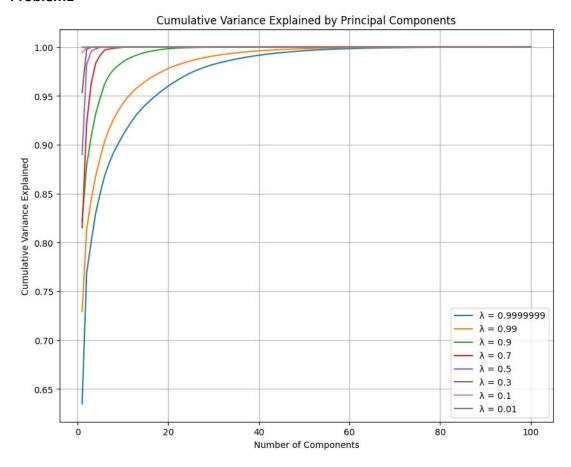
### Problem1



### Problem2

Matrix size: 100x100

Is original matrix PSD? False
Is near\_psd() matrix PSD? True

Is Higham's method matrix PSD? True

Frobenius norm difference (near\_psd): 43.220803907840704 Frobenius norm difference (Higham): 56.507550083496135

Runtime (near psd): 0.0222 seconds

Runtime (Higham's method): 1.0724 seconds

Matrix size: 200x200

Is original matrix PSD? False
Is near\_psd() matrix PSD? True

Is Higham's method matrix PSD? False

Frobenius norm difference (near\_psd): 90.93783139832286 Frobenius norm difference (Higham): 121.16279655813064

Runtime (near\_psd): 0.0242 seconds

Runtime (Higham's method): 2.6277 seconds

Matrix size: 300x300

Is original matrix PSD? False

Is near\_psd() matrix PSD? True

Is Higham's method matrix PSD? False

Frobenius norm difference (near\_psd): 139.29967282579483 Frobenius norm difference (Higham): 187.11574461366075

Runtime (near\_psd): 0.0237 seconds

Runtime (Higham's method): 2.3743 seconds

Matrix size: 400x400

Is original matrix PSD? False
Is near psd() matrix PSD? True

Is Higham's method matrix PSD? False

Frobenius norm difference (near\_psd): 187.27495997073552 Frobenius norm difference (Higham): 253.09728277035427

Runtime (near\_psd): 0.0429 seconds

Runtime (Higham's method): 4.5026 seconds

Matrix size: 500x500

Is original matrix PSD? False
Is near\_psd() matrix PSD? True

Is Higham's method matrix PSD? False

Frobenius norm difference (near\_psd): 236.08161762273485 Frobenius norm difference (Higham): 320.45679323732674

Runtime (near\_psd): 0.0821 seconds

Runtime (Higham's method): 10.3035 seconds

## Problem3

Simulating from covariance matrix: pearson\_var Direct simulation completed in 0.28 seconds.

PCA simulation (100% variance) completed in 0.28 seconds.

PCA simulation (75% variance) completed in 0.06 seconds.

PCA simulation (50% variance) completed in 0.03 seconds.

Simulating from covariance matrix: pearson\_ew\_var

Direct simulation completed in 0.26 seconds.

PCA simulation (100% variance) completed in 0.26 seconds.

PCA simulation (75% variance) completed in 0.05 seconds.

PCA simulation (50% variance) completed in 0.03 seconds.

Simulating from covariance matrix: ew\_corr\_var

Direct simulation completed in 0.23 seconds.

PCA simulation (100% variance) completed in 0.28 seconds.

PCA simulation (75% variance) completed in 0.05 seconds.

PCA simulation (50% variance) completed in 0.02 seconds.

Simulating from covariance matrix: ew\_corr\_ew\_var
Direct simulation completed in 0.26 seconds.

PCA simulation (100% variance) completed in 0.29 seconds.

PCA simulation (75% variance) completed in 0.05 seconds.

PCA simulation (50% variance) completed in 0.02 seconds.

### Timings (in seconds):

Covariance Matrix: pearson\_var

direct: 0.28 seconds pca\_100: 0.28 seconds pca\_75: 0.06 seconds pca\_50: 0.03 seconds

Covariance Matrix: pearson\_ew\_var

direct: 0.26 seconds pca\_100: 0.26 seconds pca\_75: 0.05 seconds pca\_50: 0.03 seconds

Covariance Matrix: ew\_corr\_var

direct: 0.23 seconds pca\_100: 0.28 seconds pca\_75: 0.05 seconds pca\_50: 0.02 seconds

Covariance Matrix: ew\_corr\_ew\_var

direct: 0.26 seconds pca\_100: 0.29 seconds pca\_75: 0.05 seconds pca\_50: 0.02 seconds

# Frobenius Norms:

Covariance Matrix: pearson\_var

direct: 0.0002 pca\_100: 0.0002 pca\_75: 0.0011 pca\_50: 0.0021

Covariance Matrix: pearson\_ew\_var

direct: 0.0002 pca\_100: 0.0003 pca\_75: 0.0013 pca\_50: 0.0028

Covariance Matrix: ew\_corr\_var

direct: 0.0002 pca\_100: 0.0002 pca\_75: 0.0013 pca\_50: 0.0026

Covariance Matrix: ew\_corr\_ew\_var

direct: 0.0002 pca\_100: 0.0002 pca\_75: 0.0016 pca\_50: 0.0035