

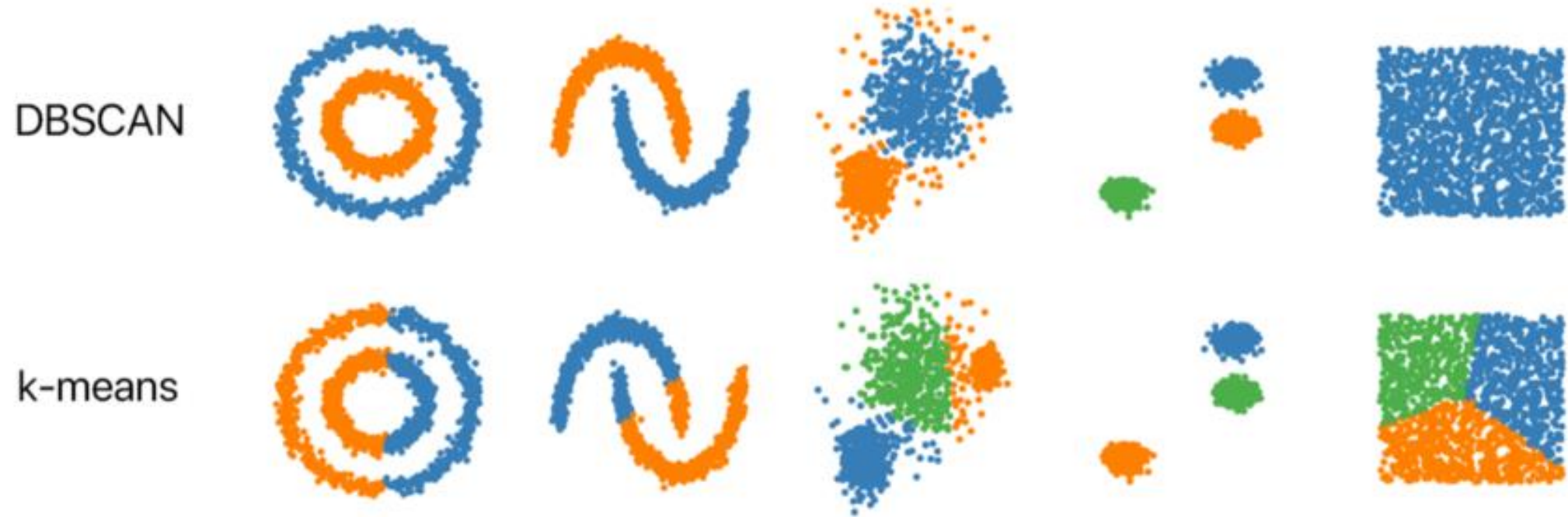
DBSCAN(Density-Based Spatial Clustering of Applications with Noise)

DBSCAN does not need to specify the number of clusters ;

can automatically detect the number of clusters based

DBSCAN can find arbitrary shape clusters that k-means are not able to find

DBSCAN can handle noise and outliers better



Some parameters used by DBSCAN

**Eps:** Maximum radius of the neighborhood

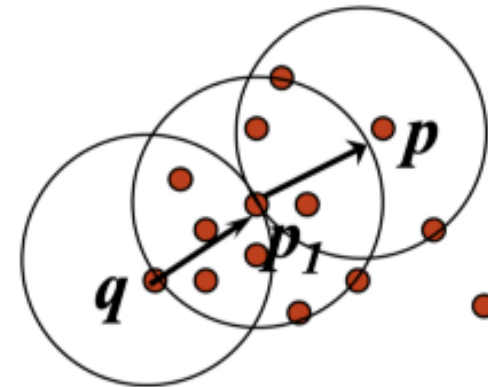
**MinPts:** Minimum number of points in an Eps-neighbourhood of that point

**Directly density-reachable:** A point  $p$  is directly density reachable from a point  $q$  w.r.t.  $Eps$ ,  $MinPts$ , if  $NEps(q) = \{p \text{ belongs to } D \mid \text{dist}(p,q) \leq Eps\}$  and  $|NEps(q)| \geq MinPts$  ;

$Minpts = 5, Eps = 1$

- Density-reachable:

