

## Besselk

### **Besselk (n, z)**

The Besselk function returns the modified Bessel function of the second kind,  $K_n(z)$ , of order  $n$  and argument  $z$ . Replaces the bessK function, which is supported for backwards compatibility only.

If  $z$  is real, Besselk returns a real value, which means that if  $z$  is also negative, it returns NaN unless  $n$  is an integer. For complex  $z$  a complex value is returned, and there are no restrictions on  $z$  except for possible overflow.

#### Details

The calculation is performed using the SLATEC library. The function supports fractional orders  $n$ , as well as real or complex arguments  $z$ .

#### See Also

The **Besseli**, **Besselj**, and **Bessely** functions.

## Bessely

### **Bessely (n, z)**

The Bessely function returns the Bessel function of the second kind,  $Y_n(z)$ , of order  $n$  and argument  $z$ . Replaces the bessY function, which is supported for backwards compatibility only.

If  $z$  is real, Bessely returns a real value, which means that if  $z$  is also negative, it returns NaN unless  $n$  is an integer. For complex  $z$  a complex value is returned, and there are no restrictions on  $z$  except for possible overflow.

#### Details

The calculation is performed using the SLATEC library. The function supports fractional and negative orders  $n$ , as well as real or complex arguments  $z$ .

#### See Also

The **Besseli**, **Besselj**, and **Besselk** functions.

## bessl

### **bessl (n, x [, algorithm [, accuracy]])**

Obsolete – use **Besseli**.

The bessl function returns the modified Bessel function of the first kind,  $I_n(x)$  of order  $n$  and argument  $x$ .

For real  $x$ , the optional parameter *algorithm* selects between a faster, less accurate calculation method and slower, more accurate methods. In addition, when *algorithm* is zero or absent, the order  $n$  is truncated to an integer.

When *algorithm* is included and is 1, *accuracy* can be used to specify the desired fractional accuracy. See Details about algorithms.

If  $x$  is complex, a complex result is returned. In this case, *algorithm* and *accuracy* are ignored. The order  $n$  can be fractional, and must be real.

#### Details

The *algorithm* parameter has three options, each selecting a different calculation method:

Algorithm	What You Get
0 (default)	Uses a calculation method that has fractional accuracy better than $10^{-6}$ everywhere and is generally better than $10^{-8}$ . This method does not handle fractional order $n$ ; the order is truncated to an integer before the calculation is performed.  Algorithm 0 is fastest by a large margin.
1	Allows fractional order. The calculation is performed using methods described in <i>Numerical Recipes in C</i> , 2nd edition, pp. 240-245.  Using algorithm 1, <i>accuracy</i> specifies the fractional accuracy that you desire. That is, if you set <i>accuracy</i> to 1e-7 (that is, $10^{-7}$ ), that means that you wish that the absolute value of $(f_{\text{actual}} - f_{\text{returned}})/f_{\text{actual}}$ be better than $10^{-7}$ . Asking for less accuracy gives some increase in speed.