

## Chapter III-7 — Analysis

```
MatrixOp/0 wave1 = var1 - wave2 // Error: Can't subtract a matrix from a scalar  
MatrixOp/0 wave1 = var1 / wave2 // Error: Can't divide a scalar by a matrix
```

Division of a scalar by a matrix can be accomplished using the reciprocal function as in:

```
MatrixOp/0 wave1 = scalar * rec(wave2)
```

The dot operator . is used to compute the generalized dot product:

```
MatrixOp/0 wave1 = wave2 . wave3 // Spaces around '.' are optional
```

The x operator designates matrix-matrix multiplication.

```
MatrixOp/0 wave1 = wave2 x wave3 // Spaces around 'x' are required!
```

The logical operators && and || are restricted to real-valued data tokens and produce unsigned byte numeric tokens with the value 0 or 1.

The two postfix operators ^t (matrix transpose) and ^h (Hermitian transpose) operate on the first token to their left:

```
MatrixOp/0 wave1 = wave2^t + wave3
```

The transpose operation has higher precedence and therefore executes before the addition.

The left token may be a compound token as in:

```
MatrixOp/0 wave1 = sumCols(wave2)^t
```

MatrixOp supports the ^ character only in the two postfix operators ^t and ^h. For exponentiation use the powR and powC functions.

## MatrixOp Multiplication and Scaling

MatrixOp provides a number of multiplication and scaling capabilities. They include matrix-scalar multiplication:

```
MatrixOp/0 wave1 = wave2 * scalar // Equivalent to a wave assignment
```

and wave-wave multiplication:

```
MatrixOp wave1 = wave2 * wave3 // Also includes layer-by-layer support
```

and matrix-matrix multiplication:

```
MatrixOp wave1 = wave2 x wave3
```

The latter is equivalent to the **MatrixMultiply** operation with the convenience of allowing you to write and execute complicated compound expressions in one line.

MatrixOp adds two specialized scaling functions that are frequently used. The scaleCols function multiplies each column by a different scalar and the scale function scales its input to a specified range.

## MatrixOp Data Rearrangement and Extraction

MatrixOp is often used to rearrange data in a matrix or to extract a subset of the data for further calculation. You can extract an element or a layer from a wave using square-bracket indexing:

```
// Extract scalar from point a of the wave  
MatrixOp destWave = wave1d[a]
```

```
// Extract scalar from element a,b of the wave  
MatrixOp destWave = wave2d[a][b]
```

```
// Extract scalar from element a,b,c of the wave  
MatrixOp destWave = wave3d[a][b][c]
```