- A point  $p$  is **density-reachable** from a point  $q$  w.r.t.  $Eps$ ,  $MinPts$  if there is a chain of points  $p_1, \dots, p_n, p_1 = q, p_n = p$  such that  $p_{i+1}$  is directly density-reachable from  $p_i$

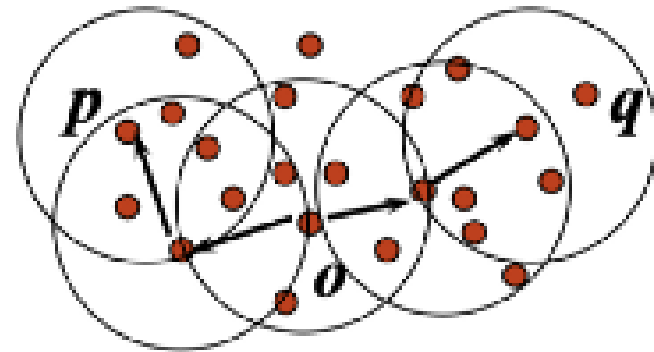


$p$  belongs to  $D \mid \text{dist}(p,q) \leq \text{Eps}\}$  and  $|N_{\text{Eps}}(q)| \geq \text{MinPts}$  ;

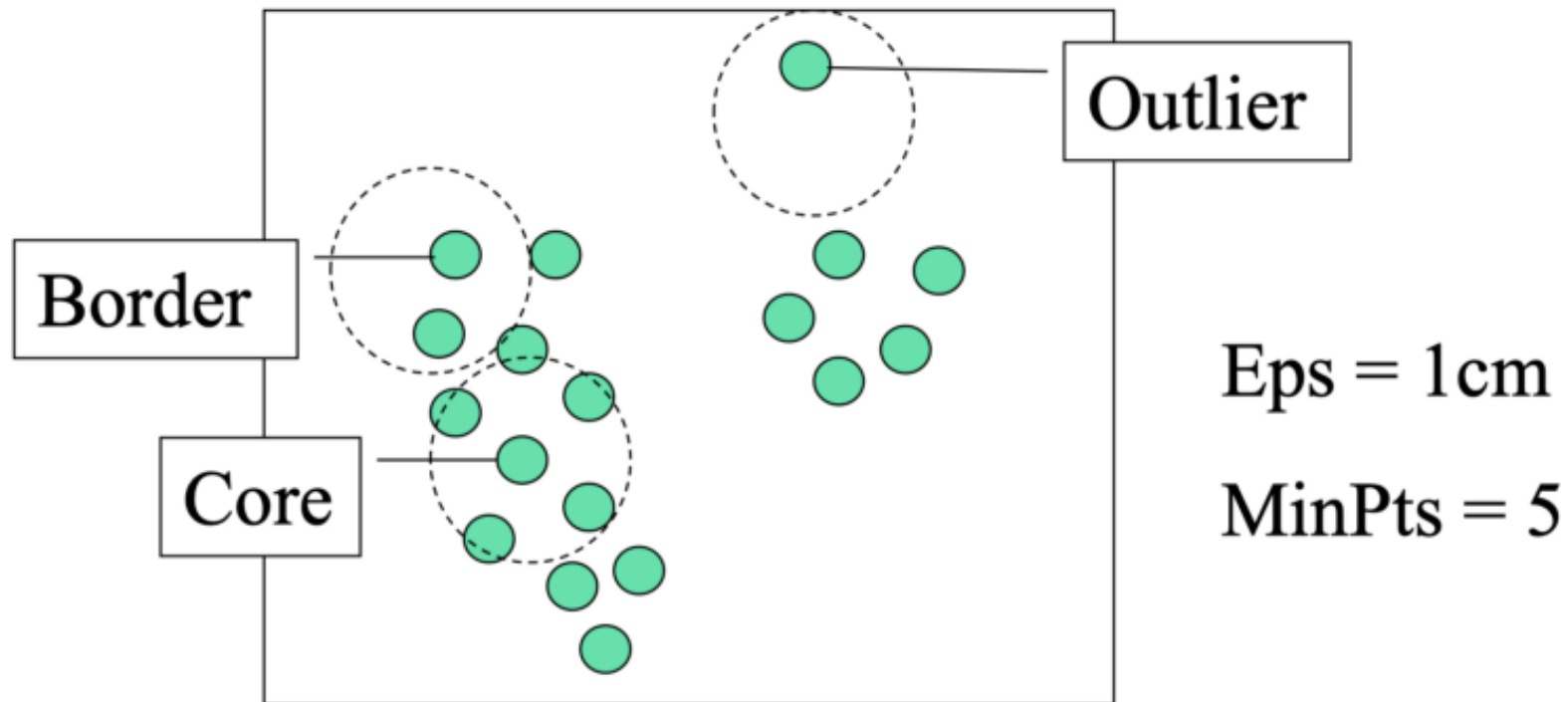
Minpts = 5, Eps = 1

- Density-connected

- A point  $p$  is **density-connected** to a point  $q$  w.r.t.  $\text{Eps}$ ,  $\text{MinPts}$  if there is a point  $o$  such that both,  $p$  and  $q$  are density-reachable from  $o$  w.r.t.  $\text{Eps}$  and  $\text{MinPts}$



