

## Tutorial Note 9: Financial Market and Goods Market in Open Economy

Solution to Exercises

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### Example 3

- (1) Note that here the US is the domestic country. So  $\epsilon = 7.8 \times \frac{1500}{10000} = 1.17$ .
- (2) This real interest rate means that 1 US good is valued at 1.17 HK good. Therefore, US goods are more valuable. Therefore, we would like to buy the iPhone in HK. Then the profit is  $1500 - 10000/7.8 = 218USD$ .
- (3) When  $\epsilon = 1$ , people will be indifferent.

### Exercises

1. The spot rate is  $E_{EUR/USD} = 0.7627$ . The cross rate is  $\tilde{E}_{EUR/USD} = E_{EUR/CHF} \times E_{CHF/USD} = 0.7550$ . Therefore, we should sell USD via the spot rate first.

Step 1: Change USD for EUR.

$$5,000,000 \text{ USD} \times 0.7627 \text{ EUR/USD} = 3,813,500 \text{ EUR}.$$

Step 2: Change EUR for CHF.

$$3,813,500 \text{ EUR} \div 0.6395 \text{ EUR/CHF} = 5,963,252.54 \text{ CHF}.$$

Step 3: Change CHF for USD.

$$5,963,252.54 \text{ CHF} \div 1.1806 \text{ CHF/USD} = 5,051,035.53 \text{ USD}.$$

By this arbitrage, we can make a profit of \$51,035.53.

If we initially sell for CHF, then we will finally get

$$5,000,000 \text{ USD} \times \frac{1.1806 \text{ CHF/USD} \times 0.6395 \text{ EUR/CHF}}{0.7627 \text{ EUR/USD}} = 4,949,480.14 \text{ USD}.$$

We lose \$ 50,519.86.

To avoid arbitrage, the EUR/CHF rate should be

$$E_{\text{EUR/CHF}}^{\text{no-arbitrage}} = \frac{E_{\text{EUR/USD}}}{E_{\text{CHF/USD}}} = 0.6460 \text{EUR/CHF}.$$

2. The absolute PPP in time  $t$  is

$$E_t = \frac{P_t^*}{P_t},$$

and that in time  $t + 1$  in expectation is

$$E_{t+1}^e = \frac{P_{t+1}^{*e}}{P_{t+1}^e}.$$

Taking ratio between the two equations, we obtain

$$\frac{E_{t+1}^e}{E_t} = \frac{\frac{P_{t+1}^{*e}}{P_{t+1}^e}}{\frac{P_t^*}{P_t}} = \frac{\frac{P_{t+1}^{*e}}{P_t^*}}{\frac{P_{t+1}^e}{P_t}} = \frac{1 + \pi_{t+1}^{*e}}{1 + \pi_{t+1}^e}.$$

3. The answer is that only IFE and relative PPP do not change.

- (a) UIP/CIP: If you buy a domestic bond, you get  $1 + i_t$  in one year. If you buy a foreign bond, you first exchange to the foreign currency with fee and get  $(1 - \tau)E_t$  foreign currency, after 1 year you get  $(1 - \tau)E_t(1 + i_t^*)$ , and you exchange the foreign currencies back to the domestic currency with fee and you get  $(1 - \tau)^2 \frac{E_t}{E_{t+1}^e} (1 + i_t^*)$ , or  $(1 - \tau)^2 \frac{E_t}{F_{t,t+1}} (1 + i_t^*)$  with a forward. Neither UIP nor CIP holds any more.
- (b) PPP: You buy a unit of goods which costs  $P$  domestic currency. You sell it in the foreign country, which earns you  $P^*$  foreign currency. Then you exchange the foreign currency back to the domestic currency and get  $(1 - \tau) \frac{P^*}{E}$ . No-arbitrage implies that  $E = \frac{P^*}{P} (1 - \tau)$ . However, if you take the ratio, with constant  $\tau$ , you still get the relative PPP relation.
- (c) IFE: The derivation of IFE theoretically does not depend on converting currencies. So there is no effect.
- (d) FEP: Since CIP does not hold any more, FEP cannot hold.

4. The trade surplus condition is that

$$Y_{\text{eqm}} < Y_{\text{TB}}.$$

In equilibrium,  $Z = Y$ . We obtain

$$Y_{\text{eqm}} = \frac{1}{1 - c_1 - b_1 + m_1}(c_0 + b_0 - c_1\bar{T} + \bar{G} + x_1\bar{Y}^*).$$

At trade balance,  $NX = 0$ . We obtain

$$Y_{\text{TB}} = \frac{x_1\bar{Y}^*}{m_1}.$$

Then  $Y_{\text{eqm}} < Y_{\text{TB}}$  implies that

$$m_1 < \frac{(1 - c_1 - b_1)x_1\bar{Y}^*}{c_0 + b_0 - c_1\bar{T} + \bar{G}}.$$

A smaller  $m_1$  reduces the import leakage in the multiplier, which raises equilibrium output  $Y$ . At the same time, because imports are  $IM = m_1Y\epsilon$ , lowering  $m_1$  reduces equilibrium imports even though income is higher. When  $m_1$  is sufficiently small, the resulting import leakage is too weak to offset the export term  $x_1\bar{Y}^*$ , so the home country runs a trade surplus.

