

Tutorial Note 4: IS-LM Framework

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Basic IS-LM Model

Deriving the Model Recall that in the goods market, the demand for goods is

$$Z = C + I + G.$$

Recall that consumption depends on disposable income $Y - T$. And in reality, investment depends on output and interest rate:

$$I = I(Y, i),$$

where I increases with Y and decreases with i . (Think about the intuition.)

Then we rewrite the demand as

$$Z = C(Y - T) + I(Y, i) + G.$$

At equilibrium, we have

$$Y = Z.$$

This determines the equilibrium output Y^* . When the nominal interest rate increases, the investment will decrease, shifting the ZZ curve downwards. We have the new equilibrium output Y' , shown as Figure 1.

If we put the interest rate and the output together, then we get the IS relation (Figure 2).

Note that all the pairs (i, Y) is a pair of **equilibrium** values of nominal interest and output.

In the derivation of the IS relation, note that the output is measured in *real term*. Therefore, we should also use real term in the money market equilibrium to derive the **LM relation**. Recall that the nominal money demand is

$$M^d = PYL(i)$$

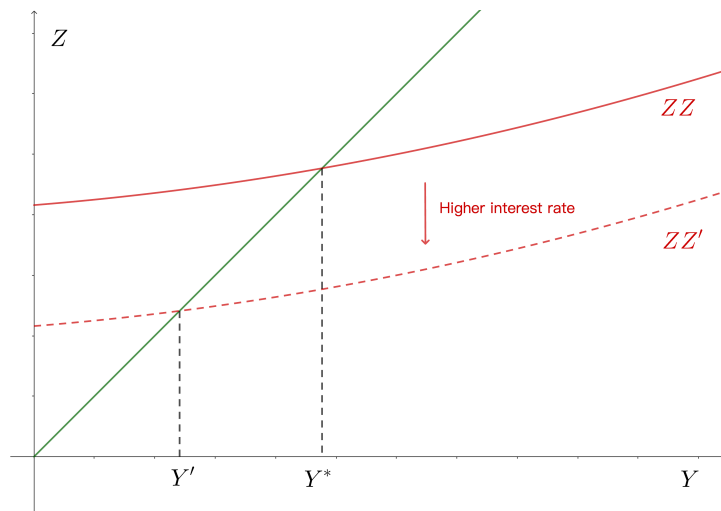


Figure 1: Goods Market Equilibrium

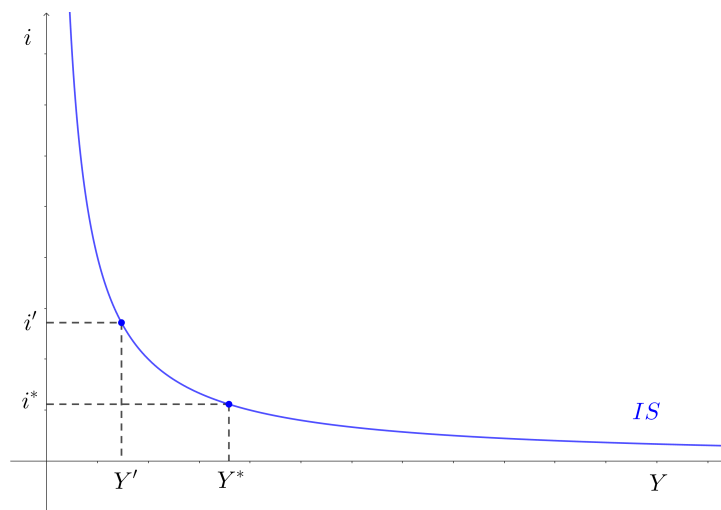


Figure 2: Deriving IS curve from goods market equilibrium

for some decreasing function $L(i)$. The real money demand is

$$\frac{M^d}{P} = YL(i).$$

At equilibrium, $M^d = M^S = M$. In the short run, we assume that prices are sticky. Hence, we have

$$\frac{M}{P} = YL(i).$$

Central banks adjust money supply M to target an interest rate $i = \bar{i}$. Hence, the LM curve is a horizontal line. Putting together with the IS curve, we get Figure 3.

