PRIMME

large-scale eigenvalue and singular value solver

Documentation

Release 2.2

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CHAPTER

ONE

PRIMME: PRECONDITIONED ITERATIVE MULTIMETHOD EIGENSOLVER

PRIMME, pronounced as *prime*, computes a few eigenvalues and their corresponding eigenvectors of a real symmetric or complex Hermitian matrix. It can also compute singular values and vectors of a square or rectangular matrix. It can find largest, smallest, or interior singular/eigenvalues and can use preconditioning to accelerate convergence. It is especially optimized for large, difficult problems, and can be a useful tool for both non-experts and experts. PRIMME is written in C99, but complete interfaces are provided for Fortran 77, MATLAB, Python, and R.

1.1 Incompatibilities

From PRIMME 2.0 to 2.1:

- Added members monitorFun and monitor to primme_params.
- Added members monitorFun and monitor to primme_svds_params.
- Renamed PRIMME_SUBSPACE_ITERATION as PRIMME_STEEPEST_DESCENT.

From PRIMME 1.x to 2.0:

- Prototype of callbacks has changed: matrixMatvec, applyPreconditioner, massMatrixMatvec and globalSumReal.
- The next parameters are PRIMME_INT: n, nLocal, maxMatvecs, iseed, numOuterIterations, numRestarts, numMatvecs and numMatvecs; use the macro PRIMME_INT_P to print the values.
- \bullet Rename the values of the enum ${\it primme_preset_method}.$
- Rename primme_Free to primme_free().
- Integer parameters in Fortran functions are of the same size as PRIMME_INT, which is integer *8 by default.
- Extra parameter in many Fortran functions to return the error code.
- Removed primme_display_stats_f77.

1.2 Changelog

Changes in PRIMME 2.2 (released on October 26, 2018):

- Improved stability for single precision.
- Improved support for the shared library.
- Updated PETSc examples in Fortran; added new examples in single precision.
- Improved support for FreeBSD and MacOS.
- · New install and uninstall actions.
- MATLAB interface support for user-defined stopping criterion (see convTestFun and convTestFun) and stopping with ctr+c.
- Optional suffix on BLAS/LAPACK function names (for OpenBLAS, see PRIMME_BLAS_SUFFIX).
- Replaced XHEGV by XHEGVX (to support ESSL).
- Fixed bugs in the library and in the Matlab interface.

Changes in PRIMME 2.1 (released on April 4, 2017):

- Improved robustness by broadcasting the result of critical LAPACK operations instead of replicating them on
 every process; this is useful when using a threaded BLAS/LAPACK or when some parallel processes may run
 on different architectures or libraries.
- New stopping criteria in QMR that improve performance for interior problems.
- MATLAB interface reimplementation with support for singular value problems, primme_svds(), with double and single precision, and compatible with Octave.
- · R interface
- Proper reporting of convergence history for singular value solvers.

Changes in PRIMME 2.0 (released on September 19, 2016):

- Changed license to BSD 3-clause.
- New support for singular value problems; see dprimme_svds ().
- New support for float and complex float arithmetic.
- Support for problem dimensions larger than 2³¹, without requiring BLAS and LAPACK compiled with 64-bits integers.
- Improve robustness and performance for interior problems; implemented advanced refined and harmonic-Ritz extractions.
- Python interface compatible with NumPy and SciPy Library.
- Added parameter to indicate the leading dimension of the input/output matrices and to return an error code in callbacks matrixMatvec, applyPreconditioner, massMatrixMatvec and globalSumReal.
- Changed to type PRIMME_INT the options n, nLocal, maxMatvecs and iseed, and the stats counters numOuterIterations, numRestarts, numMatvecs, numPreconds. Also changed realWorkSize to size_t. Fortran interface functions will expect an interger of size compatible with PRIMME_INT for all parameters with integer type: int, PRIMME_INT and size_t; see also parameter value in functions primmetop_set_member_f77(), primmetop_get_member_f77(), primme_set_member_f77() and primme_get_member_f77().

1.2. Changelog 3

- Added parameter to return an error code in Fortran interface functions: primmetop_set_member_f77(), primmetop_get_member_f77(), primme_set_member_f77() and primme get member f77().
- Added leading dimension for evecs ldevecs and preferred leading dimension for the operators ldOPs, such
 as matrixMatvec.
- Optional user-defined convergence function, convTestFun.
- Prefixed methods with PRIMME_. Rename Fortran constants from PRIMMEF77_ to PRIMME_.
- Removed primme_display_stats_f77.

Changes in PRIMME 1.2.2 (released on October 13, 2015):

- Fixed wrong symbols in libdprimme.a and libzprimme.a.
- primme_set_method() sets PRIMME_JDQMR instead of PRIMME_JDQMR_ETo1 for preset methods PRIMME_DEFAULT_MIN_TIME and PRIMME_DYNAMIC when seeking interior values.
- Fixed compilation of driver with a PETSc installation without HYPRE.
- Included the content of the environment variable INCLUDE for compiling the driver.

Changes in PRIMME 1.2.1 (released on September 7, 2015):

- Added MATLAB interface to full PRIMME functionality.
- Support for BLAS/LAPACK with 64bits integers (-DPRIMME_BLASINT_SIZE=64).
- Simplified configuration of Make_flags and Make_links (removed TOP variable and replaced defines NUM_SUM and NUM_IBM by F77UNDERSCORE).
- Replaced directories DTEST and ZTEST by TEST, that has:
 - driver.c: read matrices in MatrixMarket format and PETSc binary and call PRIMME with the parameters specified in a file; support complex arithmetic and MPI and can use PETSc preconditioners.
 - ex*.c and ex*.f: small, didactic examples of usage in C and Fortran and in parallel (with PETSc).
- Fixed a few minor bugs and improved documentation (especially the F77 interface).
- Using Sphinx to manage documentation.

Changes in PRIMME 1.2 (released on December 21, 2014):

- A Fortran compiler is no longer required for building the PRIMME library. Fortran programs can still be linked to PRIMME's F77 interface.
- Fixed some uncommon issues with the F77 interface.
- PRIMME can be called now multiple times from the same program.
- Performance improvements in the QMR inner solver, especially for complex arithmetic.
- Fixed a couple of bugs with the locking functionality.
 - In certain extreme cases where all eigenvalues of a matrix were needed.
 - The order of selecting interior eigenvalues.

The above fixes have improved robustness and performance.

- PRIMME now assigns unique random seeds per parallel process for up to 4096^3 (140 trillion) processes.
- For the PRIMME_DYNAMIC method, fixed issues with initialization and synchronization decisions across multiple processes.

• Fixed uncommon library interface bugs, coordinated better setting the method and the user setting of parameters, and improved the interface in the sample programs and makefiles.

• Other performance and documentation improvements.

1.2. Changelog 5

1.3 License Information

PRIMME is licensed under the 3-clause license BSD. Python and MATLAB interfaces have BSD-compatible licenses. Source code under tests is compatible with LGPLv3. Details can be taken from COPYING.txt:

Copyright (c) 2018, College of William & Mary All rights reserved.

1.4 Citing the code

Please cite [r1] and [r6]. Find the BibTeX in the following and also in doc/primme.bib:

```
@Article { PRIMME,
  author =
                 {Andreas Stathopoulos and James R. McCombs},
  title =
                 {{PRIMME}: {PR}econditioned {I}terative {M}ulti{M}ethod
                {E}igensolver: Methods and software description},
  journal =
                {ACM Transactions on Mathematical Software},
  volume =
               {37},
  number =
              {2},
                {2010},
  year =
  pages =
               {21:1--21:30},
@Article{svds_software,
  author = {Lingfei Wu and Eloy Romero and Andreas Stathopoulos},
            = {PRIMME{\_}SVDS: {A} High-Performance Preconditioned {SVD} Solver for
               Accurate Large-Scale Computations },
  journal
           = {SIAM Journal on Scientific Computing},
  volume
            = \{39\},
           = \{5\},
  number
           = \{S248 - -S271\},
  pages
           = \{2017\},
  year
           = \{10.1137/16M1082214\},
           = { https://doi.org/10.1137/16M1082214 },
```

More information on the algorithms and research that led to this software can be found in the rest of the papers [r2], [r3], [r4], [r5], [r7]. The work has been supported by a number of grants from the National Science Foundation.

1.5 Contact Information

For reporting bugs or questions about functionality contact Andreas Stathopoulos by email, *andreas* at *cs.wm.edu*. See further information in the webpage http://www.cs.wm.edu/~andreas/software and on github.

1.6 Directory Structure

The next directories and files should be available:

- COPYING.txt, license;
- Make_flags, flags to be used by makefiles to compile library and tests;
- Link_flags, flags needed in making and linking the test programs;
- include/, directory with headers files;
- src/, directory with the source code for libprimme:
 - include/, common headers;
 - eigs/, eigenvalue interface and implementation;
 - svds/, singular value interface and implementation;
 - tools/, tools used to generated some headers;
- Matlab/, MATLAB interface;
- Python/, Python interface;
- examples/, sample programs in C, C++ and F77, both sequential and parallel;
- tests/, drivers for testing purpose and test cases;
- lib/libprimme.a, the PRIMME library (to be made);
- makefile main make file;
- readme.txt text version of the documentation;
- doc/ directory with the HTML and PDF versions of the documentation.

1.7 Making and Linking

Make_flags has the flags and compilers used to make libprimme.a:

- *CC*, compiler program such as qcc, clang or icc.
- CFLAGS, compiler options such as -g or -O3 and macro definitions like the ones described next.

Compiler flags for the BLAS and LAPACK libraries:

- -DF77UNDERSCORE, if Fortran appends an underscore to function names (usually it does).
- -DPRIMME_BLASINT_SIZE=64, if the library integers are 64-bit integer (kind=8) type, aka ILP64 interface; usually integers are 32-bits even in 64-bit architectures (aka LP64 interface).
- -DPRIMME_BLAS_SUFFIX=<suffix>, set a suffix to BLAS/LAPACK function names; for instance, Open-Blas compiled with ILP64 may append _64 to the function names.

By default PRIMME sets the integer type for matrix dimensions and counters (PRIMME_INT) to 64 bits integer int64_t. This can be changed by setting the macro PRIMME_INT_SIZE to one of the following values:

- 0: use the regular int of your compiler.
- 32: use C99 int32_t.
- 64: use C99 int 64_t.

Note: When <code>-DPRIMME_BLASINT_SIZE=64</code> is set the code uses the type <code>int64_t</code> supported by the C99 standard. In case the compiler doesn't honor the standard, you can set the corresponding type name supported, for <code>instance-DPRIMME_BLASINT_SIZE=__int64</code>.

After customizing Make_flags, type this to generate libprimme.a:

```
make lib
```

Making can be also done at the command line:

```
make lib CC=clang CFLAGS='-03'
```

Link_flags has the flags for linking with external libraries and making the executables located in examples and tests:

- LDFLAGS, linker flags such as -framework Accelerate.
- *LIBS*, flags to link with libraries (BLAS and LAPACK are required), such as -lprimme -llapack -lblas -lqfortran -lm.

After that, type this to compile and execute a simple test:

```
$ make test
...
Test passed!
...
Test passed!
```

In case of linking problems check flags in *LDFLAGS* and *LIBS* and consider to add/remove -DF77UNDERSCORE from *CFLAGS*. If the execution fails consider to add/remove -DPRIMME_BLASINT_SIZE=64 from *CFLAGS*.

Full description of actions that make can take:

• make lib, builds the static library libprimme.a.

- make solib, builds the shared library libprimme.so.
- make install, installs header files and the static and dynamic libraries.
- make uninstall, uninstalls header files and the static and dynamic libraries.
- make matlab, builds libprimme.a compatible with MATLAB and the MATLAB module.
- make octave, builds libprimme.a and the Octave module.
- make python, builds libprimme.a and the Python module.
- make python_install, install the Python module.
- make R_install, builds and installs the R package.
- make test, build and execute simple examples.
- *make clean*, removes all *.o, a.out, and core files from src.

1.7.1 Considerations using an IDE

PRIMME can be built in other environments such as Anjuta, Eclipse, KDevelop, Qt Creator, Visual Studio and XCode. To build the PRIMME library do the following:

- 1. Create a new project and include the source files under the directory src.
- 2. Add the directories include and src/include as include directories.

To build an example code using PRIMME make sure:

- to add a reference for PRIMME, BLAS and LAPACK libraries;
- to add the directory include as an include directory.

1.8 Tested Systems

PRIMME is primary developed with GNU gcc, g++ and gfortran (versions 4.8 and later). Many users have reported builds on several other platforms/compilers:

- SUSE 13.1 & 13.2
- CentOS 6.6
- Ubuntu 18.04
- MacOS X 10.9 & 10.10
- Cygwin & MinGW
- Cray XC30
- FreeBSD 11.2

1.9 Main Contributors

- James R. McCombs
- Eloy Romero Alcalde
- Andreas Stathopoulos
- Lingfei Wu

1.9. Main Contributors

CHAPTER

TWO

EIGENVALUE PROBLEMS

2.1 C Library Interface

The PRIMME interface is composed of the following functions. To solve real symmetric and Hermitian standard eigenproblems call respectively:

PRIMME stores its data on the structure primme_params. See Parameters Guide for an introduction about its fields.

2.1.1 Running

To use PRIMME, follow these basic steps.

1. Include:

```
#include "primme.h" /* header file is required to run primme */
```

2. Initialize a PRIMME parameters structure for default settings:

```
primme_params primme;
primme_initialize (&primme);
```

3. Set problem parameters (see also *Parameters Guide*), and, optionally, set one of the preset methods:

. . .

4. Then to solve real symmetric standard eigenproblems call:

```
ret = dprimme (evals, evecs, resNorms, &primme);
```

The previous is the double precision call. There is available calls for complex double, single and complex single; check it out <code>zprimme()</code>, <code>sprimme()</code> and <code>cprimme()</code>.

The call arguments are:

- evals, array to return the found eigenvalues;
- evecs, array to return the found eigenvectors;
- resNorms, array to return the residual norms of the found eigenpairs; and
- ret, returned error code.
- 5. To free the work arrays in PRIMME:

```
primme_free (&primme);
```

2.1.2 Parameters Guide

PRIMME stores the data on the structure primme_params, which has the next fields:

```
Basic
```

```
PRIMME_INT n, matrix dimension.

void (* matrixMatvec) (...), matrix-vector product.

int numEvals, how many eigenpairs to find.

primme_target target, which eigenvalues to find.

int numTargetShifts, for targeting interior eigenpairs.

double * targetShifts

double eps, tolerance of the residual norm of converged eigenpairs.
```

For parallel programs

```
int numProcs, number of processes
int procID, rank of this process
PRIMME_INT nLocal, number of rows stored in this process
void (* globalSumReal)(...), sum reduction among processes
```

Accelerate the convergence

```
void (* applyPreconditioner) (...), preconditioner-vector product.
int initSize, initial vectors as approximate solutions.
int maxBasisSize
int minRestartSize
int maxBlockSize
```

User data

```
void * commInfo
void * matrix
void * preconditioner
```

```
void * convtest
void * monitor
Advanced options
PRIMME_INT ldevecs, leading dimension of the evecs.
int numOrthoConst, orthogonal constrains to the eigenvectors.
int dynamicMethodSwitch
int locking
PRIMME INT maxMatvecs
PRIMME_INT maxOuterIterations
int intWorkSize
size_t realWorkSize
PRIMME_INT iseed [4]
int * intWork
void * realWork
double aNorm
int printLevel
FILE * outputFile
double * ShiftsForPreconditioner
primme_init initBasisMode
struct projection params projectionParams
struct restarting_params restartingParams
struct correction_params correctionParams
struct primme_stats stats
void (* convTestFun) (...), custom convergence criterion.
PRIMME_INT 1dOPs, leading dimension to use in matrixMatvec.
void (* monitorFun) (...), custom convergence history.
```

PRIMME requires the user to set at least the dimension of the matrix (n) and the matrix-vector product (matrixMatvec), as they define the problem to be solved. For parallel programs, nLocal, procID and globalSumReal are also required.

In addition, most users would want to specify how many eigenpairs to find, and provide a preconditioner (if available).

It is useful to have set all these before calling <code>primme_set_method()</code>. Also, if users have a preference on <code>maxBasisSize</code>, <code>maxBlockSize</code>, etc, they should also provide them into <code>primme_params</code> prior to the <code>primme_set_method()</code> call. This helps <code>primme_set_method()</code> make the right choice on other parameters. It is sometimes useful to check the actual parameters that PRIMME is going to use (before calling it) or used (on return) by printing them with <code>primme_display_params()</code>.

2.1.3 Interface Description

The next enumerations and functions are declared in primme.h.

sprimme

```
int sprimme (float *evals, float *evecs, float *resNorms, primme_params *primme)
Solve a real symmetric standard eigenproblem.
```

Parameters

- **evals** array at least of size <code>numEvals</code> to store the computed eigenvalues; all processes in a parallel run return this local array with the same values.
- **resNorms** array at least of size *numEvals* to store the residual norms of the computed eigenpairs; all processes in parallel run return this local array with the same values.
- **evecs** array at least of size *nLocal* times *numEvals* to store columnwise the (local part of the) computed eigenvectors.
- **primme** parameters structure.

Returns error indicator; see Error Codes.

dprimme

int **dprimme** (double *evals, double *evecs, double *resNorms, primme_params *primme)

Solve a real symmetric standard eigenproblem.

Parameters

- **evals** array at least of size <code>numEvals</code> to store the computed eigenvalues; all processes in a parallel run return this local array with the same values.
- **resNorms** array at least of size *numEvals* to store the residual norms of the computed eigenpairs; all processes in parallel run return this local array with the same values.
- **evecs** array at least of size *nLocal* times *numEvals* to store columnwise the (local part of the) computed eigenvectors.
- **primme** parameters structure.

Returns error indicator; see Error Codes.

cprimme

```
int cprimme (float *evals, PRIMME_COMPLEX_FLOAT *evecs, float *resNorms, primme_params *primme)

Solve a Hermitian standard eigenproblem; see function sprimme().
```

zprimme

```
int zprimme (double *evals, PRIMME_COMPLEX_DOUBLE *evecs, double *resNorms, primme_params *primme)

Solve a Hermitian standard eigenproblem; see function dprimme().
```

primme initialize

```
void primme_initialize (primme_params *primme)

Set PRIMME parameters structure to the default values.
```

Parameters

• **primme** – parameters structure.

primme set method

int primme_set_method (primme_preset_method method, primme_params *primme)

Set PRIMME parameters to one of the preset configurations.

Parameters

• method – preset configuration; one of

```
PRIMME_DYNAMIC

PRIMME_DEFAULT_MIN_TIME

PRIMME_DEFAULT_MIN_MATVECS

PRIMME_Arnoldi

PRIMME_GD

PRIMME_GD_plusK

PRIMME_GD_olsen_plusK

PRIMME_JD_Olsen_plusK

PRIMME_JDQR

PRIMME_JDQR

PRIMME_JDQRR

PRIMME_JDQMR_ETol

PRIMME_STEEPEST_DESCENT

PRIMME_LOBPCG_OrthoBasis_Window
```

• primme – parameters structure.

See also Preset Methods.

primme_display_params

```
void primme_display_params (primme_params primme)
```

Display all printable settings of primme into the file descriptor outputFile.

Parameters

• **primme** – parameters structure.

primme_free

```
void primme_free (primme_params *primme)
```

Free memory allocated by PRIMME.

Parameters

• primme – parameters structure.

2.2 FORTRAN Library Interface

The next enumerations and functions are declared in primme_f77.h.

ptr

Fortran datatype with the same size as a pointer. Use integer *4 when compiling in 32 bits and integer *8 in 64 bits.

2.2.1 primme_initialize_f77

```
primme initialize f77 (primme)
```

Set PRIMME parameters structure to the default values.

Parameters

• **primme** (ptr) – (output) parameters structure.

2.2.2 primme_set_method_f77

```
primme_set_method_f77 (method, primme, ierr)
```

Set PRIMME parameters to one of the preset configurations.

Parameters

• method (integer) - (input) preset configuration. One of:

```
PRIMME_DYNAMIC

PRIMME_DEFAULT_MIN_TIME

PRIMME_DEFAULT_MIN_MATVECS

PRIMME_Arnoldi

PRIMME_GD

PRIMME_GD_plusK

PRIMME_GD_Olsen_plusK

PRIMME_JD_Olsen_plusK

PRIMME_JDQR

PRIMME_JDQR

PRIMME_JDQMR

PRIMME_JDQMR_ETO1

PRIMME_STEEPEST_DESCENT

PRIMME_LOBPCG_OrthoBasis_Window
```

See primme preset method.

- **primme** (ptr) (input) parameters structure.
- ierr (integer) (output) if 0, successful; if negative, something went wrong.

2.2.3 primme_free_f77

primme_free_f77 (primme)

Free memory allocated by PRIMME and delete all values set.

Parameters

• **primme** (ptr) – (input/output) parameters structure.

2.2.4 sprimme_f77

sprimme_f77 (evals, evecs, resNorms, primme, ierr)

Solve a real symmetric standard eigenproblem using single precision.

Parameters

- evals (*) (real) (output) array at least of size numEvals to store the computed eigenvalues; all parallel calls return the same value in this array.
- resNorms (*) (real) (output) array at least of size numEvals to store the residual norms of the computed eigenpairs; all parallel calls return the same value in this array.
- evecs (*) (real) (input/output) array at least of size nLocal times numEvals to store columnwise the (local part of the) computed eigenvectors.
- primme (ptr) parameters structure.
- **ierr** (*integer*) (output) error indicator; see *Error Codes*.

2.2.5 cprimme_f77

cprimme_f77 (evals, evecs, resNorms, primme, ierr)

Solve a Hermitian standard eigenproblem. The arguments have the same meaning as in function $sprimme_f77()$.

Parameters

- evals(*) (real) (output)
- resNorms(*) (real) (output)
- evecs (*) (complex real) (input/output)
- **primme** (ptr) (input) parameters structure.
- ierr (integer) (output) error indicator; see *Error Codes*.

2.2.6 dprimme f77

dprimme f77 (evals, evecs, resNorms, primme, ierr)

Solve a real symmetric standard eigenproblem using double precision.

Parameters

- evals (*) (double precision) (output) array at least of size numEvals to store the computed eigenvalues; all parallel calls return the same value in this array.
- resNorms (*) (double precision) (output) array at least of size numEvals to store the residual norms of the computed eigenpairs; all parallel calls return the same value in this array.

- evecs (*) (double precision) (input/output) array at least of size nLocal times numEvals to store columnwise the (local part of the) computed eigenvectors.
- **primme** (ptr) parameters structure.
- ierr (integer) (output) error indicator; see *Error Codes*.

2.2.7 zprimme f77

zprimme_f77 (evals, evecs, resNorms, primme, ierr)

Solve a Hermitian standard eigenproblem. The arguments have the same meaning as in function $dprimme_f77()$.

Parameters

- evals(*) (double precision) (output)
- resNorms(*) (double precision) (output)
- evecs (*) (complex double precision) (input/output)
- **primme** (ptr) (input) parameters structure.
- **ierr** (*integer*) (output) error indicator; see *Error Codes*.

2.2.8 primme set member f77

primme_set_member_f77 (primme, label, value)

Set a value in some field of the parameter structure.

Parameters

- **primme** (ptr) (input) parameters structure.
- label (integer) field where to set value. One of:

```
PRIMME n
PRIMME_matrixMatvec
PRIMME_applyPreconditioner
PRIMME_numProcs
PRIMME_procID
PRIMME_comminfo
PRIMME nLocal
PRIMME_globalSumReal
PRIMME numEvals
PRIMME_target
PRIMME_numTargetShifts
PRIMME_targetShifts
PRIMME locking
PRIMME_initSize
PRIMME_numOrthoConst
PRIMME_maxBasisSize
PRIMME_minRestartSize
PRIMME maxBlockSize
```

```
PRIMME maxMatvecs
PRIMME_maxOuterIterations
PRIMME intWorkSize
PRIMME_realWorkSize
PRIMME iseed
PRIMME intWork
PRIMME realWork
PRIMME_aNorm
PRIMME eps
PRIMME_printLevel
PRIMME outputFile
PRIMME matrix
PRIMME_preconditioner
PRIMME_restartingParams_scheme.
PRIMME restartingParams maxPrevRetain
PRIMME_correctionParams_precondition
PRIMME correctionParams robustShifts
PRIMME_correctionParams_maxInnerIterations
PRIMME_correctionParams_projectors_LeftQ
PRIMME_correctionParams_projectors_LeftX
PRIMME correctionParams projectors RightQ
PRIMME_correctionParams_projectors_RightX
PRIMME_correctionParams_projectors_SkewQ
PRIMME_correctionParams_projectors_SkewX
PRIMME correctionParams convTest
PRIMME correctionParams_relTolBase
PRIMME stats numOuterIterations
PRIMME_stats_numRestarts
PRIMME_stats_numMatvecs
PRIMME stats numPreconds
PRIMME stats elapsedTime
PRIMME_dynamicMethodSwitch
PRIMME massMatrixMatvec
```

• **value** – (input) value to set.

If the type of the option is integer (int, PRIMME_INT, size_t), the type of value should be as long as PRIMME_INT, which is integer *8 by default.

Note: Don't use this function inside PRIMME's callback functions, e.g., matrixMatvec or applyPreconditioner, or in functions called by these functions.

2.2.9 primmetop_get_member_f77

primmetop_get_member_f77 (primme, label, value)
Get the value in some field of the parameter structure.

Parameters

- **primme** (ptr) (input) parameters structure.
- label (integer) (input) field where to get value. One of the detailed in function primmetop_set_member_f77().
- **value** (output) value of the field.

If the type of the option is integer (int, PRIMME_INT, size_t), the type of value should be as long as PRIMME_INT, which is integer *8 by default.

Note: Don't use this function inside PRIMME's callback functions, e.g., matrixMatvec or applyPreconditioner, or in functions called by these functions. In those cases use primme_get_member_f77().

Note: When label is one of PRIMME_matrixMatvec, PRIMME_applyPreconditioner, PRIMME_commInfo, PRIMME_intWork, PRIMME_realWork, PRIMME_matrix and PRIMME_preconditioner, the returned value is a C pointer (void*). Use Fortran pointer or other extensions to deal with it. For instance:

```
use iso_c_binding
MPI_Comm comm

comm = MPI_COMM_WORLD
call primme_set_member_f77(primme, PRIMME_commInfo, comm)
...
subroutine par_GlobalSumDouble(x,y,k,primme)
use iso_c_binding
implicit none
...
MPI_Comm, pointer :: comm
type(c_ptr) :: pcomm

call primme_get_member_f77(primme, PRIMME_commInfo, pcomm)
call c_f_pointer(pcomm, comm)
call MPI_Allreduce(x,y,k,MPI_DOUBLE,MPI_SUM,comm,ierr)
```

Most users would not need to retrieve these pointers in their programs.

2.2.10 primmetop_get_prec_shift_f77

```
primmetop_get_prec_shift_f77 (primme, index, value)
```

Get the value in some position of the array ShiftsForPreconditioner.

Parameters

- **primme** (ptr) (input) parameters structure.
- index (integer) (input) position of the array; the first position is 1.
- **value** (output) value of the array at that position.

2.2.11 primme_get_member_f77

primme_get_member_f77 (primme, label, value)

Get the value in some field of the parameter structure.

Parameters

- primme (ptr) (input) parameters structure.
- label (integer) (input) field where to get value. One of the detailed in function primmetop_set_member_f77().
- value (output) value of the field.

If the type of the option is integer (int, PRIMME_INT, size_t), the type of value should be as long as PRIMME_INT, which is integer *8 by default.

Note: Use this function exclusively inside PRIMME's callback functions, e.g., matrixMatvec or applyPreconditioner, or in functions called by these functions. Otherwise, e.g., from the main program, use the function primmetop_get_member_f77().

Note: When label is one of PRIMME_matrixMatvec, PRIMME_applyPreconditioner, PRIMME_commInfo, PRIMME_intWork, PRIMME_realWork, PRIMME_matrix and PRIMME_preconditioner, the returned value is a C pointer (void*). Use Fortran pointer or other extensions to deal with it. For instance:

```
use iso_c_binding
MPI_Comm comm

comm = MPI_COMM_WORLD
call primme_set_member_f77(primme, PRIMME_commInfo, comm)
...
subroutine par_GlobalSumDouble(x,y,k,primme)
use iso_c_binding
implicit none
...
MPI_Comm, pointer :: comm
type(c_ptr) :: pcomm

call primme_get_member_f77(primme, PRIMME_commInfo, pcomm)
call c_f_pointer(pcomm, comm)
call MPI_Allreduce(x,y,k,MPI_DOUBLE,MPI_SUM,comm,ierr)
```

Most users would not need to retrieve these pointers in their programs.

2.2.12 primme_get_prec_shift_f77

primme_get_prec_shift_f77 (primme, index, value)

Get the value in some position of the array ShiftsForPreconditioner.

Parameters

- primme (ptr) (input) parameters structure.
- **index** (*integer*) (input) position of the array; the first position is 1.

• **value** – (output) value of the array at that position.

Note: Use this function exclusively inside the function matrixMatvec, massMatrixMatvec, or applyPreconditioner. Otherwise use the function primmetop_get_prec_shift_f77().

2.3 Python Interface

Primme.eigsh (A, k=6, M=None, sigma=None, which='LM', v0=None, ncv=None, maxiter=None, tol=0, return_eigenvectors=True, Minv=None, OPinv=None, mode='normal', ortho=None, return_stats=False, maxBlockSize=0, minRestartSize=0, maxPrevRetain=0, method=None, return history=False. **kargs)

Find k eigenvalues and eigenvectors of the real symmetric square matrix or complex Hermitian matrix A.

Solves $A \star x[i] = w[i] \star x[i]$, the standard eigenvalue problem for w[i] eigenvalues with corresponding eigenvectors x[i].

If M is specified, solves A * x[i] = w[i] * M * x[i], the generalized eigenvalue problem for w[i] eigenvalues with corresponding eigenvectors x[i]

Parameters

- **A** (An N x N matrix, array, sparse matrix, or LinearOperator) the operation A * x, where A is a real symmetric matrix or complex Hermitian.
- \mathbf{k} (int, optional) The number of eigenvalues and eigenvectors to be computed. Must be $1 \le \mathbf{k} \le \min(A.\text{shape})$.
- **M** (An N x N matrix, array, sparse matrix, or LinearOperator) (not supported yet) the operation M * x for the generalized eigenvalue problem

$$A * x = w * M * x.$$

M must represent a real, symmetric matrix if A is real, and must represent a complex, Hermitian matrix if A is complex. For best results, the data type of M should be the same as that of A.

- sigma (real, optional) Find eigenvalues near sigma.
- **v0** (N x i, ndarray, optional) Initial guesses to the eigenvectors.
- ncv (int, optional) The maximum size of the basis
- which (str ['LM' | 'SM' | 'LA' | 'SA']) Which k eigenvectors and eigenvalues to find:

'LM': Largest in magnitude eigenvalues; the farthest from sigma

'SM': Smallest in magnitude eigenvalues; the closest to sigma

'LA': Largest algebraic eigenvalues

'SA': Smallest algebraic eigenvalues

'CLT': closest but left to sigma

'CGT': closest but greater than sigma

When sigma == None, 'LM', 'SM', 'CLT', and 'CGT' treat sigma as zero.

- maxiter (int, optional) Maximum number of iterations.
- **tol** (*float*) Required accuracy for eigenpairs (stopping criterion). The default value is sqrt of machine precision.
- Minv ((not supported yet)) The inverse of M in the generalized eigenproblem.
- **OPinv** (N x N matrix, array, sparse matrix, or LinearOperator, optional) Preconditioner to accelerate the convergence. Usually it is an approximation of the inverse of (A sigma*M).

- return_eigenvectors (bool, optional) Return eigenvectors (True) in addition to eigenvalues
- mode (string ['normal' | 'buckling' | 'cayley']) Only 'normal' mode is supported.
- **ortho** (N x i, ndarray, optional) Seek the eigenvectors orthogonal to these ones. The provided vectors *should* be orthonormal. Useful to avoid converging to previously computed solutions.
- maxBlockSize (int, optional) Maximum number of vectors added at every iteration
- minRestartSize (int, optional) Number of approximate eigenvectors kept during restart.
- maxPrevRetain (int, optional) Number of approximate eigenvectors kept from previous iteration in restart. Also referred as +k vectors in GD+k.
- method (int, optional) Preset method, one of:
 - DEFAULT_MIN_TIME : a variant of JDQMR,
 - DEFAULT MIN MATVECS: GD+k
 - DYNAMIC : choose dynamically between these previous methods.

See a detailed description of the methods and other possible values in².

- return_stats (bool, optional) If True, the function returns extra information (see stats in Returns).
- **return_history** (bool, optional) If True, the function returns performance information at every iteration (see hist in Returns).

Returns

- w (array) Array of k eigenvalues ordered to best satisfy "which".
- $\mathbf{v}(array)$ An array representing the k eigenvectors. The column $\mathbf{v}[:, i]$ is the eigenvector corresponding to the eigenvalue $\mathbf{w}[i]$.
- stats (dict, optional (if return_stats)) Extra information reported by PRIMME:
 - "numOuterIterations": number of outer iterations
 - "numRestarts": number of restarts
 - "numMatvecs": number of A*v
 - "numPreconds": number of OPinv*v
 - "elapsedTime": time that took
 - "estimateMinEVal": the leftmost Ritz value seen
 - "estimateMaxEVal": the rightmost Ritz value seen
 - "estimateLargestSVal": the largest singular value seen
 - "rnorms" : ||A*x[i] x[i]*w[i]||
 - "hist" : (if return_history) report at every outer iteration of:
 - * "elapsedTime": time spent up to now

² Preset Methods, http://www.cs.wm.edu/~andreas/software/doc/readme.html#preset-methods

- * "numMatvecs": number of A*v spent up to now
- * "nconv": number of converged pair
- * "eval": eigenvalue of the first unconverged pair
- * "resNorm": residual norm of the first unconverged pair

Raises PrimmeError – When the requested convergence is not obtained.

The PRIMME error code can be found as err attribute of the exception object.

See also:

scipy.sparse.linalg.eigs() eigenvalues and eigenvectors for a general (nonsymmetric) matrix A
Primme.svds() singular value decomposition for a matrix A

Notes

This function is a wrapper to PRIMME functions to find the eigenvalues and eigenvectors¹.

References

Examples

```
>>> import Primme, scipy.sparse
>>> A = scipy.sparse.spdiags(range(100), [0], 100, 100) # sparse diag. matrix
>>> evals, evecs = Primme.eigsh(A, 3, tol=1e-6, which='LA')
>>> evals # the three largest eigenvalues of A
array([ 99., 98., 97.])
>>> new_evals, new_evecs = Primme.eigsh(A, 3, tol=1e-6, which='LA', ortho=evecs)
>>> new_evals # the next three largest eigenvalues
array([ 96., 95., 94.])
```

¹ PRIMME Software, https://github.com/primme/primme

2.4 MATLAB Interface

function [varargout] = primme_eigs(varargin)

primme_eigs () finds a few eigenvalues and their corresponding eigenvectors of a real symmetric or Hermitian matrix, A, by calling PRIMME.

