

hw3

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1 MSAI349: Homework 3

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Our written responses for discussing our design choices are at the bottom of this notebook. This notebook also includes several plots where the title indicates the dataset name, loss function used, the hidden layer size (k), and the regularizer used (if any).

```
[2]: # Import Block
import torch.nn as nn
import torch
from torch import Tensor
from torch.optim import Optimizer
from tqdm import tqdm

from typing import Callable, Tuple
import matplotlib.pyplot as plt
import matplotlib
import pandas as pd
import numpy as np
```

2 Plotting Code

Plotting code provided in starter code

```
[3]: # %matplotlib inline

#####
# Some simple plotting utilities
#####

def plot_data(data: np.ndarray,
              labels: np.ndarray,
              ax: matplotlib.axes.Axes = None):
    """
    A helper function to plot our data sets
```

PARAMETERS

data A numpy array of 2 columns (dimensions) and 2*examples_per_class_
→rows

labels A numpy vector with 2*examples_per_class, with a +1 or -1 in each
 element. The jth element is the label of the jth example

ax An optional matplotlib axis object to plot to
"""

require shape (n, 2)

assert data.ndim == 2

assert data.shape[-1] == 2

if type(data) == torch.Tensor:
 data = data.numpy()

plot the data

pos_idx = np.where(labels == 1)

neg_idx = np.where(labels == -1)

if ax **is** None:

 ax = plt

ax.plot(
 data.T[0, pos_idx],
 data.T[1, pos_idx],
 'r^',
 label='positive'
)

ax.plot(
 data.T[0, neg_idx],
 data.T[1, neg_idx],
 'bo',
 label='negative'
)

ax.axis('equal')

handles, labels = plt.gca().get_legend_handles_labels()

by_label = dict(zip(labels, handles))

plt.legend(by_label.values(), by_label.keys(), loc="upper right")

if ax **is** None:

 plt.show()

def plot_decision_surface(model=None,
 axis_limits=(-5, 5, -5, 5),

```

        ax: matplotlib.axes.Axes = None
    ):

    """
    Creates a grid of points, measures what a model would label each
    point as, and uses this data to draw a region for class +1 and a region for
    class -1.

    PARAMETERS
    -----
    model          A callable model that can take 2-d real-valued input and produce
                   a +1 or -1 label for each data point.

    axis_limits    An array-like object with 4 floats [lowest_horizontal,
    ↪highest_horizontal,
    ↪lowest_vertical, highest_vertical]. This sets the limits over
    ↪which
                   the decision surface will be calculated and plotted.

    ax             An optional matplotlib axis object to plot to

    RETURNS
    -----
    my_contour     a matplotlib.contour.QuadContourSet with the contour
    """

    # Create a grid of points spanning the entire space displayed in the axis.
    # This will let us draw the decision boundary later
    xx, yy = np.meshgrid(np.arange(axis_limits[0], axis_limits[1], .05),
                        np.arange(axis_limits[2], axis_limits[3], .05))
    data = np.concatenate([xx.reshape([1, -1]), yy.reshape([1, -1])]).T

    # Predict the class of each point in XGrid, using the classifier.
    # This shows our regions determined by the classifier
    if isinstance(model, nn.Module):
        with torch.no_grad():
            pl = model(torch.tensor(data).to(dtype=torch.float32))
            predicted_labels = np.sign(pl.numpy())
    else:
        predicted_labels = model(data)

    predicted_labels = predicted_labels.reshape(xx.shape)

    # Put the result into a color plot
    if ax is None:
        ax = plt

    ax.contourf(xx, yy, predicted_labels, cmap=plt.cm.Paired)

```

```

ax.axis('equal')
ax.axis('tight')

if ax is None:
    plt.show()

def compute_bounds(features):
    min1, max1 = features[:, 0].min()-1, features[:, 0].max()+1
    min2, max2 = features[:, 1].min()-1, features[:, 1].max()+1
    return (min1, max1, min2, max2)

def plot_decision_regions(
    features, targets, model,
    axis=None, transform=None,
    bounds=None,
    title='Decision Surface'):
    """
    Slightly different plotting approach than above. Used in backprop demo.

    This function produces a single plot containing a scatter plot of the
    features, targets, and decision region of the model.

    Args:
        features (np.ndarray): 2D array containing real-valued inputs.
        targets (np.ndarray): 1D array containing binary targets.
        model: a learner with .predict() method
        axis: the axis on which to plot. If None, create a new plot
        title: title of the plot
    Returns:
        None (plots to the active figure)
    """

    # define bounds of the domain
    if bounds is None:
        min1, max1, min2, max2 = compute_bounds(features)
    else:
        min1, max1, min2, max2 = bounds

    # define grid for visualizing decision regions
    x1grid = np.arange(min1, max1, 0.1)
    x2grid = np.arange(min2, max2, 0.1)

    xx, yy = np.meshgrid(x1grid, x2grid)

    # flatten grid to a vector

```

```

r1, r2 = xx.flatten(), yy.flatten()
r1, r2 = r1.reshape((len(r1), 1)), r2.reshape((len(r2), 1))

# horizontally stack vectors to create x1,x2 input for the model
grid = np.hstack((r1, r2))

# if we're transforming the features, do that now
# this allows xx and yy to still be in 2D for the visualization
# but grid has been transformed so it matches up with the fit model
if transform is not None:
    grid = transform(grid)

# generate predictions over grid
# Cast grid to a tensor if model is a PyTorch model
if isinstance(model, nn.Module):
    grid = torch.tensor(grid).to(dtype=torch.float32)
yhat = model.predict(grid)

# reshape the predictions back into a grid
zz = yhat.reshape(xx.shape)

if axis is None:
    fig, axis = plt.subplots()

# plot the grid of x, y and z values as a surface
binary_cmap = matplotlib.colors.ListedColormap(['#9ce8ff', '#ffc773'])
axis.contourf(xx, yy, zz, cmap=binary_cmap, alpha=0.7)

# plot "negative" class:
row_idx_neg = np.where(targets < 0.5)[0]
axis.scatter(
    features[row_idx_neg, 0], features[row_idx_neg, 1],
    label='negative')

# plot "positive" class:
row_idx_pos = np.where(targets > 0.5)[0]
axis.scatter(
    features[row_idx_pos, 0], features[row_idx_pos, 1],
    label='positive')

axis.set_title(title)
axis.set_xlim(min1, max1)
axis.set_ylim(min2, max2)

axis.legend(loc="upper left")

```

3 Part 1 & 2

PyTorch Implementaion with MCE and MSE.

```
[4]: class NeuralNet(nn.Module):
    def __init__(self, input_size: int, hl_size: int, output_size: int,
        ↪regularizer: str = None):
        """Initialize the network with the size of each layer

        Args:
            input_size (int): Number of features in the dataset
            hl_size (int): hidden layer size
            output_size (int): output size (1 for MSE loss, 2 for MCE loss)
            regularizer (str, optional): Regularization term [norm, orthogonal].
        ↪ Defaults to None.
        """
        super(NeuralNet, self).__init__()
        self.input_size = input_size
        self.hl_size = hl_size
        self.output_size = output_size
        self.linear1 = nn.Linear(input_size, hl_size)
        self.sigmoid1 = nn.Sigmoid()
        self.linear2 = nn.Linear(hl_size, output_size)
        if output_size == 2:
            self.output = nn.Softmax()
        elif output_size == 1:
            self.output = nn.Sigmoid()
        self.regularizer = regularizer
        self.regularizer_lambda = 0.01
        self.device = torch.device(
            "cuda" if torch.cuda.is_available() else "cpu")
        print(f"Using {self.device} for training")

    def forward(self, x: Tensor) -> Tensor:
        """Forward pass for the neural network

        Args:
            x (Tensor): Input data in the form of a tensor

        Returns:
            Tensor: data after the network has processed it (output tensor)
        """
        x = self.linear1(x)
        x = self.sigmoid1(x)
        x = self.linear2(x)
        x = self.output(x)
        return x
```

```

def train_model(self, model: nn.Module, num_epochs: int, X_train: Tensor,
    ↪ y_train: Tensor, X_valid: Tensor, y_valid: Tensor, loss_func: Callable,
    ↪ optimizer: Optimizer) -> list:
    """Use Stochastic Gradient Descent to train one example at a time

    Args:
        model (nn.Module): Model created by the forward pass
        num_epochs (int): Number of times to train the entire dataset
        X_train (Tensor): Training data without labels
        y_train (Tensor): Labels for the training data
        X_valid (Tensor): Validation data without labels
        y_valid (Tensor): Labels for the validation data
        loss_func (Callable): callable function to perform the loss
    ↪ calculation on the output
        optimizer (Optimizer): Built in optimizer to perform momentum based
    ↪ learning
    """

    training_learning_curve = []
    validation_learning_curve = []
    for epoch in range(num_epochs):
        model.train()
        training_loss = 0
        for i in range(len(X_train)):

            x = X_train[i]
            y = y_train[i]

            y_pred = model(x)
            loss = loss_func(y_pred, y)

            if self.regularizer == "norm":
                input_layer_weights = model.linear1.weight
                regularizer_value = torch.sum(input_layer_weights ** 2)
                loss += self.regularizer_lambda * regularizer_value
            elif self.regularizer == "orthogonal":
                # encourage orthogonality in the intermediate decision
                # boundaries learned in the first layer
                input_layer_weights = model.linear1.weight
                dot_products = torch.mm(
                    input_layer_weights, input_layer_weights.t()
                )
                identity = torch.eye(dot_products.shape[0])
                orthogonality_loss = torch.sum(
                    (dot_products - identity) ** 2)
                loss += self.regularizer_lambda * orthogonality_loss

```

```

        optimizer.zero_grad()
        loss.backward()
        optimizer.step()

        # Accumulate loss for the epoch
        training_loss += loss.item()
        # Learning curve should be average loss per epoch
        training_learning_curve.append(training_loss / len(X_train))
        # Validation Phase
        model.eval()
        with torch.no_grad():
            validation_loss = 0
            for i in range(len(X_valid)):
                x_valid = X_valid[i]
                y_val = y_valid[i]

                y_valid_pred = model(x_valid)
                loss = loss_func(y_valid_pred, y_val)
                validation_loss += loss.item()
            # Learning curve should be average loss per epoch
            validation_learning_curve.append(
                validation_loss / len(X_valid))

    return training_learning_curve, validation_learning_curve

def predict(self, X: Tensor) -> Tensor:
    """Predict the output of the network

    Args:
        X (Tensor): Input data without labels

    Returns:
        Tensor: Predicted output of the network
    """
    model = self
    model.eval()
    with torch.no_grad():
        return model(X)

def validate_test(self, model: nn.Module, X_test: Tensor, y_test: Tensor,
    ↪ loss_func_label: str) -> float:
    """Test the validation and test set accuracies by dividing the correct
    ↪ predictions by the total predictions

    Args:
        model (nn.Module): Model created by the forward pass
        X_test (Tensor): Testing/Validation data without labels

```


y_test (Tensor): Labels for the testing/validation data
loss_func_label (str): Specifies either MSE or MCE loss

Returns:

float: accuracy evaluation metric to see how well the network is
→performing

```
"""
model.eval() # Set the model to 'evaluation' mode
# Disable gradient calculation for testing
with torch.no_grad():
    correct = 0
    total = 0
    for i in range(len(X_test)):
        x = X_test[i]
        y = y_test[i]

        if loss_func_label == "MCE":
            # Second probability in output: (Second probability so we
            →can keep the logic the same for clipping)
            pred = model(x)[1]
        elif loss_func_label == "MSE":
            pred = model(x)

        # Clipping: If the second element has higher than a 50%
        →probability, then it is of class 1, otherwise class 0
        pred = 1 if pred >= 0.5 else 0

        if pred == y:
            correct += 1

    total += 1

accuracy = correct / total

return accuracy
```

class HyperParams:

```
    def __init__(self, hidden_layer_size: int, learning_rate: float, loss_func:
    →str):
        self._hl_size = hidden_layer_size
        self._lr = learning_rate
        self._output_size = 2 if loss_func == "MCE" else 1

    def __hash__(self):
        return hash((self._hl_size, self._lr, self._output_size))
```

```

    def __repr__(self):
        return f"[HLSize: {self.hl_size}, LR: {self.lr}, Loss: {'MCE' if self.
↪output_size == 2 else 'MSE'}]"

    @property
    def hl_size(self):
        return self._hl_size

    @property
    def lr(self):
        return self._lr

    @property
    def output_size(self):
        return self._output_size

class NeuralNetEvaluator:
    def __init__(
        self,
        training_data: dict[str: str],
        test_data: dict[str: str],
        validation_data: dict[str: str],
        loss_functions: dict[str: Callable]):
        self.training_data = training_data
        self.test_data = test_data
        self.validation_data = validation_data
        self.loss_functions = loss_functions
        self.used_regularizer = ""

        # Store the evaluated models as a dictionary that maps
        # a tuple of the dataset name and the hyperparams to a
        # dictionary of accuracy_names to accuracy values
        # Example Entry: ("dataset_name", HyperParams): {"valid_accuracy": 0.5,
↪"test_accuracy": 0.6}
        self.evaluated_models: dict[
            Tuple[str, HyperParams]: dict[str: float]
        ] = {}
        # Store the best models as a map of
        # dataset_name_loss to the model itself
        self.all_models: dict[str: dict[HyperParams: NeuralNet]] = {}
        self.best_models: dict[str: NeuralNet] = {}

    def train_model(
        self,
        dataset_name: str,
        loss_func_name: str,

