

Like Hamming, Jaccard is intended for boolean data, but tests for "not equal".

$$d(u, v) = \frac{|\{j | u_j \neq v_j\}|}{|\{j | u_j \neq 0 \text{ or } v_j \neq 0\}|}$$

HCluster Vector Dissimilarity Calculation Methods for Boolean Data

The remaining metrics are for boolean data. Any data is accepted and each value is converted to a boolean value by testing for $u_j \neq 0$.

The following definitions are used:

$$a = |\{j | u_j \wedge v_j\}|$$

$$b = |\{j | u_j \wedge (\neg v_j)\}|$$

$$c = |\{j | (\neg u_j) \wedge v_j\}|$$

$$d = |\{j | (\neg u_j) \wedge (\neg v_j)\}|$$

D is the vector length, $D = a + b + c + d$.

$dm = \text{Yule}$

$$d(u, v) = \frac{2bc}{ad + bc}$$

$dm = \text{Dice}$

$$d(u, v) = \frac{b + c}{2a + b + c}, \quad d(0, 0) = 0$$

$dm = \text{RogersTanimoto}$

$$d(u, v) = \frac{2(b + c)}{b + c + D}$$

$dm = \text{RusselRao}$

$$d(u, v) = \frac{b + c + d}{D}$$

$dm = \text{SokalSneath}$

$$d(u, v) = \frac{2(b + c)}{a + 2(b + c)}, \quad d(0, 0) = 0$$

$dm = \text{Kulsinski}$

$$d(u, v) = \frac{1}{2} \cdot \left(\frac{b}{a + b} + \frac{c}{a + c} \right)$$