- D = primme_eigs (A) returns a vector of A's 6 largest magnitude eigenvalues.
- D = primme_eigs (Afun, dim) accepts a function Afun instead of a matrix. Afun is a function handle and y = Afun(x) returns the matrix-vector product $A \times x$. In all the following syntaxes, A can be replaced by Afun, dim.
- $D = primme_{eigs}(A, k)$ finds the k largest magnitude eigenvalues. k must be less than the dimension of the matrix A.
- D = primme_eigs (A, k, target) returns k eigenvalues such that: If target is a real number, it finds the closest eigenvalues to target. If target is
 - 'LA' or 'SA', eigenvalues with the largest or smallest algebraic value.
 - 'LM' or 'SM', eigenvalues with the largest or smallest magnitude if OPTS.targetShifts is empty. If target is a real or complex scalar including 0, primme_eigs() finds the eigenvalues closest to target.

In addition, if some values are provided in OPTS.targetShifts, it finds eigenvalues that are farthest ('LM') or closest ('SM') in absolute value from the given values.

Examples:

k=1, 'LM', OPTS.targetShifts=[] returns the largest magnitude eig(A). k=1, 'SM', OPTS.targetShifts=[] returns the smallest magnitude eig(A). k=3, 'SM', OPTS.targetShifts=[2, 5] returns the closest eigenvalue in absolute sense to 2, and the two closest eigenvalues to 5.

- 'CLT' or 'CGT', find eigenvalues closest to but less or greater than the given values in OPTS. targetShifts.
- D = primme_eigs (A, k, target, OPTS) specifies extra solver parameters. Some default values are indicated in brackets {}:
 - aNorm: the estimated 2-norm of A {0.0 (estimate the norm internally)}
 - tol: convergence tolerance: NORM(A*X(:,i)-X(:,i)*D(i,i)) < tol*NORM(A) (see eps) {10⁴ times the machine precision}
 - maxBlockSize: maximum block size (useful for high multiplicities) {1}
 - disp: different level reporting (0-3) (see HIST) {no output 0}
 - isreal: whether A represented by Afun is real or complex {false}
 - targetShifts: shifts for interior eigenvalues (see target) {[]}
 - v0: any number of initial guesses to the eigenvectors (see initSize {[]}
 - orthoConst: external orthogonalization constraints (see numOrthoConst {[]}
 - locking: 1, hard locking; 0, soft locking
 - p: maximum size of the search subspace (see maxBasisSize)
 - minRestartSize: minimum Ritz vectors to keep in restarting
 - maxMatvecs: maximum number of matrix vector multiplications {Inf}

- maxit: maximum number of outer iterations (see maxOuterIterations) {Inf}
- scheme: the restart scheme {'primme_thick'}
- maxPrevRetain: number of Ritz vectors from previous iteration that are kept after restart {typically >0}
- robustShifts: setting to true may avoid stagnation or misconvergence
- maxInnerIterations: maximum number of inner solver iterations
- LeftQ: use the locked vectors in the left projector
- LeftX: use the approx. eigenvector in the left projector
- Right Q: use the locked vectors in the right projector
- RightX: use the approx. eigenvector in the right projector
- SkewQ: use the preconditioned locked vectors in the right projector
- SkewX: use the preconditioned approx. eigenvector in the right projector
- relTolBase: a legacy from classical JDQR (not recommended)
- convTest: how to stop the inner QMR Method
- convTestFun: function handler with an alternative convergence criterion. If FUN (EVAL, EVEC, RNORM) returns a nonzero value, the pair (EVAL, EVEC) with residual norm RNORM is considered converged.
- iseed: random seed
- D = primme_eigs (A, k, target, OPTS, METHOD) specifies the eigensolver method. METHOD can be one of the next strings:
 - 'PRIMME_DYNAMIC', (default) switches dynamically to the best method
 - 'PRIMME_DEFAULT_MIN_TIME', best method for low-cost matrix-vector product
 - 'PRIMME_DEFAULT_MIN_MATVECS', best method for heavy matvec/preconditioner
 - 'PRIMME_Arnoldi', Arnoldi not implemented efficiently
 - 'PRIMME_GD', classical block Generalized Davidson
 - 'PRIMME_GD_plusk', GD+k block GD with recurrence restarting
 - 'PRIMME_GD_Olsen_plusk', GD+k with approximate Olsen precond.
 - 'PRIMME_JD_Olsen_plusK', GD+k, exact Olsen (two precond per step)
 - 'PRIMME RQI', Rayleigh Quotient Iteration. Also INVIT, but for INVIT provide OPTS.targetShifts
 - 'PRIMME_JDQR', Original block, Jacobi Davidson
 - 'PRIMME_JDQMR', Our block JDQMR method (similar to JDCG)
 - 'PRIMME_JDQMR_ETo1', Slight, but efficient JDQMR modification
 - 'PRIMME_STEEPEST_DESCENT', equivalent to GD(block,2*block)
 - 'PRIMME_LOBPCG_OrthoBasis', equivalent to GD(nev,3*nev)+nev
 - 'PRIMME_LOBPCG_OrthoBasis_Window' equivalent to GD(block,3*block)+block nev>block
- D = primme_eigs(A,k,target,OPTS,METHOD,P)
- D = primme_eigs(A, k, target, OPTS, METHOD, P1, P2) uses preconditioner P or P = P1*P2 to accelerate convergence of the method. Applying P \setminus x should approximate (A-sigma*eye(N)) \setminus x, for

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sigma near the wanted eigenvalue(s). If P is [] then a preconditioner is not applied. P may be a function handle PFUN such that PFUN (x) returns $P \setminus x$.

 $[X,D] = primme_eigs(...)$ returns a diagonal matrix D with the eigenvalues and a matrix X whose columns are the corresponding eigenvectors.

[X,D,R] = primme_eigs (...) also returns an array of the residual norms of the computed eigenpairs.

[X,D,R,STATS] = primme_eigs(...) returns a struct to report statistical information about number of matvecs, elapsed time, and estimates for the largest and smallest algebraic eigenvalues of A.

[X,D,R,STATS,HIST] = primme_eigs(...) it returns the convergence history, instead of printing it. Every row is a record, and the columns report:

- HIST (:, 1): number of matvecs
- HIST(:,2): time
- HIST (:, 3): number of converged/locked pairs
- HIST(:, 4): block index
- HIST (:, 5): approximate eigenvalue
- HIST(:, 6): residual norm
- HIST(:, 7): QMR residual norm

OPTS.disp controls the granularity of the record. If OPTS.disp == 1, HIST has one row per converged eigenpair and only the first three columns are reported; if OPTS.disp == 2, HIST has one row per outer iteration and only the first six columns are reported; and otherwise HIST has one row per QMR iteration and all columns are reported.

Examples:

```
A = diag(1:100);
d = primme_eigs(A,10) % the 10 largest magnitude eigenvalues
d = primme_eigs(A,10,'SM') % the 10 smallest magnitude eigenvalues
d = primme_eigs(A,10,25.0) % the 10 closest eigenvalues to 25.0
opts.targetShifts = [2 20];
d = primme_eigs(A, 10, 'SM', opts) % 1 eigenvalue closest to 2 and
                                  % 9 eigenvalues closest to 20
opts = struct();
opts.tol = 1e-4; % set tolerance
opts.maxBlockSize = 2; % set block size
[x,d] = primme_eigs(A, 10, 'SA', opts, 'DEFAULT_MIN_TIME')
opts.orthoConst = x;
[d,rnorms] = primme_eigs(A,10,'SA',opts) % find another 10 with the default method
% Compute the 6 eigenvalues closest to 30.5 using ILU(0) as a preconditioner
% by passing the matrices L and U.
A = \text{sparse}(\text{diag}(1:50) + \text{diag}(\text{ones}(49,1), 1) + \text{diag}(\text{ones}(49,1), -1));
[L,U] = ilu(A, struct('type', 'nofill'));
d = primme_{eigs}(A, k, 30.5, [], [], L, U);
% Compute the 6 eigenvalues closest to 30.5 using Jacobi preconditioner
```

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```
% by passing a function.
Pfun = @(x)(diag(A) - 30.5)\x;
d = primme_eigs(A, 6, 30.5, [], [], Pfun) % find the closest 5 to 30.5
See also: MATLAB eigs, primme_svds()
```

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2.5 Parameters Description

2.5.1 Types

The following data types are macros used in PRIMME as followed.

PRIMME INT

Integer type used in matrix dimensions (such as n and nLocal) and counters (such as numMatvecs).

The integer size is controlled by the compilation flag PRIMME_INT_SIZE, see *Making and Linking*.

PRIMME COMPLEX FLOAT

Macro that is complex float in C and std::complex<float> in C++.

PRIMME COMPLEX DOUBLE

Macro that is complex double in C and std::complex<double> in C++.

2.5.2 primme params

primme params

Structure to set the problem matrices and eigensolver options.

```
PRIMME INT n
```

Dimension of the matrix.

Input/output:

```
primme_initialize() sets this field to 0;
this field is read by dprimme().
```

```
void (*matrixMatvec) (void *x, PRIMME_INT *ldx, void *y, PRIMME_INT *ldy, int *blockSize, primme params *primme, int *ierr)
```

Block matrix-multivector multiplication, $\hat{y} = Ax$ in solving $Ax = \lambda x$ or $Ax = \lambda Bx$.

Parameters

- **x** matrix of size *nLocal* **x** blockSize in column-major order with leading dimension ldx.
- 1dx the leading dimension of the array x.
- **y** matrix of size *nLocal* x blockSize in column-major order with leading dimension ldy.
- **1dy** the leading dimension of the array y.
- **blockSize** number of columns in x and y.
- **primme** parameters structure.
- ierr output error code; if it is set to non-zero, the current call to PRIMME will stop.

The actual type of x and y depends on which function is being calling. For dprimme(), it is double, for zprimme() it is $PRIMME_COMPLEX_DOUBLE$, for sprimme() it is $PRIMME_COMPLEX_FLOAT$.

```
primme_initialize() sets this field to NULL;
this field is read by dprimme().
```

Note: If you have performance issues with leading dimension different from nLocal, set 1dOPs to nLocal.

Block preconditioner-multivector application, $y = M^{-1}x$ where M is usually an approximation of $A - \sigma I$ or $A - \sigma B$ for finding eigenvalues close to σ . The function follows the convention of matrixMatvec.

Input/output:

```
primme_initialize() sets this field to NULL;
this field is read by dprimme().
```

```
void (*massMatrixMatvec) (void *x, PRIMME_INT *ldx, void *y, PRIMME_INT *ldy, int *block-
Size, primme params *primme, int *ierr)
```

Block matrix-multivector multiplication, y = Bx in solving $Ax = \lambda Bx$. The function follows the convention of matrixMatvec.

Input/output:

```
primme_initialize() sets this field to NULL;
this field is read by dprimme().
```

Warning: Generalized eigenproblems not implemented in current version. This member is included for future compatibility.

int numProcs

Number of processes calling dprimme () or zprimme () in parallel.

Input/output:

```
primme_initialize() sets this field to 1;
this field is read by dprimme().
```

int procID

The identity of the local process within a parallel execution calling <code>dprimme()</code> or <code>zprimme()</code>. Only the process with id 0 prints information.

Input/output:

```
primme_initialize() sets this field to 0;
dprimme() sets this field to 0 if numProcs is 1;
this field is read by dprimme().
```

int nLocal

Number of local rows on this process.

Input/output:

```
primme_initialize() sets this field to -1;
dprimme() sets this field to n if numProcs is 1;
this field is read by dprimme().
```

void *commInfo

A pointer to whatever parallel environment structures needed. For example, with MPI, it could be a pointer to the MPI communicator. PRIMME does not use this. It is available for possible use in user functions defined in matrixMatvec, applyPreconditioner, massMatrixMatvec and globalSumReal.

```
primme_initialize() sets this field to NULL;
```

void (*globalSumReal) (void *sendBuf, void *recvBuf, int *count, primme_params *primme, int *ierr)

Global sum reduction function. No need to set for sequential programs.

Parameters

- sendBuf array of size count with the local input values.
- recvBuf array of size count with the global output values so that the i-th element of recvBuf is the sum over all processes of the i-th element of sendBuf.
- count array size of sendBuf and recvBuf.
- **primme** parameters structure.
- ierr output error code; if it is set to non-zero, the current call to PRIMME will stop.

The actual type of sendBuf and recvBuf depends on which function is being calling. For dprimme() and zprimme() it is double, and for sprimme() and cprimme() it is float. Note that count is the number of values of the actual type.

Input/output:

```
primme_initialize() sets this field to an internal function;
dprimme() sets this field to an internal function if numProcs is 1 and globalSumReal is
NULL;
this field is read by dprimme().
```

When MPI is used, this can be a simply wrapper to MPI_Allreduce() as shown below:

When calling sprimme () and cprimme () replace MPI_DOUBLE by `MPI_FLOAT.

int numEvals

Number of eigenvalues wanted.

```
primme_initialize() sets this field to 1;
    this field is read by primme_set_method() (see Preset Methods) and dprimme().
primme_target target
    Which eigenpairs to find:
```

```
primme_smallest Smallest algebraic eigenvalues; targetShifts is ignored.
primme_largest Largest algebraic eigenvalues; targetShifts is ignored.
primme_closest_geq Closest to, but greater or equal than the shifts in targetShifts.
primme_closest_leq Closest to, but less or equal than the shifts in targetShifts.
```

```
primme_closest_abs Closest in absolute value to the shifts in targetShifts.
```

primme_largest_abs Furthest in absolute value to the shifts in targetShifts.

Input/output:

```
primme_initialize() sets this field to primme_smallest;
this field is read by dprimme().
```

int numTargetShifts

Size of the array targetShifts. Used only when target is primme_closest_geq, primme_closest_leq, primme_closest_abs or primme_largest_abs. The default values is 0.

Input/output:

```
primme_initialize() sets this field to 0;
this field is read by dprimme().
```

double *targetShifts

```
Array of shifts, at least of size numTargetShifts. Used only when target is primme_closest_geq, primme_closest_leq, primme_closest_abs or primme_largest_abs.
```

Eigenvalues are computed in order so that the i-th eigenvalue is the closest (or closest but left or closest but right, see target) to the i-th shift. If numTargetShifts < numEvals, the last shift given is used for all the remaining i's.

Input/output:

```
primme_initialize() sets this field to NULL;
this field is read by dprimme().
```

Note: Considerations for interior problems:

- PRIMME will try to compute the eigenvalues in the order given in the <code>targetShifts</code>. However, for code efficiency and robustness, the shifts should be ordered. Order them in ascending (descending) order for shifts closer to the lower (higher) end of the spectrum.
- If some shift is close to the lower (higher) end of the spectrum, use either primme_closest_geq (primme_closest_leq) or primme_closest_abs.
- primme_closest_leq and primme_closest_geq are more efficient than primme_closest_abs.
- For interior eigenvalues larger maxBasisSize is usually more robust.
- To find the largest magnitude eigenvalues set target to primme_largest_abs, numTargetShifts to 1 and targetShifts to an array with a zero value.

int printLevel

The level of message reporting from the code. All output is written in outputFile.

One of:

- 0: silent.
- 1: print some error messages when these occur.
- 2: as in 1, and info about targeted eigenpairs when they are marked as converged:

```
#Converged $1 eval[ $2 ]= $3 norm $4 Mvecs $5 Time $7
or locked:
#Lock epair[ $1 ]= $3 norm $4 Mvecs $5 Time $7
```

• 3: in as 2, and info about targeted eigenpairs every outer iteration:

```
OUT $6 conv $1 blk $8 MV $5 Sec $7 EV $3 |r| $4
```

Also, if it is used the dynamic method, show JDQMR/GDk performance ratio and the current method in use.

• 4: in as 3, and info about targeted eigenpairs every inner iteration:

```
INN MV $5 Sec $7 Eval $3 Lin|r| $9 EV|r| $4
```

• 5: in as 4, and verbose info about certain choices of the algorithm.

Output key:

- \$1: Number of converged pairs up to now.
- \$2: The index of the pair currently converged.
- \$3: The eigenvalue.
- \$4: Its residual norm.
- \$5: The current number of matrix-vector products.
- \$6: The current number of outer iterations.
- \$7: The current elapsed time.
- \$8: Index within the block of the targeted pair .
- \$9: QMR norm of the linear system residual.

In parallel programs, output is produced in call with *procID* 0 when *printLevel* is from 0 to 4. If *printLevel* is 5 output can be produced in any of the parallel calls.

Input/output:

```
primme_initialize() sets this field to 1;
this field is read by dprimme().
```

Note: Convergence history for plotting may be produced simply by:

```
grep OUT outpufile | awk '{print 88" "$14}' > out grep INN outpufile | awk '{print $3" "$11}' > inn
```

Then in gnuplot:

```
plot 'out' w lp, 'inn' w lp
```

double aNorm

An estimate of the norm of A, which is used in the default convergence criterion (see eps).

If aNorm is less than or equal to 0, the code uses the largest absolute Ritz value seen. On return, aNorm is then replaced with that value.

Input/output:

```
primme_initialize() sets this field to 0.0; this field is read and written by dprimme().
```

double eps

If convTestFun is NULL, an eigenpairs is marked as converged when the 2-norm of the residual vector is less than eps*aNorm. The residual vector is $Ax - \lambda x$ or $Ax - \lambda Bx$.

The default value is machine precision times 10^4 .

Input/output:

```
primme_initialize() sets this field to 0.0;
this field is read and written by dprimme().
```

FILE *outputFile

Opened file to write down the output.

Input/output:

```
primme_initialize() sets this field to the standard output;
this field is read by dprimme() and primme_display_params().
```

int dynamicMethodSwitch

If this value is 1, it alternates dynamically between PRIMME_DEFAULT_MIN_TIME and PRIMME_DEFAULT_MIN_MATVECS, trying to identify the fastest method.

On exit, it holds a recommended method for future runs on this problem:

```
-1: use PRIMME_DEFAULT_MIN_MATVECS next time.
```

- -2: use PRIMME_DEFAULT_MIN_TIME next time.
- -3: close call, use PRIMME_DYNAMIC next time again.

Input/output:

```
primme_initialize() sets this field to 0;
written by primme_set_method() (see Preset Methods);
this field is read by dprimme().
```

Note: Even for expert users we do not recommend setting <code>dynamicMethodSwitch</code> directly, but through <code>primme_set_method()</code>.

Note: The code obtains timings by the <code>gettimeofday</code> Unix utility. If a cheaper, more accurate timer is available, modify the <code>PRIMMESRC/COMMONSRC/wtime.c</code>

int locking

If set to 1, hard locking will be used (locking converged eigenvectors out of the search basis). If set to 0, the code will try to use soft locking (à la ARPACK), when large enough minRestartSize is available.