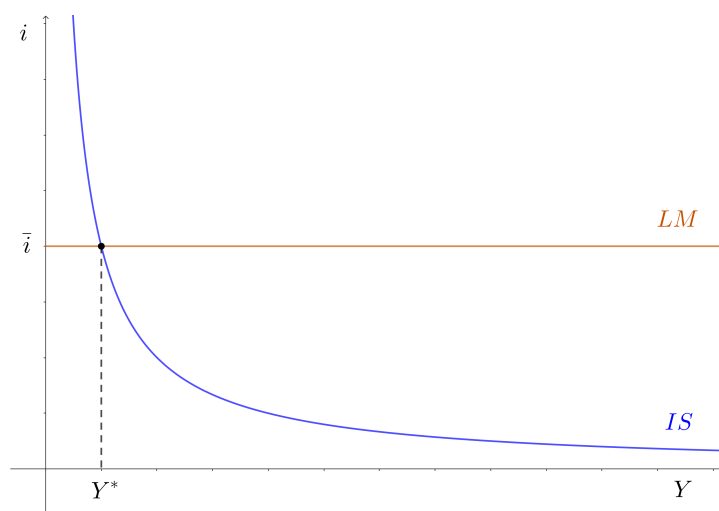


Figure 3: IS-LM Framework

They together yield the **general equilibrium** interest rate and output, (\bar{i}, Y^*) .

Exercise 1. *Chapter 5, Question 5 in Blanchard, Olivier (2021), Macroeconomics, 8th ed., Pearson.*

Exercise 2. (1) *At a given interest rate level, a temporary reduction in government purchases will*

- A. *increase desired saving, causing the IS curve to shift down and to the left.*
- B. *increase desired saving, causing the IS curve to shift up and to the right.*
- C. *decrease desired saving, causing the IS curve to shift down and to the left.*

D. decrease desired saving, causing the IS curve to shift up and to the right.

(2) When all markets in the economy are simultaneously in equilibrium, we say

A. markets are complete.

B. markets are perfect.

C. there is disequilibrium.

D. there is general equilibrium.

(3) If government spending and taxes increase by the same amount, the IS curve will

A. shift to the left.

B. shift to the right.

C. stay unchanged.

D. have an ambiguous shift.

Introducing Financial Sector

The Fisher Equation By no-arbitrage condition, we have

$$1 + r_t = \frac{(1 + i_t)P_t}{P_{t+1}^e}.$$

Since

$$\pi_{t+1}^e = \frac{P_{t+1}^e - P_t}{P_t},$$

we obtain

$$1 + r_t = \frac{1 + i_t}{1 + \pi_{t+1}^e}.$$

By an approximation, we obtain the **Fisher Equation**:

$$r_t \approx i_t = \pi_{t+1}^e.$$

Example 1 (No-arbitrage condition). *Consider a one-year risk-free bond with face value \$1,000. Suppose the risk-free interest rate is 5%. The bond is sold at \$980 today.*

- (1) *Is there any arbitrage opportunity? Describe how to make a profit. Assume that you are allowed to lend and borrow at the risk-free interest rate.*
- (2) *To avoid arbitrage, the issuer would like to provide some coupon. Coupon is some reward to the investors in addition to the interests which is distributed at the end of each period (annually, semi-annually, etc., depending on the specified rule. Assume that coupon is distributed annually here). Then what should be the coupon rate, i.e., the ratio of the amount of coupon to the face value?*

Risk Premium To hedge the default risk, the bank always charge a risk premium x other than the real rate for firm financing. Therefore, instead of having $I = I(Y, i)$, we have

$$I = I(Y, r + x) = I(Y, i - \pi^e + x).$$

Example 2 (No-arbitrage condition). *Consider a zero-coupon one-year bond with face value \$1,000. The risk-free interest rate is 5%. However, there is default risk on this bond. It has probability of 20% to pay only \$800 back to the investor and 80% probability to pay \$1,000 back.*

