# Parallelizing Dijkstra algorithm

Project Report in Parallel Systems

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### 1. Introduction

Given a graph, let G=(V,E) be a directed graph where |V|=n, |E|=m, let s be a distinguished vertex of the graph, and w be the non-negative value to the weight of each edge, which represents the distance between the two vertexes.

In graph theory, the purpose of Dijkstra's algorithm is to find the shortest path between the given source vertex *s* and all other vertices in the graph. You can apply this algorithm in different fields, for example, road networks or everything that is convertible in a graph.

Based on the algorithm, we build a routing table (Table 1) for node s as described in the example below (Figure 1), where the highlighted cells show the minimum weighted distance. The sequential implementation of the Dijkstra algorithms is in Figure 2.

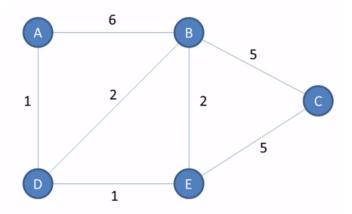


Figure 1: Graph example

	В	С	D	E
Α	6	00	1	00
AD	3	7		2
ADE	4	7		
ADEB		9		

Table 1: Routing table example

# 2. PARALLEL APPROACH

The sequential implementation of the Dijkstra algorithm has some disadvantages. For instance, if the graph increases in

```
void dijkstra(std::vector<Node> &start){
   std::priority_queue<Node, std::vector<Node>, std::less<> > queue;
    queue.push(start[0]); //start enters the queue
   while(!queue.empty()){
       Node current = queue.top():
                                     //get first node
        queue.pop(); //removes first node
        for(long unsigned int i = 0;i<current.out.size();++i){
            Node* destination node;
            for (Node &tmp: start) {
               if (strncmp(current.out[i].otherNode, tmp.name.c_str(), 21) == 0) {
                    destination node = &tmp;
            unsigned long long int tmpDistance = current.distance+current.out[i].weight;
            if(tmpDistance<destination_node->distance){
                destination node->distance = tmpDistance
                queue.push(*destination_node);
```

Figure 2: Dijkstra algorithm

size, the sequential program may require much more time, which is a problem for time-sensitive applications.

As a solution to address this problem, we propose a parallelization of the algorithm using a *farm/worker* architecture with the help of Boost MPI and *multi-threading* with OpenMP. Workers and Emitter use the message passing paradigm to communicate and broadcast node-related information. The emitter cycle is done in parallel using multiprocessing.

Each processor p[0,k] will receive from the Emitter one by one a subgroup of edges of size  $\delta = V/k$ , some integer values needed to calculate the distance, and calculates the distance from the starting node. If the calculated distance is lower than the one stored in the collector, the processor p will send the new result to the collector. This process will continue until every vertex is scanned and every edge is checked.

## A. Theoretical performance

The processors will go through every edge of the graph inside their assigned subgroup. The running time is estimated to be  $\Theta(V/k)$ . Moreover, if the distance calculated is lower, each processor p communicate its result to the collector. Then, in the worst case scenario, the running time will be  $\Theta(V)$ . Other operations such as replacing the previous values should take time  $\Theta(1)$ . Therefore, the span of our theoretical solution is:

$$t(V, E, k) = \Theta(V/k) + \Theta(V) + \Theta(1) \tag{1}$$

However, in the practical solution, we observe that the time complexity is  $\Theta(V^2 + V/k)$  because of the message passing

that makes the software relatively slower. The worker has to call for other functions in the middle of the execution and wait for them to respond. For the sequential algorithm, on the other hand, the estimated time complexity is  $\Theta(V^2)$ .

Hence, after comparing the running times, we concluded that the parallel algorithm cannot be faster in these conditions. Additionally, the running time of this algorithm depends on the number of nodes and the graph edges. We randomize the graph generation and the edge quantity. Because of this, we have no control over the results we get, and our calculations are pretty rough.

### 3. IMPLEMENTATION

This implementation is not optimal as the parallel algorithm does not always find the best path. We know that the sequential version always finds the optimal way. We test the output of the two codes, sequential and parallel, looking if they are equal, and, as shown by the keyword "False", the two results are not the same, meaning that the parallel does not always find the optimal route. We can say that this happens due to parallelization and read/write concurrency. As an example, we can take two different vertices that have an edge that goes to the same vertex, both may do the check at the same moment, and in both cases, it may evaluate to true. Since workers are not atomic, the worker who assigned the distance as last will have its value stored in the final graph.

The approach explained in Section 2 is implemented as depicted in Figure 3 and the results are shown in Figure 4.

# 4. EXPERIMENTS

We conducted some tests on four processors, with two threads per processor, for the sequential and parallel implementation. We tested the code using graphs of different sizes V.

The sequential version is faster than the parallel one. For example, it takes only 1 ms to evaluate a graph with 60 nodes. The parallel version is relatively slow. Because of that, we stopped the evaluation at 150 nodes. We believe that the results are still quite descriptive.

It might look like the parallel version does not follow any rising function, as the time needed is lower for 90 nodes rather than 80 nodes. That is due to the uncontrollable randomization factor used during the graph creation that prevents a well-connected graph.

Table 2 represents the results.

