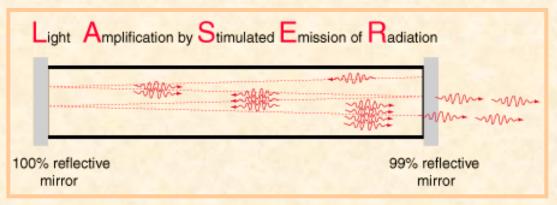
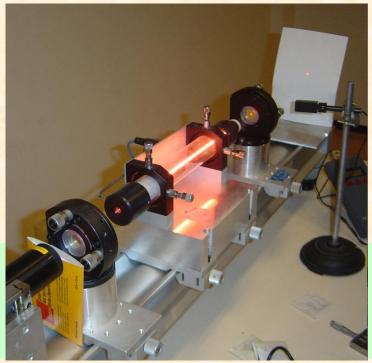
Lasing Principles & Conditions





Distribution of Atoms

Energy Levels: Permitted orbits with specific amount of energy;

- Ground State
- Excited States

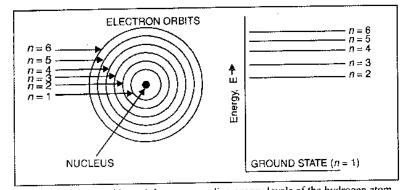


Fig. 1.3. Electron orbits and the corresponding energy levels of the hydrogen atom

■ **POPULATION:** Number of atoms per unit volume that occupy a given energy state (N).

Population of an energy state depends on the temperature T, according to Boltzmann's Equation

 $N = e^{-E/KT}$; where K is the Boltzmann's constant

- ☐ Atoms distributed differently in different energy states;
 - tends to be at lowest possible energy level.

Thermal Equilibrium

At temperature above 0K,

- Atoms alway have some thermal energy;
- Distributed among available energy levels according to their energy.

*At Thermal Equilibrium;

> Population at each energy level decreases with increase of energy level,

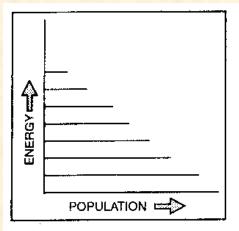


Fig. 1.4. Relative populations of energy levels as a function of energy above the ground state at thermal

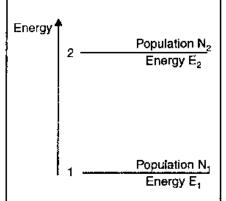


Fig. 1.5. Two energy level system.

For energy levels E_1 and E_2 ,

Populations can be computed with Boltzmann's equation

$$N_1 = e^{-E_1/KT}$$
 & $N_2 = e^{-E_2/KT}$

• Ratio of populations, N_2/N_1 is called *Relative Population*.

$$\frac{N_2}{N_1} = e^{-(E_2 - E_1)/KT}$$

or
$$N_2 = N_1 e^{-\Delta E/KT}$$
 ; $\Delta E = E_2 - E_1$

- **Relative Population** (N_2/N_1) ; dependent on two factors
 - \gt Energy difference (E₂-E₁)
 - > Temperature, T
- * At Lower Temperature; All atoms are in the ground states.
- * At higher Temperature; Atoms move to higher states

- In a material at thermal equilibrium, more atoms are in the lower energy state than in the higher energy state.
 - > The fraction of excited atoms would be large, if the energy levels are close or temperature is very high.

In limiting case,

- \square When, $E_2 E_1 \rightarrow 0$; $N_2 = N_1$
- \square When, $T \rightarrow \infty$; $N_2 = N_1$

Important Conclusion:

As long as the material is in thermal equilibrium, the population of the higher state cannot exceed the population of lower states.

Excitation and De-excitation

Excitation: Electron in the ground state receives an amount of energy equal to the difference of energy of ground state and one of the excited states, absorbs energy and jumps to the excited state.

