

Engineering Optics

Lecture 6

by

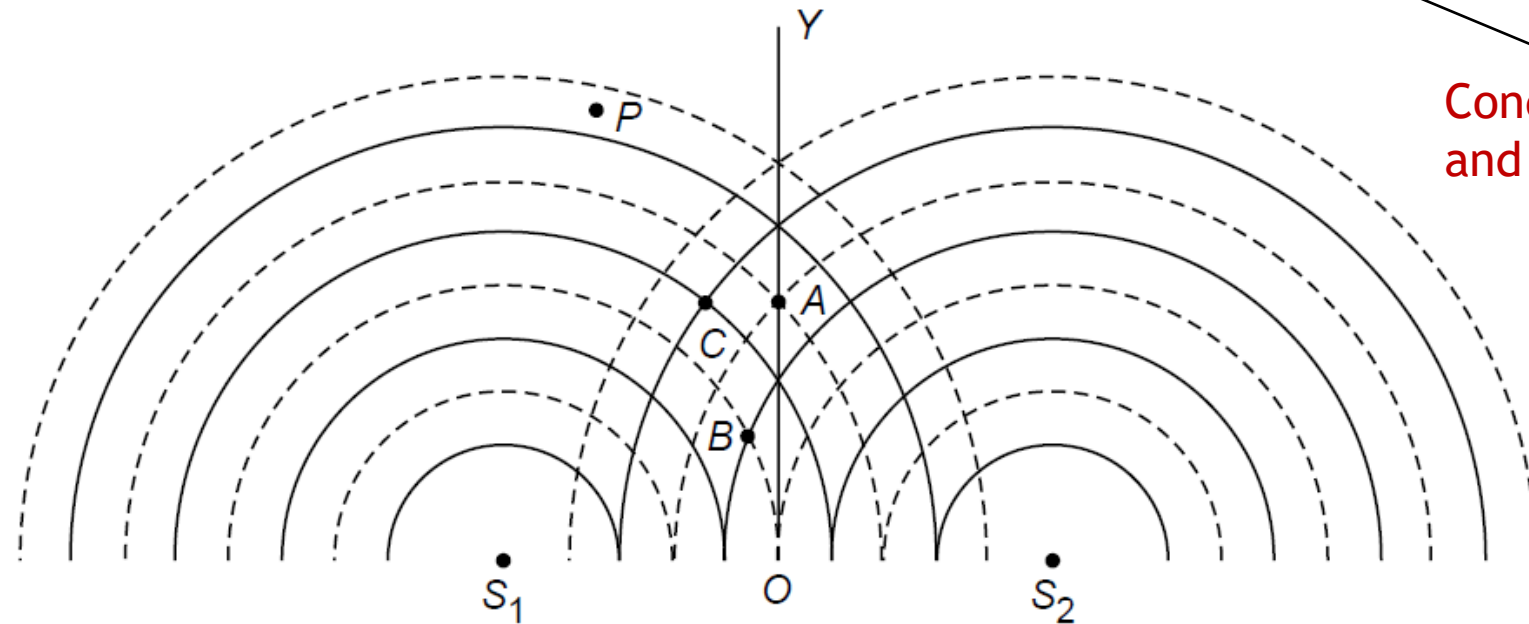
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Interference between two waves e.g. on *surface of water*

Example-1: when the sources are vibrating in phase

Refer. '14.2 INTERFERENCE PATTERN PRODUCED ON THE SURFACE OF WATER'



Conditions for maxima
and minima?

Waves emanating from two point sources S_1 and S_2 vibrating in phase. The solid and the dashed curves represent the positions of the crests and troughs, respectively.