- (1) *If the risky bond has its bond rate equal to the risk-free rate, then what should be the bond price?*
- (2) *If the risky bond has the same price as the risk-free bond today, what will be the risk premium?*

Solvency, Liquidity, and Bank Runs **Solvency** measures a financial intermediary's ability to pay its liabilities. At a simplified level, you can just compare the cash it owns and the liabilities it owes. **Liquidity** measures how easy an asset can be transformed into cash. They are related in the following sense:

- If the assets are illiquid, i.e., hard to be transformed into cash, then the financial intermediary is likely to be more insolvent and to have more risk of going bankrupt.

- If the liabilities are liquid, *i.e.*, easy to be asked to pay in cash, then the financial intermediary is likely to be more insolvent and to have more risk of going bankrupt.

Exercise 3. *Chapter 6, Question 4 in Blanchard, Olivier (2021), Macroeconomics, 8th ed., Pearson.*

Extended IS-LM Framework

To understand financial shocks using the IS-LM framework, we need two main modifications:

- Distinguish nominal interest rate from the real interest rate;
- Incorporate risks into the model.

Then we have the following IS relation and LM relation:

$$\text{IS relation : } Y = C(Y - T) + I(Y, r + x) + G$$

$$\text{LM relation : } r = \bar{r}.$$

By the Fisher equation, there is a lower bound for the real interest rate: $r \geq -\pi^e$.

Example 3. *Consider the following behavioral equations:*

$$C = 200 + 0.5(Y - T)$$

$$I = 500 - 2000(r + x) + 0.3Y$$

and the real money demand:

$$\frac{M^d}{P} = Y(0.8 - 5\bar{i}).$$

Suppose that $G = 100$ and $T = 200$. The price level is 10, and the nominal money supply is 13000. The expected inflation is 2%, and the risk premium is 5%.

(1) Solve for the equilibrium output. What is the target nominal interest rate?

- (2) *Can the central bank expand the money supply to 21,000? What nominal interest rate is it targeting?*
- (3) *What is the lower bound for real interest rate target? What is the upper bound for nominal money supply?*
- (4) *Keep the target rate as in part (1). Find the upper bound of tax such that there exists a positive equilibrium output.*
- (5) *Suppose that people become pessimistic on the economy, and become more risk averse on assets. What is the effect of this? Illustrate this economy in a diagram. Explain your figure in words.*

Policy Analyses Exercises

Example 4. *Consider an economy like Argentina in 2001. Due to rampant corruption from the government, massive tax evasion, and money laundering activities, both consumers and investors become very pessimistic about the Argentine economy. Suppose initially, the economy is in an equilibrium.*

- (1) *Explain what happens to the economy in the short run when people become pessimistic about the economy. What will happen to output and the real interest rate?*
- (2) *If you are the government of Argentina, what would you do with government spending in order to offset the effects of the pessimism? What will happen to output, the real interest rate, investment, and the consumption as the result of the government's action?*
- (3) *If you are the central bank of Argentina, what kind of monetary policy that you can implement in order to offset the effects of the pessimism? What will happen to output, the real interest rate, investment, and the consumption as the result of the central bank's action?*

Exercise 4. *Continue with Example 4. Suppose the Argentine government has very limited fiscal space, and it is already running very high budget deficit so that the government is very likely to default on its debt, and simultaneously, the nominal interest rate in Argentina is very close to zero, or the zero lower bound (ZLB).*

(1) Is it still appropriate to use the policy suggested in part (2)? Why?

(2) Is it still appropriate to use the policy suggested in part (3)? Why?

(3) What kind of policies can be implemented in order to offset the effects of the pessimism? Please suggest at least 1 policy and explain why it works.

Exercise 5. *Chapter 6, Question 9 in Blanchard, Olivier (2021), Macroeconomics, 8th ed., Pearson.*