- Photons of energy $hv = (E_2 E_1)$ induce electron transitions from energy level E_1 to E_2
 - ⇒ Induced or Stimulated Absorption

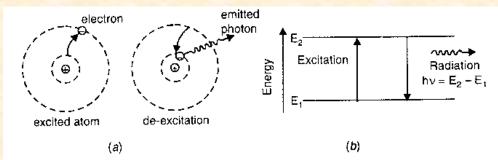
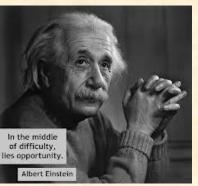


Fig. 1.6. (a) Absorbing energy, electron jumps from an inner orbit to an outer orbit. When the electron returns to the inner orbit, it emits the same energy in the form of a photon. (b) energy level representation of excitation and deexcitation of the atom

- Electron cannot stay in the excited state for a longer time.
- Has to get rid of the excess energy in order to come to the lower energy level.
 - > Only mechanism is through emission of a photon.

<u>De-excitation</u>: The excited electron emits a photon of energy, $hv = (E_2 - E_1)$ and jumps from excited state to the ground state \Rightarrow **Spontaneous Emission**



Einstein's Prediction

- □ 1917, Einstein predicted that there must be second emission process to establish thermodynamic equilibrium.
- Atoms move to excited state under action of incident light
- Excited atoms tend to return randomly to the lower energy state.
- It is likely that a stage may be reached when all atoms are excited
 - > Violation of thermal equilibrium condition
- **❖** Einstein suggested ⇒ There could be an additional emission mechanism, by which the excited atoms can make downward transitions.
 - ➤ Predicted that the photons in the light field induce the excited atoms to fall to lower energy state and give up their excess energy in the form of photons.

Stimulated Emission

Three Processes

A medium consisting of identical atoms in thermal equilibrium having;

- Energy levels E₁ and E₂
- Population N₁ and N₂

(a) Absorption

Atoms in the lower energy level E_1 absorb the incident photon and jumps to the excited state E_2

$$A + h\nu \rightarrow A^*$$

> Induced or Stimulated absorption

Rate of absorption

$$\mathbf{R}_{abs} = \mathbf{B}_{12} \, \rho(\mathbf{v}) \, \mathbf{N}_1$$

 N_1 - population at lower level E_1 , $\rho(v)$ - energy density of incident light

B₁₂ - constant of proportionality; *Einstein coefficient for induced absorption*.

 \triangleright Indicate the probability of an induced transition from level $1 \rightarrow 2$

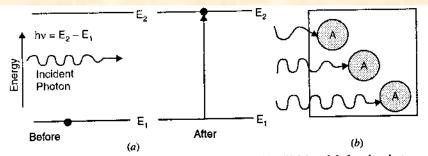


Fig. 1.7. Absorption process (a) Induced absorption (b) Material absorbs photons.

(b) Spontaneous Emission

- An excited atom can stay in excited level for an average lifetime τ_{sp} , it is not stimulated by any other agent during this short stay.
- Excited atom undergoes a transition to the lower energy level at its own by giving excess energy in the form of a photon

$$A^* \rightarrow A + h\nu$$

⇒ Spontaneous Emission

Rate of Spontaneous transitions

$$\mathbf{R}_{\mathrm{sp}} = \mathbf{A}_{21} \; \mathbf{N}_2$$

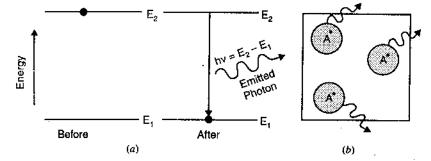


Fig. 1.8. Spontaneous emission process (a) emission (b) Material emits photons haphazardiy.

- A₂₁ *Einstein coefficient for Spontaneous emission* and is a function of frequency and properties of the material.
 - \triangleright Probability of a spontaneous transition from level 2 \rightarrow 1

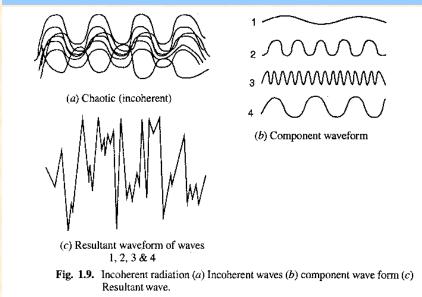
$$A_{21} = 1/\tau_{sp}$$
; τ_{sp} - the lifetime of spontaneous emission

Important Features:

- No outside control
- Probabilistic in nature
- Incoherent Light
- Not monochromatic
- Lack of directionality

Incoherent Radiation:

 Results from superposition of wave trains of random phases.