Answer

at A

$$y = y_1 + y_2 \\ = 2a \cos \omega t$$

$$S_2C - S_1C = \lambda$$

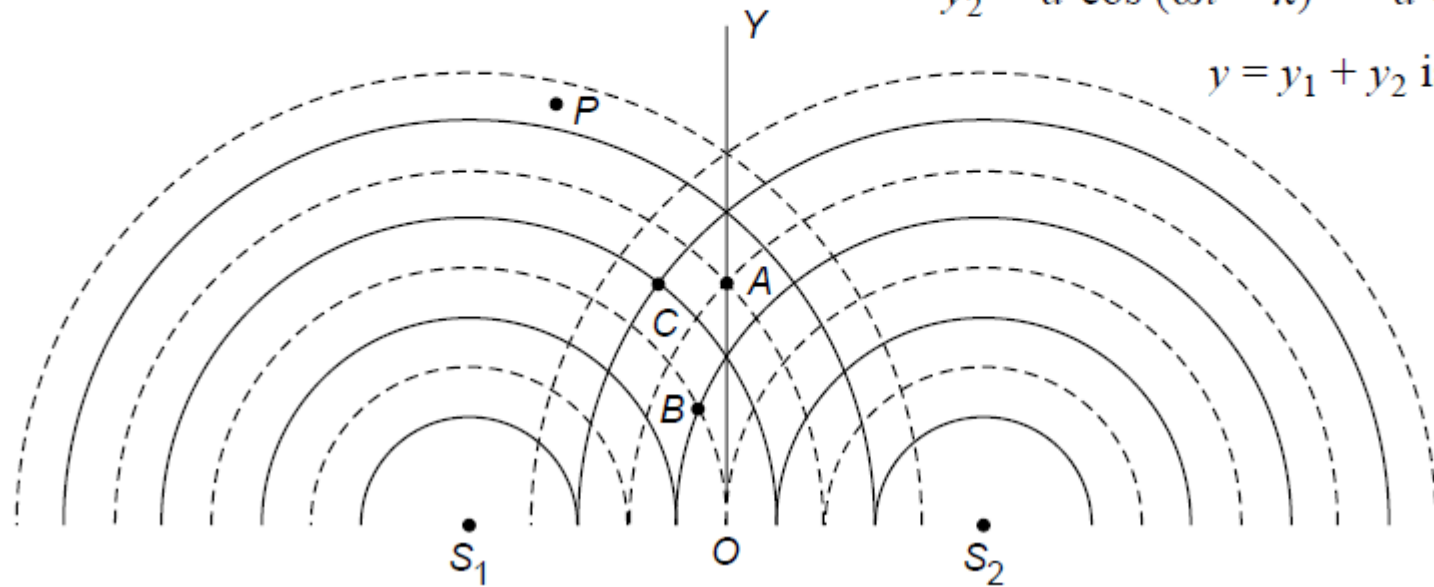
$$S_2P \sim S_1P = n\lambda \quad (\text{maxima})$$

$$S_2B - S_1B = \lambda/2$$

$$y_1 = a \cos \omega t$$

$$y_2 = a \cos (\omega t - \pi) = -a \cos \omega t$$

$y = y_1 + y_2$ is zero at all times.