```

```

        regularizer: str,
        hyperparams: HyperParams):
    # Assign hyperparams to default if not provided
    # Convert data to tensors
    X_train = pd.read_csv(self.training_data[dataset_name])
    X_test = pd.read_csv(self.test_data[dataset_name])
    X_validation = pd.read_csv(self.validation_data[dataset_name])
    # Seperate labels
    y_train = X_train["label"].values
    y_test = X_test["label"].values
    y_validation = X_validation["label"].values
    # Drop labels
    X_train = X_train.drop("label", axis=1).values
    X_test = X_test.drop("label", axis=1).values
    X_validation = X_validation.drop("label", axis=1).values
    # Convert to tensors for numpy to use
    X_train = torch.tensor(X_train, dtype=torch.float32)
    X_test = torch.tensor(X_test, dtype=torch.float32)
    X_validation = torch.tensor(X_validation, dtype=torch.float32)
    # For MCE, we need to convert the labels to long
    if loss_func_name == "MCE":
        y_train = torch.tensor(y_train, dtype=torch.long)
        y_test = torch.tensor(y_test, dtype=torch.long)
        y_validation = torch.tensor(y_validation, dtype=torch.long)
    elif loss_func_name == "MSE":
        y_train = torch.tensor(y_train, dtype=torch.float32)
        y_test = torch.tensor(y_test, dtype=torch.float32)
        y_validation = torch.tensor(y_validation, dtype=torch.float32)
    # Build network with loss function and optimizer
    if regularizer is not None or regularizer != "":
        self.used_regularizer = regularizer
    neural_network = NeuralNet(
        X_train.shape[1],
        hl_size=hyperparams.hl_size,
        output_size=2 if loss_func_name == "MCE" else 1,
        regularizer=regularizer if regularizer != "" else None
    )
    loss_func = self.loss_functions[loss_func_name]
    optimizer = torch.optim.Adam(
        neural_network.parameters(),
        lr=hyperparams.lr
    )
    # Train the model
    training_losses, validation_losses = neural_network.train_model(
        neural_network,
        num_epochs=500,
        X_train=X_train,

```

```

        y_train=y_train,
        X_valid=X_validation,
        y_valid=y_validation,
        loss_func=loss_func,
        optimizer=optimizer
    )
    # Evaluate the model
    valid_accuracy = neural_network.validate_test(
        neural_network,
        X_validation,
        y_validation,
        loss_func_name
    )
    test_accuracy = neural_network.validate_test(
        neural_network,
        X_test,
        y_test,
        loss_func_name
    )
    # Save the accuracy to the evaluated models
    key = (dataset_name, hyperparams)
    self.evaluated_models[key] = {
        "valid_accuracy": valid_accuracy,
        "test_accuracy": test_accuracy,
        "training_losses": training_losses,
        "validation_losses": validation_losses
    }
    dataset_loss = f"{dataset_name}_{loss_func_name}"
    if dataset_loss not in self.all_models:
        self.all_models[dataset_loss] = {}
    self.all_models[dataset_loss][hyperparams] = neural_network
    print(
        f"Finished training {dataset_name} with Hyperparams: {hyperparams}"
    )
    ↪ +
    f" with loss function: {
        loss_func_name} and regularizer: {"None" if regularizer == ""
    ↪ else regularizer}"
    )

def print_evaluated_models(self):
    unique_datasets = set([key[0] for key in self.evaluated_models.keys()])
    print(
        f'Evaluated {len(self.evaluated_models)} models over ' +
        f'{len(unique_datasets)} datasets'
    )
    for key in self.evaluated_models.keys():
        dataset_name, hyper_params = key

```

```

        valid_accuracy = self.evaluated_models[key]["valid_accuracy"]
        test_accuracy = self.evaluated_models[key]["test_accuracy"]
        print("=====")
        print(f"{dataset_name} with Hyperparams: {hyper_params}")
        print(f"Validation Accuracy: {valid_accuracy}")
        print(f"Test Accuracy: {test_accuracy}")
        print("=====\\n")

    def find_best_hyperparams_for_dataset(self, dataset_name: str,
    ↪loss_func_name: str):
        # This assumes that the models are already trained and stored
        best_test_accuracy = 0
        best_valid_accuracy = 0
        best_hyperparams = None
        # dataset_models should be all the models where the dataset_name is the
    ↪key
        loss_output_size = 2 if loss_func_name == "MCE" else 1
        dataset_models = [
            key for key in self.evaluated_models.keys() if key[0] ==
    ↪dataset_name and key[1].output_size == loss_output_size
        ]
        for key in dataset_models:
            dataset, hp = key
            valid_accuracy = self.evaluated_models[key]["valid_accuracy"]
            test_accuracy = self.evaluated_models[key]["test_accuracy"]
            if valid_accuracy > best_valid_accuracy:
                best_test_accuracy = test_accuracy
                best_valid_accuracy = valid_accuracy
                best_hyperparams = hp
            dataset_loss = f"{dataset_name}_{loss_func_name}"
            model_dict = self.all_models[dataset_loss]
            # Find the entry that matches the best hyperparams
            best_model = model_dict[best_hyperparams]
            self.best_models[dataset_loss] = best_model
            return best_hyperparams, best_valid_accuracy, best_test_accuracy

    def plot_learning_curves(self, dataset_name: str, best_hp: HyperParams):
        # Plot the learning curve for training and validation loss as
        # a function of training epochs
        # find the epoch_losses for the best hyperparams
        key = (dataset_name, best_hp)
        loss = "MCE" if best_hp.output_size == 2 else "MSE"
        training_losses = self.evaluated_models[key]["training_losses"]
        validation_losses = self.evaluated_models[key]["validation_losses"]
        plt.figure()
        if self.used_regularizer is not None or self.used_regularizer != "":
            reg_tag = f"_{self.used_regularizer}"

```

```

plt.plot(
    range(len(training_losses)), training_losses,
    label=f"{dataset_name}_{loss}_{
        best_hp.hl_size}{reg_tag}_training_loss"
)
plt.plot(
    range(len(validation_losses)), validation_losses,
    label=f"{dataset_name}_{loss}_{
        best_hp.hl_size}{reg_tag}_validation_loss"
)
plt.xlabel("Epochs")
plt.ylabel("Loss")
plt.title(
    f"{dataset_name} (k={best_hp.hl_size}, " +
    f"reg={'None' if self.used_regularizer == '' else self.
used_regularizer})" +
    f", loss={loss}) Learning Curve"
)
plt.legend(["Training Loss", "Validation Loss"])
plt.savefig(
    f"plots/{dataset_name}_{best_hp.hl_size}_{
        loss}{reg_tag}_learning_curve.png"
)

def plot_learned_decision_surfaces(self, dataset_name: str, loss_func_name:
str, regularizer: str):
    # Plot the learned decision surface along with observations from the
test set
    if loss_func_name == "MCE":
        print(f"Cannot plot decision surface for MCE loss function")
        return
    dataset_loss = f"{dataset_name}_{loss_func_name}"
    # plot_decision_surface(model=self.best_models[dataset_loss])
    X_test = pd.read_csv(self.test_data[dataset_name])
    y_test = X_test["label"].values
    print(f'Drawing Decision Region for {dataset_loss}_{regularizer}')
    fig, ax = plt.subplots()
    k = self.best_models[dataset_loss].hl_size
    plot_decision_regions(
        features=X_test.drop("label", axis=1).values,
        targets=y_test,
        model=self.best_models[dataset_loss],
        axis=ax,
        title=f"{dataset_loss}_{regularizer} (k={k}) Decision Regions"
    )
    plt.savefig(

```

```

        f"plots/
↪{dataset_name}_{regularizer}_{loss_func_name}_decision_regions.png"
    )

def evaluate_models_on_all_datasets():
    print(f"WARNING: This script will take a long time to run ...")
    evaluator = NeuralNetEvaluator(
        training_data={"xor": "xor_train.csv",
                       "center_surround": "center_surround_train.csv",
                       "spiral": "spiral_train.csv",
                       "two_gaussians": "two_gaussians_train.csv"},
        test_data={"xor": "xor_test.csv",
                   "center_surround": "center_surround_test.csv",
                   "spiral": "spiral_test.csv",
                   "two_gaussians": "two_gaussians_test.csv"},
        validation_data={"xor": "xor_valid.csv",
                         "center_surround": "center_surround_valid.csv",
                         "spiral": "spiral_valid.csv",
                         "two_gaussians": "two_gaussians_valid.csv"},
        loss_functions={"MCE": nn.CrossEntropyLoss(), "MSE": nn.MSELoss()}
    )
    datasets = ["xor", "center_surround", "spiral", "two_gaussians"]
    hidden_layer_sizes = [2, 3, 5, 7, 9]
    losses = ["MCE", "MSE"]
    # After running and manually inspecting the results,
    # these are the best HPs for each dataset and loss function
    # These should also be used when using regularizers
    best_hps_map = {
        "xor_MCE": HyperParams(7, 0.01, "MCE"),
        "xor_MSE": HyperParams(9, 0.01, "MSE"),
        "center_surround_MCE": HyperParams(3, 0.01, "MCE"),
        "center_surround_MSE": HyperParams(3, 0.01, "MSE"),
        "spiral_MCE": HyperParams(9, 0.01, "MCE"),
        "spiral_MSE": HyperParams(9, 0.01, "MSE"),
        "two_gaussians_MCE": HyperParams(2, 0.01, "MCE"),
        "two_gaussians_MSE": HyperParams(3, 0.01, "MSE")
    }
    for dataset in tqdm(datasets, desc="Datasets"):
        for loss in losses:
            dataset_loss = f"{dataset}_{loss}"
            hp = best_hps_map[dataset_loss]
            evaluator.train_model(dataset, loss, "", hp)
    # Uncomment this block to train models with different hyperparams

```

```

# for dataset in tqdm(datasets, desc="Datasets"):
#     for hl_size in hidden_layer_sizes:
#         for loss in losses:
#             hp = HyperParams(hl_size, 0.01, loss)
#             evaluator.train_model(dataset, loss, hp)
evaluator.print_evaluated_models()
for dataset in datasets:
    for loss_name in losses:
        best_hp, valid_acc, test_acc = evaluator.
↪find_best_hyperparams_for_dataset(
        dataset, loss_name
    )
    print("=====")
    print(f"Best Hyperparams for {dataset}: {best_hp}")
    print(f"Validation Accuracy: {valid_acc}")
    print(f"Test Accuracy: {test_acc}")
    print("=====\\n")
    evaluator.plot_learning_curves(dataset, best_hp)

```

```

[5]: # Run the evaluation
evaluate_models_on_all_datasets()

```

WARNING: This script will take a long time to run ...

Datasets: 0%| | 0/4 [00:00<?, ?it/s]

Using cuda for training

/home/sharwin/fall_2024/MSAI349_Machine_Learning/nn-venv/lib/python3.12/site-packages/torch/nn/modules/module.py:1736: UserWarning: Implicit dimension choice for softmax has been deprecated. Change the call to include dim=X as an argument.

```
return self._call_impl(*args, **kwargs)
```

Finished training xor with Hyperparams: [HLSize: 7, LR: 0.01, Loss: MCE] with loss function: MCE and regularizer: None

Using cuda for training

/home/sharwin/fall_2024/MSAI349_Machine_Learning/nn-venv/lib/python3.12/site-packages/torch/nn/modules/loss.py:608: UserWarning: Using a target size (torch.Size([])) that is different to the input size (torch.Size([1])). This will likely lead to incorrect results due to broadcasting. Please ensure they have the same size.

```
return F.mse_loss(input, target, reduction=self.reduction)
```

Datasets: 25%| | 1/4 [00:43<02:09, 43.16s/it]

Finished training xor with Hyperparams: [HLSize: 9, LR: 0.01, Loss: MSE] with loss function: MSE and regularizer: None

Using cuda for training

/home/sharwin/fall_2024/MSAI349_Machine_Learning/nn-venv/lib/python3.12/site-

packages/torch/nn/modules/module.py:1736: UserWarning: Implicit dimension choice for softmax has been deprecated. Change the call to include dim=X as an argument.

```
return self._call_impl(*args, **kwargs)
```

Finished training center_surround with Hyperparams: [HLSize: 3, LR: 0.01, Loss: MCE] with loss function: MCE and regularizer: None

Using cuda for training

/home/sharwin/fall_2024/MSAI349_Machine_Learning/nn-venv/lib/python3.12/site-packages/torch/nn/modules/loss.py:608: UserWarning: Using a target size (torch.Size([])) that is different to the input size (torch.Size([1])). This will likely lead to incorrect results due to broadcasting. Please ensure they have the same size.

```
return F.mse_loss(input, target, reduction=self.reduction)
```

Datasets: 50%| | 2/4 [01:22<01:22, 41.14s/it]

Finished training center_surround with Hyperparams: [HLSize: 3, LR: 0.01, Loss: MSE] with loss function: MSE and regularizer: None

Using cuda for training

/home/sharwin/fall_2024/MSAI349_Machine_Learning/nn-venv/lib/python3.12/site-packages/torch/nn/modules/module.py:1736: UserWarning: Implicit dimension choice for softmax has been deprecated. Change the call to include dim=X as an argument.

```
return self._call_impl(*args, **kwargs)
```

Finished training spiral with Hyperparams: [HLSize: 9, LR: 0.01, Loss: MCE] with loss function: MCE and regularizer: None

Using cuda for training

/home/sharwin/fall_2024/MSAI349_Machine_Learning/nn-venv/lib/python3.12/site-packages/torch/nn/modules/loss.py:608: UserWarning: Using a target size (torch.Size([])) that is different to the input size (torch.Size([1])). This will likely lead to incorrect results due to broadcasting. Please ensure they have the same size.

```
return F.mse_loss(input, target, reduction=self.reduction)
```

