

## PolygonArea

*coefsWaveName* is a wave that contains the polynomial coefficients. The number of points in the wave determines the number of terms in the polynomial and therefore the polynomial degree.

In a complex expression, poly2D requires *x1* and *y1* to be complex numbers, and returns a complex value. The wave containing the coefficients may be real or complex. Real coefficients are interpreted as cmplx(coef, 0). Passing complex coefficients in a real expression will use only the real part of the coefficients.

### Details

The coefficients wave contains polynomial coefficients for low degree terms first. All coefficients for terms of a given degree must be present, even if they are zero. Among coefficients for a given degree, those for terms having higher powers of X are first. Thus, poly2D returns, for a coefficient wave *cw*:

$$f(x,y) = cw[0] + cw[1]*x + cw[2]*y + cw[3]*x^2 + cw[4]*x*y + cw[5]*y^2 + \dots$$

A 2D polynomial of degree N has  $(N+1)(N+2)/2$  terms.

### Poly2D Example 1

Fill *mat1* with the polynomial  $1 + 2*x + 2.5*y + 3*x^2 + 3.5*xy + 4*y^2$  evaluated over the range  $x = (-1, 1)$  and  $y = (-1, 1)$ :

```
Function Poly2DEExample1()
    Make/O coefs1 = {1, 2, 2.5, 3, 3.5, 4}
    Make/N=(20,20)/O mat1
    SetScale/I x, -1, 1, mat1
    SetScale/I y, -1, 1, mat1
    mat1 = poly2D(coefs1, x, y)
    Display; AppendMatrixContour mat1
End
```

The polynomial is second degree, so the first command above made the wave *coefs* with six elements because  $(2+1)(2+2)/2 = 6$ .

### Poly2D Example 2

Fill *mat2* with the polynomial  $1 + 2*x + 3*y + 4*x^2 + 4*y^2 + 5*x^3 + 6*y^3$  evaluated over the range  $x = (-1, 1)$  and  $y = (-1, 1)$ . The first zero eliminates the second-order cross term  $x*y$  and the second and third zeros eliminate the third-order cross terms  $x^2*y$  and  $x*y^2$ :

```
Function Poly2DEExample2()
    Make/O coefs2 = {1, 2, 3, 4, 0, 4, 5, 0, 0, 6}
    Make/N=(20,20)/O mat2
    SetScale/I x, -1, 1, mat2
    SetScale/I y, -1, 1, mat2
    mat2 = poly2D(coefs2, x, y)
    Display; AppendMatrixContour mat2
End
```

### Poly2D Example 3

This example illustrates using poly2D in a complex expression:

```
Function Poly2DEExample3()
    Make/N=(200,200)/C/O cMat3           // Complex-valued matrix
    SetScale/I x -pi,pi,cMat3
    SetScale/I y -pi,pi,cMat3
    Make/D/O coefs3={1,1.5,2,2.5,3,3.5}
    cMat3 = poly2d(coefs3, cmplx(sin(x),cos(y)), cmplx(cos(x),sin(y)))
    Display; AppendImage cMat3
    ModifyImage cMat3 ctab= {*,*,Rainbow256,0}
    ModifyImage cMat3 imCmplxMode=3      // Display the complex phase
End
```

## PolygonArea

### PolygonArea (*xWave*, *yWave*)

The PolygonArea function returns the area of a simple, closed, convex or nonconvex planar polygon described by consecutive vertices in *xWave* and *yWave*.

A simple polygon has no internal “holes” and its boundary curve does not intersect itself. Both *xWave* and *yWave* must be 1D, real, numerical waves of the same dimensions. The minimum number of vertices is 3. The function uses the shoelace algorithm to compute the area (see theorem 1.3.3 in the reference below). If there is any error in the input, the function returns NaN.