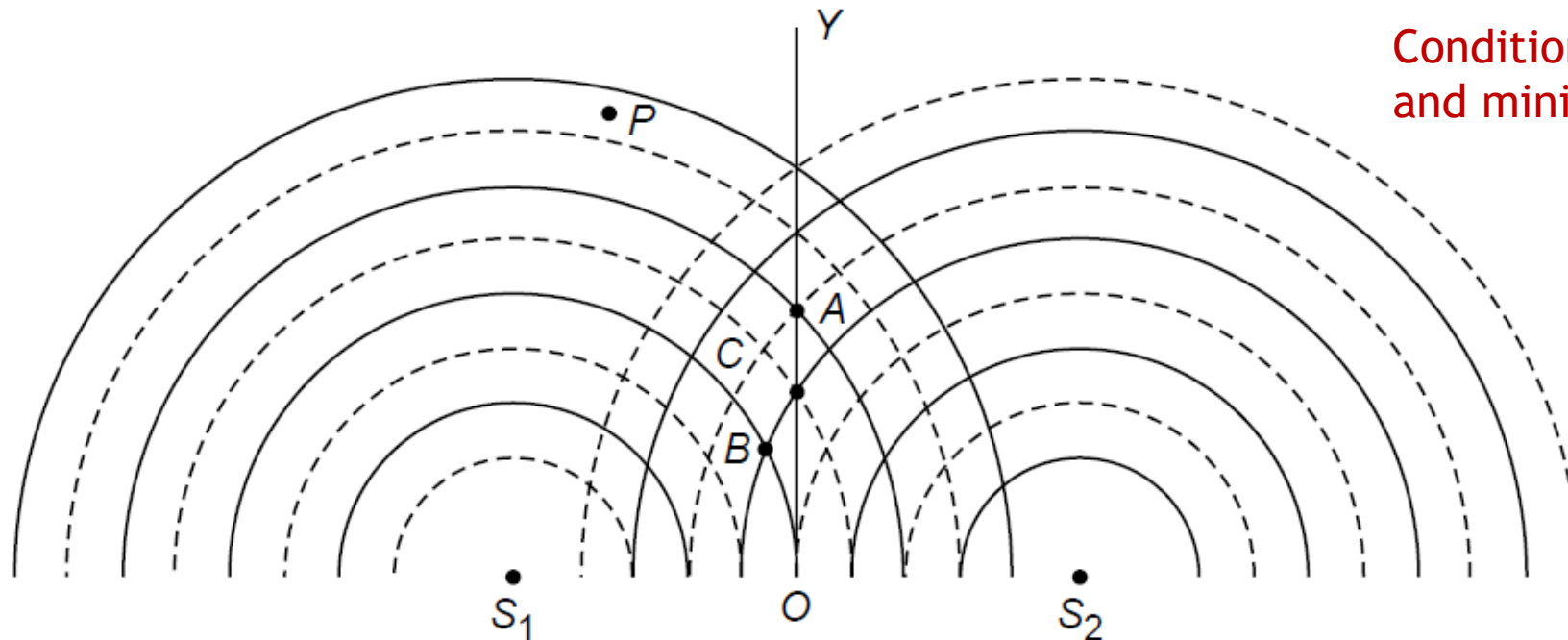


$$S_2P \sim S_1P = n\lambda \quad (\text{maxima})$$

$$S_2P \sim S_1P = \left(n + \frac{1}{2}\right)\lambda \quad (\text{minima})$$

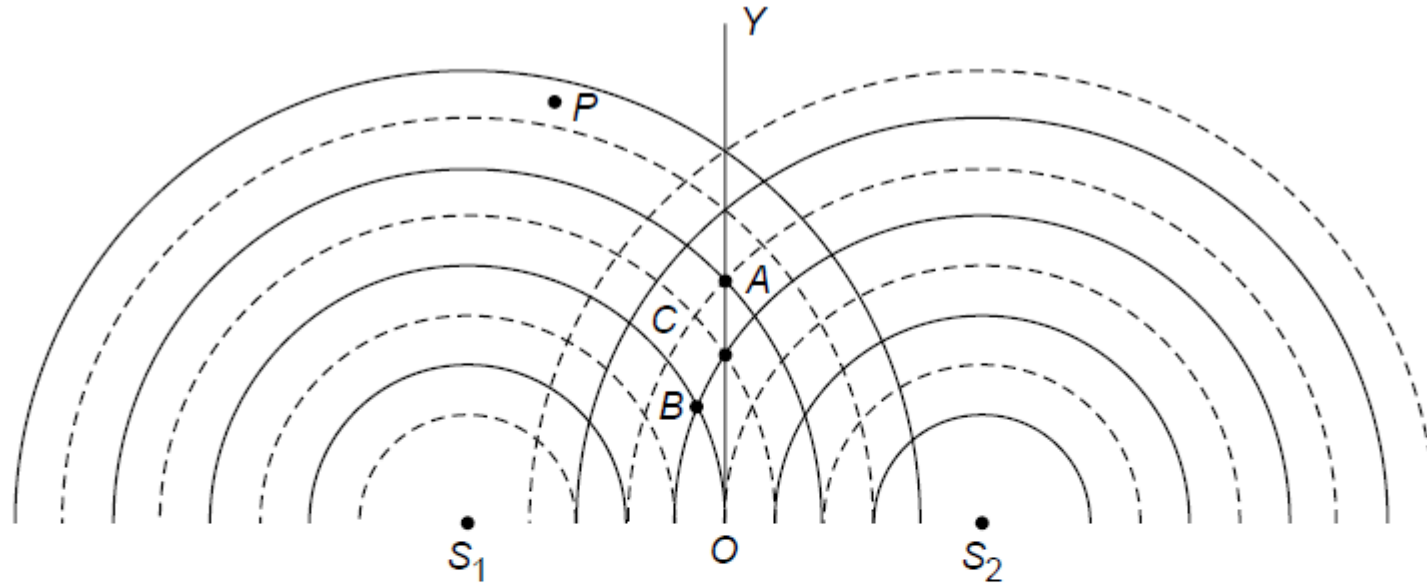
Interference between two waves

- ▶ Example-2: when the sources are vibrating out of phase
- ▶ Refer. '14.2 INTERFERENCE PATTERN PRODUCED ON THE SURFACE OF WATER'



Conditions for maxima
and minima?

Waves emanating from two point sources S_1 and S_2 vibrating out of phase.



Waves emanating from two point sources S_1 and S_2 vibrating out of phase.

$$S_2B - S_1B = \lambda/2$$

$$S_2P \sim S_1P = \left(n + \frac{1}{2}\right)\lambda \quad (\text{maxima})$$

$$S_2P \sim S_1P = n\lambda \quad (\text{minima})$$

Coherence: constant phase relationship

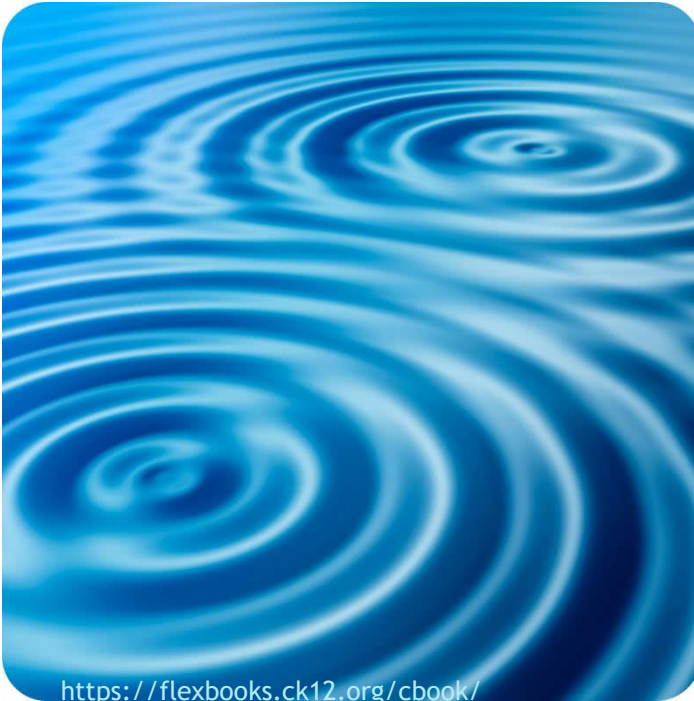
- ▶ Whenever the phase difference is constant, a stationary interference pattern is produced.
- ▶ The positions of the maxima and minima \rightarrow depend on the phase difference
- ▶ Two sources which vibrate with a fixed phase difference between them are said to be **coherent**.

Constantly changing phase

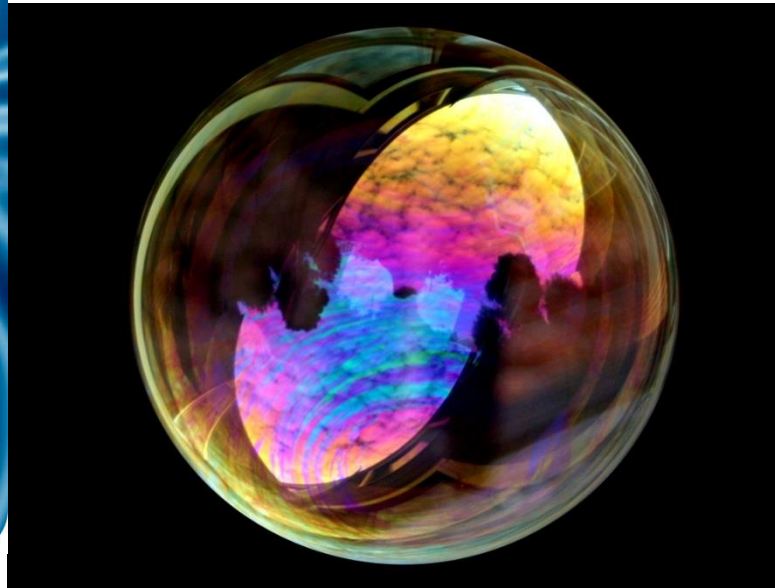
- ▶ Changing phase difference → sometimes in phase, sometimes out of phase,
- ▶ No stationary interference can be observed,
- ▶ sources are said to be **incoherent**

Interference

Superposition of waves → resultant wave



<https://flexbooks.ck12.org/cbook/ck-12-physics-flexbook-2.0/section/11.5/primary/lesson/wave-interference-ms-ps>



Soap bubble

https://simple.wikipedia.org/wiki/Interference#/media/File:Soap_bubble_sky.jpg



Oil on water

https://simple.wikipedia.org/wiki/Interference#/media/File:Soap_bubble_sky.jpg

Few points to note

- ▶ The wave theory for EM nature of light provides a natural basis from which to proceed.
- ▶ As we have seen, it obeys the important Superposition Principle.
- ▶ The resultant electric-field intensity \mathbf{E} , at a point in space where two or more lightwaves overlap, is equal to the vector sum of the individual constituent disturbances.
- ▶ Optical interference corresponds to the interaction of two or more lightwaves yielding a resultant irradiance that deviates from the sum of the component irradiances.
- ▶ After being superimposed, the individual waves separate and continue on, completely unaffected by their previous encounter.

Question:

- ▶ If you use two conventional light sources (such as two sodium lamps) illuminating two pinholes, will you observe interference pattern on the screen?

- ▶ Each atom emitting light for about 10^{-10} s, i.e., light emitted by an atom is essentially a pulse lasting for only 10^{-10} s.
- ▶ such a short pulse consists of about 1 million oscillations;
- ▶ Even if the atoms were emitting under similar conditions, waves from different atoms would differ in their initial phases.
- ▶ Consequently, light coming out from S1 and S2 will have a fixed phase relationship for about 10^{-10} s, if any
- ▶ Interference pattern will keep on changing every billionth of a second.
- ▶ The eye can notice intensity changes which last at least for 0.1 s, and hence we will observe a uniform intensity.
- ▶ If we have a camera whose time of shutter opening can be made less than 10^{-10} s, then the film will record an interference pattern.
- ▶ light beams from two independent sources do not have any fixed relationship, as such, they do not produce any stationary interference pattern.

Thank You