- core point if it has more than a specified number of points (MinPts) within Eps. These are points that are at the interior of a cluster A.  
border point has fewer than MinPts within Eps, but is in the neighborhood of a core point.  
outlier(noise) point, which is the points that are neither core nor border points.



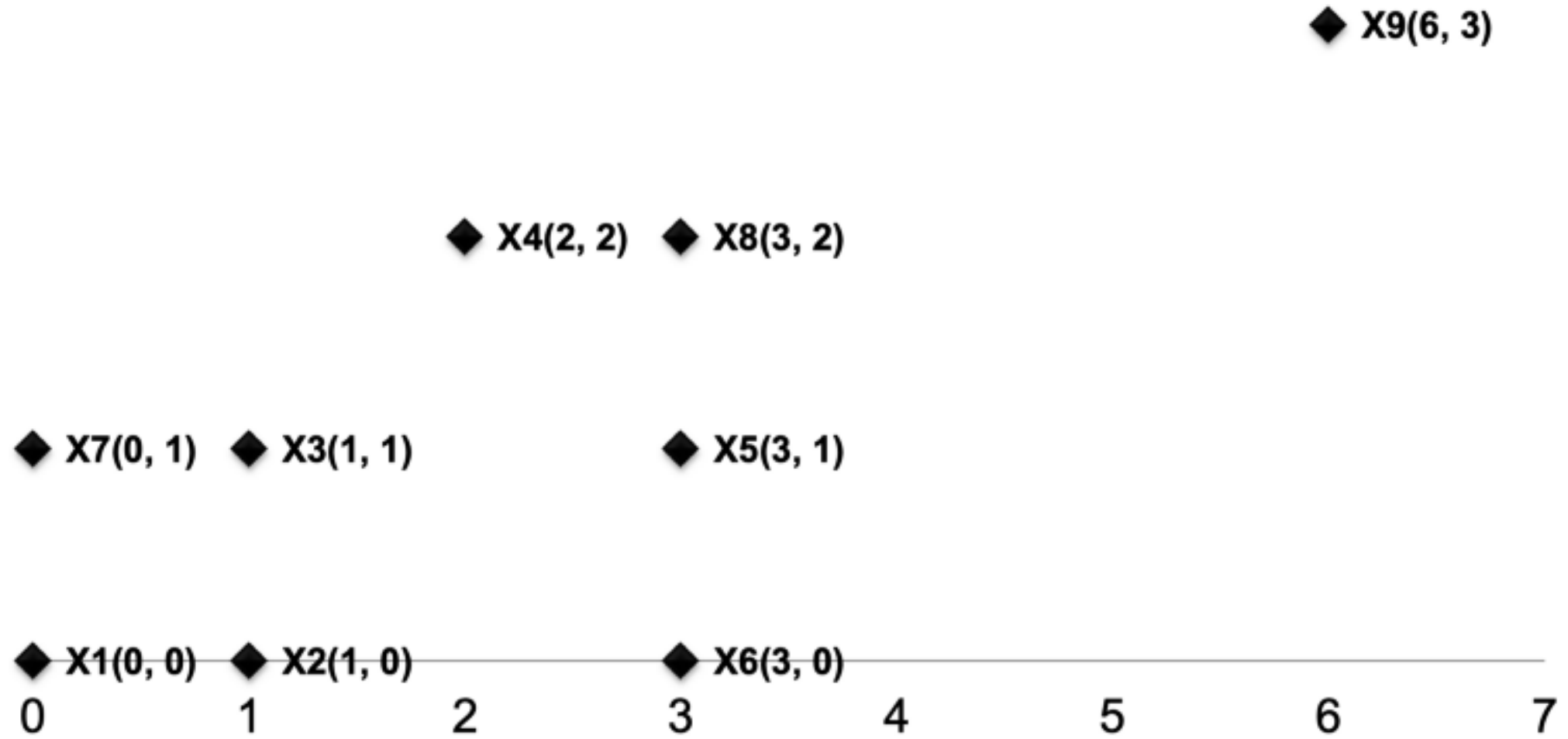
1. Arbitrary select a point  $p$
2. Retrieve all points density-reachable from  $p$  based on  $Eps$  and  $MinPts$
3. If  $p$  is a core point, a cluster is formed
4. If  $p$  is a border point, no points are density-reachable from  $p$  and DBSCAN visits the next point of the database
5. Continue the process until all of the points have been processed

