

**bessY**

```
bessY(n, x [, algorithm [, accuracy]])
```

Obsolete – use **BesselY**.

The bessY function returns the Bessel function of the second kind,  $Y_n(x)$  of order  $n$  and argument  $x$ .

For real  $x$ , the optional parameter *algorithm* selects between a faster, less accurate calculation method and slower, more accurate methods. In addition, when *algorithm* is zero or absent, the order  $n$  is truncated to an integer.

When *algorithm* is included and is 1, *accuracy* can be used to specify the desired fractional accuracy. See Details about algorithms.

If  $x$  is complex, a complex result is returned. In this case, *algorithm* and *accuracy* are ignored. The order  $n$  can be fractional, and must be real.

**Details**

See the **bessI** function for details on algorithms, accuracy and speed of execution.

When *algorithm* is 1, pairs of values for bessJ and bessY are calculated simultaneously. The values are stored, and a subsequent call to bessY after a call to bessJ (or vice versa) with the same  $n$ ,  $x$ , and *accuracy* will be very fast.

**beta**

```
beta(a, b)
```

The beta function returns for real or complex arguments as

$$B(a,b) = \frac{\Gamma(a)\Gamma(b)}{\Gamma(a+b)},$$

with  $\text{Re}(a), \text{Re}(b) > 0$ .  $\Gamma$  is the gamma function.

**See Also**

The **gamma** function.

**betai**

```
betai(a, b, x [, accuracy])
```

The betai function returns the regularized incomplete beta function  $I_x(a,b)$ ,

$$I_x(a,b) = \frac{B(x;a,b)}{B(a,b)}.$$

Here

$$B(x;a,b) = \int_0^x t^{a-1} (1-t)^{b-1} dt.$$

where  $a, b > 0$ , and  $0 \leq x \leq 1$ .

Optionally, *accuracy* can be used to specify the desired fractional accuracy.

**Details**

The *accuracy* parameter specifies the fractional accuracy that you desire. That is, if you set *accuracy* to  $10^{-7}$ , that means that you wish that the absolute value of  $(f_{\text{actual}} - f_{\text{returned}})/f_{\text{actual}}$  be less than  $10^{-7}$ .

Larger values of *accuracy* (poorer accuracy) result in evaluation of fewer terms of a series, which means the function executes somewhat faster.

A single-precision level of accuracy is about  $3 \times 10^{-7}$ , double-precision is about  $2 \times 10^{-16}$ . The betai function will return full double-precision accuracy for small values of  $a$  and  $b$ . Achievable accuracy declines as  $a$  and  $b$  increase: