Chapter 14:

Aggregate Supply and the Short-Run Trade-Off Between Inflation and Unemployment

Learning objectives

- two models of aggregate supply in which output depends positively on the price level in the short run

- the short-run tradeoff between inflation and unemployment known as the Phillips curve

Two models of aggregate supply

1. The sticky-price model
2. The imperfect-information model.
   Both models imply:

$$Y = \overline{Y} + \alpha(P - P^e)$$

agg. output

natural rate of output

a positive parameter

the actual price level

the expected price level

The sticky-price model

- Reasons for sticky prices:
  - long-term contracts between firms and customers
  - menu costs
  - firms do not wish to annoy customers with frequent price changes
- Assumption:
  - Firms set their own prices (e.g. as in monopolistic competition)

The sticky-price model

- An individual firm's desired price is

$$p = P + a(Y - \overline{Y})$$

where $a > 0$.

Suppose two types of firms:

- firms with flexible prices, set prices as above
- firms with sticky prices, must set their price before they know how P and Y will turn out:

$$p = P^e + a(Y^e - \overline{Y}^e)$$

The sticky-price model

$$p = P^e + a(Y^e - \bar{Y}^e)$$

- Assume firms w/ sticky prices expect that output will equal its natural rate. Then,

$$p = P^e$$

- To derive the aggregate supply curve, we first find an expression for the overall price level.

- Let **s** denote the fraction of firms with sticky prices. Then, we can write the overall price level as

The sticky-price model

$$P = sP^e + (1-s)[P + a(Y - \bar{Y})]$$

price set by sticky price firms

price set by flexible price firms

- Subtract $(1-s)P$ from both sides:

$$sP = sP^e + (1-s)[a(Y - \bar{Y})]$$

- Divide both sides by s:

$$P = P^e + \left[\frac{(1-s)a}{s}\right](Y - \bar{Y})$$

The sticky-price model

$$P = P^e + \left[\frac{(1-s)a}{s}\right](Y - \bar{Y})$$

- High P^e ⟹ High P
  If firms expect high prices, then firms who must set prices in advance will set them high.
  Other firms respond by increasing prices.

- High Y ⟹ High P
  When income is high, the demand for goods is high. Firms with flexible prices set high prices.
  The greater the fraction of flexible price firms, the smaller is s and the bigger is the effect of $\triangle Y$ on P.

The sticky-price model

$$P = P^e + \left[\frac{(1-s)a}{s}\right](Y - \bar{Y})$$

- Finally, derive *AS* equation by solving for Y:

$$Y = \bar{Y} + \alpha(P - P^e),$$

$$\text{where} \quad \alpha = \frac{s}{(1-s)a}$$

The sticky-price model

The sticky-price model implies a pro-cyclical(顺周期) real wage:

Suppose aggregate output/income falls. Then,

- Firms see a fall in demand for their products.

- Firms with sticky prices reduce production, and hence reduce their demand for labor.

- The leftward shift in labor demand causes the real wage to fall.

The imperfect-information model

Assumptions:

- all wages and prices perfectly flexible, all markets clear

- each supplier produces one good, consumes many goods

- each supplier knows the nominal price of the good he/she produces, but does not know the overall price level

The imperfect-information model

- Supply of each good depends on its relative price: the nominal price of the good divided by the overall price level.

- Supplier doesn't know price level at the time he/she makes her production decision, so uses the expected price level, P^e.

- Suppose P rises but P^e does not.

  Then supplier thinks her relative price has risen, so she produces more.

  With many producers thinking this way, Y will rise whenever P rises above P^e.

Summary & implications

$$\boldsymbol{Y} = \overline{\boldsymbol{Y}} + \boldsymbol{\alpha}(\boldsymbol{P} - \boldsymbol{P}^e)$$

