

## StatsLinearRegression

The confidence intervals are calculated differently depending on the hypothesis for the value of the correlation coefficient. If /RHO is not used the confidence intervals are computed using the critical value  $F_{c2}$ , otherwise they are computed using the critical  $Z_{c2}$  and sigmaZ.

### References

Zar, J.H., *Biostatistical Analysis*, 4th ed., 929 pp., Prentice Hall, Englewood Cliffs, New Jersey, 1999.

### See Also

Chapter III-12, **Statistics** for a function and operation overview; **StatsCircularCorrelationTest**, **StatsMultiCorrelationTest**, and **StatsRankCorrelationTest**.

## StatsLinearRegression

**StatsLinearRegression** [*flags*] [*wave0*, *wave1*,...]

The StatsLinearRegression operation performs regression analysis on the input wave(s). Output is to the W\_StatsLinearRegression wave in the current data folder or optionally to a table. Additionally, the M\_DunnettMCElevations, M\_TukeyMCSlopes, and M\_TukeyMCElevations waves may be created as specified.

### Flags

- /ALPH = *val*                Sets the significance level (default *val*=0.05).
- /B=*beta0*                    Tests the hypothesis that the slope  $b = \textit{beta0}$  (default is 0). The results are expressed by the t-statistic, which can be compared with the tc value for the two-tailed test. Get the critical value for a one-tailed test using StatsStudentCDF(1-alpha, N-2). It does not work with /MYVW.
- /BCIW                        Computes two confidence interval waves for the high side and the low side of the confidence interval. The new waves are named with \_CH and \_CL suffixes respectively appended to the Y wave name and are created in the current data folder. For multiple runs a numeric suffix will also be appended to the names.
- /BPIW[=*mAdditional*]        Computes prediction interval waves for the high side and the low side of the confidence interval on a single additional measurement (default). Use *mAdditional* to specify additional measurements. The new waves are named with \_PH and \_PL suffixes respectively appended to the Y wave name and are created in the current data folder. For multiple runs a numeric suffix will also be appended to the names.
- /DET=*controlIndex*        Performs Dunnett's multicomparison test for the elevations. The test requires more than two Y waves for regression, the test for the slopes should not reject the equal slope hypothesis, and the test for the elevations should reject the equal elevation hypothesis. *controlIndex* is the zero-based index of the Y wave representing the control (X waves do not count in the index specification). The test compares the elevation of every Y wave with the specified control.
- Output is to the M\_DunnettMCElevations wave in the current data folder or optionally to a table. For every Y wave and control Y wave combination, the results include SE, q, q' (shown as qp), and the conclusion with 1 to accept the hypothesis of equal elevations or 0 to reject it. Use /TAIL to determine the critical value and the sense of the test. If you use /TUK you will also get the Tukey test for the set of elevations.
- /MYVW={*xWave*, *yWave*}      Specifies that the input consists of multiple Y values for each X value. It ignores all other inputs and the results are appropriate only for multiple Y values at each X point.
- yWave* is a 2D wave of values arranged in columns. Use NaNs for padding where rows do not have the same number of entries as others. It will use the X scaling of *yWave* when *xWave* is null, /MYVW={\*, *yWave*}.

|                         |  |
|-------------------------|--|
|                         | <p>It first tests the hypothesis (<math>H_0</math>) that the population regression is linear in an analysis of variance calculation. It generates results 1-7 (see Details) as well as: Among Groups SS, Among Groups DF, Within Groups SS, Within Groups DF, Deviations from Linearity SS, Deviations from Linearity DF, F statistic defined by the ratio of Deviation from Linearity MS to Within Groups MS, and the critical value <math>F_c</math>.</p> <p>Next, it tests the hypothesis that the slope <math>\beta=0</math>. If the original <math>H_0</math> was accepted, the new F statistic=<math>\text{regressionMS}/\text{residualMS}</math>. Otherwise the with the critical <math>F=\text{regressionMS}/\text{WithinGroupsMS}</math> with a corresponding critical value. Finally, it reports the values of the coefficient of determination <math>r^2</math> and the standard error of the estimate <math>S_{YX}</math>.</p>                       |
| /PAIR                   | Specifies that the input waves are XY pairs, where each pair must be an X wave followed by a Y wave.   |
| /Q                      | No results printed in the history area.  |
| /RTO                    | Reflects the regression through the origin.  |
| /T= $k$                 | <p>Displays results in a table. <math>k</math> specifies the table behavior when it is closed.</p> <p><math>k=0</math>: Normal with dialog (default).</p> <p><math>k=1</math>: Kills with no dialog.</p> <p><math>k=2</math>: Disables killing.</p>  |
| /TAIL= $tCode$          | Sets the sense of the test when applying Dunnett's test (see /DET). $tCode$ is 1 or 2 for a one-tail critical value and 4 for a two-tail critical value.   |
| /TUK                    | <p>Performs a Tukey-type test on multiple regressions on two or more Y waves. There are two possible Tukey-type tests: The first is performed if the hypothesis of equal slopes is rejected. It compares all combinations of two Y waves to identify if some of the waves have equal slopes. Output is to the M_TukeyMCSlopes wave in the current data folder or optionally to a table. For every Y wave pair, the results include the difference between slopes (absolute value), <math>q</math>, the critical value <math>q_c</math>, and the conclusion set to 1 for accepting the equality of the pair of slopes or 0 for rejecting the hypothesis.</p> <p>The second Tukey-type test is performed if all the slopes are the same but the elevations are not. The test (see /DET) compares all possible pairs of elevations to determine which satisfy the hypothesis of equality. Output is to the M_TukeyMCElevations wave in the current data folder.</p> |
| /WSTR= $waveListString$ | <p>Specifies a string containing a semicolon-separated list of waves that contain sample data. Use <math>waveListString</math> instead of listing each wave after the flags.</p>   |
| /Z                      | Ignores errors.  |

