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Standard Deviation



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1 Introduction

Standard deviation is a measure that is utilized to evaluate the measure of variation or dispersion of a set of information values. A low standard deviation demonstrates that the information tends to be near the mean (additionally called the expected value) of the set, while a high standard deviation shows that the information is spread out over a wider scope of values.[1]

The standard deviation of a random variable, statistical population, data set, or probability distribution is the square root of its variance. It is algebraically simpler, though in practice less robust, than the average absolute deviation. A useful property of the standard deviation is that, unlike the variance, it is expressed in the same units as the data. [Wikipedia]

In other words, the standard deviation σ (sigma) is the square root of the variance of X; i.e., it is the square root of the average value of $(X - \mu)^2$.

Population Standard Deviation

$$\sigma = \sqrt{\frac{\sum (x_i - \mu)^2}{N}}$$

Sample Standard Deviation

$$\sigma = \sqrt{\frac{\sum (x_i - \bar{x})^2}{n - 1}}$$

1.1 Properties of Standard Deviation

- Standard deviation is only used to measure spread or dispersion around the mean of a data set.
- Standard deviation is never negative.
- Standard deviation is sensitive to outliers. A single outlier can raise the standard deviation and in turn, distort the picture of spread.
- For data with approximately the same mean, the greater the spread, the greater the standard deviation.

• If all values of a data set are the same, the standard deviation is zero (because each value is equal to the mean)[5]

2 Requirements and constraints

- R1—At least two numbers are required to calculate standard deviation.
- R2—Need to know if data set is a population data or sample data before calculation standard deviation.
- R3— Values in data set must be different (if identical, $\sigma = 0$)
- R4—User would enter data values separated by comma, otherwise it would be consider as a one value.
- R5—User would enter the numbers only(Separated by commas)
- R6—Clear Button to reset the value.

3 Pseudo code

```
Algorithm 1: standard deviation algorithm [1]
  Result: standard deviation
  Let n \leftarrow 0, Sum \leftarrow 0, SumSquare \leftarrow 0 size \leftarrow arraysize \setminus \setminus initialization;
  if n==0 then
      return 0.0;
  else
      while n is not equal to size do
          n \leftarrow n + 1 \setminus \text{incrementing } n;
          Sum \leftarrow Sum + x \setminus adding all numbers in array to calculate mean;
           SumSquare \leftarrow SumSquare + x \times x \setminus adding square of all numbers;
      end
      if Sample data then
           Var = (SumSquare - (Sum \times Sum) / n) / (n - 1) \setminus if data is
            sample data set, division by n - 1 to calculate variance;
      else
           Var = (SumSquare - (Sum \times Sum) / n) / (n) \setminus if data set is
            population, divison by number of values in set to calculate
            variance;
      end
      Stdev = Square root(Var) \setminus square root of variance;
  end
  [4]
```

3.1 Advantages

- Improves the readability of the approach to calculate standard deviation.
- Works as a rough documentation, so the program can be understood easily when a pseudo code is written out.
- Explain what exactly each line of a program should do with comments.
- It can be read and understood easily by non programmers.[3]

3.2 Disadvantages

• It was difficult to write a pseudo code before writing the actual code.

- Pseudo code does not covers the whole logic of the program.
- Difficult for non technical person to understand the flow of program(indication of next step from previous step)

References

- [1] [Wikipedia]wikipedia.org
- [2] [stackexchange]tex.stackexchange.com
- [3] www.techwalla.com
- [4] www.scribd.com
- [5] www150.statcan.gc.ca