$\boldsymbol{P} > \boldsymbol{P}^e$

$\boldsymbol{P} = \boldsymbol{P}^e$

$\boldsymbol{P} < \boldsymbol{P}^e$

P

LRAS

SRAS

Y

$\overline{Y}$
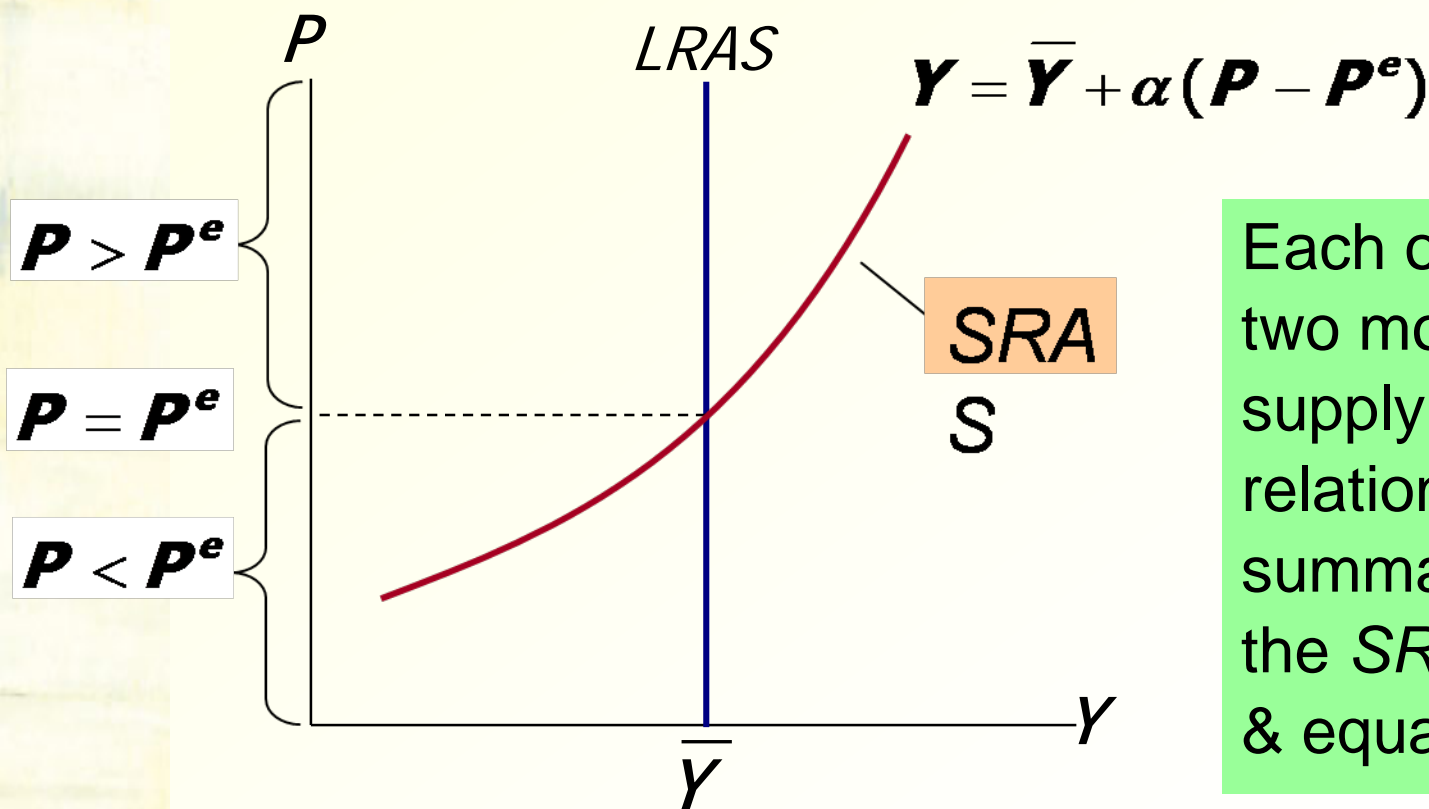
Each of the two models of agg. supply imply the relationship summarized by the *SRAS* curve & equation

Summary & implications

Suppose a positive *AD* shock moves output above its natural rate and *P* above the level people had expected.

Over time, P^e rises, *SRAS* shifts up, and output returns to its natural rate.