Net intensity is proportional to the number of radiating atoms

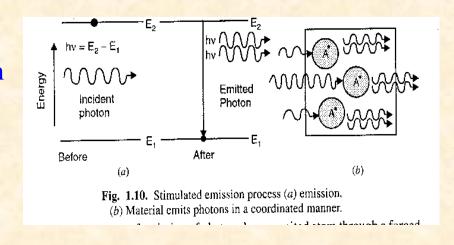
$$I_{Total} = N I$$

> Dominates in conventional light sources.

(c) Stimulated Emission

- An atom in excited state need not to "wait" for spontaneous emission to occur.
- If a photon with appropriate energy ($hv = E_2 E_1$) interacts with excited atom, it can trigger the atom to undergo transition to the lower energy level and to emit another photon.
- Process of emission of photons by an excited atom through a forced transition occurring under the influence of an external agent is called Induced or Stimulated emission.

$$A^* + hv = A = 2 hv$$

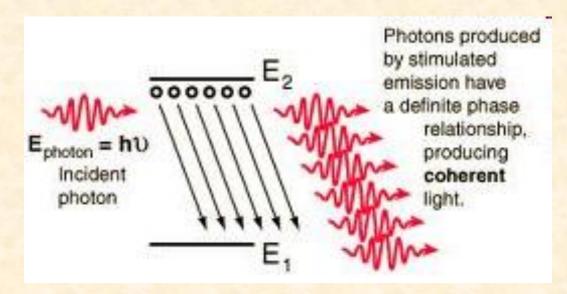


Rate of stimulated emission

 $\mathbf{R}_{st} = \mathbf{B}_{21} \, \rho(\mathbf{v}) \, \mathbf{N}_2$; $\mathbf{B}_{21} - Einstein \ coefficient \ for \ Stimulated \ emission$

Important Features:

- Controllable from outside
- Emitted photon propagates in same direction as that of stimulating photon.
- Have exactly same frequency, phase and plane of polarization.
- Light produced is directional, coherent and monochromatic.



Light Amplification

- Multiplication of photons
- All in phase and travel in same direction
 - > All the coherent waves interfere constructively.
 - > Resultant amplitude is continuously growing.
 - > Result is amplified light.

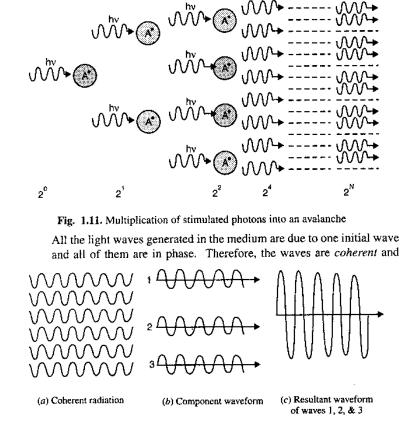


Fig. 1.12. Coherent radiation (a) coherent waves (b) component wave form (c) Resultant wave

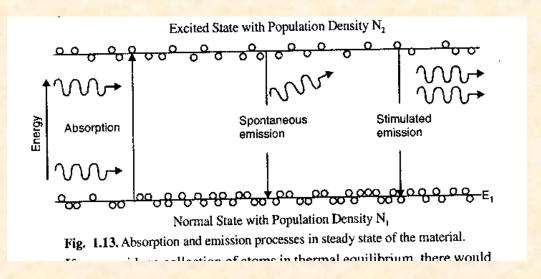
High Intensity

 Because of constructive interference of waves, net intensity of the resultant light is proportional to square of the number of atoms emitting light

$$I_{Total} = N^2 I \implies$$
 High intensity light

Steady State Condition

☐ All three processes occur together with a balance between absorption and emission.



*At Thermal Equilibrium

- Spontaneously emitted photons can induce stimulated emission from another excited atom
- It is also likely to be absorbed by lower level atoms.
 - ➤ Higher probability because of larger population of N₁

Einstein Relations

Under thermal equilibrium

■ Mean population N₁ and N₂ in the lower and upper energy levels must remain constant

Condition requires that

■ Number of transitions from $E_2 \rightarrow E_1$ must be equal to the number of transitions from $E_1 \rightarrow E_2$

$$B_{12} \rho(\nu) N_1 = A_{21}N_2 + B_{21}\rho(\nu) N_2$$

$$\rho(\nu) (B_{12} N_1 - B_{21}N_2) = A_{21}N_2$$

$$\rho(v) = \frac{A_{21}N_2}{(B_{12}N_1 - B_{21}N_2)}$$

Dividing both the numerator and denominator on R.H.S. with B₁₂ N₂

$$\rho(v) = \frac{A_{21}/B_{12}}{(N_1/N_2 - B_{21}/B_{12})} \dots (1)$$

As $N_1/N_2 = e^{[E_2-E_1]/KT} = e^{hv/KT}$

$$\therefore \qquad \rho(\nu) = \frac{A_{21}}{B_{12}} \left[\frac{1}{e^{h\nu/kT} - B_{21}/B_{12}} \right]$$

❖ To maintain thermal equilibrium, the system must release energy in the form of EM radiations. Must be identical with black body radiation and be consistent with Planck's radiation law for any value of T.

According to Planck's law

$$\rho(v) = (8\pi h v^3 \frac{\mu^3}{c^3}) \frac{1}{e^{hv/k\Gamma} - 1} \dots (2)$$

 $\mu \rightarrow$ refractive index of medium, $c \rightarrow$ velocity of light in free space

• Energy density $\rho(v)$ derived will be consistent with Planck's law

only if

$$B_{21} = B_{12}$$
 ... (3a)

$$A_{21}/B_{12} = (8\pi h v^3 \mu^3/c^3)$$
 ... (3b)

$$\therefore B_{12} = B_{21} = \frac{c^3}{8\pi h v^3 \mu^3} A_{21} \qquad ...(4)$$

- Equations (3a) and (3b) are known as Einstein relations and Eqn.(4) gives the relationship between A and B coefficients.
- \Leftrightarrow EQN.(3a) \Rightarrow Coefficients for absorption and stimulated emission are numerically equal.
 - ➤ When an atom with two energy levels is placed in the radiation field, the probability for an induced absorption is equal to the probability for a stimulated emission.
- ❖ EQN. (3b) ⇒ Ratio of coefficients of spontaneous versus stimulated emission is proportional to the third power of frequency of radiation.
 - > Difficult to achieve laser action in higher frequency; X-rays.

Conditions for Large Stimulated Emissions

\square Key to Laser Action \rightarrow Existence of Stimulated Emission

- ❖ In practice, absorption and spontaneous emission always occur together with stimulated emission.
- **Determine the conditions under which the number of stimulated emissions can be made larger than other two processes?**

A) Ratio of Stimulated transitions to Spontaneous transitions

$$R_1 = \frac{\text{Stimulated transitions}}{\text{Spon tan eous transitions}} = \frac{B_{21}\rho(\nu)N_2}{A_{21}N_2} = \left(\frac{B_{21}}{A_{21}}\right)\rho(\nu)$$

Using value of $\rho(v)$ from Planck's law, we get

$$R_{1} = \frac{B_{21}}{A_{21}} \left[\frac{8\pi h v^{3} \mu^{3}}{c^{3}} \frac{1}{e^{hv/kT} - 1} \right]$$

From Einstein relations,
$$\frac{B_{21}}{A_{21}} = \frac{B_{12}}{A_{21}} = \frac{c^3}{8\pi h v^3 \mu^3}$$

$$R_{1} = \left(\frac{c^{3}}{8\pi h v^{3} \mu^{3}}\right) \left[\frac{8\pi h v^{3} \mu^{3}}{c^{3}} \frac{1}{e^{hv/kT} - 1}\right] = \frac{1}{e^{hv/kT} - 1}$$

! If we assume $v = 5 \times 10^{14}$ Hz (yellow light) and T=2000K, the value of hv/kT is 11.99.