Datasets: 75%| | 3/4 [02:02<00:40, 40.35s/it]

Finished training spiral with Hyperparams: [HLSize: 9, LR: 0.01, Loss: MSE] with loss function: MSE and regularizer: None

Using cuda for training

/home/sharwin/fall_2024/MSAI349_Machine_Learning/nn-venv/lib/python3.12/site-packages/torch/nn/modules/module.py:1736: UserWarning: Implicit dimension choice for softmax has been deprecated. Change the call to include dim=X as an argument.

```
return self._call_impl(*args, **kwargs)
```

Finished training two_gaussians with Hyperparams: [HLSize: 2, LR: 0.01, Loss: MCE] with loss function: MCE and regularizer: None

Using cuda for training

```
/home/sharwin/fall_2024/MSAI349_Machine_Learning/nn-venv/lib/python3.12/site-  
packages/torch/nn/modules/loss.py:608: UserWarning: Using a target size  
(torch.Size([])) that is different to the input size (torch.Size([1])). This  
will likely lead to incorrect results due to broadcasting. Please ensure they  
have the same size.
```

```
    return F.mse_loss(input, target, reduction=self.reduction)
```

```
Datasets: 100%|          | 4/4 [02:42<00:00, 40.59s/it]
```

```
Finished training two_gaussians with Hyperparams: [HLSize: 3, LR: 0.01, Loss:  
MSE] with loss function: MSE and regularizer: None
```

```
Evaluated 8 models over 4 datasets
```

```
=====
```

```
xor with Hyperparams: [HLSize: 7, LR: 0.01, Loss: MCE]
```

```
Validation Accuracy: 0.72
```

```
Test Accuracy: 0.745
```

```
=====
```

```
=====
```

```
xor with Hyperparams: [HLSize: 9, LR: 0.01, Loss: MSE]
```

```
Validation Accuracy: 0.95
```

```
Test Accuracy: 0.945
```

```
=====
```

```
=====
```

```
center_surround with Hyperparams: [HLSize: 3, LR: 0.01, Loss: MCE]
```

```
Validation Accuracy: 0.965
```

```
Test Accuracy: 0.735
```

```
=====
```

```
=====
```

```
center_surround with Hyperparams: [HLSize: 3, LR: 0.01, Loss: MSE]
```

```
Validation Accuracy: 0.955
```

```
Test Accuracy: 0.72
```

```
=====
```

```
=====
```

```
spiral with Hyperparams: [HLSize: 9, LR: 0.01, Loss: MCE]
```

```
Validation Accuracy: 0.99
```

```
Test Accuracy: 1.0
```

```
=====
```

```
=====
```

```
spiral with Hyperparams: [HLSize: 9, LR: 0.01, Loss: MSE]
```

```
Validation Accuracy: 0.99
```

```
Test Accuracy: 1.0
```

```
=====
```

```
=====
```

two_gaussians with Hyperparams: [HLSize: 2, LR: 0.01, Loss: MCE]
Validation Accuracy: 0.965
Test Accuracy: 0.91

two_gaussians with Hyperparams: [HLSize: 3, LR: 0.01, Loss: MSE]
Validation Accuracy: 0.98
Test Accuracy: 0.91

Best Hyperparams for xor: [HLSize: 7, LR: 0.01, Loss: MCE]
Validation Accuracy: 0.72
Test Accuracy: 0.745

Best Hyperparams for xor: [HLSize: 9, LR: 0.01, Loss: MSE]
Validation Accuracy: 0.95
Test Accuracy: 0.945

Best Hyperparams for center_surround: [HLSize: 3, LR: 0.01, Loss: MCE]
Validation Accuracy: 0.965
Test Accuracy: 0.735

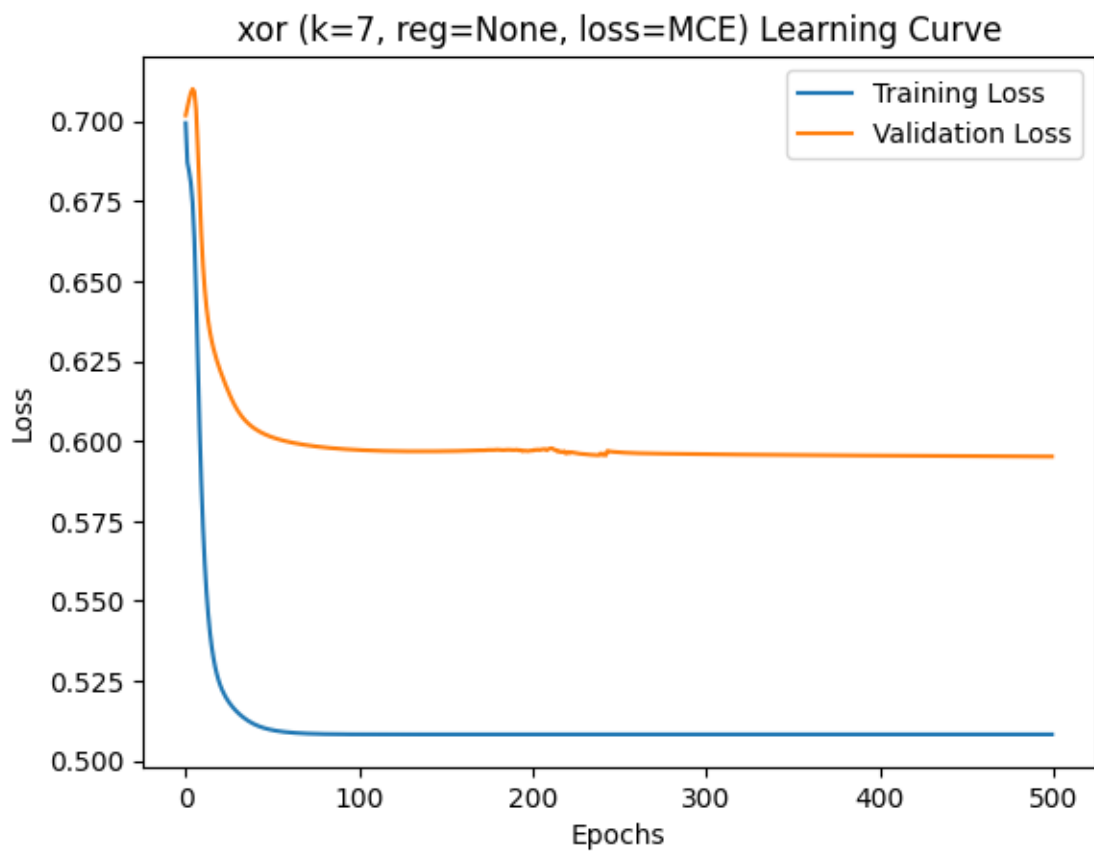
Best Hyperparams for center_surround: [HLSize: 3, LR: 0.01, Loss: MSE]
Validation Accuracy: 0.955
Test Accuracy: 0.72

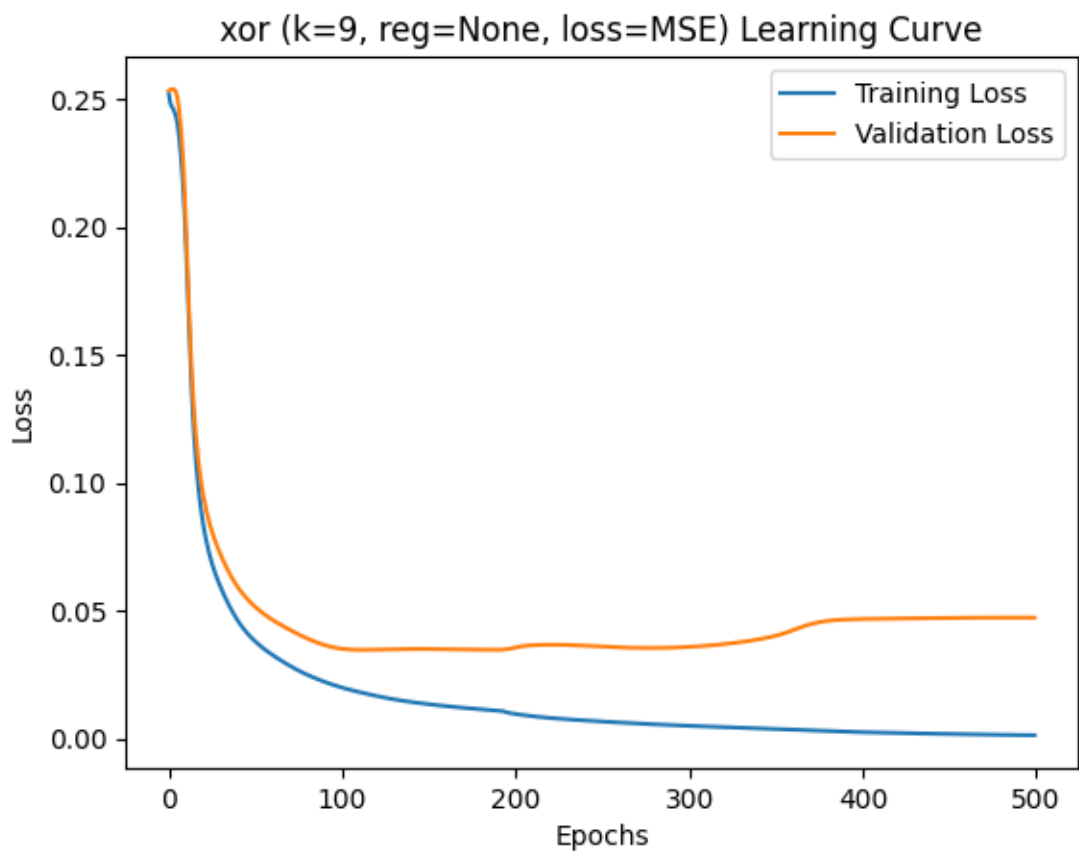
Best Hyperparams for spiral: [HLSize: 9, LR: 0.01, Loss: MCE]
Validation Accuracy: 0.99
Test Accuracy: 1.0

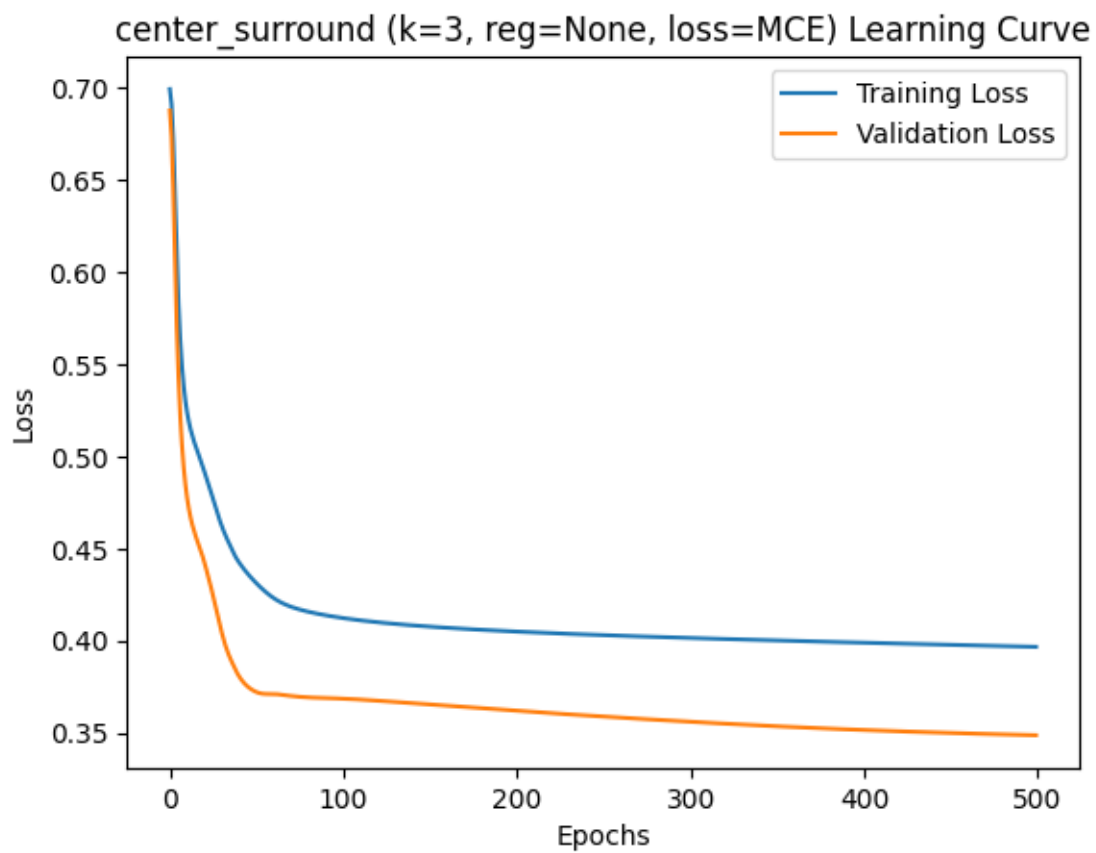
Best Hyperparams for spiral: [HLSize: 9, LR: 0.01, Loss: MSE]
Validation Accuracy: 0.99
Test Accuracy: 1.0