5. (a) The  $ZZ$  and  $NX$  lines shift up. Domestic output and domestic net exports increase.
- (b) Domestic investment will increase because output increases. Assuming taxes are fixed and do not respond to income, there is no effect on the deficit.
- (c)  $NX = S - I + T - G$ . Since the budget deficit is unchanged, and  $I$  and  $NX$  increase,  $S$  must increase.
- (d) Except for  $G$  and (for our purposes)  $T$ , the variables in equation (18.5) (in the textbook) are endogenous. An exogenous shock such as an increase in foreign output can affect all of the endogenous variables simultaneously.
6. (a) There must be a real depreciation.

- (b)  $Y = C + I + G + NX$ . If  $NX$  increases while  $Y$  remains,  $C + I + G$  must fall. The government can reduce  $G$  or increase  $T$ , which will reduce  $C$ .

7. (a)

$$Y = C + I + G + X - IM$$

$$Y = c_0 + c_1(Y - T) + d_0 + d_1Y + G + x_1Y^* - m_1Y$$

$$Y = \frac{1}{1 - c_1 - d_1 + m_1} [c_0 - c_1T + d_0 + G + x_1Y^*].$$

- (b) Output increases by the multiplier, which equals  $\frac{1}{1 - c_1 - d_1 + m_1}$ . The condition  $0 < m_1 < c_1 + d_1 < 1$  ensures that the multiplier is defined, positive, and greater than one. As compared to the original multiplier,  $\frac{1}{1 + c_1}$ , there are two additional parameters:  $d_1$ , which captures the effect of an additional unit of income on investment, and  $m_1$ , which captures the effect of an additional unit of income on imports. The investment effect tends to increase the multiplier; the import effect tends to reduce the multiplier.
- (c) When government purchases increase by one unit, net exports fall by  $m_1\Delta Y = \frac{m_1}{1 - c_1 - d_1 + m_1}$ . Note that the change in output is simply the multiplier.
- (d) The larger economy will likely have the smaller value of  $m_1$ . Larger economies tend to produce a wider variety of goods, and therefore to spend more of an additional unit of income on domestic goods than smaller economies do.
- (e) Small economy:  $\Delta Y = 1.1$ ,  $\Delta NX = 0.6$ . Large economy:  $\Delta Y = 2$ ,  $\Delta NX = 0.2$ .
- (f) Fiscal policy has a larger effect on output in the large economy, but a larger effect on net exports in the small economy.

8. (a) It is convenient to wait to substitute for  $G$  until the last step.

$$Y = C + I + G + X - IM = 10 + 0.8(Y - 10) + 10 + G + 0.3Y^* - 0.3Y$$

$$Y = [1/(1 - .8 + 0.3)](12 + G + 0.3Y^*) = 2(12 + G + 0.3Y^*) = 44 + 0.6Y^*$$

When foreign output is fixed, the multiplier is 2 ( $=1/(1-0.8+0.3)$ ). The closed economy multiplier is 5 ( $=1/(1-0.8)$ ). In the open economy, some of an increase in autonomous expenditure falls on foreign goods, so the multiplier is smaller.

- (b) Since the countries are identical,  $Y = Y^* = 110$ . Taking into account the endogeneity of foreign income, the multiplier equals  $\frac{1}{1-0.8-0.3 \times 0.6+0.3} = 3.125$ . The multiplier is higher than the open economy multiplier in part (a) because it takes into account the fact that an increase in domestic income leads to an increase in foreign income (as a result of an increase in domestic imports of foreign goods). The increase in foreign income leads to an increase in domestic exports.
- (c) If  $Y = 125$ , then  $Y^* = 44 + 0.6(125) = 119$ . Using these two facts and the equation  $Y = 2(12 + G + 0.3Y^*)$  yields  $125 = 24 + 2G + 0.6(119)$ , which implies  $G = 14.8$ . In the domestic economy,  $NX = 0.3(119) - 0.3(125) = 1.8$  and  $T - G = 10 - 14.8 = -4.8$ . In the foreign economy,  $NX^* = 1.8$  and  $T^* - G^* = 0$ .
- (d) If  $Y = Y^* = 125$ , then  $125 = 24 + 2G + 0.6(125)$ , which implies  $G = G^* = 13$ . In both countries, net exports are zero, but the budget deficit is 3.
- (e) In part, fiscal coordination is difficult to achieve because of the benefits of doing nothing and waiting for another economy to undertake a fiscal expansion, as indicated from part (c).