$$\therefore R_1 = \frac{1}{e^{11.99} - 1} = 6 \times 10^{-6}$$

- > Shows that in the optical region spontaneous emissions dominate over the stimulated emissions.
- For large number of stimulated emissions, the light field density $\rho(\nu)$ present within the material is required to be enhanced.
- B) Ratio of Stimulated transitions to Absorption transitions

$$R_2 = \frac{\text{Stimulated transitions}}{\text{Absorption transitions}} = \frac{B_{21}\rho(\nu)N_2}{B_{12}\rho(\nu)N_1}$$

As,
$$B_{21} = B_{12}$$
 : $R_2 = \frac{N_2}{N_1}$

- At Thermodynamic Equilibrium, $N_2/N_1 <<< 1$
 - ➤ Absorption transitions overwhelm Stimulated transitions ⇒ A photon of light field on hitting a medium has a much higher probability of being absorbed in the ground state than of stimulating an excited atom.
- If on the other hand, $N_2 > N_1$, photons are more likely to cause stimulated emission than absorption.
 - To achieve more stimulated emissions, the population N_2 of the excited state should be made larger than the population N_1 of the lower energy state.
 - ☐ Two conditions to be satisfied for Stimulated emissions to overwhelm the Spontaneous emissions are:
 - Population of excited level should be greater than that at the lower energy level and
 - Radiation density in the medium should be very large.

Condition for Light Amplification

- *A beam of light propagating through a material medium may absorb or produce more photons.
 - Since the probabilities of absorption and stimulated emissions are same, both **attenuation** and **amplification** of the light beam occur simultaneously.
 - > Amplification can predominate only if there are more atoms in the higher level than in the lower level.
- ❖ As the beam travels through the medium, some photons are absorbed due to absorption transitions and some photons are generated due to emission transitions ⇒ Difference will decide loss or gain
- Let 'α' be the absorption coefficient of the medium, the intensity, I after traveling distance 'x' in medium is

$$I = I_0 e^{-\alpha x}$$

⇒ Light intensity decreases exponentially with distance in the medium

■ **Absorption coefficient,** " α " can be related to the difference in populations; (N_1-N_2) of two energy levels by computing the net loss of photons from the light beam, which is the difference between the net rates of absorption and stimulated emission transitions.

$$\alpha = (N_1 - N_2) \frac{B_{12}hv}{v}$$
; $v = c/\mu$ is the velocity of light in medium

- * For a material in thermal equilibrium, $N_1 > N_2$ and α is always positive.
- \square If N_2 is somehow made greater than N_1 , then ' α ' becomes a negative quantity and the relation takes the form

$$I = I_0 e^{(-\alpha)x} = I_0 e^{\gamma x}$$

where γ is referred as the gain coefficient per unit length

➤ Gain coefficient 'γ' is a positive quantity ⇒ implies that the intensity grows exponentially as the light beam travels through the medium. This is clearly Amplification of light.

Gain Coefficient

$$\gamma = (N_2 - N_1) \frac{B_{12}h\upsilon}{v} \Rightarrow$$
 Sommetion for Amplification

' γ ' will be positive if $(N_2-N_1) > 0$, i.e.

$$N_2 > N_1$$

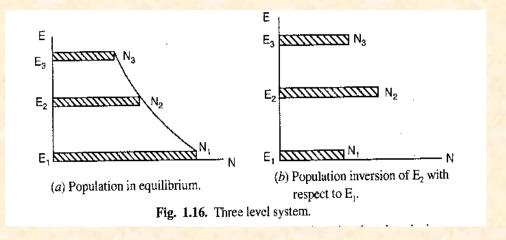
> **Population Inversion**, because it is the inverse of the normal situation.

© Conditions for γ (Gain Coefficient) \Rightarrow Population inversion is a necessary condition to be satisfied for causing the amplification of incident light.