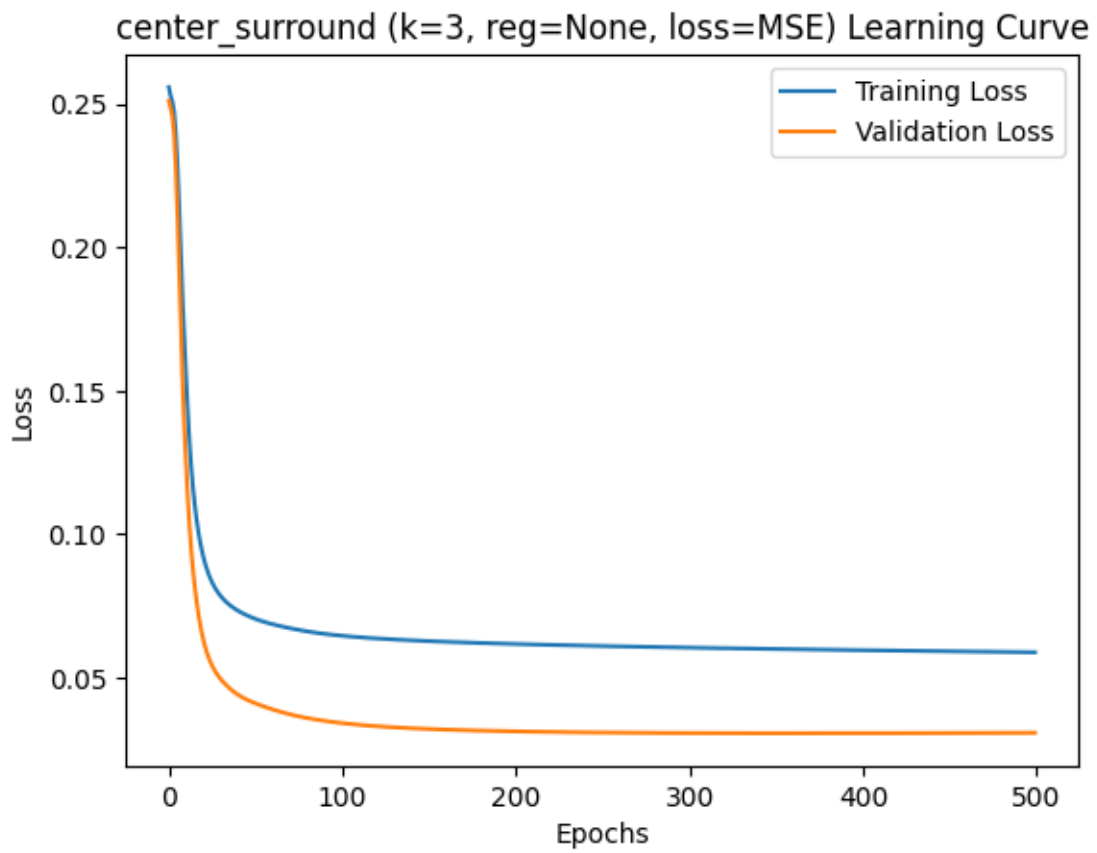
```
=====
Best Hyperparams for two_gaussians: [HLSize: 2, LR: 0.01, Loss: MCE]
Validation Accuracy: 0.965
Test Accuracy: 0.91
=====
```

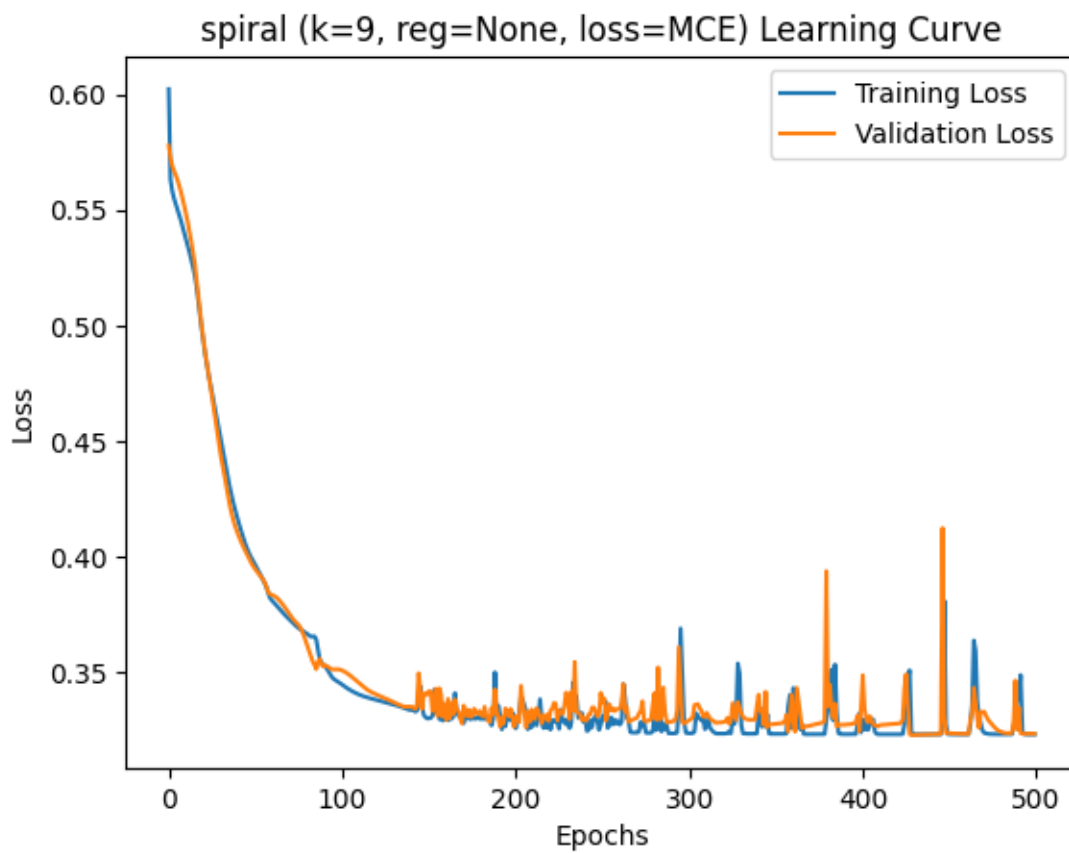
```
=====
Best Hyperparams for two_gaussians: [HLSize: 3, LR: 0.01, Loss: MSE]
Validation Accuracy: 0.98
Test Accuracy: 0.91
=====
```