SRAS equation: $Y = \bar{Y} + \alpha(P - P^e)$

P

$LRAS$

SRAS$_2$

SRAS$_1$

$P_3 = P_3^e$

P_2

$P_2^e = P_1 = P_1^e$

AD_2

AD_1

Y

$Y_3 = Y_1 = \bar{Y}$

Y_2
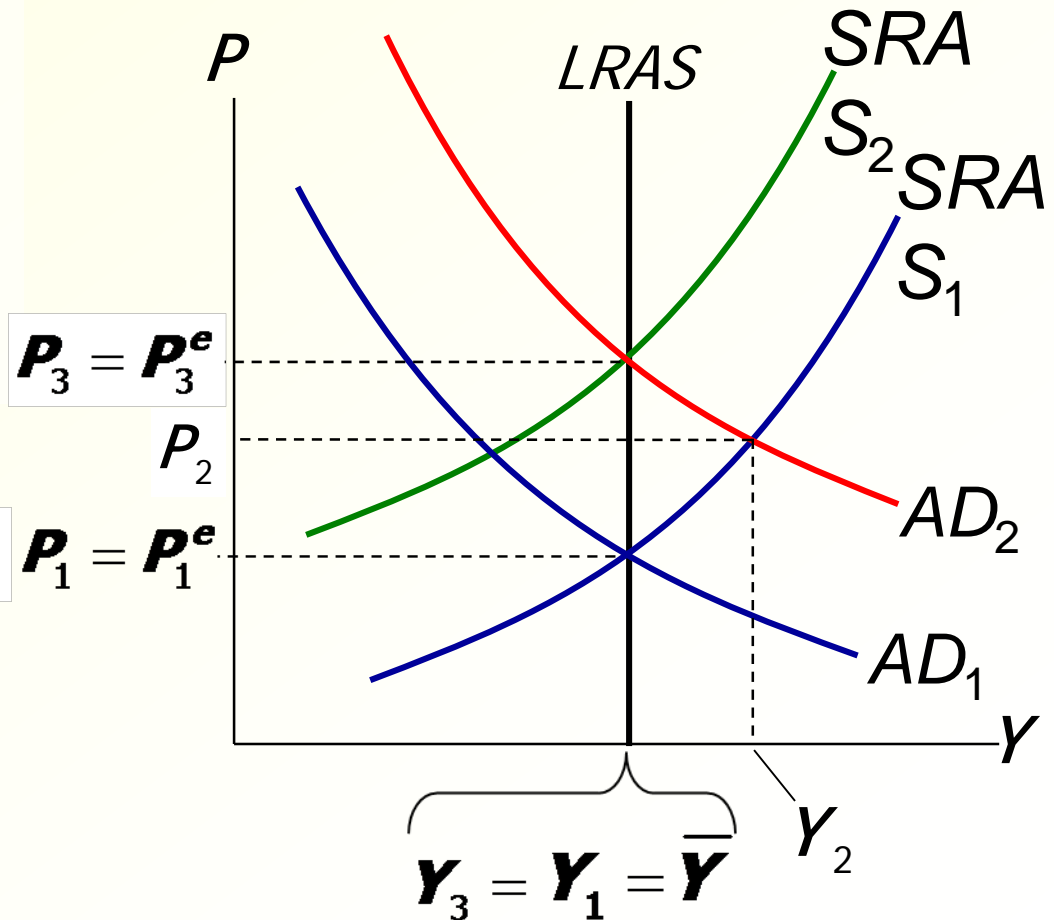
Inflation, Unemployment and the Phillips Curve

The **Phillips curve** states that π depends on

- expected inflation, π^e

- **cyclical unemployment**: the deviation of the actual rate of unemployment from the natural rate

- supply shocks, ν

$$\pi = \pi^e - \beta(u - u^n) + \nu$$

where $\beta > 0$ is an exogenous constant.

Deriving the Phillips Curve from *SRAS*

(1) $\quad Y = \bar{Y} + \alpha(P - P^e)$

(2) $\quad P = P^e + (1/\alpha)(Y - \bar{Y})$

(3) $\quad P = P^e + (1/\alpha)(Y - \bar{Y}) + v$

(4) $\quad (P - P_{-1}) = (P^e - P_{-1}) + (1/\alpha)(Y - \bar{Y}) + v$

(5) $\quad \pi = \pi^e + (1/\alpha)(Y - \bar{Y}) + v$

(6) $\quad (1/\alpha)(Y - \bar{Y}) = -\beta(u - u^n)$

(7) $\quad \pi = \pi^e - \beta(u - u^n) + v$

The Phillips Curve and *SRAS*

$$\text{SRAS:} \quad Y = \bar{Y} + \alpha(P - P^e)$$

$$\text{Phillips curve:} \quad \pi = \pi^e - \beta(u - u^n) + v$$

- *SRAS* curve:
  output is related to unexpected movements in the price level

- Phillips curve:
  unemployment is related to unexpected movements in the inflation rate

Adaptive expectations

- **Adaptive expectations**: economic agents form their expectations of future inflation based on recently observed inflation.

