA}^2$$

5. Volume Density:

$$\begin{aligned} \text{Volume Density} &= \text{Number of atoms in the unit cell} / \text{Volume of the unit cell} = 4/a^3 = 4/4.05^3 \\ &= 4/6.64 \cdot 10^{(-23)} = 6.02 \cdot 10^{(22)} \text{ atoms/cm}^3 \end{aligned}$$

6. Packing Factor:

$$\text{Packing Factor} = \text{Volume occupied by atoms in the unit cell} / \text{Volume of the unit cell}$$

$$\text{Volume occupied by the atoms in the unit cell} = 4 \cdot$$

$$\text{Packing Factor} = 0.735$$

### Backup Question 2:

Calculate the following parameters for W (BCC,  $a=3.165$ ):

The number of atoms per unit cell.

The nearest neighbor distance.

The atomic radius  $r$ .

The surface density.

The volume density of atoms in the crystal.

The packing factor of the crystal.

Solution 1:

1. Number of Atoms per Unit Cell:

$$\text{Number of atoms per unit cell} = 8 \cdot \frac{1}{8} + 1 = 2$$

2. Nearest Neighbour Distance:

In an FCC structure, the nearest neighbours are located along the face diagonals. The face diagonal can be calculated as:

The nearest neighbor distance  $d_{nn}$  is half of the face diagonal:

$$\text{Nearest Neighbour Distance, } d_{nn} = 2.74 \text{ \AA}$$

3. Atomic Radius,  $r$ :

$$r = 1.58 \text{ \AA}$$

4. Surface Density on the (100) Plane:

$$\text{Number of atoms per surface} = 4 \cdot \frac{1}{4} = 1$$

$$\text{Area} = a^2 = 3.165^2 = 10.02 \text{ \AA}^2$$

$$\text{Surface Density} = \frac{\text{Number of atoms on the plane}}{\text{Area of the plane}} = \frac{1}{10.02} = 0.1 \text{ atoms/\AA}^2$$

5. Volume Density:

$$\begin{aligned} \text{Volume Density} &= \frac{\text{Number of atoms in the unit cell}}{\text{Volume of the unit cell}} = \frac{2}{a^3} = \frac{2}{3.165^3} \\ &= 2/3.17 \cdot 10^{(-23)} \text{ cm}^3 = 6.31 \cdot 10^{(22)} \text{ atoms/cm}^3 \end{aligned}$$

6. Packing Factor:

$$\text{Packing Factor} = \frac{\text{Volume occupied by atoms in the unit cell}}{\text{Volume of the unit cell}}$$

$$\text{Volume occupied by the atoms in the unit cell} = 2 \cdot$$

$$\text{Packing Factor} = 0.524$$