

EECS16A Imaging 3

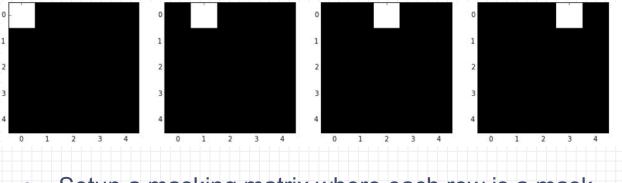


Announcements

Midterm I is this week, Friday 7/10

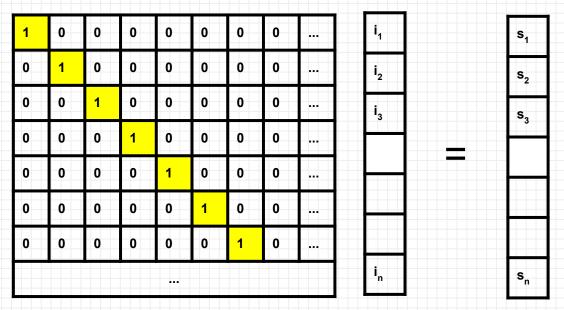
- Buffer labs are next week, 7/13 & 7/14
 - You can make up one missed lab from the Imaging Module, if needed
 - Held during your regular lab section (this one)
 - Touchscreen 1 starts on Wednesday 7/15

Last time: Single-pixel scanning



- Setup a masking matrix where each row is a mask
 - Measured each pixel individually once

Last time: Matrix-vector multiplication



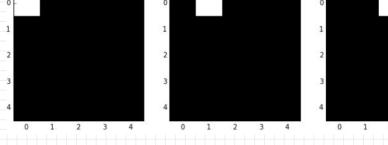
Masking Matrix H

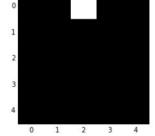
Unknown, vectorized image, \vec{l}

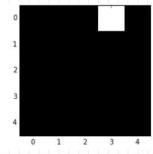
Recorded Sensor readings, \vec{S}

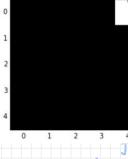


Last time: Single-pixel scanning





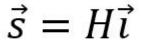








- Measured each pixel individually once
- How did we reconstruct our image, once we had s?
- What are the requirements of our masking matrix H?





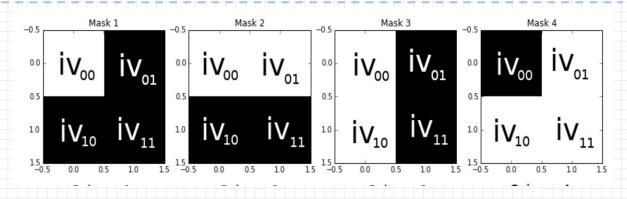
Questions from Imaging 2

Goal: Understand which measurements are good measurements

- ✓ Can we always reconstruct our image → need invertible H
- ? Are all invertible matrices equally good as scanning matrices?
- ? What happens if we mess up a single scan?



Today: Multi-pixel scanning



- Can we measure multiple pixels at a time?
 - Measurements are now linear combinations of pixels
- How can we reconstruct our scanned image?



Why do we care?

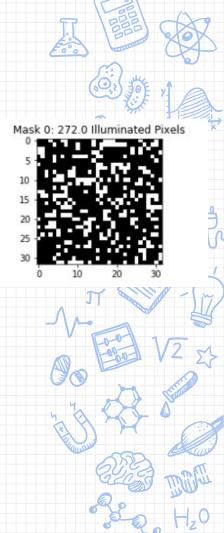
- Improve image quality by averaging
 - Good measurements → good average

- Redundancy is useful
 - Averaging measurements is better than using bad measurement values
 - Does not "solve" bad measurements, but makes us tolerant of some errors