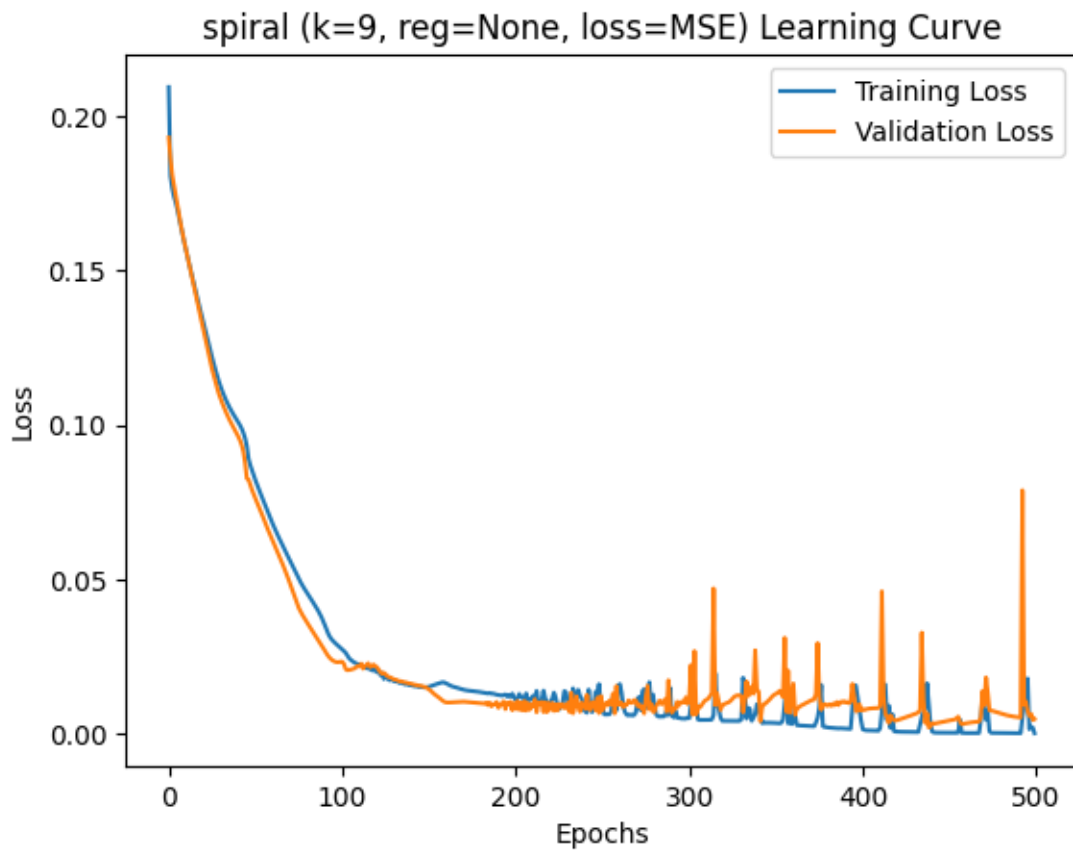


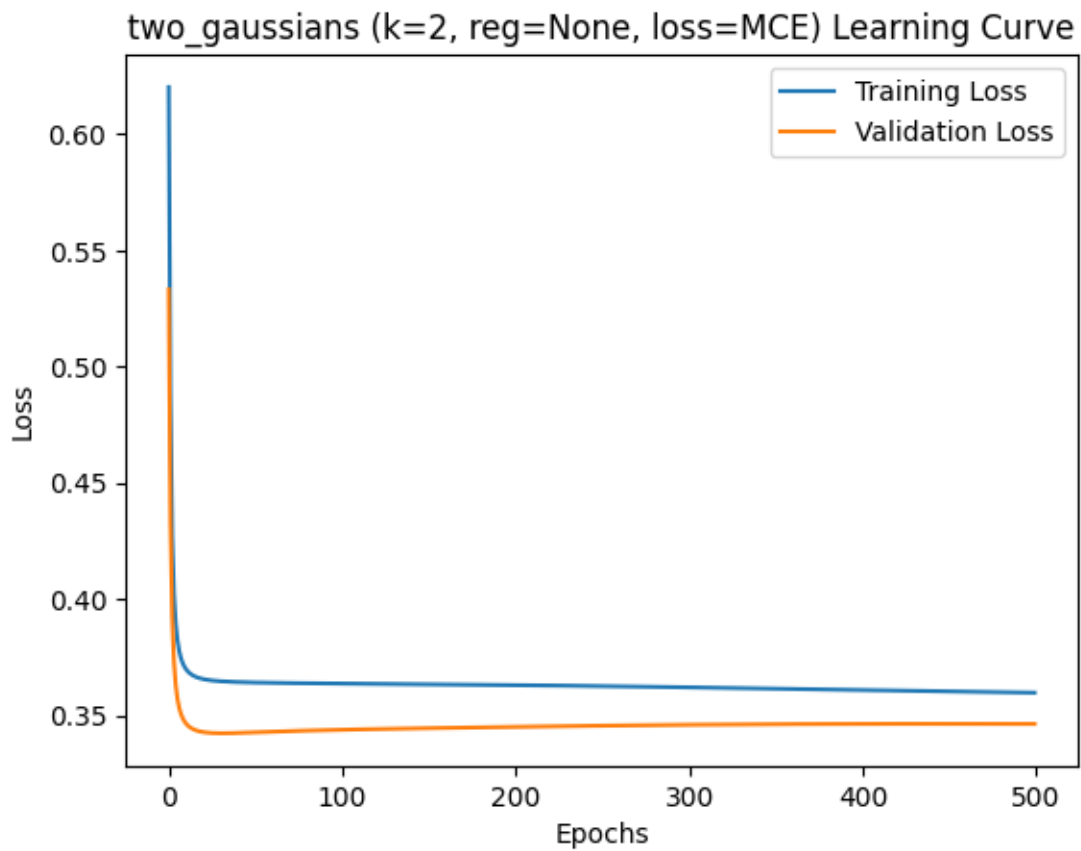


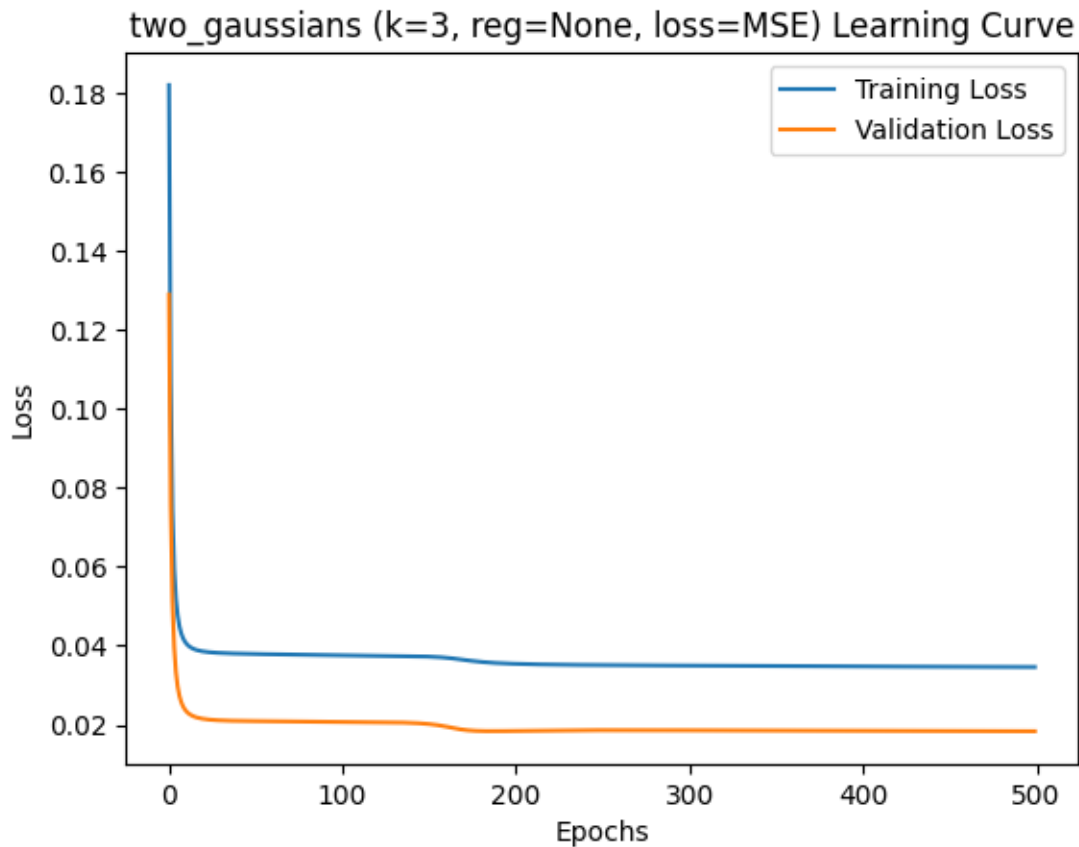












4 Part 3: Manual Gradients and Updates

```
[16]: class Node():
    def __init__(self, input_size, output_size):
        self.weights = np.random.randn(input_size, output_size)
        self.biases = np.zeros((1, output_size))

    def forward(self, inputs):
        return np.dot(inputs, self.weights) + self.biases

class NeuralNetwork():
    def __init__(self, input_data, hl_size, lr):
        self.hl_size = hl_size
        self.data = np.array(input_data)
        self.learning_rate = lr
        self.layer1 = Node(input_data.shape[0], self.hl_size)
        self.layer2 = Node(self.hl_size, 1) #One for binary classification
```

```

def tanh(self, x):
    return (np.exp(x) - np.exp(-x)) / (np.exp(x) + np.exp(-x))

def sigmoid(self, x):
    return 1 / (1 + np.exp(-x))

def mse(self, y_true, y_pred):
    return np.mean((y_true - y_pred)**2)

def forward_pass(self):
    self.z1 = self.layer1.forward(self.data.T)
    self.a1 = self.sigmoid(self.z1)
    self.z2 = self.layer2.forward(self.a1)
    self.a2 = self.sigmoid(self.z2)
    return self.a2

def backward(self, y_pred, X, y_true):
    dL_da2 = y_pred - y_true
    da2_dz2 = y_pred * (1 - y_pred) #sigmoid derivative
    dL_dz2 = dL_da2 * da2_dz2
    dz2_dw2 = self.a1

    dL_dw2 = np.dot(dz2_dw2.T, dL_dz2)
    dL_b2 = np.sum(dL_dz2, axis=0, keepdims=True)

    dL_da1 = np.dot(dL_dz2, self.layer2.weights.T)
    dL_dz1 = dL_da1 * (self.a1 * (1 - self.a1))

    X = X.reshape(-1, 1)
    dL_dw1 = np.dot(X, dL_dz1)
    dL_b1 = np.sum(dL_dz1, axis=0, keepdims=True)

    self.layer1.weights -= self.learning_rate * dL_dw1
    self.layer1.biases -= self.learning_rate * dL_b1
    self.layer2.weights -= self.learning_rate * dL_dw2
    self.layer2.biases -= self.learning_rate * dL_b2

def train(self, num_epochs, X_train, y_train, X_valid, y_valid, nn):
    #Stochastic Gradient descent
    training_learning_curve = []
    validation_learning_curve = []
    ##### Training Phase #####
    for i in range(num_epochs):
        training_loss = 0
        for j in range(len(X_train)):

```

```

        input_data = X_train[j]
        label = y_train[j]

        nn.data = input_data
        nn.label = label

        y_pred = nn.forward_pass()
        loss = nn.mse(y_train[j], y_pred)
        nn.backward(y_pred, input_data, y_train[j])
        training_loss += loss
        training_learning_curve.append(training_loss / len(X_train))
#### Finished Training ####
#### Validation Phase ####
validation_loss = 0
for i in range(len(X_valid)):
    input_data = X_valid[i]
    label = y_valid[i]

    nn.data = input_data
    nn.label = label

    y_pred = nn.forward_pass()
    loss = nn.mse(y_valid[i], y_pred)
    validation_loss += loss
    validation_learning_curve.append(validation_loss / len(X_valid))
#### Finished Validation ####
return training_learning_curve, validation_learning_curve

def evaluate(self, X, y, nn):
    correct = 0
    total = 0
    for j in range(len(X)):
        input_data = X[j]
        nn.data = input_data

        y_pred = nn.forward_pass()

        if y_pred >= 0.5:
            y_pred = 1
        elif y_pred < 0.5:
            y_pred = 0

        if y_pred == y[j]:
            correct += 1

    total += 1

```

```

        accuracy = correct / total
        return accuracy

def predict(self, X):
    y_pred = []
    for i in range(len(X)):
        input_data = X[i]
        self.data = input_data
        y_pred.append(self.forward_pass())
    return np.array(y_pred)

def plot_learning_curve(self, datasetname, train_curve, valid_curve):
    plt.figure()
    plt.plot(train_curve, label='Training Loss')
    plt.plot(valid_curve, label='Validation Loss')
    plt.title(f'{datasetname} Manual Learning Curve')
    plt.xlabel('Epochs')
    plt.ylabel('Loss')
    plt.legend(['Training Loss', 'Validation Loss'])
    plt.savefig(f'plots/{datasetname}_manual_NN_learning_curve.png')

def plot_decision_boundary(self, datasetname, X_test, y_test):
    fig, ax = plt.subplots()
    plot_decision_regions(
        features=X_test,
        targets=y_test,
        model=self,
        axis=ax,
        title=f"{datasetname} Manual Decision Regions"
    )
    plt.savefig(f"plots/{datasetname}_manual_decision_regions.png")

def main():
    hidden_layer_size = 9
    learning_rate = 0.01
    num_epochs = 700
    np.random.seed(11)
    label_string = 'label'
    valid_accuracy_list = []
    test_accuracy_list = []
    dataset_names = ["center_surround", "spiral", "two_gaussians", "xor"]
    train_list = ["center_surround_train.csv", "spiral_train.csv",
                  "two_gaussians_train.csv", "xor_train.csv"]
    test_list = ["center_surround_test.csv", "spiral_test.csv",
                 "two_gaussians_test.csv", "xor_test.csv"]
    valid_list = ["center_surround_valid.csv", "spiral_valid.csv",
                  "two_gaussians_valid.csv", "xor_valid.csv"]

```

```

for i in range(len(train_list)):
    X_train = pd.read_csv(train_list[i])
    X_test = pd.read_csv(test_list[i])
    X_valid = pd.read_csv(valid_list[i])

    # Seperate labels
    y_train = X_train[label_string].values
    y_test = X_test[label_string].values
    y_valid = X_valid[label_string].values

    # Drop labels
    X_train = X_train.drop(label_string, axis=1).values
    X_test = X_test.drop(label_string, axis=1).values
    X_valid = X_valid.drop(label_string, axis=1).values

    nn = NeuralNetwork(X_train[0], hidden_layer_size, learning_rate)

    train_curve, valid_curve = nn.train(
        num_epochs,
        X_train,
        y_train,
        X_valid,
        y_valid,
        nn
    )

    valid_accuracy = nn.evaluate(X_valid, y_valid, nn)
    test_accuracy = nn.evaluate(X_test, y_test, nn)

    valid_accuracy_list.append(valid_accuracy)
    test_accuracy_list.append(test_accuracy)

    dataset_name = dataset_names[i]
    nn.plot_learning_curve(dataset_name, train_curve, valid_curve)
    nn.plot_decision_boundary(dataset_name, X_test, y_test)

for i in range(len(test_list)):
    print(f"Validation Accuracy for dataset {valid_list[i]}:␣
↪{valid_accuracy_list[i]}")
    print(f"Test Accuracy for dataset {test_list[i]}:␣
↪{test_accuracy_list[i]}\n")

main()

```

Validation Accuracy for dataset center_surround_valid.csv: 0.97

Test Accuracy for dataset center_surround_test.csv: 0.75

Validation Accuracy for dataset spiral_valid.csv: 0.925

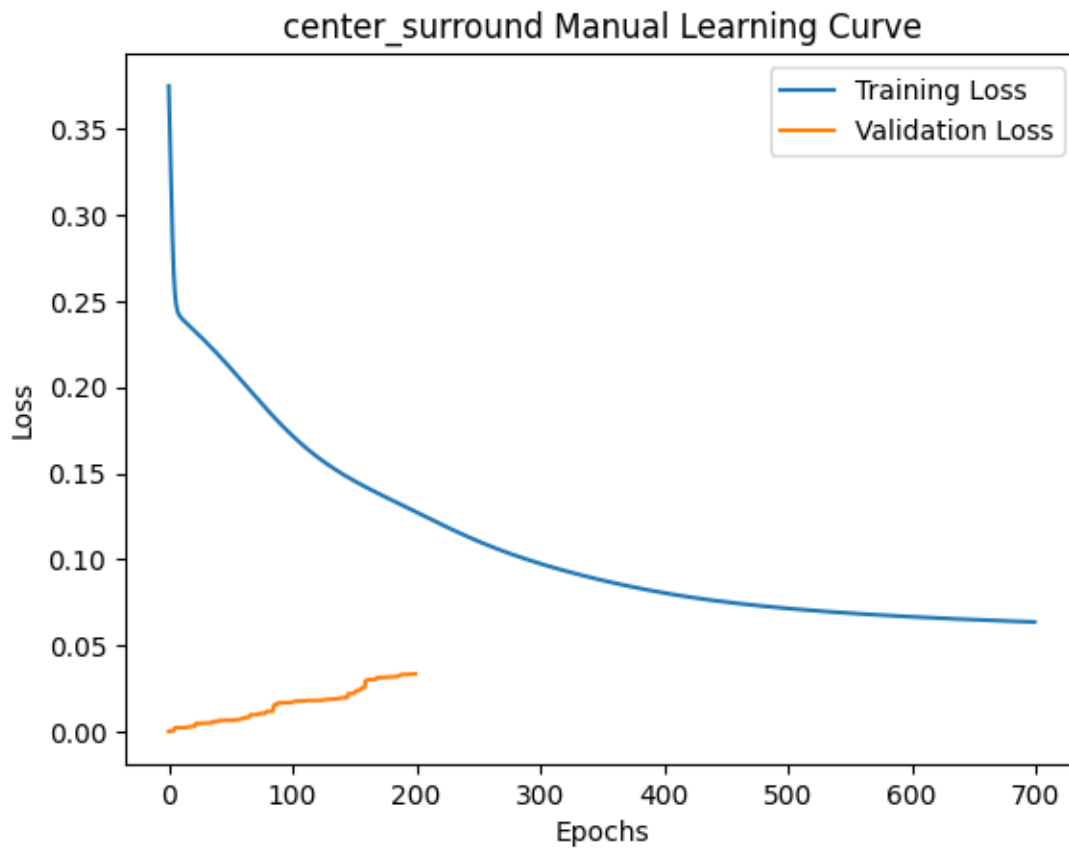
Test Accuracy for dataset spiral_test.csv: 0.945

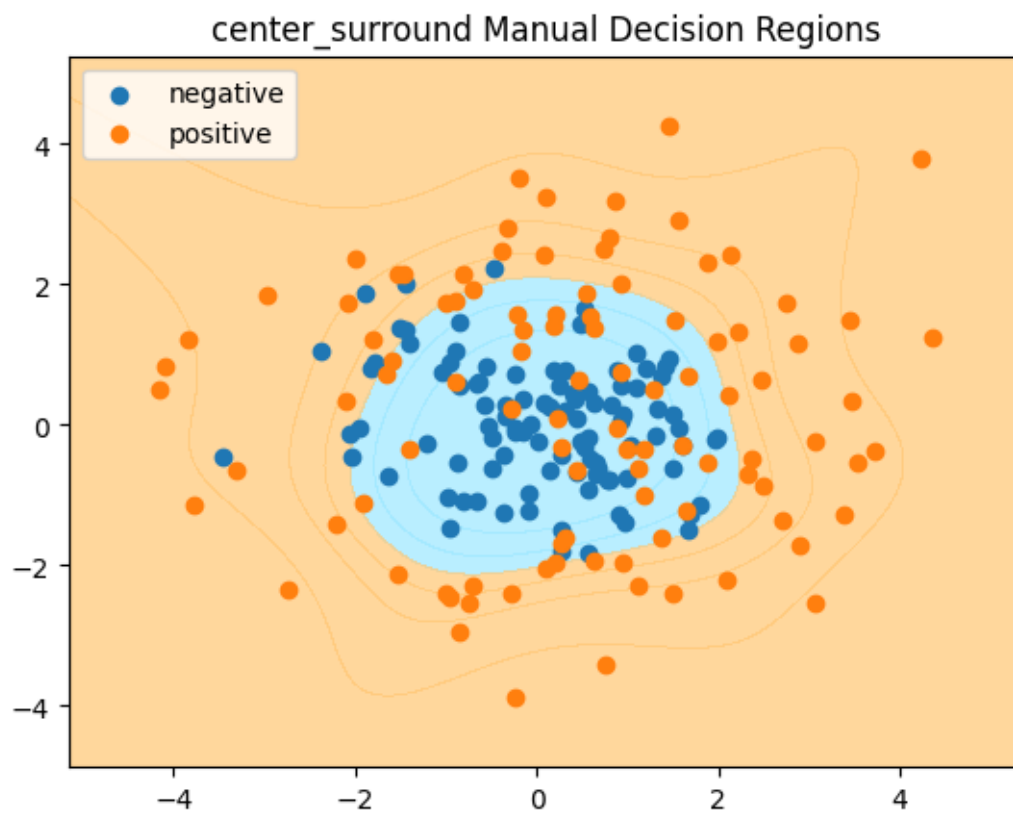
Validation Accuracy for dataset two_gaussians_valid.csv: 0.98