```
primme_initialize() sets this field to -1;
written by primme_set_method() (see Preset Methods);
this field is read by dprimme().
```

int initSize

On input, the number of initial vector guesses provided in evecs argument in dprimme() or zprimme().

On output, <code>initSize</code> holds the number of converged eigenpairs. Without <code>locking</code> all <code>numEvals</code> approximations are in <code>evecs</code> but only the <code>initSize</code> ones are converged.

During execution, it holds the current number of converged eigenpairs. In addition, if locking is used, these are accessible in evals and evecs.

Input/output:

```
primme_initialize() sets this field to 0;
this field is read and written by dprimme().
```

PRIMME_INT ldevecs

The leading dimension of evecs. The default is nLocal.

Input/output:

```
primme_initialize() sets this field to -1;
this field is read by dprimme().
```

int numOrthoConst

Number of vectors to be used as external orthogonalization constraints. These vectors are provided in the first <code>numOrthoConst</code> positions of the evecs argument in <code>dprimme()</code> or <code>zprimme()</code> and must be orthonormal.

PRIMME finds new eigenvectors orthogonal to these constraints (equivalent to solving the problem with $(I-YY^*)A(I-YY^*)$ and $(I-YY^*)B(I-YY^*)$ matrices where Y are the given constraint vectors). This is a handy feature if some eigenvectors are already known, or for finding more eigenvalues after a call to dprimme() or zprimme(), possibly with different parameters (see an example in TEST/ $ex_zseq.c$).

Input/output:

```
primme_initialize() sets this field to 0;
this field is read by dprimme().
```

int maxBasisSize

The maximum basis size allowed in the main iteration. This has memory implications.

Input/output:

```
primme_initialize() sets this field to 0;
this field is read and written by primme_set_method() (see Preset Methods);
this field is read by dprimme().
```

int minRestartSize

Maximum Ritz vectors kept after restarting the basis.

Input/output:

```
primme_initialize() sets this field to 0;
this field is read and written by primme_set_method() (see Preset Methods);
this field is read by dprimme().
```

int maxBlockSize

The maximum block size the code will try to use.

The user should set this based on the architecture specifics of the target computer, as well as any a priori knowledge of multiplicities. The code does *not* require that maxBlockSize > 1 to find multiple eigenvalues. For some methods, keeping to 1 yields the best overall performance.

Input/output:

```
primme_initialize() sets this field to 1;
this field is read and written by primme_set_method() (see Preset Methods);
this field is read by dprimme().
```

Note: Inner iterations of QMR are not performed in a block fashion. Every correction equation from a block is solved independently.

PRIMME INT maxMatvecs

Maximum number of matrix vector multiplications (approximately equal to the number of preconditioning operations) that the code is allowed to perform before it exits.

Input/output:

```
primme_initialize() sets this field to INT_MAX;
this field is read by dprimme().
```

PRIMME INT maxOuterIterations

Maximum number of outer iterations that the code is allowed to perform before it exits.

Input/output:

```
primme_initialize() sets this field to INT_MAX;
this field is read by dprimme().
```

int intWorkSize

If dprimme () or zprimme () is called with all arguments as NULL except for primme_params then PRIMME returns immediately with intWorkSize containing the size in bytes of the integer workspace that will be required by the parameters set in PRIMME.

Otherwise if <code>intWorkSize</code> is not 0, it should be the size of the integer work array *in bytes* that the user provides in <code>intWork</code>. If <code>intWorkSize</code> is 0, the code will allocate the required space, which can be freed later by calling <code>primme free()</code>.

Input/output:

```
primme_initialize() sets this field to 0;
this field is read and written by dprimme().
```

size t realWorkSize

If dprimme() or zprimme() is called with all arguments as NULL except for primme_params then PRIMME returns immediately with realWorkSize containing the size in bytes of the real workspace that will be required by the parameters set in PRIMME.

Otherwise if realWorkSize is not 0, it should be the size of the real work array in bytes that the user provides in realWork. If realWorkSize is 0, the code will allocate the required space, which can be freed later by calling $primme_free()$.

Input/output:

```
\label{eq:primme_initialize} \textit{primme_initialize()} \ \ \text{sets this field to 0;} \\ \textit{this field is read and written by } \ \textit{dprimme()}.
```

int *intWork

Integer work array.

If NULL, the code will allocate its own workspace. If the provided space is not enough, the code will return the error code -37.

On exit, the first element shows if a locking problem has occurred. Using locking for large *numEvals* may, in some rare cases, cause some pairs to be practically converged, in the sense that their components are in the basis of evecs. If this is the case, a Rayleigh Ritz on returned evecs would provide the accurate eigenvectors (see [r4]).

Input/output:

```
primme_initialize() sets this field to NULL;
this field is read and written by dprimme().
```

void *realWork

Real work array.

If NULL, the code will allocate its own workspace. If the provided space is not enough, the code will return the error code -36.

Input/output:

```
primme_initialize() sets this field to NULL;
this field is read and written by dprimme().
```

PRIMME INT iseed

The PRIMME_INT iseed[4] is an array with the seeds needed by the LAPACK dlarnv and zlarnv.

The default value is an array with values -1, -1, -1 and -1. In that case, iseed is set based on the value of procID to avoid every parallel process generating the same sequence of pseudorandom numbers.

Input/output:

```
primme_initialize() sets this field to [-1, -1, -1, -1]; this field is read and written by dprimme().
```

void *matrix

This field may be used to pass any required information in the matrix-vector product matrixMatvec.

Input/output:

```
primme_initialize() sets this field to NULL;
```

void *preconditioner

This field may be used to pass any required information in the preconditioner function applyPreconditioner.

Input/output:

```
primme_initialize() sets this field to NULL;
```

double *ShiftsForPreconditioner

Array of size blockSize provided during execution of dprimme () and zprimme () holding the shifts to be used (if needed) in the preconditioning operation.

For example if the block size is 3, there will be an array of three shifts in ShiftsForPreconditioner. Then the user can invert a shifted preconditioner for each of the block vectors $(M-ShiftsForPreconditioner_i)^{-1}x_i$. Classical Davidson (diagonal) preconditioning is an example of this.

this field is read and written by dprimme ().

primme init initBasisMode

Select how the search subspace basis is initialized up to *minRestartSize* vectors if not enough initial vectors are provided (see *initSize*):

- primme_init_krylov, with a block Krylov subspace generated by the matrix problem and the last initial vectors if given or a random vector otherwise; the size of the block is maxBlockSize.
- primme init random, with random vectors.
- primme_init_user, the initial basis will have only initial vectors if given, or a single random vector.

Input/output:

```
primme_initialize() sets this field to primme_init_krylov;
this field is read by dprimme().
```

primme_projection projectionParams.projection

Select the extraction technique, i.e., how the approximate eigenvectors x_i and eigenvalues λ_i are computed from the search subspace \mathcal{V} :

- primme_proj_RR, Rayleigh-Ritz, $Ax_i Bx_i\lambda_i \perp \mathcal{V}$.
- primme_proj_harmonic, Harmonic Rayleigh-Ritz, $Ax_i Bx_i\lambda_i \perp (A \tau B)\mathcal{V}$, where τ is the current target shift (see targetShifts).
- primme_proj_refined, refined extraction, compute x_i with $||x_i|| = 1$ that minimizes $||(A \tau B)x_i||$; the eigenvalues are computed as the Rayleigh quotients, $\lambda_i = \frac{x_i^* A x_i}{x_i^* B x_i}$.

Input/output:

```
primme_initialize() sets this field to primme_proj_default;
primme_set_method() and dprimme() sets it to primme_proj_RR if it is
primme_proj_default.
```

primme_restartscheme restartingParams.scheme

Select a restarting strategy:

- primme_thick, Thick restarting. This is the most efficient and robust in the general case.
- primme_dtr, Dynamic thick restarting. Helpful without preconditioning but it is expensive to implement.

Input/output:

```
primme_initialize() sets this field to primme_thick;
written by primme_set_method() (see Preset Methods);
this field is read by dprimme().
```

int restartingParams.maxPrevRetain

Number of approximations from previous iteration to be retained after restart (this is the locally optimal restarting, see [r2]). The restart size is *minRestartSize* plus *maxPrevRetain*.

Input/output:

```
primme_initialize() sets this field to 0;
this field is read and written by primme_set_method() (see Preset Methods);
this field is read by dprimme().
```

int correctionParams.precondition

Set to 1 to use preconditioning. Make sure applyPreconditioner is not NULL then!

```
primme_initialize() sets this field to 0;
this field is read and written by primme_set_method() (see Preset Methods);
this field is read by dprimme().
```

int correctionParams.robustShifts

Set to 1 to use robust shifting. It tries to avoid stagnation and misconvergence by providing as shifts in *ShiftsForPreconditioner* the Ritz values displaced by an approximation of the eigenvalue error.

Input/output:

```
primme_initialize() sets this field to 0;
written by primme_set_method() (see Preset Methods);
this field is read by dprimme().
```

int correctionParams.maxInnerIterations

Control the maximum number of inner QMR iterations:

- 0: no inner iterations:
- >0: perform at most that number of inner iterations per outer step;
- <0: perform at most the rest of the remaining matrix-vector products up to reach maxMatvecs.

Input/output:

```
primme_initialize() sets this field to 0;
this field is read and written by primme_set_method() (see Preset Methods);
this field is read by dprimme().
```

See also convTest.

double correctionParams.relTolBase

Parameter used when convTest is primme decreasing LTolerance.

Input/output:

```
primme_initialize() sets this field to 0;
written by primme_set_method() (see Preset Methods);
this field is read by dprimme().
```

primme_convergencetest correctionParams.convTest

Set how to stop the inner QMR method:

- primme_full_LTolerance: stop by iterations only;
- primme_decreasing_LTolerance, stop when relTolBase^{-outIts} where outIts is the number of outer iterations and retTolBase is set in relTolBase; This is a legacy option from classical JDQR and we recommend **strongly** against its use.
- primme_adaptive, stop when the estimated eigenvalue residual has reached the required tolerance (based on Notay's JDCG).
- primme_adaptive_ETolerance, as primme_adaptive but also stopping when the estimated eigenvalue residual has reduced 10 times.

```
primme_initialize() sets this field to primme_adaptive_ETolerance;
written by primme_set_method() (see Preset Methods);
this field is read by dprimme().
```

Note: Avoid to set maxInnerIterations to -1 and convTest to primme_full_LTolerance.

See also maxInnerIterations.

int correctionParams.projectors.LeftQ

int correctionParams.projectors.LeftX

int correctionParams.projectors.RightQ

int correctionParams.projectors.RightX

int correctionParams.projectors.SkewQ

int correctionParams.projectors.SkewX

Control the projectors involved in the computation of the correction appended to the basis every (outer) iteration.

Consider the current selected Ritz value Λ and vectors X, the residual associated vectors $R = AX - X\Lambda$, the previous locked vectors Q, and the preconditioner M^{-1} .

When maxInnerIterations is 0, the correction D appended to the basis in GD is:

RightX	SkewX	D
0	0	$M^{-1}R$ (Classic GD)
1	0	$M^{-1}(R - \Delta X)$ (cheap Olsen's Method)
1	1	$(I - M^{-1}X(X^*M^{-1}X)^{-1}X^*)M^{-1}R$ (Olsen's Method)
0	1	error

Where Δ is a diagonal matrix that $\Delta_{i,i}$ holds an estimation of the error of the approximate eigenvalue $\Lambda_{i,i}$. The values of RightQ, SkewQ, LeftX and LeftQ are ignored.

When maxInnerIterations is not 0, the correction D in Jacobi-Davidson results from solving:

$$P_O^l P_X^l (A - \sigma I) P_X^r P_O^r M^{-1} D' = -R, \quad D = P_X^r P_O^l M^{-1} D'.$$

For LeftO:

$$\begin{aligned} &0{:}\; P_Q^l = I;\\ &1{:}\; P_Q^l = I - QQ^*. \end{aligned}$$

For LeftX:

$$\begin{aligned} &0{:}\; P_X^l = I;\\ &1{:}\; P_X^l = I - XX^*. \end{aligned}$$

For RightQ and SkewQ:

RightQ	SkewQ	P_Q^r
0	0	I
1	0	$I - QQ^*$
1	1	$I - KQ(Q^*KQ)^{-1}Q^*$
0	1	error

For RightX and SkewX:

RightX	SkewX	P_X^r
0	0	I
1	0	$I - XX^*$
1	1	$I - KX(X^*KX)^{-1}X^*$
0	1	error

Input/output:

```
primme_initialize() sets all of them to 0;
this field is written by primme_set_method() (see Preset Methods);
this field is read by dprimme().
```

See [r3] for a study about different projector configurations in JD.

PRIMME_INT ldOPs

Recommended leading dimension to be used in *matrixMatvec*, *applyPreconditioner* and *massMatrixMatvec*. The default value is zero, which means no user recommendation. In that case, PRIMME computes IdOPs internally to get better memory performance.

Input/output:

```
primme_initialize() sets this field to -1;
this field is read by dprimme().
```

void (*monitorFun) (void *basisEvals, int *basisSize, int *basisFlags, int *iblock, int *block-Size, void *basisNorms, int *numConverged, void *lockedEvals, int *num-Locked, int *lockedFlags, void *lockedNorms, int *inner_its, void *LSRes, primme_event *event, struct primme_params *primme, int *ierr)

Convergence monitor. Used to customize how to report solver information during execution (iteration number, matvecs, time, unconverged and converged eigenvalues, residual norms, targets, etc).

- **basisEvals** array with approximate eigenvalues of the basis.
- basisSize size of the arrays, basisEvals, basisFlags and basisNorms.
- basisFlags state of every approximate pair in the basis.
- **iblock** indices of the approximate pairs in the block targeted during current iteration.
- blockSize size of array iblock.
- **basisNorms** array with residual norms of the pairs in the basis.
- **numConverged** number of pairs converged in the basis plus the number of the locked pairs (note that this value isn't monotonic).
- lockedEvals array with the locked eigenvalues.
- numLocked size of the arrays lockedEvals, lockedFlags and lockedNorms.
- lockedFlags state of each locked eigenpair.
- **lockedNorms** array with the residual norms of the locked pairs.
- inner_its number of performed QMR iterations in the current correction equation. It resets for each block vector.
- LSRes residual norm of the linear system at the current QMR iteration.
- event event reported.

- **primme** parameters structure; the counter in stats are updated with the current number of matrix-vector products, iterations, elapsed time, etc., since start.
- ierr output error code; if it is set to non-zero, the current call to PRIMME will stop.

This function is called at the following events:

• *event == primme_event_outer_iteration: every outer iterations.

For this event the following inputs are provided: basisEvals, basisNorms, basisSize, basisFlags, iblock and blockSize.

basisNorms[iblock[i]] has the residual norm for the selected pair in the block. PRIMME avoids computing the residual of soft-locked pairs, basisNorms[i] for i<iblock[0]. So those values may correspond to previous iterations. The values basisNorms[i] for i>iblock[blockSize-1] are not valid.

If *locking* is enabled, lockedEvals, numLocked, lockedFlags and lockedNorms are also provided.

inner_its and LSRes are not provided.

• *event == primme_event_inner_iteration: every QMR iteration.

basisEvals[0] and basisNorms[0] provides the approximate eigenvalue and the residual norm of the pair which is improved in the current correction equation. If convTest is primme_adaptive or primme_adaptive_ETolerance, basisEvals[0] and basisNorms[0] are updated every QMR iteration.

inner_its and LSRes are also provided.

lockedEvals, numLocked, lockedFlags and lockedNorms may not be provided.

• *event == primme_event_converged: a new eigenpair in the basis passed the convergence criterion.

iblock[0] is the index of the newly converged pair in the basis which will be locked or soft-locked. The following are provided: basisEvals, basisNorms, basisSize, basisFlags and blockSize[0] == 1.

lockedEvals, numLocked, lockedFlags and lockedNorms may not be provided.

inner_its and LSRes are not provided.

*event == primme_event_locked: new pair was added to the locked eigenvectors.

lockedEvals, numLocked, lockedFlags and lockedNorms are provided. The last element of lockedEvals, lockedFlags and lockedNorms corresponds to the recent locked pair.

basisEvals, numConverged, basisFlags and basisNorms may not be provided.

inner_its and LSRes are not provided.

The values of basisFlags and lockedFlags are:

- 0: unconverged.
- 1: internal use; only in basisFlags.
- 2: passed convergence test convTestFun.
- 3: *practically converged* because the solver may not be able to reduce the residual norm further without recombining the locked eigenvectors.

Input/output:

primme_initialize() sets this field to NULL;

```
dprimme() sets this field to an internal function if it is NULL;
this field is read by dprimme().
```

void *monitor

This field may be used to pass any required information to the function monitorFun.

Input/output:

```
primme_initialize() sets this field to NULL;
```

PRIMME_INT stats.numOuterIterations

Hold the number of outer iterations. The value is available during execution and at the end.

Input/output:

```
primme_initialize() sets this field to 0;
written by dprimme().
```

PRIMME_INT stats.numRestarts

Hold the number of restarts during execution and at the end.

Input/output:

```
primme_initialize() sets this field to 0;
written by dprimme().
```

PRIMME INT stats.numMatvecs

Hold how many vectors the operator in *matrixMatvec* has been applied on. The value is available during execution and at the end.

Input/output:

```
primme_initialize() sets this field to 0;
written by dprimme().
```

PRIMME_INT stats.numPreconds

Hold how many vectors the operator in *applyPreconditioner* has been applied on. The value is available during execution and at the end.

Input/output:

```
primme_initialize() sets this field to 0;
written by dprimme().
```

${\it PRIMME_INT}~{\tt stats.numGlobalSum}$

Hold how many times <code>globalSumReal</code> has been called. The value is available during execution and at the end.

Input/output:

```
primme_initialize() sets this field to 0;
written by dprimme().
```

double stats.volumeGlobalSum

Hold how many REAL have been reduced by *globalSumReal*. The value is available during execution and at the end.