### Details

Inputs may consist of Y waves or XY wave pairs. If X data are not used, the X values are inferred from the Y wave scaling. For multiple waves where only some have pairs, use the /PAIR flag and enter \* in each place where the X values should be computed.

For each input StatsLinearRegression calculates:

1. Least squares regression line  $y=a+b*x$ .
2. Mean value of X:  $xBar$ .
3. Mean value of Y:  $yBar$ .
4. Sum of the squares  $(x_i-xBar)^2$ .
5. Sum of the squares  $(y_i-yBar)^2$ .
6. Sum of the product  $(x_i y_i - xyBar)$ .
7. Standard error of the estimate  $s_{\alpha}^2 = \frac{\sum (y_i - \hat{y}_i)^2}{n-2}$ .
8. F statistic for the hypothesis  $\beta=0$ .
9. Critical F value  $F_c$ .
10. Coefficient of determination  $r^2$ .
11. Standard error of the regression coefficient  $S_b$ .
12. t-statistic for the hypothesis  $\beta=\beta_0$ , NaN if /B is not specified.
13. Critical value  $t_c$  for the t-statistic above (used to calculate L1 and L2).
14. Lower confidence interval boundary (L1) for the regression coefficient.
15. Upper confidence interval boundary (L2) for the regression coefficient.

For two Y waves with the same slope, it computes a common slope (bc) and then tests the equality of the elevations (a). In both cases it computes a t-statistic and compares it with a critical value. If the elevations are also the same then it computes the common elevation (ac) and the pooled means of X and Y in (xp) and (yp).

For more than two Y waves it computes:

$$A_c = \sum_{j=1}^W A_j; \quad A_j \equiv \sum x_i^2 = \sum_{i=0}^{n_j-1} X_i^2 - \frac{1}{n_j} \left( \sum_{i=0}^{n_j-1} X_i \right)^2$$

$$B_c = \sum_{j=1}^W B_j; \quad B_j \equiv \sum xy = \sum_{i=0}^{n_j-1} XY - \frac{1}{n_j} \left( \sum_{i=0}^{n_j-1} X_i \right) \left( \sum_{i=0}^{n_j-1} Y_i \right)$$

$$C_c = \sum_{j=1}^W C_j; \quad C_j \equiv \sum y^2 = \sum_{i=0}^{n_j-1} Y_i^2 - \frac{1}{n_j} \left( \sum_{i=0}^{n_j-1} Y_i \right)^2$$

$$SSp = \sum_{j=1}^W C_j - \frac{B_j^2}{A_j}$$

$$SSc = Cc - \frac{B_c^2}{A_c^2}$$

$$SSt = \sum_{j=1}^W \sum_{i=0}^{n_j} Y_{ji}^2 - \frac{1}{N} \left( \sum_{j=1}^W \sum_{i=0}^{n_j} Y_{ji} \right)^2 - \frac{\left( \sum_{j=1}^W \sum_{i=0}^{n_j} X_{ji} Y_{ji} - \frac{1}{N} \left( \sum_{j=1}^W \sum_{i=0}^{n_j} X_{ji} \right) \left( \sum_{j=1}^W \sum_{i=0}^{n_j} Y_{ji} \right) \right)^2}{\sum_{j=1}^W \sum_{i=0}^{n_j} X_{ji}^2 - \frac{1}{N} \left( \sum_{j=1}^W \sum_{i=0}^{n_j} X_{ji} \right)^2}$$