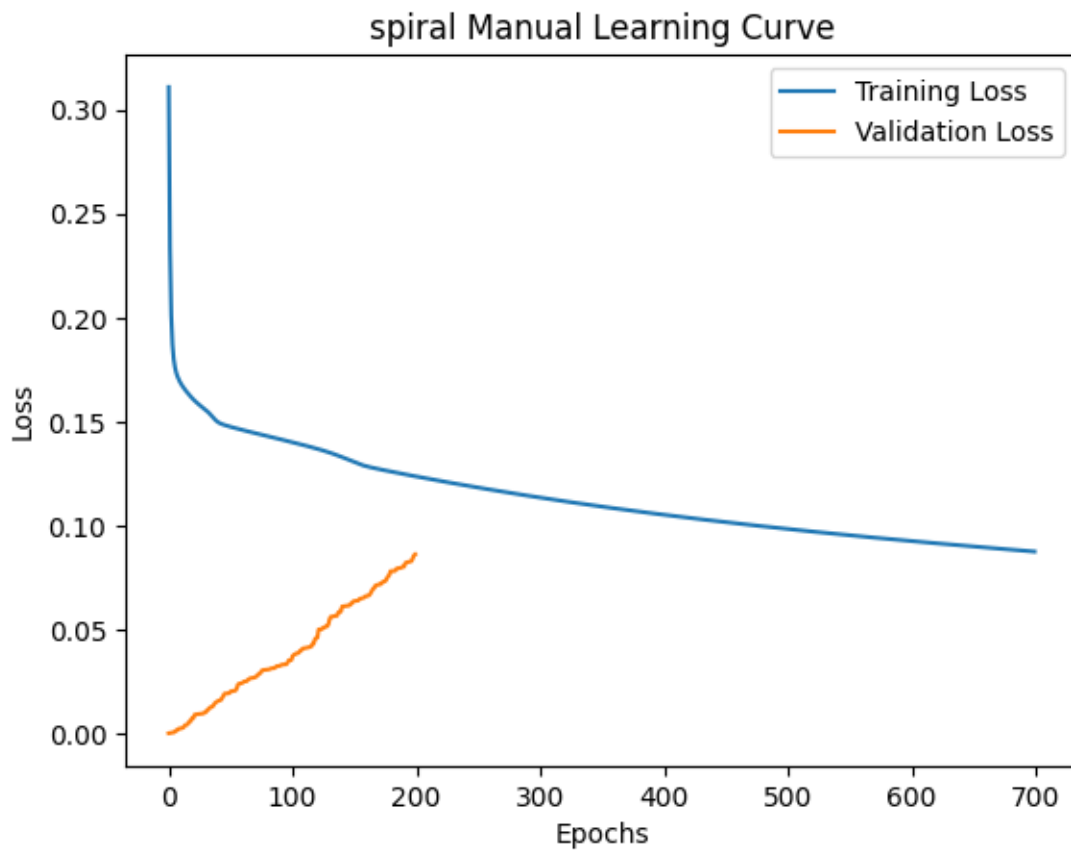
Test Accuracy for dataset two_gaussians_test.csv: 0.91

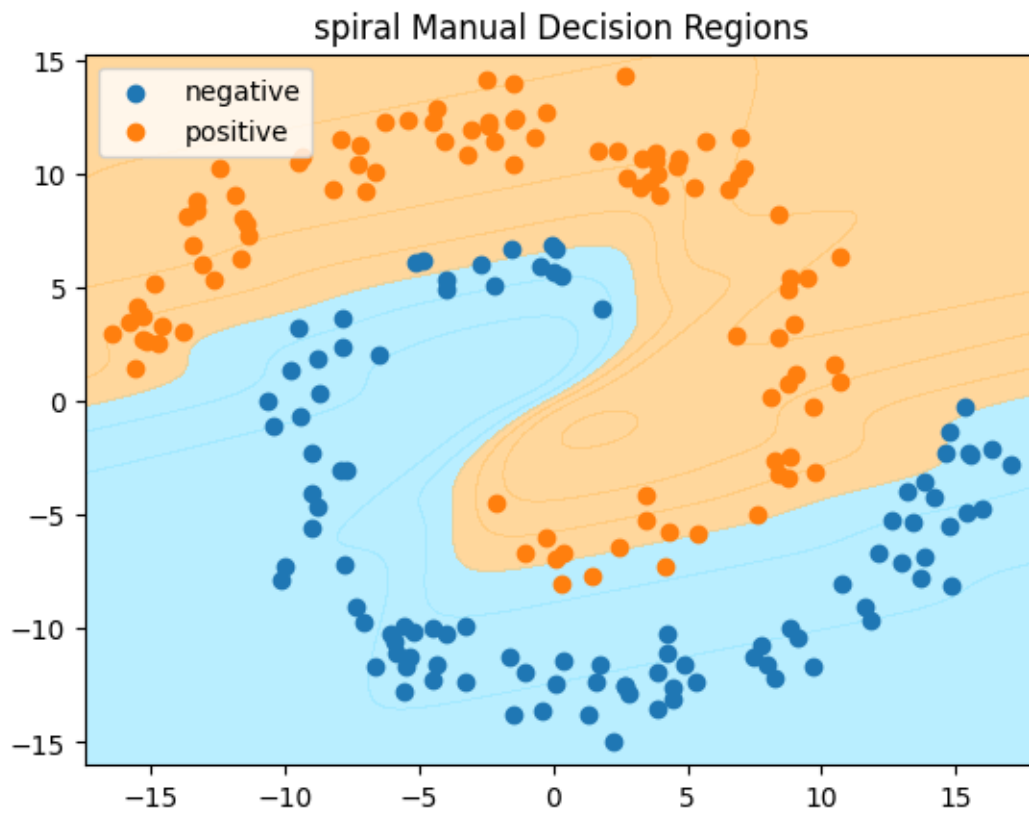
Validation Accuracy for dataset xor_valid.csv: 0.915

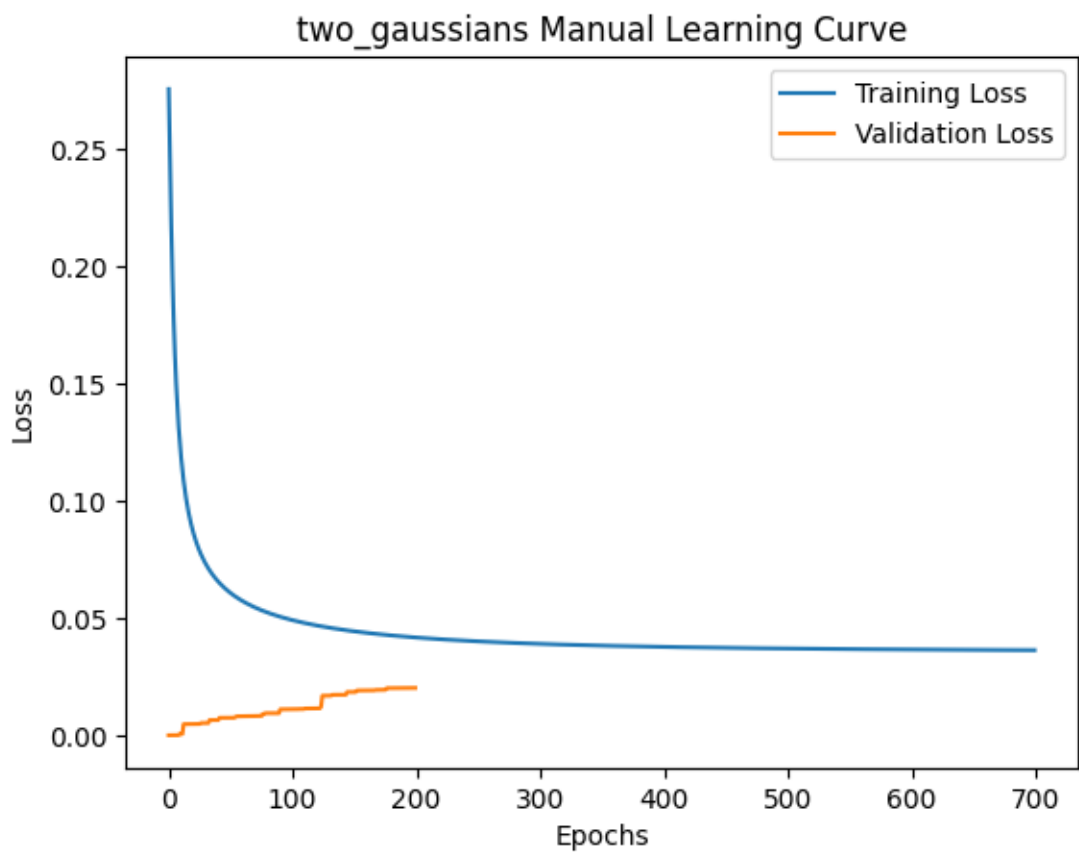
Test Accuracy for dataset xor_test.csv: 0.905