## 5. References

- Github repository of the project, [Online]. Available: https://github.com/HarlockOfficial/dva336\_labs/tree/ main/Project, Accessed 2021-01-20
- Djikstra algorithm page on Wikipedia, [Online]. Available: https://en.wikipedia.org/wiki/Dijkstra%27s\_algorithm, Accessed 2021-01-20
- Boost Mpi library documentation, [Online]. Available: https://www.boost.org/doc/libs/1\_75\_0/doc/html/mpi. html, Accessed 2021-01-20

```
oid dijkstra_emitter(std::vector<Node> &start, boost::mpi::communicator world){
     std::priority queue<Node, std::vector<Node>, std::less<> > queue:
     queue.push(start[0]); //start enters the queu
      while(!queue.empty()){
         Node current = queue.top():
                                        //qet first node
         queue.pop(); //removes first node
         unsigned long long int current_distance = current.distance;
         #pragma omp parallel for
         for(int i=0;i<current.out.size();++i){ // NOLINT(modernize-loop-convert)</pre>
             int free_worker_id;
             unsigned long long int destination_distance;
             for (const Node &tmp: start) {
                 if (strncmp(current.out[i].otherNode, tmp.name.c_str(), 21) == 0) {
                     destination_distance = tmp.distance;
                 }
             #pragma omp critical
                 world.recv(boost::mpi::any_source, FREE_WORKER_TAG, free_worker_id);
                 current.out[i].send(world, free_worker_id, ASSIGN_WORK_TAG);
                 world.send(free_worker_id, ASSIGN_WORK_TAG, current_distance)
                 world.send(free worker id, ASSIGN WORK TAG + 1, destination distance);
             Edge e = Edge::irecv(world, boost::mpi::any_source, WORKER_TO_COLLECTOR_TAG);
             if(strcmp(e.parentNode,"exit_empty")==0 || strcmp(e.otherNode, "exit_empty")==0){
             unsigned long long int current_destination_node_distance;
            world.recv(e.edge_src, WORKER_TO_COLLECTOR_TAG+1, current_destination_node_distance);
            for(auto & i : start){
                if(strcmp(i.name.c str(), e.otherNode)==0){
                    i.distance = current_destination_node_distance;
                    queue.push(i);
                    break:
   Edge e{};
    strncpy(e.parentNode, "exit", 21);
   strncpy(e.otherNode, "exit", 21);
   for(int worker_id = SPLITTER_ID+1; worker_id<THREAD_COUNT;++worker_id){</pre>
       e.send(world, worker_id, ASSIGN_WORK_TAG);
void dijkstra_worker(const std::vector<Node>& graph, boost::mpi::communicator world){
   while(true){
       //notify that worker is free
        world.send(SPLITTER_ID, FREE_WORKER_TAG, world.rank());
        Edge e = Edge::recv(world, SPLITTER_ID, ASSIGN_WORK_TAG);
        //will happen only in the end
       if(strcmp(e.parentNode, "exit")==0){
       unsigned long long int node_distance;
        unsigned long long int destination_node_distance;
       world.recv(SPLITTER_ID, ASSIGN_WORK_TAG, node_distance);
world.recv(SPLITTER_ID, ASSIGN_WORK_TAG+1, destination_node_distance);
          unsigned long long int tmpDistance = node_distance+e.weight;
          if (tmpDistance < destination node distance) {
              Edge tmpOut{};
               destination_node_distance = tmpDistance
               strcpy(tmpOut.parentNode, e.parentNode);
               strcpy(tmpOut.otherNode, e.otherNode);
               tmpOut.weight = e.weight;
               tmpOut.send(world, SPLITTER ID, WORKER TO COLLECTOR TAG);
               world, send(SPLITTER ID, WORKER TO COLLECTOR TAG + 1, destination node distance):
```

Figure 3: Parallelization of Dijkstra algorithm

4) OpenMP API, [Online]. Available: https://www.openmp.org/wp-content/uploads/
 OpenMP-API-Specification-5-1.pdf, Accessed 2021-01-20

	Sequential algorithm	Parallel algorithm
Number of	Time in milliseconds	
nodes		
10	0	1649
20	0	2177
30	0	6799
40	0	11946
50	0	19122
60	1	26630
70	2	167370
80	3	593498
90	3	110600
100	5	440518
110	7	769909
120	8	2257315
130	10	6706111
140	13	8767596
150	15	17144207

Table 2: Results of the sequential and parallel algorithm

admir		alBox:~/Desktop/dva336_labs/Project\$ ./test_code.py
node		1649 milliseconds sequential dijkstra: 0 milliseconds output equals: False
node		2177 milliseconds sequential dijkstra: 0 milliseconds output equals: False
node		6799 milliseconds sequential dijkstra: 0 milliseconds output equals: False
node		11948 milliseconds sequential dijkstra: 0 milliseconds output equals: False
node		19122 milliseconds sequential dijkstra: 0 milliseconds output equals: False
node		26630 milliseconds sequential dijkstra: 1 milliseconds output equals: False
node		167370 milliseconds sequential dijkstra: 2 milliseconds output equals: False
node		593498 milliseconds sequential dijkstra: 3 milliseconds output equals: False
node		110600 milliseconds sequential dijkstra: 3 milliseconds output equals: False
node		: 440518 milliseconds sequential dijkstra: 5 milliseconds output equals: False
node		: 769909 milliseconds sequential dijkstra: 7 milliseconds output equals: False
node		: 2257315 milliseconds sequential dijkstra: 8 milliseconds output equals: False
node		: 6706111 milliseconds sequential dijkstra: 10 milliseconds output equals: False
node		: 8767596 milliseconds sequential dijkstra: 13 milliseconds output equals: False
node	150 parallel diikstra	: 17144207 milliseconds sequential diikstra: 15 milliseconds output equals: False

Figure 4: Results of the experiments in Command Prompt