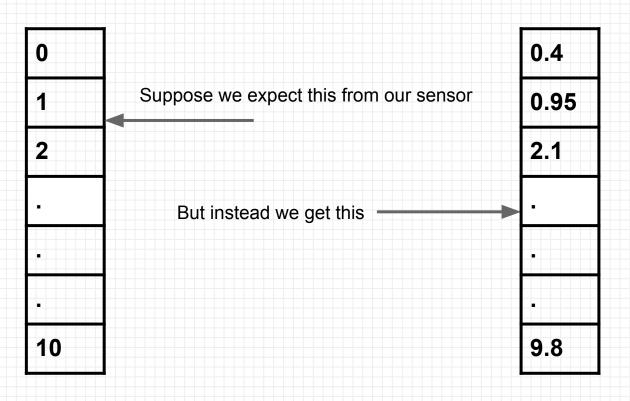


How do we do it?

- Change masks to illuminate multiple pixels per scan
 - Multiple 1's in each row of masking matrix H
 - Measure linear combinations of pixels instead of single pixels
- BUT multiple pixels → more noise
 - Noise = random variation in our measurement that we don't want (ex: room light getting into box)
 - Signal = data that we do want (light from pixel illumination)
- Too much noise → hard to distinguish signal from noise
 - Want high signal, low noise
 - High signal-to-noise ratio (SNR)

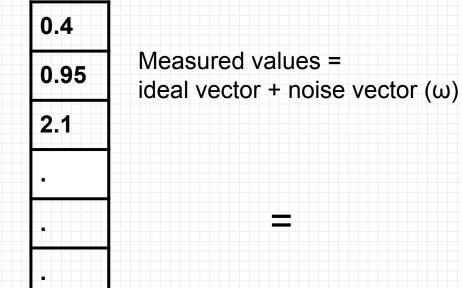


What is noise?



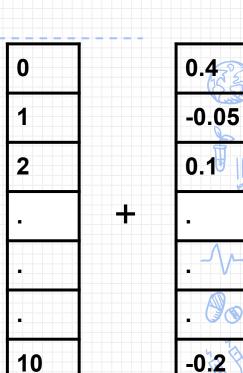


What is Noise?

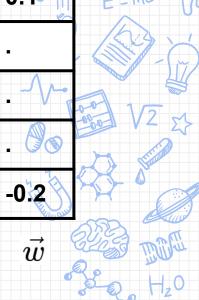




9.8



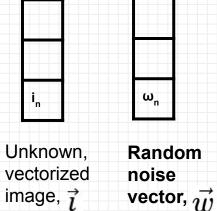
 \vec{s}_{ideal}

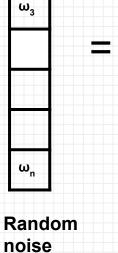


How does noise affect our system?

1	0	0	0	0	0	0	0	
0	1	0	0	0	0	0	0	
0	0	1	0	0	0	0	0	
0	0	0	1	0	0	0	0	
0	0	0	0	1	0	0	0	
0	0	0	0	0	1	0	0	•••
0	0	0	0	0	0	1	0	

Masking Matrix H





ω,

Recorded Sensor readings, \vec{S}



A more realistic system

Sensor readings =
 image vectors applied to H + noise vector

$$ec{s}=ec{Hi}+ec{w}$$

• We can't reconstruct i, but we can estimate it

$$ec{i}_{est} = H^{-1}ec{s} = ec{i} + H^{-1}ec{w}$$

Be careful about the noise term or else it could blow up !!



Eigenvalues for inverse matrices

 H Is an NxN matrix that we know is linearly independent (invertible).

 $\lambda_1 \overset{\dots}{} \lambda_N$

- No eigenvalue = 0
- Assume H has N linearly independent eigenvectors
- $Hv_i = \lambda_i v_i$ for i = 1...N
- N lin. ind. vectors can span \mathbb{R}^N
 - They span the noise vector
- The inverse of H has eigenvalues
 (as proven in homework)

$$H^{-1}v_i = \frac{1}{\lambda_i}v_i \text{ for } i = 1...N$$

How do eigenvalues affect noise?