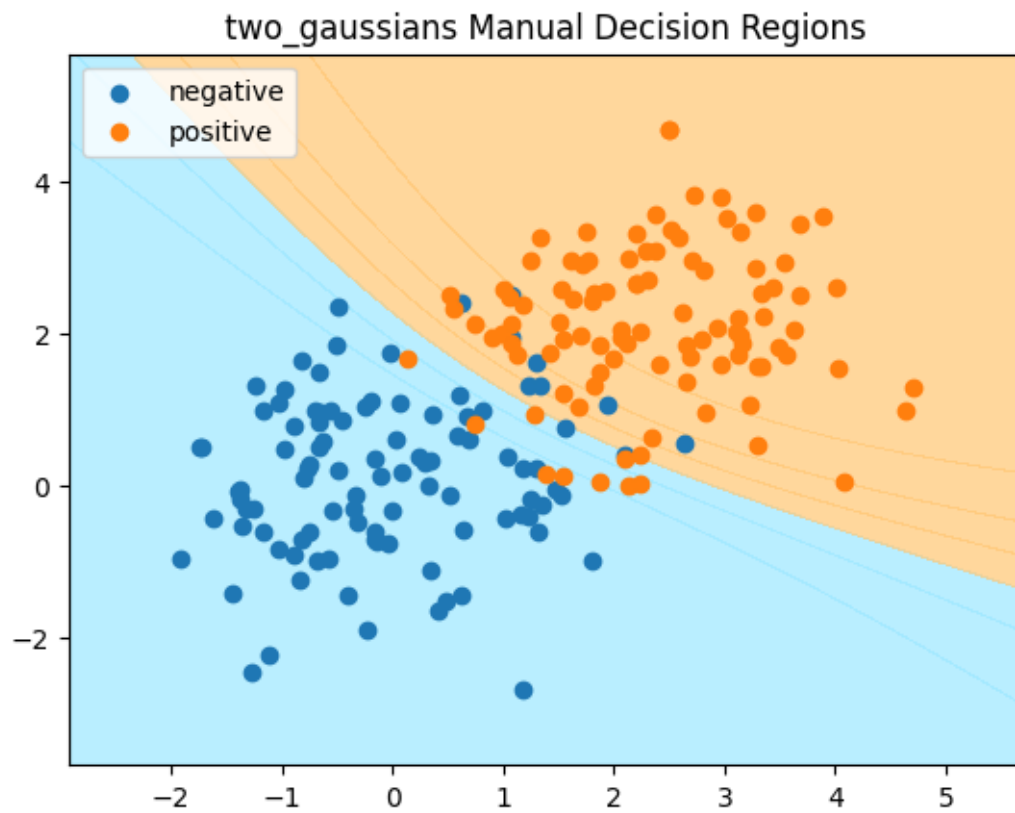


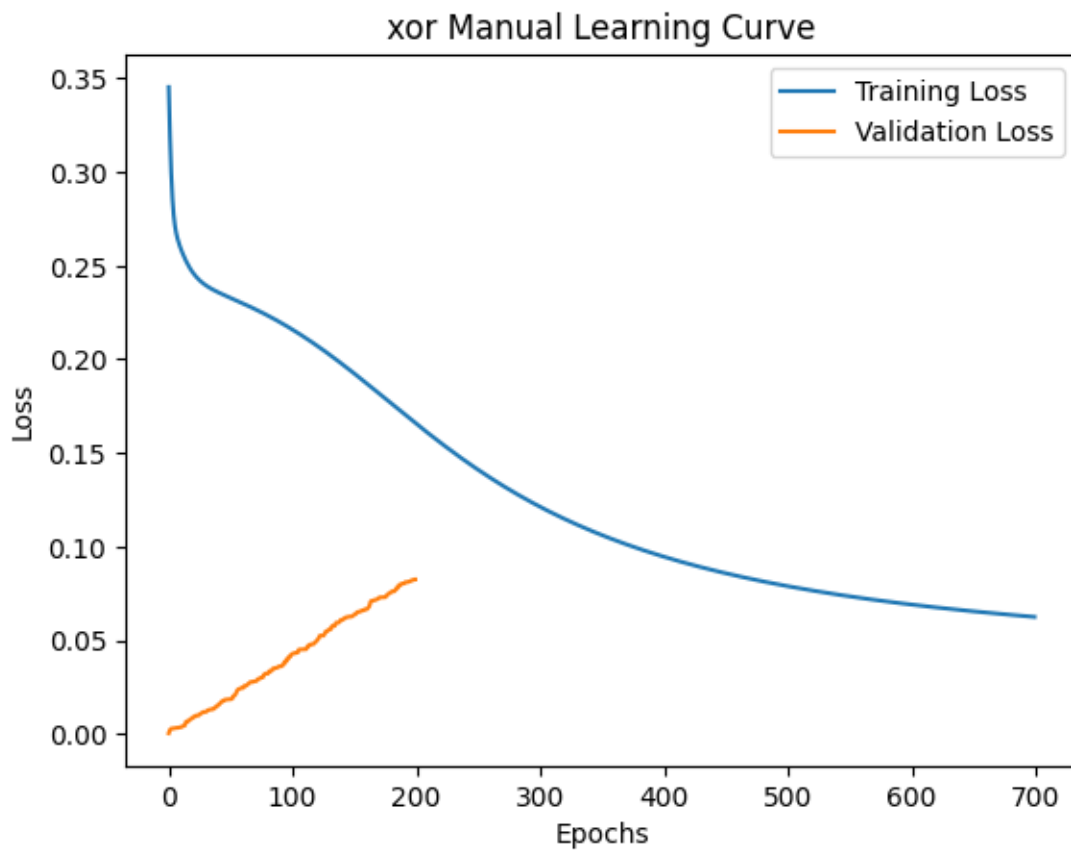


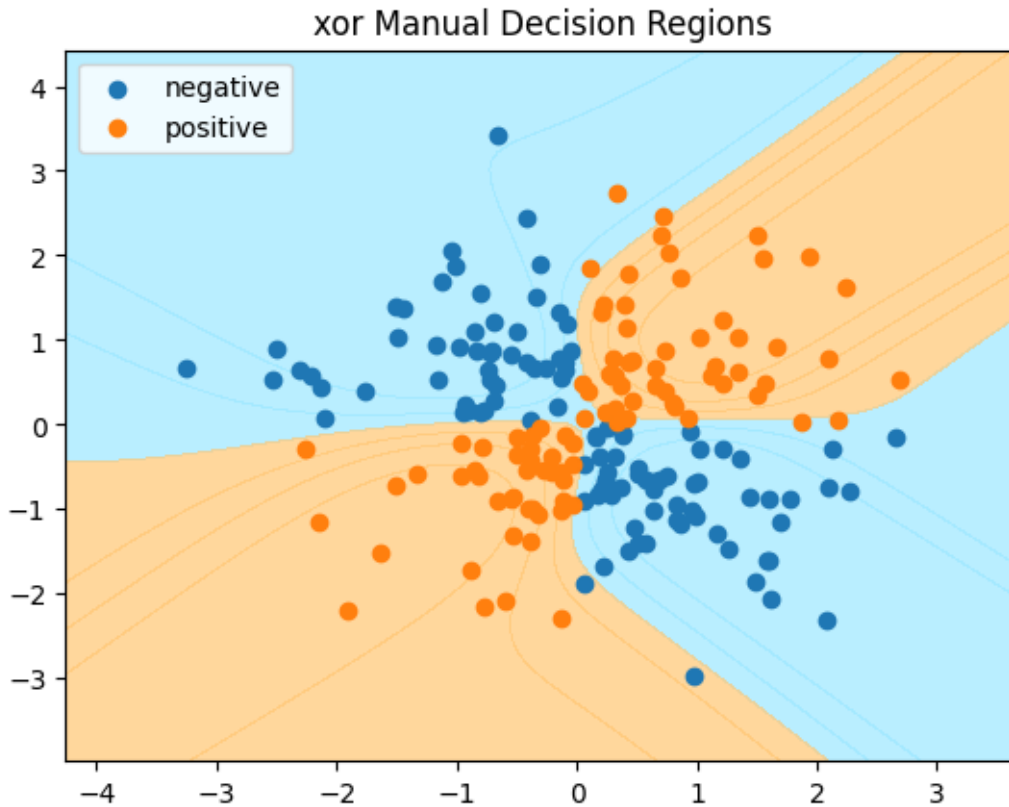












5 Part 4: Regularizers

Repeat parts 1 and 2 with regularizers.

```
[7]: def evaluate_models_on_all_datasets():
    print(f"WARNING: This script will take a long time to run ...")
    evaluator = NeuralNetEvaluator(
        training_data={"xor": "xor_train.csv",
                       "center_surround": "center_surround_train.csv",
                       "spiral": "spiral_train.csv",
                       "two_gaussians": "two_gaussians_train.csv"},
        test_data={"xor": "xor_test.csv",
                   "center_surround": "center_surround_test.csv",
                   "spiral": "spiral_test.csv",
                   "two_gaussians": "two_gaussians_test.csv"},
        validation_data={"xor": "xor_valid.csv",
                         "center_surround": "center_surround_valid.csv",
                         "spiral": "spiral_valid.csv",
```

```

        "two_gaussians": "two_gaussians_valid.csv"
    },
    loss_functions={"MCE": nn.CrossEntropyLoss(), "MSE": nn.MSELoss()}
)
datasets = ["xor", "center_surround", "spiral", "two_gaussians"]
hidden_layer_sizes = [2, 3, 5, 7, 9]
losses = ["MSE"]
regularizers = ["", "norm", "orthogonal"]
# After running and manually inspecting the results,
# these are the best HPs for each dataset and loss function
# These should also be used when using regularizers
best_hps_map = {
    "xor_MCE": HyperParams(7, 0.01, "MCE"),
    "xor_MSE": HyperParams(9, 0.01, "MSE"),
    "center_surround_MCE": HyperParams(3, 0.01, "MCE"),
    "center_surround_MSE": HyperParams(3, 0.01, "MSE"),
    "spiral_MCE": HyperParams(9, 0.01, "MCE"),
    "spiral_MSE": HyperParams(9, 0.01, "MSE"),
    "two_gaussians_MCE": HyperParams(2, 0.01, "MCE"),
    "two_gaussians_MSE": HyperParams(3, 0.01, "MSE")
}
for reg in regularizers:
    for dataset in tqdm(datasets, desc="Datasets"):
        for loss in losses:
            dataset_loss = f"{dataset}_{loss}"
            hp = best_hps_map[dataset_loss]
            evaluator.train_model(dataset, loss, reg, hp)
# Uncomment this block to train models with different hyperparams
# for dataset in tqdm(datasets, desc="Datasets"):
#     for hl_size in hidden_layer_sizes:
#         for loss in losses:
#             hp = HyperParams(hl_size, 0.01, loss)
#             evaluator.train_model(dataset, loss, hp)
            evaluator.print_evaluated_models()
        for dataset in datasets:
            for loss_name in losses:
                best_hp, valid_acc, test_acc = evaluator.
↪ find_best_hyperparams_for_dataset(
                    dataset, loss_name
                )
                print("=====")
                print(
                    f'Best Hyperparams for {dataset}: ' +
                    f'{best_hp} Reg={'None' if reg == '' else reg}'
                )
                print(f"Validation Accuracy: {valid_acc}")
                print(f"Test Accuracy: {test_acc}")

```



```

print("=====\n")
evaluator.plot_learning_curves(dataset, best_hp)
evaluator.plot_learned_decision_surfaces(
    dataset, loss_name, reg)
print(f"===== Finished training and evaluating models =====")

```

```

[8]: # Run the evaluation
evaluate_models_on_all_datasets()

```

WARNING: This script will take a long time to run ...

Datasets: 0% | 0/4 [00:00<?, ?it/s]

Using cuda for training

/home/sharwin/fall_2024/MSAI349_Machine_Learning/nn-venv/lib/python3.12/site-packages/torch/nn/modules/loss.py:608: UserWarning: Using a target size (torch.Size([])) that is different to the input size (torch.Size([1])). This will likely lead to incorrect results due to broadcasting. Please ensure they have the same size.

```

    return F.mse_loss(input, target, reduction=self.reduction)

```

Datasets: 25% | 1/4 [00:21<01:03, 21.27s/it]

Finished training xor with Hyperparams: [HLSize: 9, LR: 0.01, Loss: MSE] with loss function: MSE and regularizer: None

Using cuda for training

/home/sharwin/fall_2024/MSAI349_Machine_Learning/nn-venv/lib/python3.12/site-packages/torch/nn/modules/loss.py:608: UserWarning: Using a target size (torch.Size([])) that is different to the input size (torch.Size([1])). This will likely lead to incorrect results due to broadcasting. Please ensure they have the same size.

```

    return F.mse_loss(input, target, reduction=self.reduction)

```

Datasets: 50% | 2/4 [00:42<00:42, 21.08s/it]

Finished training center_surround with Hyperparams: [HLSize: 3, LR: 0.01, Loss: MSE] with loss function: MSE and regularizer: None

Using cuda for training

/home/sharwin/fall_2024/MSAI349_Machine_Learning/nn-venv/lib/python3.12/site-packages/torch/nn/modules/loss.py:608: UserWarning: Using a target size (torch.Size([])) that is different to the input size (torch.Size([1])). This will likely lead to incorrect results due to broadcasting. Please ensure they have the same size.

```

    return F.mse_loss(input, target, reduction=self.reduction)

```

Datasets: 75% | 3/4 [01:03<00:21, 21.01s/it]

Finished training spiral with Hyperparams: [HLSize: 9, LR: 0.01, Loss: MSE] with loss function: MSE and regularizer: None

Using cuda for training

```
/home/sharwin/fall_2024/MSAI349_Machine_Learning/nn-venv/lib/python3.12/site-
packages/torch/nn/modules/loss.py:608: UserWarning: Using a target size
(torch.Size([])) that is different to the input size (torch.Size([1])). This
will likely lead to incorrect results due to broadcasting. Please ensure they
have the same size.
```

```
    return F.mse_loss(input, target, reduction=self.reduction)
```

```
Datasets: 100%|      | 4/4 [01:23<00:00, 20.88s/it]
```

```
Finished training two_gaussians with Hyperparams: [HLSize: 3, LR: 0.01, Loss:
MSE] with loss function: MSE and regularizer: None
```

```
Evaluated 4 models over 4 datasets
```

```
=====
```

```
xor with Hyperparams: [HLSize: 9, LR: 0.01, Loss: MSE]
```

```
Validation Accuracy: 0.945
```

```
Test Accuracy: 0.945
```

```
=====
```

```
=====
```

```
center_surround with Hyperparams: [HLSize: 3, LR: 0.01, Loss: MSE]
```

```
Validation Accuracy: 0.965
```

```
Test Accuracy: 0.72
```

```
=====
```

```
=====
```

```
spiral with Hyperparams: [HLSize: 9, LR: 0.01, Loss: MSE]
```

```
Validation Accuracy: 0.995
```

```
Test Accuracy: 1.0
```

```
=====
```

```
=====
```

```
two_gaussians with Hyperparams: [HLSize: 3, LR: 0.01, Loss: MSE]
```

```
Validation Accuracy: 0.975
```

```
Test Accuracy: 0.91
```

```
=====
```

```
=====
```

```
Best Hyperparams for xor: [HLSize: 9, LR: 0.01, Loss: MSE] Reg=None
```

```
Validation Accuracy: 0.945
```

```
Test Accuracy: 0.945
```

```
=====
```

```
Drawing Decision Region for xor_MSE_
```

```
=====
```

```
Best Hyperparams for center_surround: [HLSize: 3, LR: 0.01, Loss: MSE] Reg=None
```

```
Validation Accuracy: 0.965
```

```
Test Accuracy: 0.72
```

```
=====
```

Drawing Decision Region for center_surround_MSE_

=====

Best Hyperparams for spiral: [HLSize: 9, LR: 0.01, Loss: MSE] Reg=None

Validation Accuracy: 0.995

Test Accuracy: 1.0

=====

Drawing Decision Region for spiral_MSE_

=====

Best Hyperparams for two_gaussians: [HLSize: 3, LR: 0.01, Loss: MSE] Reg=None

Validation Accuracy: 0.975

Test Accuracy: 0.91

=====

Drawing Decision Region for two_gaussians_MSE_

Datasets: 0%| | 0/4 [00:00<?,
?it/s]/home/sharwin/fall_2024/MSAI349_Machine_Learning/nn-
venv/lib/python3.12/site-packages/torch/nn/modules/loss.py:608: UserWarning:
Using a target size (torch.Size([])) that is different to the input size
(torch.Size([1])). This will likely lead to incorrect results due to
broadcasting. Please ensure they have the same size.

return F.mse_loss(input, target, reduction=self.reduction)

Using cuda for training

Datasets: 25%| | 1/4 [00:23<01:11, 23.81s/it]

Finished training xor with Hyperparams: [HLSize: 9, LR: 0.01, Loss: MSE] with
loss function: MSE and regularizer: norm

Using cuda for training

/home/sharwin/fall_2024/MSAI349_Machine_Learning/nn-venv/lib/python3.12/site-
packages/torch/nn/modules/loss.py:608: UserWarning: Using a target size
(torch.Size([])) that is different to the input size (torch.Size([1])). This
will likely lead to incorrect results due to broadcasting. Please ensure they
have the same size.

return F.mse_loss(input, target, reduction=self.reduction)

Datasets: 50%| | 2/4 [00:47<00:47, 23.89s/it]

Finished training center_surround with Hyperparams: [HLSize: 3, LR: 0.01, Loss:
MSE] with loss function: MSE and regularizer: norm