```
primme_initialize() sets this field to 0;
written by dprimme().
```

double stats.elapsedTime

Hold the wall clock time spent by the call to <code>dprimme()</code> or <code>zprimme()</code>. The value is available at the end of the execution.

Input/output:

```
primme_initialize() sets this field to 0;
written by dprimme().
```

double stats.timeMatvec

Hold the wall clock time spent by *matrixMatvec*. The value is available at the end of the execution.

Input/output:

```
primme_initialize() sets this field to 0;
written by dprimme().
```

double stats.timePrecond

Hold the wall clock time spent by *applyPreconditioner*. The value is available at the end of the execution.

Input/output:

```
primme_initialize() sets this field to 0;
written by dprimme().
```

double stats.timeOrtho

Hold the wall clock time spent by orthogonalization. The value is available at the end of the execution.

Input/output:

```
primme_initialize() sets this field to 0; written by dprimme().
```

double stats.timeGlobalSum

Hold the wall clock time spent by globalSumReal. The value is available at the end of the execution.

Input/output:

```
primme_initialize() sets this field to 0;
written by dprimme().
```

double stats.estimateMinEVal

Hold the estimation of the smallest eigenvalue for the current eigenproblem. The value is available during execution and at the end.

Input/output:

```
primme_initialize() sets this field to 0;
written by dprimme().
```

double stats.estimateMaxEVal

Hold the estimation of the largest eigenvalue for the current eigenproblem. The value is available during execution and at the end.

Input/output:

```
primme_initialize() sets this field to 0;
written by dprimme().
```

double stats.estimateLargestSVal

Hold the estimation of the largest singular value (i.e., the absolute value of the eigenvalue with largest absolute value) for the current eigenproblem. The value is available during execution and at the end.

Input/output:

```
primme_initialize() sets this field to 0;
written by dprimme().
```

double stats.maxConvTol

Hold the maximum residual norm of the converged eigenvectors. The value is available during execution and at the end.

Input/output:

```
primme_initialize() sets this field to 0;
written by dprimme().
```

```
void (*convTestFun) (double *eval, void *evec, double *resNorm, int *isconv, primme_params *primme, int *ierr)
```

Function that evaluates if the approximate eigenpair has converged. If NULL, it is used the default convergence criteria (see eps).

Parameters

- **eval** the approximate value to evaluate.
- **evec** one dimensional array of size *nLocal* containing the approximate vector; it can be NULL.
- resNorm the norm of the residual vector.
- isconv (output) the function sets zero if the pair is not converged and non zero otherwise.
- **primme** parameters structure.
- ierr output error code; if it is set to non-zero, the current call to PRIMME will stop.

The actual type of evec depends on which function is being calling. For <code>dprimme()</code>, it is double, for <code>zprimme()</code> it is <code>PRIMME_COMPLEX_DOUBLE</code>, for <code>sprimme()</code> it is <code>float</code> and for <code>cprimme()</code> it is <code>PRIMME_COMPLEX_FLOAT</code>.

Input/output:

```
primme_initialize() sets this field to NULL;
this field is read by dprimme().
```

void *convtest

This field may be used to pass any required information to the function convTestFun.

```
primme_initialize() sets this field to NULL;
```

2.6 Preset Methods

primme_preset_method

PRIMME DEFAULT MIN TIME

Set as PRIMME_JDQMR_ETol when target is either primme_smallest or primme_largest, and as PRIMME_JDQMR otherwise. This method is usually the fastest if the cost of the matrix vector product is inexpensive.

PRIMME DEFAULT MIN MATVECS

Currently set as PRIMME_GD_Olsen_plusK; this method usually performs fewer matrix vector products than other methods, so it's a good choice when this operation is expensive.

PRIMME DYNAMIC

Switches to the best method dynamically; currently, between methods PRIMME_DEFAULT_MIN_TIME and PRIMME_DEFAULT_MIN_MATVECS.

With PRIMME_DYNAMIC primme_set_method() sets dynamicMethodSwitch = 1 and makes the same changes as for method PRIMME_DEFAULT_MIN_TIME.

PRIMME Arnoldi

Arnoldi implemented à la Generalized Davidson.

With PRIMME Arnoldi primme set method() sets:

- locking = 0;
- maxPrevRetain = 0;
- precondition = 0;
- maxInnerIterations = 0.

PRIMME GD

Generalized Davidson.

With PRIMME_GD primme_set_method() sets:

- locking = 0;
- maxPrevRetain = 0;
- robustShifts = 1;
- maxInnerIterations = 0;
- RightX = 0;
- SkewX = 0.

PRIMME_GD_plusK

GD with locally optimal restarting.

With PRIMME_GD_plusK primme_set_method() sets maxPrevRetain = 2 if maxBlockSize is 1 and numEvals > 1; otherwise it sets maxPrevRetain to maxBlockSize. Also:

- locking = 0;
- maxInnerIterations = 0;
- RightX = 0;
- SkewX = 0.

PRIMME_GD_Olsen_plusK

GD+k and the cheap Olsen's Method.

With $PRIMME_GD_Olsen_plusK$ primme_set_method() makes the same changes as for method $PRIMME_GD_plusK$ and sets RightX = 1.

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PRIMME_JD_Olsen_plusK

GD+k and Olsen's Method.

With $PRIMME_JD_Olsen_plusK$ primme_set_method() makes the same changes as for method $PRIMME_GD_plusK$ and also sets robustShifts = 1, RightX to 1, and SkewX to 1.

PRIMME RQI

(Accelerated) Rayleigh Quotient Iteration.

With PRIMME_RQI primme_set_method() sets:

```
• locking = 1;
• maxPrevRetain = 0;
• robustShifts = 1;
• maxInnerIterations = -1;
• LeftQ = 1;
• LeftX = 1;
• RightQ = 0;
• RightX = 1;
• SkewQ = 0;
• SkewX = 0;
• convTest = primme_full_LTolerance.
```

Note: If numTargetShifts > 0 and targetShifts are provided, the interior problem solved uses these shifts in the correction equation. Therefore RQI becomes INVIT (inverse iteration) in that case.

PRIMME JDOR

Jacobi-Davidson with fixed number of inner steps.

With PRIMME_JDQR primme_set_method() sets:

```
locking = 1;
maxPrevRetain = 1;
robustShifts = 0;
maxInnerIterations = 10 if it is 0;
LeftQ = 0;
LeftX = 1;
RightQ = 1;
RightX = 1;
SkewQ = 1;
SkewX = 1;
relTolBase = 1.5;
convTest = primme_full_LTolerance.
```

PRIMME_JDQMR

Jacobi-Davidson with adaptive stopping criterion for inner Quasi Minimum Residual (QMR).

With PRIMME_JDQMR primme_set_method() sets:

```
locking = 0;
maxPrevRetain = 1 if it is 0
maxInnerIterations = -1;
LeftQ = precondition;
LeftX = 1;
RightQ = 0;
RightX = 0;
SkewQ = 0;
```

```
• SkewX = 1;
```

• convTest = primme_adaptive.

PRIMME_JDQMR_ETol

JDQMR but QMR stops after residual norm reduces by a 0.1 factor.

With PRIMME_JDQMR_ETol primme_set_method() makes the same changes as for the method PRIMME_JDQMR and sets convTest = primme_adaptive_ETolerance.

PRIMME STEEPEST DESCENT

Steepest descent.

With PRIMME_STEEPEST_DESCENT primme_set_method() sets:

```
• locking = 1;
```

- maxBasisSize = numEvals * 2;
- minRestartSize = numEvals;
- maxBlockSize = numEvals;
- scheme = primme_thick;
- maxPrevRetain = 0;
- robustShifts = 0;
- maxInnerIterations = 0;
- RightX = 1;
- SkewX = 0.

PRIMME_LOBPCG_OrthoBasis

LOBPCG with orthogonal basis.

With PRIMME LOBPCG OrthoBasis primme set method() sets:

```
• locking = 0;
```

- maxBasisSize = numEvals * 3;
- minRestartSize = numEvals;
- maxBlockSize = numEvals;
- scheme = primme_thick;
- maxPrevRetain = numEvals;
- robustShifts = 0;
- maxInnerIterations = 0;
- RightX = 1;
- SkewX = 0.

${\tt PRIMME_LOBPCG_OrthoBasis_Window}$

LOBPCG with sliding window of maxBlockSize < 3 * numEvals.

With PRIMME_LOBPCG_OrthoBasis_Window primme_set_method() sets:

- locking = 0;
- maxBasisSize = maxBlockSize * 3;
- minRestartSize = maxBlockSize;
- scheme = primme_thick;
- maxPrevRetain = maxBlockSize;
- robustShifts = 0;
- maxInnerIterations = 0;
- RightX = 1;
- SkewX = 0.

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2.7 Error Codes

The functions <code>dprimme()</code> and <code>zprimme()</code> return one of the next values:

- 0: success.
- 1: reported only amount of required memory.
- -1: failed in allocating int or real workspace.
- -2: malloc failed in allocating a permutation integer array.
- -3: main_iter() encountered problem; the calling stack of the functions where the error occurred was printed in stderr.
- -4: if argument primme is NULL.
- -5: if n < 0 or nLocal < 0 or nLocal > n.
- -6: if numProcs < 1.
- -7: if matrixMatvec is NULL.
- -8: if applyPreconditioner is NULL and precondition > 0.
- -9: if massMatrixMatvec is not NULL (generalized Hermitian problem is not supported yet).
- -10: if numEvals > n.
- -11: if numEvals < 0.
- -12: if eps > 0 and eps < machine precision.
- -13: if target is not properly defined.
- -14: if target is one of primme_closest_geq, primme_closest_leq, primme_closest_abs or primme_largest_abs but numTargetShifts <= 0 (no shifts).
- -15: if target is one of primme_closest_geq, primme_closest_leq, primme_closest_abs or primme_largest_abs but targetShifts is NULL (no shifts array).
- -16: if numOrthoConst < 0 or numOrthoConst > n. (no free dimensions left).
- -17: if maxBasisSize < 2.
- -18: if minRestartSize < 0 or minRestartSize shouldn't be zero.
- -19: if maxBlockSize < 0 or maxBlockSize shouldn't be zero.
- -20: if maxPrevRetain < 0.
- -21: if scheme is not one of primme_thick or primme_dtr.
- -22: if initSize < 0.
- -23: if locking == 0 and initSize > maxBasisSize.
- -24: if locking and initSize > numEvals.
- -25: if maxPrevRetain + minRestartSize >= maxBasisSize.
- -26: if minRestartSize >= n.
- -27: if printLevel < 0 or printLevel > 5.
- -28: if convTest is not one of primme_full_LTolerance, primme_decreasing_LTolerance, primme_adaptive_ETolerance or primme_adaptive.
- -29: if convTest == primme_decreasing_LTolerance and relTolBase <= 1.

- -30: if evals is NULL, but not evecs and resNorms.
- -31: if evecs is NULL, but not evals and resNorms.
- -32: if resNorms is NULL, but not evecs and evals.
- -33: if locking == 0 and minRestartSize < numEvals.
- -34: if ldevecs < nLocal.
- -35: if *1dOPs* is not zero and less than *nLocal*.
- -36: not enough memory for realWork.
- -37: not enough memory for intWork.
- -38: if locking == 0 and target is primme_closest_leq or primme_closest_geq.

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CHAPTER

THREE

SINGULAR VALUE PROBLEMS

3.1 C Library Interface

The PRIMME SVDS interface is composed of the following functions. To solve real and complex singular value problems call respectively:

Other useful functions:

```
void primme_svds_initialize (primme_svds_params *primme_svds)
int primme_svds_set_method (primme_svds_preset_method method,
    primme_preset_method methodStage1,
    primme_preset_method methodStage2, primme_svds_params *primme_svds)
void primme_svds_display_params (primme_svds_params primme_svds)
void primme_svds_free (primme_svds_params *primme_svds)
```

PRIMME SVDS stores its data on the structure <code>primme_svds_params</code>. See <code>Parameters Guide</code> for an introduction about its fields.

3.1.1 Running

To use PRIMME SVDS, follow these basic steps.

1. Include:

```
#include "primme.h" /* header file is required to run primme */
```

2. Initialize a PRIMME SVDS parameters structure for default settings:

```
primme_svds_params primme_svds;
primme_svds_initialize (&primme_svds);
```

3. Set problem parameters (see also *Parameters Guide*), and, optionally, set one of the *preset methods*:

```
primme_svds.matrixMatvec = matrixMatvec; /* MV product */
primme_svds.m = 1000; /* set the matrix dimensions */
primme_svds.n = 100;
```

4. Then to solve a real singular value problem call:

```
ret = dprimme svds (svals, svecs, resNorms, &primme svds);
```

The previous is the double precision call. There is available calls for complex double, single and complex single; check <code>zprimme_svds()</code>, <code>sprimme_svds()</code> and <code>cprimme_svds()</code>.

To solve complex singular value problems call:

```
ret = zprimme_svds (svals, svecs, resNorms, &primme_svds);
```

The call arguments are:

- svals, array to return the found singular values;
- svecs, array to return the found left and right singular vectors;
- resNorms, array to return the residual norms of the found triplets; and
- ret, returned error code.
- 5. To free the work arrays in PRIMME SVDS:

```
primme_svds_free (&primme_svds);
```

3.1.2 Parameters Guide

PRIMME SVDS stores the data on the structure primme_svds_params, which has the next fields:

Basic

```
PRIMME_INT m, number of rows of the matrix.