Consider the following data to be clustered;

$x_1(0,0)$ ,  $x_2(1,0)$ ,  $x_3(1,1)$ ,  $x_4(2,2)$ ,  $x_5(3,1)$ ,  $x_6(3,0)$ ,  $x_7(0,1)$ ,  $x_8(3,2)$ ,  $x_9(6,3)$

$Eps = 1$  and  $MinPts = 3$ . Find all core points, border points and noise points, and show the final clusters using DBSCAN algorithm

## Data Points



## **N(p), Eps-neighborhood of point p**

$$N(x_1) = \{x_1, x_2, x_7\}$$

$$N(x_2) = \{x_2, x_1, x_3\}$$

$$N(x_3) = \{x_3, x_2, x_7\}$$

$$N(x_4) = \{x_4, x_8\}$$

$$N(x_5) = \{x_5, x_6, x_8\}$$

$$N(x_6) = \{x_6, x_5\}$$

$$N(x_7) = \{x_7, x_1, x_3\}$$

$$N(x_8) = \{x_8, x_4, x_5\}$$

$$N(x_9) = \{x_9\}$$

If the size of  $N(p)$  is at least  $\text{MinPts}$ , then  $p$  is said to be a core point.

$\text{MinPts}$  is 3, thus the size of  $N(p)$  is at least 3. **Thus core points are:  $\{x_1, x_2, x_3, x_5, x_7, x_8\}$**

given a point  $p$ ,  $p$  is said to be a border point if it is not a core point but  $N(p)$  contains at least one core point.  $N(x_4) = \{x_4, x_8\}$ ,  $N(x_6) = \{x_6, x_5\}$ . here  $x_8$  and  $x_5$  are core points, So both  **$x_4$  and  $x_6$  are border points.**

Arbitrary select a point  $p$ , now we choose  $x_1$

Retrieve all points density-reachable from  $x_1$ :  $\{x_2, x_3, x_7\}$

Here  $x_1$  is a core point, a cluster is formed. So we have Cluster\_1:  $\{x_1, x_2, x_3, x_7\}$

Next, we choose  $x_5$ , Retrieve all points density-reachable from  $x_5$ :  $\{x_8, x_4, x_6\}$

Here  $x_5$  is a core point, a cluster is formed. So we have Cluster\_2:  $\{x_5, x_4, x_8, x_6\}$

Next, we choose  $x_9$ ,  $x_9$  is a noise point, noise points do NOT belong to any clusters.



## Data Points

Noise Point

◆  $x_9(6, 3)$

Cluster 1

◆  $x_7(0, 1)$  ◆  $x_3(1, 1)$

◆  $x_1(0, 0)$  ◆  $x_2(1, 0)$

◆  $x_4(2, 2)$  ◆  $x_8(3, 2)$

◆  $x_5(3, 1)$

◆  $x_6(3, 0)$

Cluster\_2

0

1

2

3

4

5

6

7