The noise vector can be written as:

$$\vec{\omega} = \alpha_1 \vec{v_1} + \alpha_2 \vec{v_2} + \cdots + \alpha_n \vec{v_n}$$

Including effect of H^{-1}

$$H^{-1}\vec{\omega} = H^{-1}(\alpha_1 \vec{v_1} + \alpha_2 \vec{v_2} + \cdots + \alpha_n \vec{v_n})$$

Rewritten with eigenvalues:

$$H^{-1}\overrightarrow{\omega} = \frac{1}{\lambda_1}\alpha_1\overrightarrow{v_1} + \frac{1}{\lambda_2}\alpha_2\overrightarrow{v_2} + \cdots \frac{1}{\lambda_n}\alpha_n\overrightarrow{v_n}$$



Linking it all together

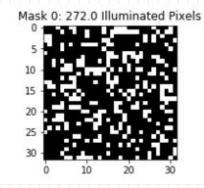
$$\vec{l}_{est} = H^{-1}\vec{s} + H^{-1}\vec{\omega}$$

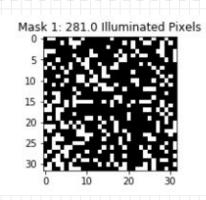
$$H^{-1}\vec{\omega} = \frac{1}{\lambda_1}\alpha_1\vec{v}_1 + \frac{1}{\lambda_2}\alpha_2\vec{v}_2 + \cdots + \frac{1}{\lambda_n}\alpha_n\vec{v}_n$$

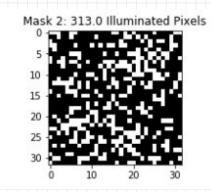
- Remember: want small noise term for high signal-to-noise ratio
- The noise is directly related to the eigenvalues.
- Do we want small or large eigenvalues for the H matrix in order to get a good image?

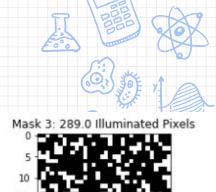


Possible Scanning Matrix: Random











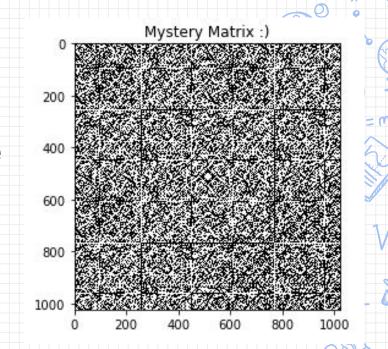
- Usually invertible
- O But what are its eigenvalues?



A more systematic scanning matrix:

Hadamard matrix!

- Constructed to have large eigenvalues
 - Just what we need!



Software Simulator Setup

- Upload ("simple") image of an object (or use 16A logo)
- 2. Convert image to 32x32 form for the simulator
- 3. Project masks (rows of H) onto it and "measure" **s** using matrix multiplication
- 4. Multiply with H inverse to find **i** (=H⁻¹**s**)

The simulator handles noise addition in step 3 using a parameter sigma



Using the Software Simulator

- 1. Start display view in another browser tab
- 2. Enter the imagePath and run the simulator + shift to display tab
- 3. Observe masks being projected onto the image + return to notebook tab
- 4. Observe generated sensor reading
- 5. Reconstruct image by multiplying with H inverse

Repeat steps 2-5 for each imaging experiment

Pointers

- READ CAREFULLY Long lab with lots of reading; heavily tests understanding of eigen-stuff (important for the exam)
- 2. You see the noisy sensor reading generated at the end instead of being generated entry by entry (i.e. just one masking simulation visual per experiment, no more cumulative simulation)
- 3. Choose an image that focuses on a single object and is not too detailed
- 4. Use a simple imagePath name
- 5. Before starting the imaging experiments, launch the display view in a separate tab using the link in the notebook
- 6. Enter imagePath correctly for each simulation block
- 7. Shift to the display tab as soon as you run a simulation block and return to the notebook once the visual has finished executing P.S.