Population Inversion

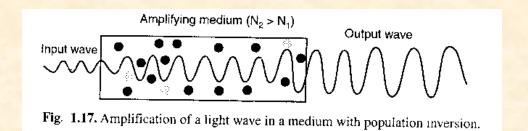
- ☐ Laser operation requires obtaining Stimulated emission exclusively.
 - > To achieve a high percentage of stimulated emission, a majority of atoms should be at the higher energy level than at the lower level.
 - * The non-equilibrium state in which the population N_2 of the upper energy level exceeds to a large extent the population N_1 of the lower energy level is known as the **state of population inversion**.
- Extending the Boltzmann's distribution, to this non-equilibrium state of P.I. $\Rightarrow N_2$ can exceed N_1 only if the temperature be negative.
- The state of P.I. is sometimes referred to as a **negative temperature state**.
 - > Does not mean that we can attain temperatures below absolute zero,
 - > Terminology implies that P.I. is a non-equilibrium state and is attained at normal temperatures.

- * For a system with three energy states E_1 , E_2 and E_3 in equilibrium, the uppermost level E_3 is populated least and the lowest level E_1 is populated most
 - > Since the population in the three states is such that $N_3 < N_2 < N_1$, the system absorbs photons rather than emit photons.
 - If the system is supplied with external energy such that N_2 exceeds $N_1 \Rightarrow$ System reached Population Inversion
 - P.I. taken place between the levels E_2 and E_1 ,



Under P.I. condition, stimulated emission can produce a cascade of light.

- ➤ The first few randomly emitted spontaneous photons trigger stimulated emission of more photons and those stimulated photons induce still more stimulated emissions and so on.
- ➤ As long as $N_2 > N_1$, stimulated emissions are more likely than absorption \Rightarrow light gets amplified.



The moment, the population at lower level becomes equal to or larger than at the excited state, *P.I. ends*, stimulated emissions diminish and amplification of light ceases.

How to achieve P.I.?

- **Pumping:** Process by which atoms are raised from the lower level to the upper level.
- Energy is to be supplied somehow to the laser medium to raise atoms from the lower level to the excited level and for maintaining population at the excited level at a value greater than that of the lower energy.
 - Usual method ⇒ **Heat the material**. Will it do the job?
 - Heating the material only increases the average energy of atoms but does not make N₂ greater than N₁.
 - > P.I. cannot be achieved by heating the material.

Pumping Methods

- To create the state of P.I. \Rightarrow selectively excite the atoms in the material to particular energy levels.
- Most common methods of pumping make use of Light and Electrons.

Optical Pumping

- Use of photons to excite the atoms
 - A light source used to illuminate the laser medium
 - Photons of appropriate frequency excite the atoms to upper levels.
 - Atoms drop to the metastable level to create the state of P.I.
- Optical pump sources: Flash discharge tubes, Continuously operation lamps, Spark gaps or an auxiliary laser.
- Optical pumping is suitable for laser medium- <u>transparent to pump light</u>.
- Mostly used for solid state crystalline and liquid tunable dye lasers.

Electrical Pumping

 Can be used only in case of laser materials that can conduct electricity without destroying lasing activity.

Limited to gases.

- In case of a gas laser, a high voltage pulse initially ionizes the gas so that it conducts electricity.
- An electric current flowing through the gas excites atoms to the excited level from where they drop to the metastable upper laser level leading to **P.I**.

Direct Conversion

- In semiconductor lasers also electrical pumping is used, but here it is not the atoms that are excited. It is the current carriers; {e-h} pairs which are excited and a population inversion is achieved in the junction region.
- Electrons recombine with holes in the junction regions producing laser light.
 - > A direct conversion of electrical energy into light energy

Active Centre & Active Medium

- All types of atoms not suitable for laser operation.
 - > In a medium consisting of different species of atoms, only a small fraction of atoms of a particular species are suitable for stimulated emission and laser action.
 - > Those atoms which cause light amplification are called **Active Centers**.
 - > Rest of the medium acts as host and supports active centers is called an **Active Medium**.
- An active medium is thus a medium which, when excited, reaches the state of population inversion, and eventually causes light amplification.
- Active medium may be a solid, a liquid or a gas.