PRIMME_INT n, number of columns of the matrix.

void (* matrixMatvec) (...), matrix-vector product.

int numSvals, how many singular triplets to find.

primme_svds_target target, which singular values to find.

double eps, tolerance of the residual norm of converged triplets.
```

For parallel programs

```
int numProcs, number of processes
int procID, rank of this process
PRIMME_INT mLocal, number of rows stored in this process
PRIMME_INT nLocal, number of columns stored in this process
void (* qlobalSumReal) (...), sum reduction among processes
```

Accelerate the convergence

```
void (* applyPreconditioner) (...), preconditioner-vector product.
int initSize, initial vectors as approximate solutions.
int maxBasisSize
int minRestartSize
int maxBlockSize
```

User data

```
void * commInfo
void * matrix
void * preconditioner
void * convtest
void * monitor
```

```
Advanced options
int numTargetShifts, for targeting interior singular values.
double * targetShifts
int numOrthoConst, orthogonal constrains to the singular vectors.
int locking
PRIMME_INT maxMatvecs
int intWorkSize
size t realWorkSize
PRIMME_INT iseed [4]
int * intWork
void * realWork
double aNorm
int printLevel
FILE * outputFile
primme_svds_operator method
primme_svds_operator methodStage2
primme params primme
primme_params primmeStage2
void (* convTestFun) (...), custom convergence criterion.
void (* monitorFun) (...), custom convergence history.
```

PRIMME SVDS requires the user to set at least the matrix dimensions $(m \times n)$ and the matrix-vector product (matrixMatvec), as they define the problem to be solved. For parallel programs, mLocal, nLocal, procID and globalSumReal are also required.

In addition, most users would want to specify how many singular triplets to find, and provide a preconditioner (if available).

It is useful to have set all these before calling <code>primme_svds_set_method()</code>. Also, if users have a preference on <code>maxBasisSize</code>, <code>maxBlockSize</code>, etc, they should also provide them into <code>primme_svds_params</code> prior to the <code>primme_svds_set_method()</code> call. This helps <code>primme_svds_set_method()</code> make the right choice on other parameters. It is sometimes useful to check the actual parameters that PRIMME SVDS is going to use (before calling it) or used (on return) by printing them with <code>primme_svds_display_params()</code>.

3.1.3 Interface Description

The next enumerations and functions are declared in primme.h.

sprimme svds

int **sprimme_svds** (float *svals, float *svecs, float *resNorms, primme_svds_params *primme_svds)
Solve a real singular value problem.

Parameters

- **svals** array at least of size *numSvals* to store the computed singular values; all processes in a parallel run return this local array with the same values.
- **resNorms** array at least of size *numSvals* to store the residual norms of the computed triplets; all processes in parallel run return this local array with the same values.
- **svecs** array at least of size (*mLocal* + *nLocal*) times *numSvals* to store columnwise the (local part of the) computed left singular vectors and the right singular vectors.
- primme_svds parameters structure.

Returns error indicator; see *Error Codes*.

On input, svecs should start with the content of the numOrthoConst left vectors, followed by the initSize left vectors, followed by the numOrthoConst right vectors and followed by the initSize right vectors. The i-th left vector starts at svecs[i* mLocal]. The i-th right vector starts at svecs[(numOrthoConst + initSize)* mLocal + i* nLocal].

On return, the i-th left singular vector starts at svecs[(numOrthoConst+i)* mLocal]. The i-th right singular vector starts at svecs[(numOrthoConst+initSize)* mLocal+(numOrthoConst+i)* nLocal]. The first vector has i=0.

dprimme svds

int **dprimme_svds** (double *svals, double *svecs, double *resNorms, primme_svds_params *primme_svds)

Solve a real singular value problem.

Parameters

- **svals** array at least of size *numSvals* to store the computed singular values; all processes in a parallel run return this local array with the same values.
- **resNorms** array at least of size *numSvals* to store the residual norms of the computed triplets; all processes in parallel run return this local array with the same values.
- **svecs** array at least of size (*mLocal* + *nLocal*) times *numSvals* to store columnwise the (local part of the) computed left singular vectors and the right singular vectors.
- primme_svds parameters structure.

Returns error indicator; see Error Codes.

On input, svecs should start with the content of the numOrthoConst left vectors, followed by the initSize left vectors, followed by the numOrthoConst right vectors and followed by the initSize right vectors. The i-th left vector starts at svecs[i* mLocal]. The i-th right vector starts at svecs[(numOrthoConst + initSize)* mLocal + i* nLocal].

On return, the i-th left singular vector starts at svecs[(numOrthoConst+i)* mLocal]. The i-th right singular vector starts at svecs[(numOrthoConst+initSize)* mLocal+(numOrthoConst+i)* nLocal]. The first vector has i=0.

cprimme svds

int cprimme_svds (float *svals, PRIMME_COMPLEX_FLOAT *svecs, float *resNorms, primme_svds_params *primme_svds)

Solve a complex singular value problem; see function dprimme_svds().

zprimme_svds

int zprimme_svds (double *svals, PRIMME_COMPLEX_DOUBLE *svecs, double *resNorms, primme_svds_params *primme_svds)

Solve a complex singular value problem; see function dprimme_svds().

primme svds initialize

void primme_svds_initialize (primme_svds_params *primme_svds)

Set PRIMME SVDS parameters structure to the default values.

Parameters

• primme_svds - parameters structure.

primme_svds_set_method

int primme_svds_set_method (primme_svds_preset_method method, primme_preset_method methodStage1, primme_preset_method methodStage2, primme_svds_params *primme_svds)

Set PRIMME SVDS parameters to one of the preset configurations.

Parameters

- **method** preset method to compute the singular triplets; one of
 - primme_svds_default, currently set as primme_svds_hybrid.
 - $primme_svds_normalequations$, compute the eigenvectors of A^*A or AA^* .
 - primme_svds_augmented, compute the eigenvectors of the augmented matrix, $\begin{pmatrix} 0 & A^* \\ A & 0 \end{pmatrix}$.
 - primme_svds_hybrid, start with primme_svds_normalequations; use the resulting approximate singular vectors as initial vectors for primme svds augmented if the required accuracy was not achieved.
- methodStage1 preset method to compute the eigenpairs at the first stage; see available values at primme_set_method().
- methodStage2 preset method to compute the eigenpairs with the second stage of primme_svds_hybrid; see available values at primme_set_method().
- primme_svds parameters structure.

See also Preset Methods.

primme_svds_display_params

void primme_svds_display_params (primme_svds_params primme_svds)

Display all printable settings of primme_svds into the file descriptor outputFile.

Parameters

• **primme_svds** – parameters structure.

primme_svds_free

void **primme_svds_free** (*primme_svds_params *primme_svds*)
Free memory allocated by PRIMME SVDS.

Parameters

• primme_svds – parameters structure.

3.2 FORTRAN Library Interface

The next enumerations and functions are declared in primme_svds_f77.h.

3.2.1 sprimme_svds_f77

sprimme_svds_f77 (svals, svecs, resNorms, primme_svds)
Solve a real singular value problem using single precision.

Parameters

- **svals** (*) (real) (output) array at least of size numSvals to store the computed singular values; all processes in a parallel run return this local array with the same values.
- resNorms (*) (real) array at least of size numSvals to store the residual norms of the computed triplets; all processes in parallel run return this local array with the same values.
- svecs (*) (real) array at least of size (mLocal + nLocal) times numSvals to store columnwise the (local part of the) computed left singular vectors and the right singular vectors.
- primme_svds (ptr) parameters structure.

Returns error indicator; see Error Codes.

3.2.2 cprimme svds f77

cprimme_svds_f77 (svals, svecs, resNorms, primme_svds)

Solve a complex singular value problem using single precision.

Parameters

- **svals** (*) (real) (output) array at least of size numSvals to store the computed singular values; all processes in a parallel run return this local array with the same values.
- resNorms (*) (real) array at least of size numSvals to store the residual norms of the computed triplets; all processes in parallel run return this local array with the same values.
- **svecs** (*) (complex) array at least of size (mLocal + nLocal) times numSvals to store columnwise the (local part of the) computed left singular vectors and the right singular vectors.
- primme_svds (ptr) parameters structure.

Returns error indicator; see *Error Codes*.

3.2.3 dprimme_svds_f77

dprimme_svds_f77 (svals, svecs, resNorms, primme_svds)
Solve a real singular value problem using double precision.

Parameters

• **svals**(*) (double precision) – (output) array at least of size numSvals to store the computed singular values; all processes in a parallel run return this local array with the same values.

- resNorms (*) (double precision) array at least of size numSvals to store the residual norms of the computed triplets; all processes in parallel run return this local array with the same values.
- svecs(*) (double precision) array at least of size (mLocal + nLocal) times numSvals to store columnwise the (local part of the) computed left singular vectors and the right singular vectors.
- **primme_svds** (ptr) parameters structure.

Returns error indicator; see *Error Codes*.

3.2.4 zprimme svds f77

zprimme_svds_f77 (svals, svecs, resNorms, primme_svds)

Solve a complex singular value problem using double precision.

Parameters

- **svals**(*) (double precision) (output) array at least of size numSvals to store the computed singular values; all processes in a parallel run return this local array with the same values.
- resNorms (*) (double precision) array at least of size numSvals to store the residual norms of the computed triplets; all processes in parallel run return this local array with the same values.
- **svecs(*)** (complex*16) array at least of size (mLocal + nLocal) times numSvals to store columnwise the (local part of the) computed left singular vectors and the right singular vectors.
- primme_svds (ptr) parameters structure.

Returns error indicator; see Error Codes.

3.2.5 primme svds initialize f77

primme_svds_initialize_f77 (primme_svds)

Set PRIMME SVDS parameters structure to the default values.

Parameters

• **primme svds** (ptr) – (output) parameters structure.

3.2.6 primme svds set method f77

primme_svds_set_method_f77 (method, methodStage1, methodStage2, primme_svds, ierr)
Set PRIMME SVDS parameters to one of the preset configurations.

- method (integer) (input) preset configuration to compute the singular triplets; one of
 - PRIMME_SVDS_default, currently set as PRIMME_SVDS_hybrid.
 - PRIMME_SVDS_normalequations, compute the eigenvectors of A^*A or AA^* .
 - PRIMME_SVDS_augmented, compute the eigenvectors of the augmented matrix, $\begin{pmatrix} 0 & A^* \\ A & 0 \end{pmatrix}$.

- PRIMME_SVDS_hybrid, start with PRIMME_SVDS_normalequations; use the resulting approximate singular vectors as initial vectors for PRIMME_SVDS_augmented if the required accuracy was not achieved.
- methodStage1 (primme_preset_method) (input) preset method to compute the eigenpairs at the first stage; see available values at primme_set_method_f77().
- methodStage2 (primme_preset_method) (input) preset method to compute the eigenpairs with the second stage of PRIMME_SVDS_hybrid; see available values at primme set method f77().
- **primme_svds** (ptr) (input/output) parameters structure.
- ierr (integer) (output) if 0, successful; if negative, something went wrong.

3.2.7 primme svds display params f77

primme_svds_display_params_f77 (primme_svds)

Display all printable settings of primme_svds into the file descriptor outputFile.

Parameters

• primme svds (ptr) – (input) parameters structure.

3.2.8 primme svds free f77

primme_svds_free_f77 (primme_svds)

Free memory allocated by PRIMME SVDS and delete all values set.

Parameters

• **primme_svds** (ptr) – (input/output) parameters structure.

3.2.9 primme svds set member f77

```
primme svds set member f77 (primme svds, label, value)
```

Set a value in some field of the parameter structure.

- **primme_svds** (ptr) (input) parameters structure.
- label (integer) field where to set value. One of:

```
PRIMME_SVDS_primme

PRIMME_SVDS_primmeStage2

PRIMME_SVDS_m

PRIMME_SVDS_n

PRIMME_SVDS_matrixMatvec

PRIMME_SVDS_applyPreconditioner

PRIMME_SVDS_numProcs

PRIMME_SVDS_procID

PRIMME_SVDS_mLocal

PRIMME_SVDS_nLocal
```

```
PRIMME SVDS comminfo
PRIMME_SVDS_globalSumReal
PRIMME_SVDS_numSvals
PRIMME_SVDS_target
PRIMME_SVDS_numTargetShifts
PRIMME_SVDS_targetShifts
PRIMME_SVDS_method
PRIMME_SVDS_methodStage2
PRIMME SVDS intWorkSize
PRIMME_SVDS_realWorkSize
PRIMME SVDS intWork
PRIMME_SVDS_realWork
PRIMME_SVDS_matrix
PRIMME_SVDS_preconditioner
PRIMME SVDS locking
PRIMME_SVDS_numOrthoConst
PRIMME_SVDS_aNorm
PRIMME_SVDS_eps
PRIMME_SVDS_precondition
PRIMME_SVDS_initSize
PRIMME SVDS maxBasisSize
PRIMME_SVDS_maxBlockSize
PRIMME_SVDS_maxMatvecs
PRIMME_SVDS_iseed
PRIMME SVDS printLevel
PRIMME_SVDS_outputFile
PRIMME_SVDS_stats_numOuterIterations
PRIMME_SVDS_stats_numRestarts
PRIMME_SVDS_stats_numMatvecs
PRIMME SVDS stats numPreconds
PRIMME SVDS stats elapsedTime
```

• **value** – (input) value to set.

Note: Don't use this function inside PRIMME SVDS's callback functions, e.g., matrixMatvec or applyPreconditioner, or in functions called by these functions.

3.2.10 primme_svdstop_get_member_f77

primme_svdstop_get_member_f77 (primme_svds, label, value)
Get the value in some field of the parameter structure.

- **primme_svds** (ptr) (input) parameters structure.
- label (integer) (input) field where to get value. One of the detailed in function primmesvds_top_set_member_f77().

• **value** – (output) value of the field.

Note: Don't use this function inside PRIMME SVDS's callback functions, e.g., matrixMatvec or applyPreconditioner, or in functions called by these functions. In those cases use primme_svds_get_member_f77().

Note: When label is one of PRIMME_SVDS_matrixMatvec, PRIMME_SVDS_applyPreconditioner, PRIMME_SVDS_commInfo, PRIMME_SVDS_intWork, PRIMME_SVDS_realWork, PRIMME_SVDS_matrix and PRIMME_SVDS_preconditioner, the returned value is a C pointer (void*). Use Fortran pointer or other extensions to deal with it. For instance:

```
use iso_c_binding
MPI_Comm comm

comm = MPI_COMM_WORLD
call primme_svds_set_member_f77(primme_svds, PRIMME_SVDS_commInfo, comm)
...
subroutine par_GlobalSumDouble(x,y,k,primme_svds)
use iso_c_binding
implicit none
...
MPI_Comm, pointer :: comm
type(c_ptr) :: pcomm

call primme_svds_get_member_f77(primme_svds, PRIMME_SVDS_commInfo, pcomm)
call c_f_pointer(pcomm, comm)
call MPI_Allreduce(x,y,k,MPI_DOUBLE,MPI_SUM,comm,ierr)
```

Most users would not need to retrieve these pointers in their programs.

3.2.11 primme svds get member f77

primme_svds_get_member_f77 (primme_svds, label, value)

Get the value in some field of the parameter structure.

Parameters

- **primme_svds** (ptr) (input) parameters structure.
- label (integer) (input) field where to get value. One of the detailed in function primme_svdstop_set_member_f77().
- **value** (output) value of the field.

Note: Use this function exclusively inside PRIMME SVDS's callback functions, e.g., matrixMatvec or applyPreconditioner, or in functions called by these functions. Otherwise, e.g., from the main program, use the function primme_svdstop_get_member_f77().

Note: When label is one of PRIMME_SVDS_matrixMatvec, PRIMME_SVDS_applyPreconditioner, PRIMME_SVDS_commInfo, PRIMME_SVDS_intWork, PRIMME_SVDS_realWork, PRIMME_SVDS_matrix and PRIMME_SVDS_preconditioner, the returned value is a C pointer (void*). Use Fortran pointer or other extensions to deal with it. For instance:

```
use iso_c_binding
MPI_Comm comm

comm = MPI_COMM_WORLD
call primme_svds_set_member_f77(primme_svds, PRIMME_SVDS_commInfo, comm)
...
subroutine par_GlobalSumDouble(x,y,k,primme_svds)
use iso_c_binding
implicit none
...
MPI_Comm, pointer :: comm
type(c_ptr) :: pcomm