- A simple example:
  expected inflation = last year's actual inflation $\pi^e = \pi_{-1}$

- Then, the P.C. becomes

$$\pi = \pi_{-1} - \beta(u - u^n) + \nu$$

Inflation inertia

$$\pi \;=\; \pi_{-1} - \beta(u - u^n) + \nu$$

- In this form, the Phillips curve implies that inflation has inertia (惯性):

  - In the absence of supply shocks or cyclical unemployment, inflation will continue indefinitely at its current rate.

  - Past inflation influences expectations of current inflation, which in turn influences the wages & prices that people set.

Two causes of rising & falling inflation

$$\pi = \pi_{-1} - \beta(u - u^n) + \nu$$

- **cost-push inflation**: inflation resulting from supply shocks.

  Adverse supply shocks typically raise production costs and induce firms to raise prices, "pushing" inflation up.

- **demand-pull inflation**: inflation resulting from demand shocks.

  Positive shocks to aggregate demand cause unemployment to fall below its natural rate, which "pulls" the inflation rate up.

Graphing the Phillips curve

$$\pi = \pi^e - \beta(u - u^n) + v$$

π

β / 1

In the short run, policymakers face a trade-off between π and u.

$\pi^e + v$

The short-run Phillips Curve

u^n

u
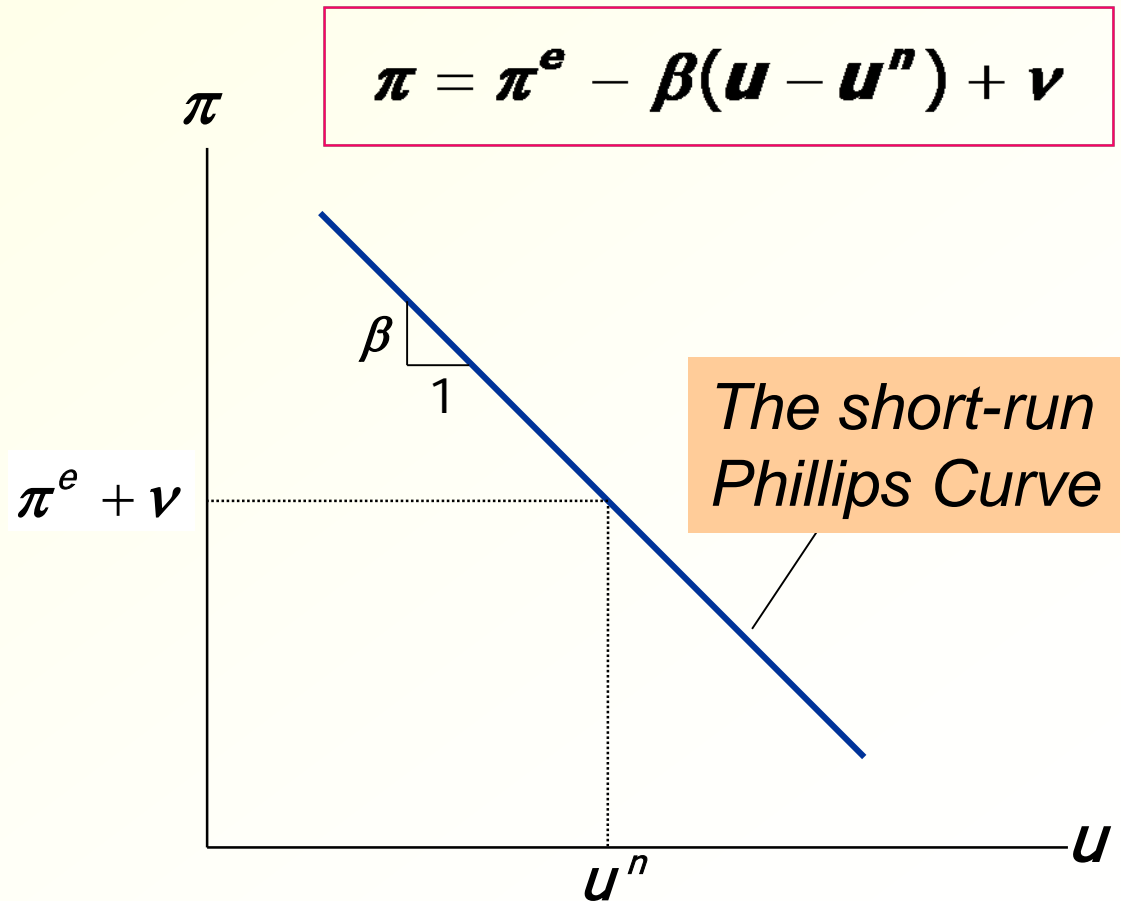
Shifting the Phillips curve

People adjust their expectations over time, so the tradeoff only holds in the short run.

E.g., an increase in π^e shifts the short-run P.C. upward.

$$\pi = \pi^e - \beta(u - u^n) + v$$

$\pi_2^e + v$

$\pi_1^e + v$

π

u^n

u
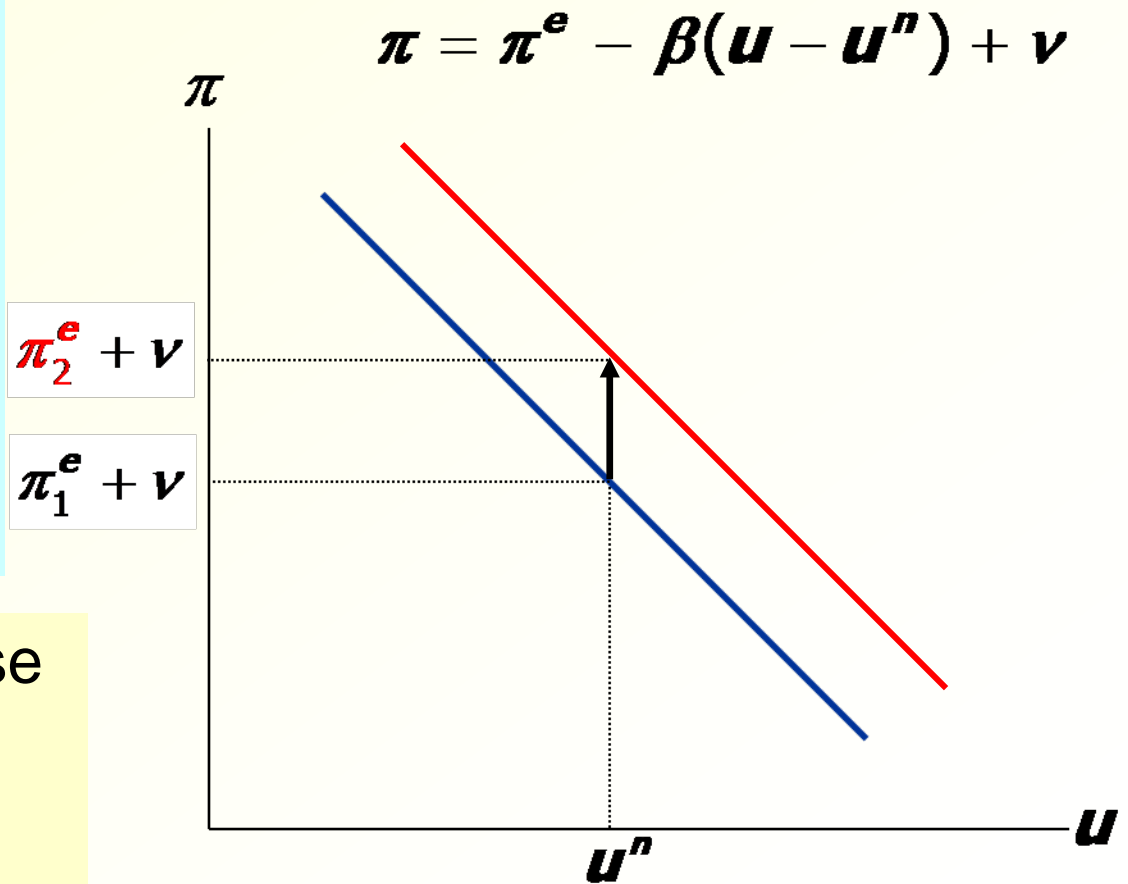
The sacrifice ratio (牺牲率)

- To reduce inflation, policymakers can contract aggregate demand, causing unemployment to rise above the natural rate.