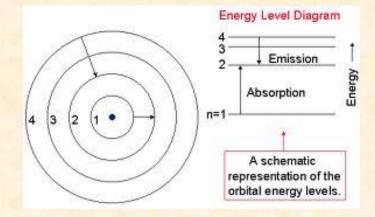
Metastable States

- An atom can be excited to a higher level by supplying energy to it. Normally, excited states have short lifetimes \approx nanoseconds (10⁻⁹ s) and release their excess energy by spontaneous emission.
- Atoms do not stay at such excited states long enough to be stimulated to emit their energy. Though, the pumping agent continuously raises the atoms to the excited level, many of them rapidly undergo spontaneous transitions to the lower energy level \Rightarrow *Population inversion cannot be established*.
- For establishing population inversion, the excited atoms are required to "wait" at the upper lasing level till a large number of atoms accumulate at that level.
- What is needed is an excited state with a longer lifetime?
 - Such longer-lived upper levels from where an excited atom does not return to lower level at once, but remains excited for an appreciable time, are known as **Metastable States**.

- Atoms stay in metastable states for about 10⁻⁶ to 10⁻³s. This is 10³ to 10⁶ times longer than the time of stay at excited levels.
 - ➤ Possible for a large number of atoms to accumulate at a metastable level. The metastable state population can exceed the population of a lower level and lead to the state of population inversion.
- If the metastable states do not exist, there could be no population inversion, no stimulated emission and hence no laser operation.
- ***** Foundation to the laser operation is the existence of metastable states.

Pumping Schemes

- * Atoms characterized by a large number of energy levels.
 - > Only two, three or four levels are pertinent to the pumping process.
 - □ Classified as
 - Two-level,
 - Three-level and
 - Four –level schemes.



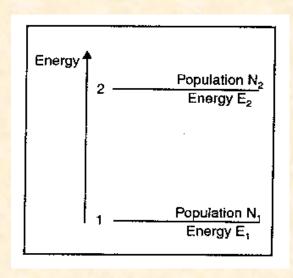
- * Two-level scheme will not lead to laser action.
- ❖ Three-level and four-level schemes are important and are widely employed.

Two Level Pumping Scheme

- Appears to be most simple and straight-forward method to establish population inversion;
 - > Pumping an excess of atoms into the higher energy state by applying intense radiation.
- A two-level pumping scheme is not suitable for attaining P.I.
 - P.I. requires the lifetime Δt of upper level E_2 must be longer.
 - Heisenberg's Uncertainty principle,

$$\Delta E_2$$
 $\Delta t \ge h/2\pi$

 \Rightarrow Smaller ΔE_2 ; the upper energy level must be narrow



Two Energy level system

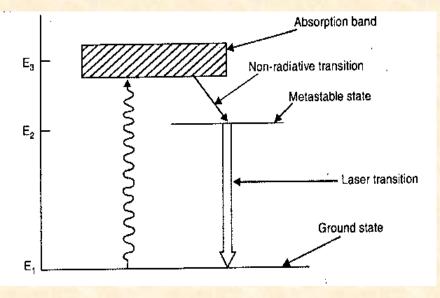
- For such system, to excite atoms, pump source should be highly monochromatic.
 - > In practice, monochromatic source of required frequency may not exist.
 - > Even if it exists, the pumping efficiency would be very low \Rightarrow enough population cannot be excited to level E_2 .
- Further, pumping radiation on one hand excites the ground state atoms and on the other hand induces transitions from the upper level to the lower level.
 - > means that pumping operation simultaneously populates and depopulates the upper level.
- Fig. Hence, P.I. cannot be attained in a two-level scheme. All that it may achieve at best is a system of equally populated levels.

Three Level Pumping Scheme

■ A three level scheme; Lower level is either the ground state or a level whose separation from the ground state is small compared to kT.

E₂-A metastable level

- Atoms accumulate at level E₂
- Build-up of atoms at E₂ continues because of pumping process.
- Population N_2 at E_2 exceeds the population N_1 at E_1 and
 - > P.I. is attained.



Three level Energy diagram

***** A photon of $hv(=E_2-E_1)$ can induce stimulated emission and laser action.

❖ Major disadvantage of a three level scheme ⇒ it requires very high pump powers.

