

Roll No.: CS23I1027

Name: TERRAGOLAM HARITH



Indian Institute of Information Technology, Design and Manufacturing, Kancheepuram  
Quiz 2 – October 2023

Course Code: MA1000

Course Title: Calculus

Batches: All Batches

Category: Core

Date of Examination: 30.10.2023

Instructors: Dr Sai / Dr Subramani / Dr Vijayakumar

Duration: 1 Hour

Maximum Marks: 25

1. Let  $a$  and  $b$  be positive numbers. Prove that the series  $\sum_{n=1}^{\infty} \frac{1}{an+b}$  diverges. (4)

2. State and prove the ratio test. (4)

3. Determine the values of  $p$  for which the alternating  $p$ -series  $\sum_{n=1}^{\infty} \frac{(-1)^{n+1}}{n^p}$  converges  
(a) absolutely; (b) conditionally. (4)

4. Find the Taylor series of the function  $f(x) = \frac{1}{x}$  about the point  $x = 2$ . Also determine the interval on which this Taylor series converges to  $f(x) = \frac{1}{x}$ . (5)

5. Suppose that the inequalities

$$\frac{1}{2} - \frac{x^2}{24} < \frac{1 - \cos x}{x^2} < \frac{1}{2}$$

hold for values of  $x$  close to zero. Compute

$$\lim_{x \rightarrow 0} \frac{1 - \cos x}{x^2}.$$

Justify your answer. (4)

6. For what values of  $b$  is

$$g(x) = \begin{cases} x, & x < -2 \\ bx^2, & x \geq -2 \end{cases}$$

continuous at every  $x$ . (4)