

**Problem Set 4 Solution**

Total Score: 100 points

**Question 1 (22 points)**

- (a) (4 points) Point  $A$ ,  $ZZ$ , axis label (2),  $Y = Z$ , value.
- (b) (8 points)  $Y \downarrow, C \downarrow, I \downarrow, NX > 0$ .  $ZZ$  curve down, no change in  $NX$  curve. 2 points for notations.
- (c) (10 points) Assume that the Marshall Lerner condition holds. (1 point) Then decreasing  $\epsilon$  leads to an increase in  $NX$ . (1 point)  $NX$  moves upwards,  $ZZ$  moves back.  $Y, I$  the same,  $C \downarrow$ .  $NX \uparrow$ . 2 points for notations.

**Question 2 (23 points)**

- (a) (6 points) Point  $A$ ,  $IM - LM$ ,  $UIP$ ,  $(E^e, i^*)$  (1 point), axis label (4,  $IS - LM$  must be  $i$ ), value.
- (b) (8 points)  $IS$  shifts to the left,  $Y, C, I \downarrow$ . No change in  $UIP$ .  $E -$ ,  $NX \uparrow$ . 2 more points for notation.
- (c) (9 points) Target lower interest rate.  $LM$  shifts downwards.  $Y -$ ,  $C \downarrow$ .  $I \uparrow$ . Equilibrium point moves downwards along  $UIP$ .  $E \downarrow$ ,  $NX \uparrow$ . 2 more points for notation.

**Question 3 (29 points)**

- (a) (8 points) In an open economy,

$$\begin{aligned} Y &= C + I + G - \frac{IM}{\epsilon} + X \\ &= 10 + 0.8(Y - 10) + 10 + G - 0.3Y + 0.3Y^* \\ &= 0.5Y + 12 + G + 0.3Y^*. \end{aligned}$$

Then  $Y = 24 + 2G + 0.6Y^*$ . The multiplier is 2. (3 points)

In a closed economy,

$$\begin{aligned} Y &= C + I + G \\ &= 10 + 0.8(Y - 10) + 10 + G \\ &= 0.8Y + 12 + G. \end{aligned}$$

Then  $Y = 60 + 5G$ . The multiplier is 5. (3 points)

The difference is from import leakage. (2 points)

- (b) (7 points) In the foreign economy,  $Y^* = 24 + 2G^* + 0.6Y$ . Substitute this into  $Y = 24 + 2G + 0.6Y^*$ . We get

$$Y = 24 + 2G + 0.6(24 + 2G^* + 0.6Y) = 38.4 + 2G + 1.2G^* + 0.36Y.$$

Then  $Y = 60 + 3.125G + 1.875G^*$ .  $Y^* = 60 + 3.125G^* + 1.875G$ . (4 points)

Plug in the numbers. We get  $Y = Y^* = 110$ .

Import leakage is now somehow returned. (2 points)

- (c) (6 points) Solve  $125 = 60 + 3.125G' + 1.875 \times 10$ . We get  $G' = 14.8$ . Then

$$Y^* = 60 + 3.125 \times 10 + 1.875 \times 14.8 = 119$$

$$NX = -0.3 \times 125 + 0.3 \times 110 = -1.8$$

$$NX^* = 1.8$$

$$T - G' = -4.8$$

$$T^* - G^* = 0.$$

- (d) (4 points) Solving the system.  $G''' = G^{*''} = 13$ .  $NX'' = NX^{*''} = 0$ .  $T - G''' = T^* - G^{*''} = -3$ .

- (e) (4 points) Government can just wait the other country to expand the balance sheet to gain its leakage "for free".

**Question 4 (26 points)**

- (a) (4 points) Use UIP and do the math.
- (b) 22 free points.