- The **sacrifice ratio** measures the percentage of a year's real GDP that must be foregone to reduce inflation by 1 percentage point.

- Estimates vary, but typically it lies between 3 and 5.

The sacrifice ratio

- Suppose policymakers wish to reduce inflation from 6 to 2 per cent.

  If the sacrifice ratio is 3, then reducing inflation by 4 points requires a loss of $4 \times 3 = 12$ per cent of one year's GDP.

- This could be achieved several ways, e.g.
  - reduce GDP by 12% for one year
  - reduce GDP by 6% for each of two years
  - reduce GDP by 3% for each of four years

- The cost of disinflation is lost GDP. One could use Okun's law to translate this cost into unemployment.

Rational expectations

Ways of modelling the formation of expectations:

- **adaptive expectations**:
  People base their expectations of future inflation on recently observed inflation.

- **rational expectations**:
  People base their expectations on all available information, including information about current and prospective future policies.

Painless disinflation (反通货膨胀)?

- Proponents of rational expectations believe
  that the sacrifice ratio may be very small:

- Suppose $u = u^n$ and $\pi = \pi^e = 6\%$,
  and suppose the central bank announces
  that it will do whatever is necessary to
  reduce inflation from 6 to 2 per cent as
  soon as possible.

- If the announcement is credible,
  then π^e will fall, perhaps by the full 4
  points.

- Then, π can fall without an increase in u.

The sacrifice ratio for the Volcker disinflation in the U.S.

- 1981: π = 9.7%

  1985: π = 3.0%

  Total disinflation = 6.7%

year	u	u^n	$u-u^n$
1982	9.5%	6.0%	3.5%
1983	9.5	6.0	3.5
1984	7.4	6.0	1.4
1985	7.1	6.0	1.1

Total 9.5%

The sacrifice ratio for the Volcker disinflation in the U.S.

- Previous slide:
  - inflation fell by 6.7%
  - total of 9.5% of cyclical unemployment
- Okun's law:
  each 1 percentage point of unemployment implies lost output of 2 percentage points. So, the 9.5% cyclical unemployment translates to 19.0% of a year's real GDP.
- Sacrifice ratio = (lost GDP)/(total disinflation)
  = 19/6.7 = 2.8 percentage points of GDP were lost for each 1 percentage point reduction in inflation.

The natural rate hypothesis
（自然率假说）

Our analysis of the costs of disinflation, and of economic fluctuations in the preceding chapters, is based on the **natural rate hypothesis**:

Changes in aggregate demand
affect output and employment in the short run.

In the long run, the economy returns to
the levels of output, employment,
and unemployment described by
the classical model (chapters 3-9).

An alternative hypothesis: hysteresis (滞后性)

- **Hysteresis**: the long-lasting influence of history on variables such as the natural rate of unemployment.

- Negative shocks may increase u^n, so economy may not fully recover:

  – The skills of cyclically unemployed workers deteriorate while unemployed, and they cannot find a job when the recession ends.

  – Cyclically unemployed workers may lose their influence on wage-setting; insiders (employed workers) may then bargain for higher wages for themselves. Then, the cyclically unemployed "outsiders" may become structurally unemployed when the recession ends.

Chapter summary

1. Two models of aggregate supply in the short run:

   - sticky-price model
   - imperfect-information model

   Both models imply that output rises above its natural rate when the price level falls below the expected price level.

Chapter summary

2. Phillips curve

- derived from the SRAS curve

- states that inflation depends on

    – expected inflation

    – cyclical unemployment

    – supply shocks

- presents policymakers with a short-run tradeoff between inflation and unemployment

Chapter summary

3. How people form expectations of inflation

- adaptive expectations
    - based on recently observed inflation
    - implies "inertia"
- rational expectations
    - based on all available information
    - implies that disinflation may be painless

Chapter summary

4. The natural rate hypothesis and hysteresis

- the natural rate hypotheses

  - states that changes in aggregate demand can only affect output and employment in the short run

- hysteresis

  - states that aggregate demand can have permanent effects on output and employment