- Terminal level of the laser transition is the ground state.
- As the ground state is heavily populated, large pumping power is to be used to depopulate the ground level to the required extent $(N_2 > N_1)$

Three level scheme can produce light only in Pulses.

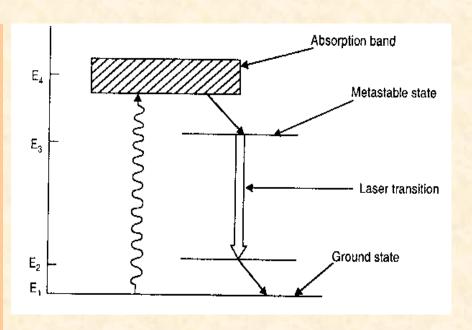
- \triangleright Once stimulated emission commences, the metastable state E_2 gets depopulated very rapidly and the population of the ground state increases quickly. As a result the population inversion ends. One has to wait till the population inversion is again established.
- > Three level lasers operate in Pulsed Mode.

Four Level Pumping Scheme

- In Four level scheme, the terminal laser level E_2 is well above the ground level such that $(E_2-E_1) >> kT$.
 - \triangleright It guarantees that the thermal equilibrium population of E_2 level is negligible.

E₃ - a metastable level

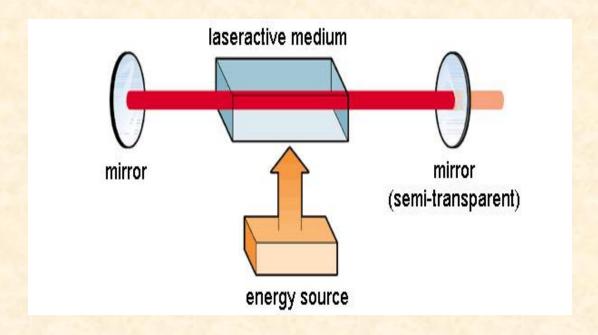
- \triangleright Laser transition takes the atoms to the level E_2
- \triangleright Atoms lose the rest of their excess energy & finally reach the ground state E_{1} .
- > Atoms are once again available for excitation.



Four level Energy diagram

- In contrast to three level scheme, the lower laser transition level in four level scheme is not the ground state and is virtually vacant.
 - It requires less pumping energy than does a three level laser. This is the major advantage of this scheme.
- Further, the lifetime of the lower laser transition level E_2 is much shorter, hence atoms in level E_2 quickly drop to the ground state.
 - ➤ This steady depletion of E₂ level helps sustain the population inversion by avoiding an accumulation of atoms in the lower lasing level.
- Four level lasers can operate in Continuous Wave mode.
- ☐ Most of the working lasers are based on Four Level Scheme

Laser Block Components



Major Components:

- Active medium
- Pumping Source
- Mirrors

Classification of Lasers

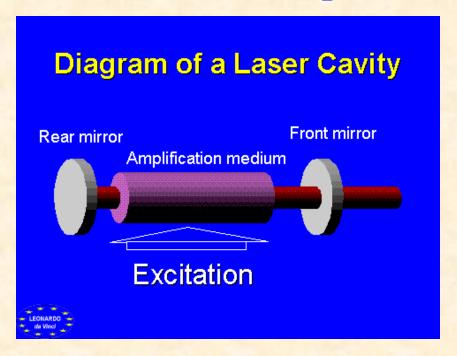
- □ Several ways to classify the different types of lasers
 - What material or element is used as active medium
 - Mode of operation : CW or Pulsed
- □ Classification may be done on basis of other parameters
 - Gain of the laser medium
 - Power delivered by laser
 - Efficiency or
 - Applications

- **Preference to classify the lasers on the basis of material used as Active Medium.**
 - Broadly divided into four categories;
 - Solid lasers
 - Gas lasers
 - Liquid lasers
 - Semiconductor lasers
 - Will discuss some of the important and practical lasers?

Laser Cavity

□ All the lasers comprise of three basic components

- Active medium,
- Excitation source and
- Reflecting mirrors



- Whether Solid State, Liquid or Gas laser, the basic mechanism is same i.e. *Laser Action*
- They differ only in terms of Active medium or Excitation process.

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