

# EXAMINATION

**Please complete the following :**

Course Code : ECON 3123

Course Title : Macroeconomic theory (I)

Date of Examination : 10-10-2025

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I confirm that I have answered the questions using only materials specifically approved for use in this examination, that all the answers are my own work, and that I have not received any assistance during the examination.

Student's Signature :

## *Answer Book*

### **Instructions :**

1. Write your answers on the **RIGHT-HAND** page. Use the left-hand page only for rough work. Any work that appears on the left-hand page will **NOT** be marked.
  2. Begin **EACH** question on a **NEW** page. Write down the question number at the top of each page.
  3. No supplementary sheets may be submitted, unless allowed by the examiner.
  4. No part of this answer book is to be taken away from the examination.

Enter the question numbers below in the **SAME ORDER** as you have answered the questions :

No. of answer books used : \_\_\_\_\_ 1

checked by Yang Lu

MC

1. ~~B~~

2. P

3. ~~B~~

4. D

5. ~~D~~

8

Q6

(a) In equilibrium,  $S = Y = C + I + G$ .

$$Y = c_0 + c_1(Y - T) + b_0 + b_1Y - b_2\bar{I} + \bar{G}$$

$$Y = c_0 + c_1(Y - t_0 - t_1Y) + b_0 + b_1Y - b_2\bar{I} + \bar{G}$$

$$Y = c_0 + c_1(1 - t_1)Y - c_1t_0 + b_0 + b_1Y - b_2\bar{I} + \bar{G}$$

$$[1 - b_1 - c_1(1 - t_1)]Y = c_0 - c_1t_0 + b_0 - b_2\bar{I} + \bar{G}$$

$$Y = \frac{1}{1 - b_1 - c_1(1 - t_1)} [c_0 - c_1t_0 + b_0 - b_2\bar{I} + \bar{G}]$$

Since  $T = t_0 + t_1Y$ , the equilibrium tax is given by

$$T = t_0 + \frac{t_1}{1 - b_1 - c_1(1 - t_1)} [c_0 - c_1t_0 + b_0 - b_2\bar{I} + \bar{G}]$$

(b) To keep the budget balanced, the government should decrease  $G$  so that it equals  $T$  by  $\frac{t_1}{1 - b_1 - c_1(1 - t_1)}$  times. From part (a), we see that  $Y = c_0 + c_1(Y - T) + b_0 + b_1Y - b_2\bar{I} + \bar{G}$ , if  $G = T$ , then the overall output  $Y$  will decrease by  $(1 - c_1)$  times of  $G$ . Since a drop in  $b_0$  decreases output  $Y$ , this ~~adjustment~~ in  $G$  strengthens the effect of drop of  $b_0$ .

(c) Since private saving  $S_p = Y - T - C$ ,

$$S_p = Y - (t_0 + t_1Y) - [c_0 + c_1(Y - T)]$$

$$S_p = Y - t_0 - t_1Y - [c_0 + c_1(Y - t_0 - t_1Y)]$$

$$S_p = Y - t_0 - t_1Y - c_0 - c_1(1 - t_1)Y + c_1t_0$$

$$S_p = (1 - t_1)Y - t_0 - c_0 - c_1(1 - t_1)Y + c_1t_0$$

$$S_p = (1 - c_1)(1 - t_1)Y - t_0 - c_0 + c_1t_0$$

This means when  $Y \downarrow$  after adjusting  $G$ , the equilibrium private saving also  $\downarrow$ .

Q7

(a) In equilibrium,  $Y = C + I + G$ , so we have

$$Y = 0.5 + 0.2(Y - T) + 0.2 + 0.3Y - 2.5(i + x) + G$$

Substitute  $T = 1$ ,  $G = 1$ ,  $x = 5\%$ .

$$Y = 0.5 + 0.2(Y - 1) + 0.2 + 0.3Y - 2.5(i + 0.05) + 1$$

$$Y = 0.5 + 0.2Y - 0.2 + 0.2 + 0.3Y - 2.5i - 0.125 + 1$$

$$0.5Y = 1.375 - 2.5i$$

10

$$Y = 2.75 - 5i$$

(b) When  $i = \bar{i} = 5\%$ ,  $Y = 2.75 - 5 \cdot 0.05 = 2.5$

As GDP deflator = 2, nominal income  $\$Y = 2.5 \cdot 2 = 5$

$M^d$  at equilibrium =  $5 \cdot (0.7 - 4 \cdot 0.05) = 2.5$

Therefore, we require  $M^s = M^d = 2.5$

Given  $C = 0.2$ ,  $\theta = 0.25$ , the money multiplier is given by

$$\frac{C + (1 - C)\theta}{1 - C\theta} = 2.5$$

The required monetary base is  $H^s = \frac{M^s}{\text{money multiplier}} = 1$

(c) Since  $Y$  and  $i = \bar{i}$  do not change,  $M^s$  is still 2.5

The new money multiplier =  $\frac{1}{0.2 + 0.8 \cdot 0.3} = \frac{1}{0.2 + 0.24} = \frac{1}{0.44} = \frac{25}{11}$ , given  $\theta = 0.3$ .

The new monetary base will be  $H^s = \frac{M^s}{\text{new money multiplier}} = \frac{2.5}{\frac{25}{11}} = 1.1$

(d) Change in  $x$  affects output  $Y$ , hence from (a), with  $i = \bar{i} = 5\%$

$$Y = 0.5 + 0.2(Y - 1) + 0.2 + 0.3Y - 2.5(i + 0.15) + 1$$

$$0.5Y = 1.125 - 2.5(0.05)$$

$$Y = 2$$

The new nominal income  $\$Y = 2 \cdot 2 = 4$

$$\text{New } M^s = 4 \cdot (0.7 - 4 \cdot 0.05) = 2$$

So the new monetary base  $H^s = \frac{M^s}{\text{money multiplier}}$ , where

money multiplier =  $\frac{25}{11}$  from (b)

$$H^s = \frac{2}{\frac{25}{11}} = 0.88$$

Q8

(a) Current price of the 2-year bond is given by

$$PV_2 = \frac{100}{(1+i+r)(1+i^e)}$$

$$= \frac{100}{(1+4\%+5\%)(1+3\%)}$$

$$= \$89.07 \quad (\text{cor to 5 sig.fig})$$

(b) Similarly, current price of 3-year bond is given by

$$PV_3 = \frac{100}{(1+i+r)(1+i^e+r)(1+i^e)}$$

$$= \frac{100}{(1+4\%+5\%)(1+3\%+5\%)(1+2\%)}$$

$$= \$83.282 \quad (\text{cor to 5 sig.fig})$$

(c) To calculate the current yield, we let current yield be  $i_c$ .

$$\text{Since } PV_3 = 83.282 = \frac{100}{(1+i_c)^3}$$

$$(1+i_c)^3 = \frac{100}{83.28}$$

$$i_c = 6.2878\% \quad (\text{cor to 5 sig.fig})$$

The current yield of the bond is 6.2878%

Y