call primme_svds_get_member_f77(primme_svds, PRIMME_SVDS_commInfo, pcomm)
call c_f_pointer(pcomm, comm)
call MPI_Allreduce(x,y,k,MPI_DOUBLE,MPI_SUM,comm,ierr)
```

Most users would not need to retrieve these pointers in their programs.

3.3 Python Interface

Primme.svds (A, k=6, ncv=None, tol=0, which='LM', v0=None, maxiter=None, return_singular_vectors=True, precAHA=None, precAAH=None, precAug=None, u0=None, orthou0=None, orthov0=None, return_stats=False, maxBlockSize=0, method=None, methodStage1=None, methodStage2=None, return_history=False, **kargs)

Compute k singular values and vectors of the matrix A.

Parameters

- A({sparse matrix, LinearOperator}) Array to compute the SVD on, of shape (M, N)
- **k** (*int*, *optional*) Number of singular values and vectors to compute. Must be 1 <= k < min(A.shape).
- ncv (int, optional) The maximum size of the basis
- tol (float, optional) Tolerance for singular values. Zero (default) means 10**4 times the machine precision.

A triplet (u, sigma, v) is marked as converged when ($\|A^*v - sigma^*u\|^{**2} + \|A.H^*u - sigma^*v\|^{**2}$)**.5 is less than "tol" * $\|A\|$, or close to the minimum tolerance that the method can achieve. See the note.

- which(str ['LM' | 'SM'] or number, optional)—Which k singular values to find:
 - 'LM': largest singular values
 - 'SM': smallest singular values
 - number : closest singular values to (referred as sigma later)
- u0 (ndarray, optional) Initial guesses for the left singular vectors.

If only u0 or v0 is provided, the other is computed. If both are provided, u0 and v0 should have the same number of columns.

- **v0** (ndarray, optional) Initial guesses for the right singular vectors.
- maxiter (int, optional) Maximum number of matvecs with A and A.H.
- precAHA ({N x N matrix, array, sparse matrix, LinearOperator}, optional) Approximate inverse of (A.H*A sigma**2*I). If provided and M>=N, it usually accelerates the convergence.
- **precAAH** ({M x M matrix, array, sparse matrix, LinearOperator}, optional) Approximate inverse of (A*A.H sigma**2*I). If provided and M<N, it usually accelerates the convergence.
- precAug ({ (M+N) x (M+N) matrix, array, sparse matrix, LinearOperator}, optional) Approximate inverse of ([zeros() A.H; zeros() A] sigma*I).
- orthou0 (ndarray, optional) Left orthogonal vector constrain.

Seek singular triplets orthogonal to orthou0 and orthov0. The provided vectors *should* be orthonormal. If only orthou0 or orthov0 is provided, the other is computed. Useful to avoid converging to previously computed solutions.

• orthov0 (ndarray, optional) - Right orthogonal vector constrain. See orthou0.

- maxBlockSize (int, optional) Maximum number of vectors added at every iteration.
- return_stats (bool, optional) If True, the function returns extra information (see stats in Returns).
- return_history (bool, optional) If True, the function returns performance information at every iteration

Returns

- **u** (*ndarray*, *shape=(M, k)*, *optional)* Unitary matrix having left singular vectors as columns. Returned if *return_singular_vectors* is True.
- \mathbf{s} (*ndarray*, *shape*=(k,)) The singular values.
- **vt** (*ndarray*, *shape=(k*, *N*), *optional*) Unitary matrix having right singular vectors as rows. Returned if *return_singular_vectors* is True.
- **stats** (*dict*, *optional* (*if return_stats*)) Extra information reported by PRIMME:
 - "numOuterIterations": number of outer iterations
 - "numRestarts": number of restarts
 - "numMatvecs": number of matvecs with A and A.H.
 - "numPreconds": cumulative number of applications of precAHA, precAAH and precAug
 - "elapsedTime": time that took
 - "rnorms" : ($\|A^*v[:,i] sigma[i]^*u[:,i]\|^* + \|A.H^*u[:,i] sigma[i]^*v[:,i]\|^* + 2$)**.5
 - "hist" : (if return_history) report at every outer iteration of:
 - * "elapsedTime": time spent up to now
 - * "numMatvecs": number of A*v and A.H*v spent up to now
 - * "nconv": number of converged triplets
 - * "sval": singular value of the first unconverged triplet
 - * "resNorm": residual norm of the first unconverged triplet

Notes

The default method used is the hybrid method, which first solves the equivalent eigenvalue problem A.H*A or A*A.H (normal equations) and then refines the solution solving the augmented problem. The minimum tolerance that this method can achieve is ||A||*epsilon, where epsilon is the machine precision. However it may not return triplets with singular values smaller than ||A||*epsilon if "tol" is smaller than ||A||*epsilon/sigma.

This function is a wrapper to PRIMME functions to find singular values and vectors¹.

References

See also:

Primme.eigsh() eigenvalue decomposition for a sparse symmetrix/complex Hermitian matrix A

scipy.sparse.linalg.eigs() eigenvalues and eigenvectors for a general (nonsymmetric) matrix A

¹ PRIMME Software, https://github.com/primme/primme

Examples

3.4 MATLAB Interface

function [varargout] = primme_svds(varargin)

primme_svds() finds a few singular values and vectors of a matrix A by calling PRIMME. A is typically large and sparse.

- S = primme_svds (A) returns a vector with the 6 largest singular values of A.
- S = primme_svds (AFUN, M, N) accepts the function handle AFUN to perform the matrix vector products with an M-by-N matrix A. AFUN (X, 'notransp') returns $A \times X$ while AFUN (X, 'transp') returns $A' \times X$. In all the following, A can be replaced by AFUN, M, N.
- S = primme_svds (A, k) computes the k largest singular values of A.
- S = primme_svds (A, k, sigma) computes the k singular values closest to the scalar shift sigma.
 - If sigma is a vector, find the singular value S(i) closest to each sigma(i), for i<=k.
 - If sigma is 'L', it computes the largest singular values.
 - if sigma is 'S', it computes the smallest singular values.
- S = primme_svds (A, k, sigma, OPTIONS) specifies extra solver parameters. Some default values are indicated in brackets {}:
 - aNorm: estimation of the 2-norm of A {0.0 (estimate the norm internally)}
 - tol: convergence tolerance NORM([A*V-U*S;A'*U-V*S]) <= tol * NORM(A) (see eps) { 1e-10 for double precision and 1e-3 for single precision}
 - maxit: maximum number of matvecs with A and A' (see maxMatvecs) {inf}
 - p: maximum basis size (see maxBasisSize)
 - disp: level of reporting 0-3 (see HIST) {0: no output}
 - isreal: if 0, the matrix is complex; else it's real {0: complex}
 - isdouble: if 0, the matrix is single; else it's double {1: double}
 - method: which equivalent eigenproblem to solve
 - 'primme_svds_normalequations': A'*A or A*A'
 - 'primme svds augmented': [0 A'; A 0]
 - 'primme_svds_hybrid': first normal equations and then augmented (default)
 - u0: initial guesses to the left singular vectors (see initSize) {[]}
 - v0: initial guesses to the right singular vectors {[]}
 - orthoConst: external orthogonalization constraints (see numOrthoConst) {[]}
 - locking: 1, hard locking; 0, soft locking
 - maxBlockSize: maximum block size
 - iseed: random seed
 - primme: options for first stage solver
 - primmeStage2: options for second stage solver
 - convTestFun: function handler with an alternative convergence criterion. If FUN(SVAL, LSVEC, RSVEC, RNORM) returns a nonzero value, the triplet (SVAL, LSVEC, RSVEC) with residual norm RNORM is considered converged.

The available options for OPTIONS.primme and primmeStage2 are the same as primme_eigs(), plus the option 'method'.

- S = primme_svds (A, k, sigma, OPTIONS, P) applies a preconditioner P as follows:
 - If P is a matrix it applies $P \setminus X$ and $P' \setminus X$ to approximate $A \setminus X$ and $A' \setminus X$.
 - If P is a function handle, PFUN, PFUN(X, 'notransp') returns P\X and PFUN(X, 'transp') returns P'\X, approximating A\X and A'\X respectively.
 - If P is a struct, it can have one or more of the following fields: P.AHA\X or P.AHA(X) returns an approximation of (A'*A)\X, P.AAH\X or P.AAH(X) returns an approximation of (A*A')\X, P.aug\X or P.aug(X) returns an approximation of [zeros(N, N) A'; A zeros(M, M)]\X.
 - If P is [] then no preconditioner is applied.
- S = primme_svds(A, k, sigma, OPTIONS, P1, P2) applies a factorized preconditioner:
 - If both P1 and P2 are nonempty, apply (P1*P2) \X to approximate A\X.
 - If P1 is [] and P2 is nonempty, then (P2'*P2) \X approximates A'*A. P2 can be the R factor of an (incomplete) QR factorization of A or the L factor of an (incomplete) LL' factorization of A'*A (RIF).
 - If both P1 and P2 are [] then no preconditioner is applied.

 $[U, S, V] = primme_svds(...)$ returns also the corresponding singular vectors. If A is M-by-N and k singular triplets are computed, then U is M-by-k with orthonormal columns, S is k-by-k diagonal, and V is N-by-k with orthonormal columns.

```
[S,R] = primme_svds(...)
```

 $[U, S, V, R] = primme_svds(...)$ returns the residual norm of each k triplet, NORM([A*V(:, i)-S(i,i)*U(:,i); A'*U(:,i)-S(i,i)*V(:,i)]).

 $[U, S, V, R, STATS] = primme_svds(...)$ returns how many times A and P were used and elapsed time. The application of A is counted independently from the application of A'.

[U, S, V, R, STATS, HIST] = primme_svds(...) returns the convergence history, instead of printing it. Every row is a record, and the columns report:

- HIST (:, 1): number of matvecs
- HIST(:,2): time
- HIST(:,3): number of converged/locked triplets
- HIST(:,4): stage
- HIST(:,5): block index
- HIST (:, 6): approximate singular value
- HIST(:,7): residual norm
- HIST(:,8): QMR residual norm

OPTS.disp controls the granularity of the record. If OPTS.disp == 1, HIST has one row per converged triplet and only the first four columns are reported; if OPTS.disp == 2, HIST has one row per outer iteration and only the first seven columns are reported; and otherwise HIST has one row per QMR iteration and all columns are reported.

Examples:

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See also: MATLAB svds, primme_eigs()

```
A = diag(1:50); A(200,1) = 0; % rectangular matrix of size 200x50
s = primme_svds(A,10) % the 10 largest singular values
s = primme_svds(A,10,'S') % the 10 smallest singular values
s = primme_svds(A, 10, 25) % the 10 closest singular values to 25
opts = struct();
opts.tol = 1e-4; % set tolerance
opts.method = 'primme_svds_normalequations' % set svd solver method
opts.primme.method = 'DEFAULT_MIN_TIME' % set first stage eigensolver method
opts.primme.maxBlockSize = 2; % set block size for first stage
[u,s,v] = primme_svds(A,10,'S',opts); % find 10 smallest svd triplets
opts.orthoConst = \{u, v\};
[s,rnorms] = primme_svds(A,10,'S',opts) % find another 10
% Compute the 5 smallest singular values of a rectangular matrix using
% Jacobi preconditioner on (A'*A)
A = \text{sparse}(\text{diag}(1:50) + \text{diag}(\text{ones}(49,1), 1));
A(200,50) = 1; % size(A) = [200 50]
P = diag(sum(abs(A).^2));
precond.AHA = @(x)P\x;
s = primme_svds(A,5,'S',[],precond) % find the 5 smallest values
% Estimation of the smallest singular value
A = diag([1 repmat(2,1,1000) 3:100]);
[~,sval,~,rnorm] = primme_svds(A,1,'S',struct('convTestFun',@(s,u,v,r)r<s*.1));
sval - rnorm % approximate smallest singular value
```

3.5 Parameter Description

3.5.1 primme_svds_params

```
primme_svds_params
```

Structure to set the problem matrix and the solver options.

```
PRIMME_INT m
```

Number of rows of the matrix.

Input/output:

```
primme_initialize() sets this field to 0;
this field is read by dprimme().
```

PRIMME INT n

Number of columns of the matrix.

Input/output:

```
primme_initialize() sets this field to 0;
this field is read by dprimme().
```

```
void (*matrixMatvec) (void *x, PRIMME_INT ldx, void *y, PRIMME_INT ldy, int *blockSize, int *transpose, primme_svds_params *primme_svds, int *ierr)
```

Block matrix-multivector multiplication, y = Ax if transpose is zero, and $y = A^*x$ otherwise.

Parameters

- **x** input array.
- ldx leading dimension of x.
- **y** output array.
- **ldy** leading dimension of y.
- blockSize number of columns in x and y.
- **transpose** if non-zero, the transpose A should be applied.
- primme_svds parameters structure.
- ierr output error code; if it is set to non-zero, the current call to PRIMME will stop.

If transpose is zero, then x and y are arrays of dimensions nLocal x blockSize and mLocal x blockSize respectively. Elsewhere they have dimensions mLocal x blockSize and nLocal x blockSize. Both arrays are in column-major order (elements in the same column with consecutive row indices are consecutive in memory).

The actual type of x and y depends on which function is being calling. For <code>dprimme_svds()</code>, it is <code>double</code>, for <code>zprimme_svds()</code> it is <code>PRIMME_COMPLEX_DOUBLE</code>, for <code>sprimme_svds()</code> it is <code>float</code> and for <code>cprimme_svds()</code> it is <code>PRIMME_COMPLEX_FLOAT</code>.

Input/output:

```
primme_initialize() sets this field to NULL;
this field is read by dprimme_svds() and zprimme_svds().
```

Note: Integer arguments are passed by reference to make easier the interface to other languages (like Fortran).

Block preconditioner-multivector application, $y = M^{-1}x$ for finding singular values close to σ . Depending on mode, M is expected to be an approximation of the following operators:

- primme_svds_op_AtA: $M \approx A^*Ax \sigma^2I$,
- primme_svds_op_AAt: $M \approx AA^*x \sigma^2I$,
- primme_svds_op_augmented: $M \approx \left(\begin{array}{cc} 0 & A^* \\ A & 0 \end{array} \right) \sigma I.$

Parameters

- **x** input array.
- **ldx** leading dimension of x.
- **y** output array.
- **ldy** leading dimension of y.
- blockSize number of columns in x and y.
- mode one of primme_svds_op_AtA, primme_svds_op_AAt on primme_svds_op_augmented.
- primme_svds parameters structure.
- ierr output error code; if it is set to non-zero, the current call to PRIMME will stop.

If mode is primme_svds_op_AtA, then x and y are arrays of dimensions nLocal x blockSize; if mode is primme_svds_op_AAt, they are mLocal x blockSize; and otherwise they are (mLocal + nLocal) x blockSize. Both arrays are in column-major order (elements in the same column with consecutive row indices are consecutive in memory).

The actual type of x and y depends on which function is being calling. For $dprimme_svds()$, it is double, for $sprimme_svds()$ it is $sprimme_svds()$ it is s

Input/output:

```
primme_initialize() sets this field to NULL;
this field is read by dprimme_svds() and zprimme_svds().
```

int numProcs

Number of processes calling dprimme_svds() or zprimme_svds() in parallel.

Input/output:

```
primme_initialize() sets this field to 1;
this field is read by dprimme() and zprimme svds().
```

int procID

The identity of the local process within a parallel execution calling <code>dprimme_svds()</code> or <code>zprimme_svds()</code>. Only the process with id 0 prints information.

Input/output:

```
primme_svds_initialize() sets this field to 0;
dprimme_svds() sets this field to 0 if numProcs is 1;
this field is read by dprimme_svds() and zprimme_svds().
```

PRIMME INT mLocal

Number of local rows on this process. The value depends on how the matrix and preconditioner is distributed along the processes.

Input/output:

```
primme_svds_initialize() sets this field to -1;
dprimme_svds() sets this field to m if numProcs is 1;
this field is read by dprimme_svds() and zprimme_svds().
```

See also: matrixMatvec and applyPreconditioner.

PRIMME INT nLocal

Number of local columns on this process. The value depends on how the matrix and preconditioner is distributed along the processes.

Input/output:

```
primme_svds_initialize() sets this field to -1;
dprimme_svds() sets this field to to n if numProcs is 1;
this field is read by dprimme_svds() and zprimme_svds().
```

void *commInfo

A pointer to whatever parallel environment structures needed. For example, with MPI, it could be a pointer to the MPI communicator. PRIMME does not use this. It is available for possible use in user functions defined in matrixMatvec, applyPreconditioner and globalSumReal.

Input/output:

```
primme_svds_initialize() sets this field to NULL;
```

```
void (*globalSumReal) (double *sendBuf, double *recvBuf, int *count, primme_svds_params *primme_svds, int *ierr)
```

Global sum reduction function. No need to set for sequential programs.

Parameters

- sendBuf array of size count with the local input values.
- recvBuf array of size count with the global output values so that the i-th element of recvBuf is the sum over all processes of the i-th element of sendBuf.
- count array size of sendBuf and recvBuf.
- primme svds parameters structure.
- ierr output error code; if it is set to non-zero, the current call to PRIMME will stop.

The actual type of <code>sendBuf</code> and <code>recvBuf</code> depends on which function is being calling. For <code>dprimme_svds()</code> and <code>zprimme_svds()</code> it is double, and for <code>sprimme_svds()</code> and <code>cprimme_svds()</code> it is float. Note that <code>count</code> is the number of values of the actual type.

Input/output:

```
primme_svds_initialize() sets this field to an internal function;
dprimme_svds() sets this field to an internal function if numProcs is 1 and
globalSumReal is NULL;
this field is read by dprimme_svds() and zprimme_svds().
```

When MPI is used, this can be a simply wrapper to MPI_Allreduce() as shown below:

```
void par_GlobalSumForDouble(void *sendBuf, void *recvBuf, int *count,
                               primme_svds_params *primme_svds, int *ierr) {
       MPI_Comm communicator = *(MPI_Comm *) primme_svds->commInfo;
       if (MPI_Allreduce(sendBuf, recvBuf, *count, MPI_DOUBLE, MPI_SUM,
                       communicator) == MPI_SUCCESS) {
           *ierr = 0;
       } else {
           *ierr = 1;
       }
    }
    When calling sprimme_svds() and cprimme_svds() replace MPI_DOUBLE by `MPI_FLOAT.
int numSvals
    Number of singular triplets wanted.
    Input/output:
        primme svds initialize() sets this field to 1;
        this field is read by primme_svds_set_method() (see Preset Methods) and
        dprimme_svds().
primme_svds_target target
    Which singular values to find:
    primme_svds_smallest Smallest singular values; targetShifts is ignored.
    primme_svds_largest Largest singular values; targetShifts is ignored.
    primme svds closest abs Closest in absolute value to the shifts in targetShifts.
    Input/output:
        primme_svds_initialize() sets this field to primme_svds_smallest;
        this field is read by dprimme_svds() and zprimme_svds().
int numTargetShifts
    Size of the array targetShifts. Used only when target is primme_svds_closest_abs. The
    default values is 0.
    Input/output:
        primme_svds_initialize() sets this field to 0;
        this field is read by dprimme_svds() and zprimme_svds().
double *targetShifts
    Array of shifts, at least of size numTargetShifts. Used only when target is
    primme_svds_closest_abs.
    Singular values are computed in order so that the i-th singular value is the closest to the i-th shift. If
    numTargetShifts < numSvals, the last shift given is used for all the remaining i's.
    Input/output:
        primme_svds_initialize() sets this field to NULL;
        this field is read by dprimme_svds() and zprimme_svds().
```

Eventually this is used by <code>dprimme()</code> and <code>zprimme()</code>. Please see considerations of

int printLevel

Note:

targetShifts.

The level of message reporting from the code. All output is written in outputFile.

One of:

- 0: silent.
- 1: print some error messages when these occur.
- 2: as in 1, and info about targeted singular triplets when they are marked as converged:

```
#Converged $1 sval[ $2 ]= $3 norm $4 Mvecs $5 Time $7 stage $10
or locked:
```

```
#Lock striplet[ $1 ]= $3 norm $4 Mvecs $5 Time $7 stage $10
```

• 3: as in 2, and info about targeted singular triplets every outer iteration:

```
OUT $6 conv $1 blk $8 MV $5 Sec $7 SV $3 |r| $4 stage $10
```

Also, if using PRIMME_DYNAMIC, show JDQMR/GD+k performance ratio and the current method in use.

• 4: as in 3, and info about targeted singular triplets every inner iteration:

```
INN MV $5 Sec $7 Sval $3 Lin|r| $9 SV|r| $4 stage $10
```

• 5: as in 4, and verbose info about certain choices of the algorithm.

Output key:

- \$1: Number of converged triplets up to now.
- \$2: The index of the triplet currently converged.
- \$3: The singular value.
- \$4: Its residual norm.
- \$5: The current number of matrix-vector products.
- \$6: The current number of outer iterations.
- \$7: The current elapsed time.
- \$8: Index within the block of the targeted triplet.
- \$9: QMR norm of the linear system residual.
- \$10: stage (1 or 2)

In parallel programs, when printLevel is 0 to 4 only procID 0 produces output. For printLevel 5 output can be produced in any of the parallel calls.

Input/output:

```
primme_svds_initialize() sets this field to 1;
this field is read by dprimme_svds() and zprimme_svds().
```

Note: Convergence history for plotting may be produced simply by:

