ECON 3123: Macroeconomic Theory I

Tutorial Note 8: IS-LM-PC Framework

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Deriving the PC Relation

To put IS-LM and PC together, we need either interest rate or output appear in the PC relation. By this, we mean that we would like to derive a step further from the Phillips curve so that, obviously easier to show, output appears.

Recall that the production function is

$$Y_t = AN_t$$

where Y_t is the output, A is the productivity, and N_t is the labour force, and that unemployment rate u_t is defined to be

$$u_t = \frac{L - N_t}{L},$$

where L is total labour force minus discouraged worker. Hence,

$$u_t = 1 - \frac{1}{A} \frac{Y_t}{L} \iff Y_t = AL(1 - u_t).$$

We can thus define the natural level of employment, N_n , and the natural level of output, Y_n :

$$N_n = L(1 - u_n), Y_n = AL(1 - u_n),$$

where u_n is the natural rate of unemployment.

Then we can rewrite the Phillips Curve equation to obtain the **PC relation**:

$$\pi_t - \pi_t^e = -\alpha(u_t - u_n)$$

$$= -\alpha \left[\left(1 - \frac{1}{A} \frac{Y_t}{L} \right) - \left(1 - \frac{1}{A} \frac{Y_n}{L} \right) \right]$$

$$= \frac{\alpha}{AL} (Y_t - Y_n).$$

Figure 1 demonstrates how a PC curve looks like in a $(Y, \pi - \pi^e)$ diagram. From the mathematical formulation, we know that the line must pass $(Y_n, 0)$. This is supported

by economics: when the market is in medium-run equilibrium, inflation expectation matches the true inflation, and the output is at the natural level. Let $\pi^e = \bar{\pi}$, the targeted inflation. Then in this diagram, the corresponding output Y_t is larger than the natural level. In this case $N_t > N_n$, and $u_t < u_n$.

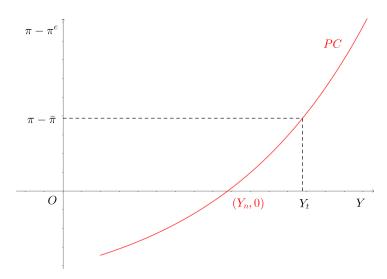


Figure 1: PC Relation

Neutrality of Money

With the medium run framework to be introduced, we are able to find the role of money in an economy. In short, in the medium run, real variables are *not* affected by the monetary policy (money supply), but only the inflation and nominal interest rate.

IS-LM-PC Framework The IS-LM framework is one for short run, and the labour market will be at the equilibrium in the medium run. Therefore, the key point is to make out how the economy changes in the process from short run to the long run.

The following figure 2 illustrates how the equilibrium moves from the short run to the medium run. Initially, in the short run (IS-LM), we have equilibrium (Y^*, r) . Assume that the central bank does not change the interest rate. Then the labour market (PC) indicates that the inflation is higher than the targeted rate. Therefore, the

central bank will, at some point, adjusts the monetary policy (say, cutting money supply) so that the real interest rate increases. It will reach a point where the equilibrium output in the IS-LM diagram matches the natural level of output derived in the labour market equilibrium. The corresponding real interest rate is thus called the natural/neutral/Wicksellian rate of interest.

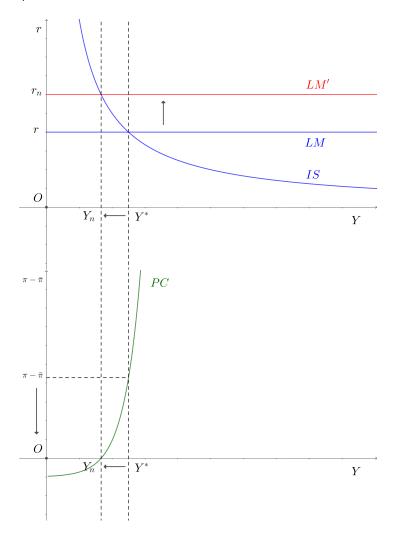


Figure 2: IS-LM-PC Framework

Money Market Equilibrium Recall that the money demand function is

$$\frac{M_t^d}{P_t} = Y_t L(r_t + \pi_{t+1}^e)$$

where L is a decreasing function of $i_t = r_t + \pi_{t+1}^e$. At medium-run equilibrium,

$$M = M^d = M^s,$$
$$Y = Y_n,$$

$$r = r_n$$
, and

$$\pi = \pi^e = \bar{\pi}.$$

Therefore, the equilibrium money supply is

$$\frac{M}{P} = Y_n L(r_n + \bar{\pi}).$$

Note that the RHS is just a constant. Hence, the real equilibrium money supply is a number. Therefore, money and price must grow at the same rate, *i.e.*,

$$\pi = g_M$$
.

Then we know that any monetary policy (changing money supply) can only affect the inflation, and thus the nominal interest rate in the medium run. Real variables are not affected. This is called the **neutrality of money**. In PhD Macroeconomics, you will know that if we bring labour-leisure tradeoff into the system, money will not be neutral any more.