### Example 5

- (1) The steps are standard. However, note that  $\epsilon^* = \epsilon^{-1}$ . Therefore, we have the following system:

$$\begin{cases} Y = \frac{1}{1 - c_1 - b_1 - \frac{m_1}{\epsilon}} \left[ c_0 - c_1 + b_0 + 1 - m_2 + x_1 \frac{Y^*}{\epsilon} \right] \\ Y^* = \frac{1}{1 - c_1 - b_1 - m_1 \epsilon} [c_0 - c_1 + b_0 + 1 - m_2 + x_1 Y \epsilon] \end{cases}$$

(2) Example 4 part (2) derives the general ML condition:

$$\left( \frac{\Delta\epsilon}{\epsilon} - \frac{\Delta IM}{IM} \right) \frac{IM/\epsilon}{X} + \frac{\Delta X}{X} > 0.$$

Plugging in the number, we have

$$LHS = [-0.5\% - (-2\%)] \times \frac{1}{2} + 3\% = 3.75\% > 0.$$

The ML condition holds.

(3) Note that  $\frac{X}{IM/\epsilon} = 2$  and hence  $\frac{IM^*/\epsilon^*}{X^*} = \frac{X \cdot \epsilon}{IM} = \frac{X}{IM/\epsilon} = 2$ . Therefore, we have the following system:

$$\begin{cases} x_1 Y^* = m_1 Y + m_2 \epsilon \\ x_1 Y = m_1 Y^* + m_2 \epsilon^{-1} \end{cases}$$

Solving this yields

$$\begin{cases} Y = m_2 \left[ \frac{\epsilon m_1 - x_1/\epsilon}{x_1^2 - m_1^2} \right] \\ Y^* = m_2 \left[ \frac{\epsilon x_1 - m_1/\epsilon}{x_1^2 - m_1^2} \right] \end{cases}$$

### Example 6

(1) The steps are standard. We obtain

$$\begin{cases} Y = \frac{1}{1 - c_1 - b_1 - \frac{\lambda^* m_1}{\epsilon}} \left[ c_0 - c_1 + b_0 + 1 - m_2 + \lambda x_1 \frac{Y^*}{\epsilon} \right] \\ Y^* = \frac{1}{1 - c_1 - b_1 - \lambda m_1 \epsilon} [c_0 - c_1 + b_0 + 1 - m_2 + \lambda^* x_1 Y \epsilon] \end{cases}$$

(2) By definition,  $NX = X - \frac{IM}{\epsilon}$ . Substituting this economy, we obtain

$$NX = \frac{1}{\epsilon} (\lambda^* x_1 Y^* - \lambda m_1 Y) - m_2.$$

Since an decrease in  $\epsilon$  leads to an increase in  $NX$ , it must be such that

$$\lambda^* x_1 Y^* - \lambda m_1 Y > 0,$$

which is the sufficient and necessary condition shown in the question.

On the other hand, this equation is equivalent to say

$$NX > -m_2.$$

- $\lambda$  (Home tradable share, *export side*): scales the export term  $\lambda x_1 Y^* / \epsilon$ . Larger  $\lambda$  makes (ML) easier to satisfy and raises  $NX$  for any  $\epsilon$ . If  $\lambda = 0$ , exports vanish, (ML) fails, and a depreciation cannot raise  $NX$ .
- $\lambda^*$  (Foreign tradable share, *import side*): scales the income-driven import term  $\lambda^* m_1 Y / \epsilon$ . Larger  $\lambda^*$  makes (ML) harder to satisfy and lowers  $NX$ . If  $\lambda^* = 0$ , income-driven imports vanish, (ML) holds trivially, and a depreciation raises  $NX$ .
- $m_2$  (FX-sensitive autonomous imports): level shifter. It does not enter (ML) and does not affect the sign of  $\frac{dNX}{d\epsilon}$  when  $Y, Y^*$  are held fixed; it only reduces the level of  $NX$  by 1-for-1. Changing  $m_2$  never alters whether a depreciation helps  $NX$  (it only shifts the  $NX(\epsilon)$  schedule vertically).

(3) (i)  $Y = Y^* = 4.29$ .

(ii)  $NX = 0.16$ .  $NX > -m_2 = -0.1$ , so the ML condition holds.

(iii)  $Y = 4.36$ ,  $Y^* = 4.18$ .  $NX = 0.17$ . Home output rises, Foreign falls, and  $NX$  increases, consistent with ML.

(iv)  $Y = 3.89$ ,  $Y^* = 4.38$ .  $NX = 0.08$ . Lower  $\lambda$  (smaller tradable share of Home) tightens export capacity. As a result,  $Y$  is lower and net export is weaker. At the same time, Foreign output rises.