```
grep OUT outpufile | awk '{print $8" "$14}' > out
grep INN outpufile | awk '{print $3" "$11}' > inn
```

Or in gnuplot:

```
plot 'out' w lp, 'inn' w lp
```

double aNorm

An estimate of the 2-norm of A, which is used in the default convergence criterion (see eps).

If aNorm is less than or equal to 0, the code uses the largest absolute Ritz value seen. On return, aNorm is then replaced with that value.

Input/output:

```
primme_svds_initialize() sets this field to 0.0;
this field is read and written by dprimme_svds() and zprimme_svds().
```

double eps

If convTestFun is NULL, a triplet (u, σ, v) is marked as converged when $\sqrt{\|Av - \sigma u\|^2 + \|A^*u - \sigma v\|^2}$ is less than eps * aNorm, or close to the minimum tolerance that the selected method can achieve in the given machine precision. See *Preset Methods*.

The default value is machine precision times 10^4 .

Input/output:

```
primme_svds_initialize() sets this field to 0.0;
this field is read by dprimme_svds() and zprimme_svds().
```

FILE *outputFile

Opened file to write down the output.

Input/output:

```
primme_svds_initialize() sets this field to the standard output;
this field is read by dprimme_svds(), zprimme_svds() and
primme_svds_display_params()
```

int locking

If set to 1, the underneath eigensolvers will use hard locking. See *locking*.

Input/output:

```
primme_svds_initialize() sets this field to -1;
written by primme_svds_set_method() (see Preset Methods);
this field is read by dprimme_svds() and zprimme_svds().
```

int initSize

On input, the number of initial vector guesses provided in svecs argument in $dprimme_svds()$ and $zprimme_svds()$.

On output, *initSize* holds the number of converged triplets. Without *locking* all *numSvals* approximations are in svecs but only the first *initSize* are converged.

During execution, it holds the current number of converged triplets.

Input/output:

```
primme_svds_initialize() sets this field to 0;
this field is read and written by dprimme_svds() and zprimme_svds().
```

int numOrthoConst

Number of vectors to be used as external orthogonalization constraints. The left and the right vector constraints are provided as input of the svecs argument in <code>sprimme_svds()</code> or other variant, and must be orthonormal.

PRIMME SVDS finds new triplets orthogonal to these constraints (equivalent to solving the problem $(I-UU^*)A(I-VV^*)$ where U and V are the given left and right constraint vectors). This is a handy feature if some singular triplets are already known, or for finding more triplets after a call to $dprimme_svds()$ or $zprimme_svds()$, possibly with different parameters (see an example in TEST/exsvd_zseq.c).

Input/output:

```
primme_svds_initialize() sets this field to 0;
this field is read by dprimme_svds() and zprimme_svds().
```

int maxBasisSize

The maximum basis size allowed in the main iteration. This has memory implications.

Input/output:

```
primme_svds_initialize() sets this field to 0;
this field is read and written by primme_svds_set_method() (see Preset Methods);
this field is read by dprimme_svds() and zprimme_svds().
```

int maxBlockSize

The maximum block size the code will try to use.

The user should set this based on the architecture specifics of the target computer, as well as any a priori knowledge of multiplicities. The code does *not* require that maxBlockSize > 1 to find multiple triplets. For some methods, keeping to 1 yields the best overall performance.

Input/output:

```
primme_svds_initialize() sets this field to 1;
this field is read and written by primme_svds_set_method() (see Preset Methods);
this field is read by dprimme_svds() and zprimme_svds().
```

PRIMME_INT maxMatvecs

Maximum number of matrix vector multiplications (approximately half the number of preconditioning operations) that the code is allowed to perform before it exits.

Input/output:

```
primme_svds_initialize() sets this field to INT_MAX;
this field is read by dprimme_svds() and zprimme_svds().
```

int intWorkSize

If <code>dprimme_svds()</code> or <code>zprimme_svds()</code> is called with all arguments as NULL except for <code>primme_svds_params</code> then it returns immediately with <code>intWorkSize</code> containing the size in bytes of the integer workspace that will be required by the parameters set.

Otherwise if <code>intWorkSize</code> is not 0, it should be the size of the integer work array *in bytes* that the user provides in <code>intWork</code>. If <code>intWorkSize</code> is 0, the code will allocate the required space, which can be freed later by calling <code>primme_svds_free()</code>.

Input/output:

```
primme_svds_initialize() sets this field to 0;
this field is read and written by dprimme_svds() and zprimme_svds().
```

size_t realWorkSize

If <code>dprimme_svds()</code> or <code>zprimme_svds()</code> is called with all arguments as NULL except for <code>primme_svds_params</code> then it returns immediately with <code>realWorkSize</code> containing the size <code>in bytes</code> of the real workspace that will be required by the parameters set.

Otherwise if realWorkSize is not 0, it should be the size of the real work array in bytes that the user provides in realWork. If realWorkSize is 0, the code will allocate the required space, which can be freed later by calling primme_svds_free().

Input/output:

```
primme_svds_initialize() sets this field to 0;
this field is read and written by dprimme_svds() and zprimme_svds().
```

int *intWork

Integer work array.

If NULL, the code will allocate its own workspace. If the provided space is not enough, the code will return the error code -21.

Input/output:

```
primme_svds_initialize() sets this field to NULL;
this field is read and written by dprimme svds() and zprimme svds().
```

void *realWork

Real work array.

If NULL, the code will allocate its own workspace. If the provided space is not enough, the code will return the error code -20.

Input/output:

```
primme_svds_initialize() sets this field to NULL;
this field is read and written by dprimme_svds() and zprimme_svds().
```

PRIMME INT iseed

The PRIMME_INT iseed[4] is an array with the seeds needed by the LAPACK dlarnv and zlarnv.

The default value is an array with values -1, -1, -1 and -1. In that case, iseed is set based on the value of procID to avoid every parallel process generating the same sequence of pseudorandom numbers.

Input/output:

```
primme_svds_initialize() sets this field to [-1, -1, -1, -1]; this field is read and written by dprimme_svds() and zprimme_svds().
```

void *matrix

This field may be used to pass any required information in the matrix-vector product matrixMatvec.

Input/output:

```
primme_svds_initialize() sets this field to NULL;
```

void *preconditioner

This field may be used to pass any required information in the preconditioner function applyPreconditioner.

Input/output:

```
primme_svds_initialize() sets this field to NULL;
```

int precondition

Set to 1 to use preconditioning. Make sure applyPreconditioner is not NULL then!

Input/output:

```
primme_svds_initialize() sets this field to 0;
this field is read and written by primme_svds_set_method() (see Preset Methods);
```

this field is read by dprimme_svds() and zprimme_svds().

primme_svds_op_operator method

Select the equivalent eigenvalue problem that will be solved:

- primme_svds_op_AtA: $A^*Ax = \sigma^2x$,
- primme_svds_op_AAt: $AA^*x = \sigma^2x$,

The options for this solver are stored in primme.

Input/output:

```
primme_svds_initialize() sets this field to primme_svds_op_none;
this field is read and written by primme_svds_set_method() (see Preset Methods);
this field is read by dprimme_svds() and zprimme_svds().
```

primme_svds_op_operator methodStage2

Select the equivalent eigenvalue problem that will be solved to refine the solution. The allowed options are primme_svds_op_none to not refine the solution and primme_svds_op_augmented to refine the solution by solving the augmented problem with the current solution as the initial vectors. See method.

The options for this solver are stored in primmeStage2.

Input/output:

```
primme_svds_initialize() sets this field to primme_svds_op_none;
this field is read and written by primme_svds_set_method() (see Preset Methods);
this field is read by dprimme_svds() and zprimme_svds().
```

primme_params primme

Parameter structure storing the options for underneath eigensolver that will be called at the first stage. See *method*.

Input/output:

```
primme_svds_initialize() initialize this structure;
this field is read and written by primme_svds_set_method() (see Preset Methods);
this field is read and written by dprimme_svds() and zprimme_svds().
```

primme_params primmeStage2

Parameter structure storing the options for underneath eigensolver that will be called at the second stage. See methodStage2.

Input/output:

```
primme_svds_initialize() initialize this structure;
this field is read and written by primme_svds_set_method() (see Preset Methods);
this field is read and written by dprimme_svds() and zprimme_svds().
```

```
void (*convTestFun) (double *sval, void *leftsvec, void *rightsvec, double *rNorm, int *isconv, primme_svds_params *primme_svds, int *ierr)
```

Function that evaluates if the approximate triplet has converged. If NULL, it is used the default convergence criteria (see eps).

Parameters

• **sval** – the approximate singular value to evaluate.

- **leftsvec** one dimensional array of size *mLocal* containing the approximate left singular vector; it can be NULL.
- **rightsvec** one dimensional array of size *nLocal* containing the approximate right singular vector; it can be NULL.
- resNorm the norm of the residual vector.
- isconv (output) the function sets zero if the pair is not converged and non zero otherwise
- primme_svds parameters structure.
- ierr output error code; if it is set to non-zero, the current call to PRIMME will stop.

The actual type of leftsvec and rightsvec depends on which function is being calling. For dprimme_svds(), it is double, for zprimme_svds() it is PRIMME_COMPLEX_DOUBLE, for sprimme_svds() it is float and for cprimme_svds() it is PRIMME_COMPLEX_FLOAT.

Warning: When solving the augmented problem (for the method <code>primme_svds_augmented</code> and at the second stage in the method <code>primme_svds_hybrid</code>), the given residual vector norm <code>resNorm</code> is an approximation of the actual residual. Also <code>leftsvec</code> and <code>rightsvec</code> may not have length 1.

Input/output:

```
svds_primme_initialize() sets this field to NULL;
this field is read and written by dprimme_svds().
```

void *convtest

This field may be used to pass any required information to the function convTestFun.

Input/output:

```
primme_svds_initialize() sets this field to NULL;
```

void (*monitorFun) (void *basisSvals, int *basisSize, int *basisFlags, int *iblock, int *block-Size, void *basisNorms, int *numConverged, void *lockedSvals, int *numLocked, int *lockedFlags, void *lockedNorms, int *inner_its, void *LSRes, primme_event *event, int *stage, primme_svds_params *primme_svds, int *ierr)

Convergence monitor. Used to customize how to report solver information during execution (stage, iteration number, matvecs, time, residual norms, targets, etc).

Parameters

- basisSvals array with approximate singular values of the basis.
- basisSize size of the arrays basisSvals, basisFlags and basisNorms.
- basisFlags state of every approximate triplet in the basis.
- **iblock** indices of the approximate triplet in the block.
- blockSize size of array iblock.
- basisNorms array with residual norms of the triplets in the basis.
- **numConverged** number of triplets converged in the basis plus the number of the locked triplets (note that this value isn't monotonic).
- lockedSvals array with the locked triplets.

- numLocked size of the arrays lockedSvals, lockedFlags and lockedNorms.
- lockedFlags state of each locked triplets.
- lockedNorms array with residual norms of the locked triplets.
- inner_its number of performed QMR iterations in the current correction equation.
- **LSRes** residual norm of the linear system at the current QMR iteration.
- event event reported.
- **stage** 0 for first stage, 1 for second stage.
- **primme_svds** parameters structure; the counter in stats are updated with the current number of matrix-vector products, iterations, elapsed time, etc., since start.
- ierr output error code; if it is set to non-zero, the current call to PRIMME will stop.

This function is called at the next events:

• *event == primme_event_outer_iteration: every outer iterations.

It is provided basisSvals, basisSize, basisFlags, iblock and blockSize.

basisNorms[iblock[i]] has the residual norms for the selected triplets in the block. PRIMME avoids computing the residual of soft-locked triplets, basisNorms[i] for i<iblock[0]. So those values may correspond to previous iterations. The values basisNorms[i] for i>iblock[blockSize-1] are not valid.

If *locking* is enabled, lockedSvals, numLocked, lockedFlags and lockedNorms are also provided.

inner_its and LSRes are not provided.

• *event == primme_event_inner_iteration: every QMR iteration.

basisSvals[0] and basisNorms[0] provides the approximate singular value and the residual norm of the triplet which is improved in the current correction equation. If convTest is primme_adaptive or primme_adaptive_ETolerance, basisSvals[0], and basisNorms[0] are updated every QMR iteration.

inner_its and LSRes are also provided.

lockedSvals, numLocked, lockedFlags, and lockedNorms may not be provided.

 *event == primme_event_converged: a new triplet in the basis passed the convergence criterion

iblock[0] is the index of the newly converged triplet in the basis which will be locked or soft locked. The following are provided: basisSvals, basisSize, basisFlags and blockSize[0] == 1.

lockedSvals, numLocked, lockedFlags and lockedNorms may not be provided.

inner_its and LSRes are not provided.

• *event == primme_event_locked: a new triplet added to the locked singular vectors.

lockedSvals, numLocked, lockedFlags and lockedNorms are provided. The last element of lockedSvals, lockedFlags and lockedNorms corresponds to the recent locked triplet.

basisSvals, numConverged, basisFlags and basisNorms may not be provided.

inner_its and LSRes are not be provided.

The values of basisFlags and lockedFlags are:

- 0: unconverged.
- 1: internal use; only in basisFlags.
- 2: passed convergence test (see *eps*).
- 3: converged because the solver may not be able to reduce the residual norm further.

Input/output:

```
primme_initialize() sets this field to NULL;
dprimme_svds() sets this field to an internal function if it is NULL;
this field is read by dprimme_svds() and zprimme_svds().
```

void *monitor

This field may be used to pass any required information to the function monitorFun.

Input/output:

```
primme_svds_initialize() sets this field to NULL;
```

PRIMME INT stats.numOuterIterations

Hold the number of outer iterations.

Input/output:

```
primme_svds_initialize() sets this field to 0;
written by dprimme_svds() and zprimme_svds().
```

PRIMME INT stats.numRestarts

Hold the number of restarts.

Input/output:

```
primme_svds_initialize() sets this field to 0;
written by dprimme_svds() and zprimme_svds().
```

PRIMME_INT stats.numMatvecs

Hold how many vectors the operator in matrixMatvec has been applied on.

Input/output:

```
primme_svds_initialize() sets this field to 0;
written by dprimme_svds() and zprimme_svds().
```

PRIMME_INT stats.numPreconds

Hold how many vectors the operator in applyPreconditioner has been applied on.

Input/output:

```
primme_svds_initialize() sets this field to 0;
written by dprimme_svds() and zprimme_svds().
```

$double \; \textbf{stats.elapsedTime}$

Hold the wall clock time spent by the call to dprimme_svds() or zprimme_svds().

Input/output:

```
primme_svds_initialize() sets this field to 0;
written by dprimme_svds() and zprimme_svds().
```

3.6 Preset Methods

primme_svds_preset_method

primme_svds_default

Set as primme svds hybrid.

primme_svds_normalequations

Solve the equivalent eigenvalue problem $A^*AV = \Sigma^2 V$ and computes U by normalizing the vectors AV. If m is smaller than n, AA^* is solved instead.

With primme_svds_normalequations $primme_svds_set_method()$ sets method to primme_svds_op_AtA if m is larger or equal than n, and to primme_svds_op_AAt otherwise; and methodStage2 is set to primme_svds_op_none.

The minimum residual norm that this method can achieve is $||A|| \epsilon \sigma^{-1}$, where ϵ is the machine precision and σ the required singular value.

primme_svds_augmented

Solve the equivalent eigenvalue problem
$$\begin{pmatrix} 0 & A^* \\ A & 0 \end{pmatrix} X = \sigma X$$
 with $X = \begin{pmatrix} V \\ U \end{pmatrix}$.

With primme_svds_augmented primme_svds_set_method() sets method to primme_svds_op_augmented and methodStage2 to primme_svds_op_none.

The minimum residual norm that this method can achieve is $||A||\epsilon$, where ϵ is the machine precision. However it may not return triplets with singular values smaller than $||A||\epsilon$.

primme_svds_hybrid

First solve the equivalent normal equations (see primme_svds_normalequations) and then refine the solution solving the augmented problem (see primme_svds_augmented).

With primme_svds_normalequations $primme_svds_set_method()$ sets method to primme_svds_op_AtA if m is larger or equal than n, and to primme_svds_op_AAt otherwise; and methodStage2 is set to primme_svds_op_augmented.

The minimum residual norm that this method can achieve is $||A||\epsilon$, where ϵ is the machine precision. However it may not return triplets with singular values smaller than $||A||\epsilon$ if eps is smaller than $||A||\epsilon\sigma^{-1}$.

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3.7 Error Codes

The functions <code>dprimme_svds()</code> and <code>zprimme_svds()</code> return one of the next values:

- 0: success,
- 1: reported only amount of required memory,
- -1: failed in allocating int or real workspace,
- -2: malloc failed in allocating a permutation integer array,
- -3: main_iter() encountered problem; the calling stack of the functions where the error occurred was printed in 'stderr'.
- -4: primme_svds is NULL,
- -5: Wrong value for m or n or mLocal or nLocal,
- -6: Wrong value for numProcs,
- -7: matrixMatvec is not set,
- -8: applyPreconditioner is not set but precondition == 1,
- -9: numProcs >1 but globalSumReal is not set,
- -10: Wrong value for numSvals, it's larger than min(m, n),
- -11: Wrong value for numSvals, it's smaller than 1,
- -13: Wrong value for target,
- -14: Wrong value for method,
- -15: Not supported combination of method and methodStage2,
- -16: Wrong value for printLevel,
- -17: svals is not set,
- -18: svecs is not set,
- -19: resNorms is not set
- -20: not enough memory for realWork
- -21: not enough memory for intWork
- -100 up to -199: eigensolver error from first stage; see the value plus 100 in *Error Codes*.
- -200 up to -299: eigensolver error from second stage; see the value plus 200 in *Error Codes*.

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