Using cuda for training

/home/sharwin/fall_2024/MSAI349_Machine_Learning/nn-venv/lib/python3.12/site-
packages/torch/nn/modules/loss.py:608: UserWarning: Using a target size
(torch.Size([])) that is different to the input size (torch.Size([1])). This
will likely lead to incorrect results due to broadcasting. Please ensure they
have the same size.

```

    return F.mse_loss(input, target, reduction=self.reduction)
Datasets: 75%|          | 3/4 [01:11<00:23, 23.75s/it]

Finished training spiral with Hyperparams: [HLSize: 9, LR: 0.01, Loss: MSE] with
loss function: MSE and regularizer: norm
Using cuda for training

/home/sharwin/fall_2024/MSAI349_Machine_Learning/nn-venv/lib/python3.12/site-
packages/torch/nn/modules/loss.py:608: UserWarning: Using a target size
(torch.Size([])) that is different to the input size (torch.Size([1])). This
will likely lead to incorrect results due to broadcasting. Please ensure they
have the same size.
    return F.mse_loss(input, target, reduction=self.reduction)
Datasets: 100%|         | 4/4 [01:34<00:00, 23.70s/it]

Finished training two_gaussians with Hyperparams: [HLSize: 3, LR: 0.01, Loss:
MSE] with loss function: MSE and regularizer: norm
Evaluated 4 models over 4 datasets
=====
xor with Hyperparams: [HLSize: 9, LR: 0.01, Loss: MSE]
Validation Accuracy: 0.455
Test Accuracy: 0.54
=====

=====
center_surround with Hyperparams: [HLSize: 3, LR: 0.01, Loss: MSE]
Validation Accuracy: 0.975
Test Accuracy: 0.72
=====

=====
spiral with Hyperparams: [HLSize: 9, LR: 0.01, Loss: MSE]
Validation Accuracy: 0.975
Test Accuracy: 0.97
=====

=====
two_gaussians with Hyperparams: [HLSize: 3, LR: 0.01, Loss: MSE]
Validation Accuracy: 0.98
Test Accuracy: 0.915
=====

=====
Best Hyperparams for xor: [HLSize: 9, LR: 0.01, Loss: MSE] Reg=norm
Validation Accuracy: 0.455
Test Accuracy: 0.54
=====

Drawing Decision Region for xor_MSE_norm

```

```
=====
Best Hyperparams for center_surround: [HLSize: 3, LR: 0.01, Loss: MSE] Reg=norm
Validation Accuracy: 0.975
Test Accuracy: 0.72
=====
```

Drawing Decision Region for center_surround_MSE_norm

```
=====
Best Hyperparams for spiral: [HLSize: 9, LR: 0.01, Loss: MSE] Reg=norm
Validation Accuracy: 0.975
Test Accuracy: 0.97
=====
```

Drawing Decision Region for spiral_MSE_norm

```
=====
Best Hyperparams for two_gaussians: [HLSize: 3, LR: 0.01, Loss: MSE] Reg=norm
Validation Accuracy: 0.98
Test Accuracy: 0.915
=====
```

Drawing Decision Region for two_gaussians_MSE_norm

Datasets: 0%| | 0/4 [00:00<?, ?it/s]

Using cuda for training

/home/sharwin/fall_2024/MSAI349_Machine_Learning/nn-venv/lib/python3.12/site-packages/torch/nn/modules/loss.py:608: UserWarning: Using a target size (torch.Size([])) that is different to the input size (torch.Size([1])). This will likely lead to incorrect results due to broadcasting. Please ensure they have the same size.

```
    return F.mse_loss(input, target, reduction=self.reduction)
```

Datasets: 25%| | 1/4 [00:27<01:21, 27.17s/it]

Finished training xor with Hyperparams: [HLSize: 9, LR: 0.01, Loss: MSE] with loss function: MSE and regularizer: orthogonal

Using cuda for training

/home/sharwin/fall_2024/MSAI349_Machine_Learning/nn-venv/lib/python3.12/site-packages/torch/nn/modules/loss.py:608: UserWarning: Using a target size (torch.Size([])) that is different to the input size (torch.Size([1])). This will likely lead to incorrect results due to broadcasting. Please ensure they have the same size.

```
    return F.mse_loss(input, target, reduction=self.reduction)
```

Datasets: 50%| | 2/4 [00:53<00:53, 26.67s/it]

Finished training center_surround with Hyperparams: [HLSize: 3, LR: 0.01, Loss: MSE] with loss function: MSE and regularizer: orthogonal

Using cuda for training

```
/home/sharwin/fall_2024/MSAI349_Machine_Learning/nn-venv/lib/python3.12/site-  
packages/torch/nn/modules/loss.py:608: UserWarning: Using a target size  
(torch.Size([])) that is different to the input size (torch.Size([1])). This  
will likely lead to incorrect results due to broadcasting. Please ensure they  
have the same size.
```

```
    return F.mse_loss(input, target, reduction=self.reduction)
```

```
Datasets: 75%|          | 3/4 [01:20<00:26, 26.68s/it]
```

```
Finished training spiral with Hyperparams: [HLSize: 9, LR: 0.01, Loss: MSE] with  
loss function: MSE and regularizer: orthogonal
```

```
Using cuda for training
```

```
/home/sharwin/fall_2024/MSAI349_Machine_Learning/nn-venv/lib/python3.12/site-  
packages/torch/nn/modules/loss.py:608: UserWarning: Using a target size  
(torch.Size([])) that is different to the input size (torch.Size([1])). This  
will likely lead to incorrect results due to broadcasting. Please ensure they  
have the same size.
```

```
    return F.mse_loss(input, target, reduction=self.reduction)
```

```
Datasets: 100%|         | 4/4 [01:47<00:00, 26.81s/it]
```

```
Finished training two_gaussians with Hyperparams: [HLSize: 3, LR: 0.01, Loss:  
MSE] with loss function: MSE and regularizer: orthogonal
```

```
Evaluated 4 models over 4 datasets
```

```
=====
```

```
xor with Hyperparams: [HLSize: 9, LR: 0.01, Loss: MSE]
```

```
Validation Accuracy: 0.875
```

```
Test Accuracy: 0.93
```

```
=====
```

```
=====
```

```
center_surround with Hyperparams: [HLSize: 3, LR: 0.01, Loss: MSE]
```

```
Validation Accuracy: 0.985
```

```
Test Accuracy: 0.735
```

```
=====
```

```
=====
```

```
spiral with Hyperparams: [HLSize: 9, LR: 0.01, Loss: MSE]
```

```
Validation Accuracy: 0.99
```

```
Test Accuracy: 0.995
```

```
=====
```

```
=====
```

```
two_gaussians with Hyperparams: [HLSize: 3, LR: 0.01, Loss: MSE]
```

```
Validation Accuracy: 0.98
```

```
Test Accuracy: 0.91
```

```
=====
```

```
=====
```

```
Best Hyperparams for xor: [HLSize: 9, LR: 0.01, Loss: MSE] Reg=orthogonal
```

Validation Accuracy: 0.875

Test Accuracy: 0.93

=====

Drawing Decision Region for xor_MSE_orthogonal

=====

Best Hyperparams for center_surround: [HLSize: 3, LR: 0.01, Loss: MSE]

Reg=orthogonal

Validation Accuracy: 0.985

Test Accuracy: 0.735

=====

Drawing Decision Region for center_surround_MSE_orthogonal

=====

Best Hyperparams for spiral: [HLSize: 9, LR: 0.01, Loss: MSE] Reg=orthogonal

Validation Accuracy: 0.99

Test Accuracy: 0.995

=====

/tmp/ipykernel_9583/1396162206.py:351: RuntimeWarning: More than 20 figures have
been opened. Figures created through the pyplot interface
(`matplotlib.pyplot.figure`) are retained until explicitly closed and may
consume too much memory. (To control this warning, see the rcParam
`figure.max_open_warning`). Consider using `matplotlib.pyplot.close()`.
plt.figure()

Drawing Decision Region for spiral_MSE_orthogonal

=====

Best Hyperparams for two_gaussians: [HLSize: 3, LR: 0.01, Loss: MSE]

Reg=orthogonal

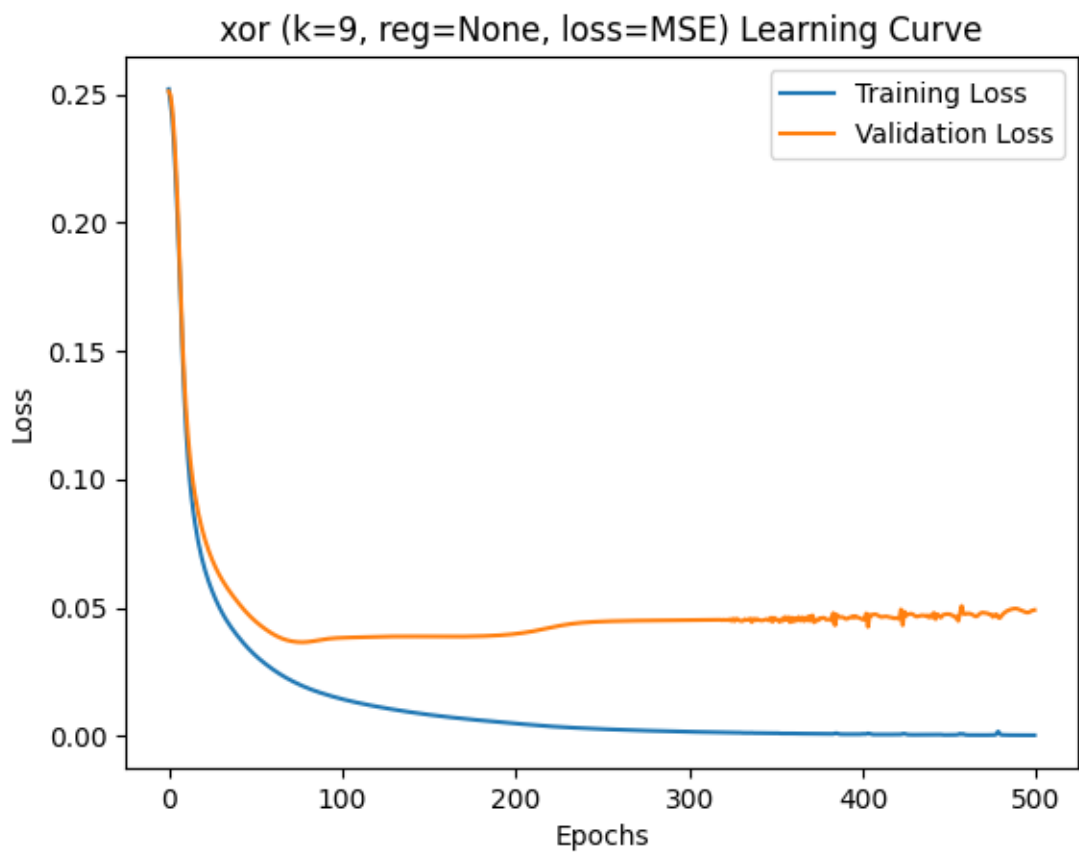
Validation Accuracy: 0.98

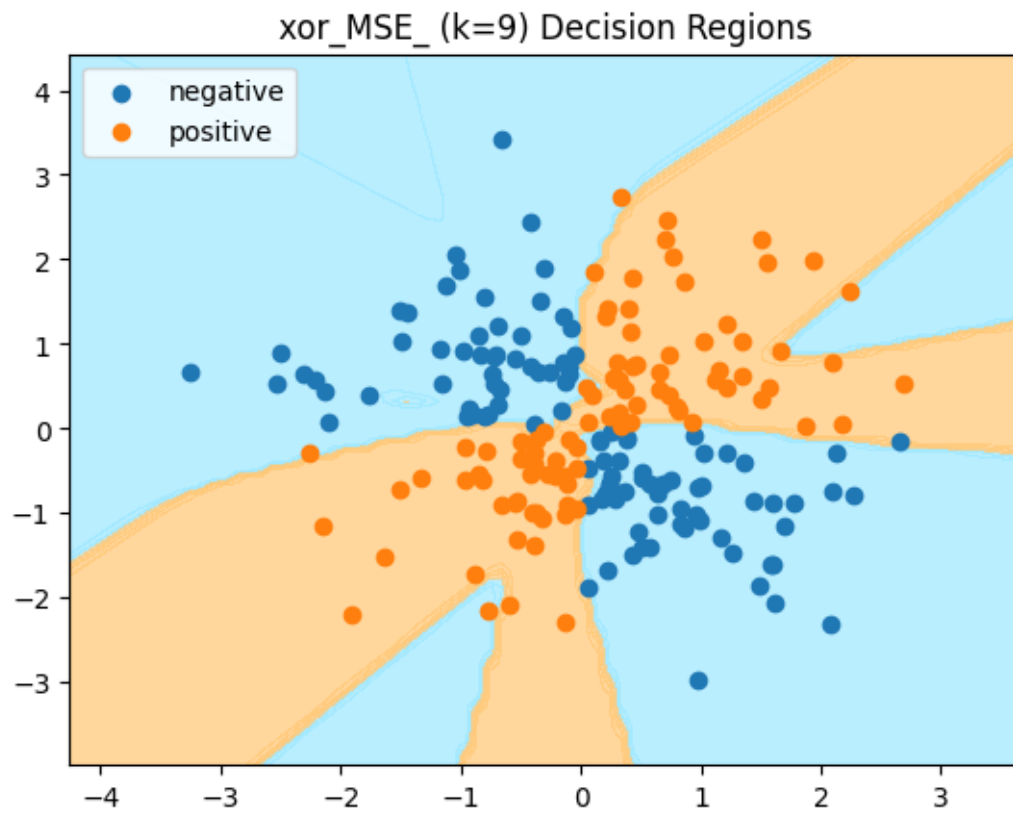
Test Accuracy: 0.91

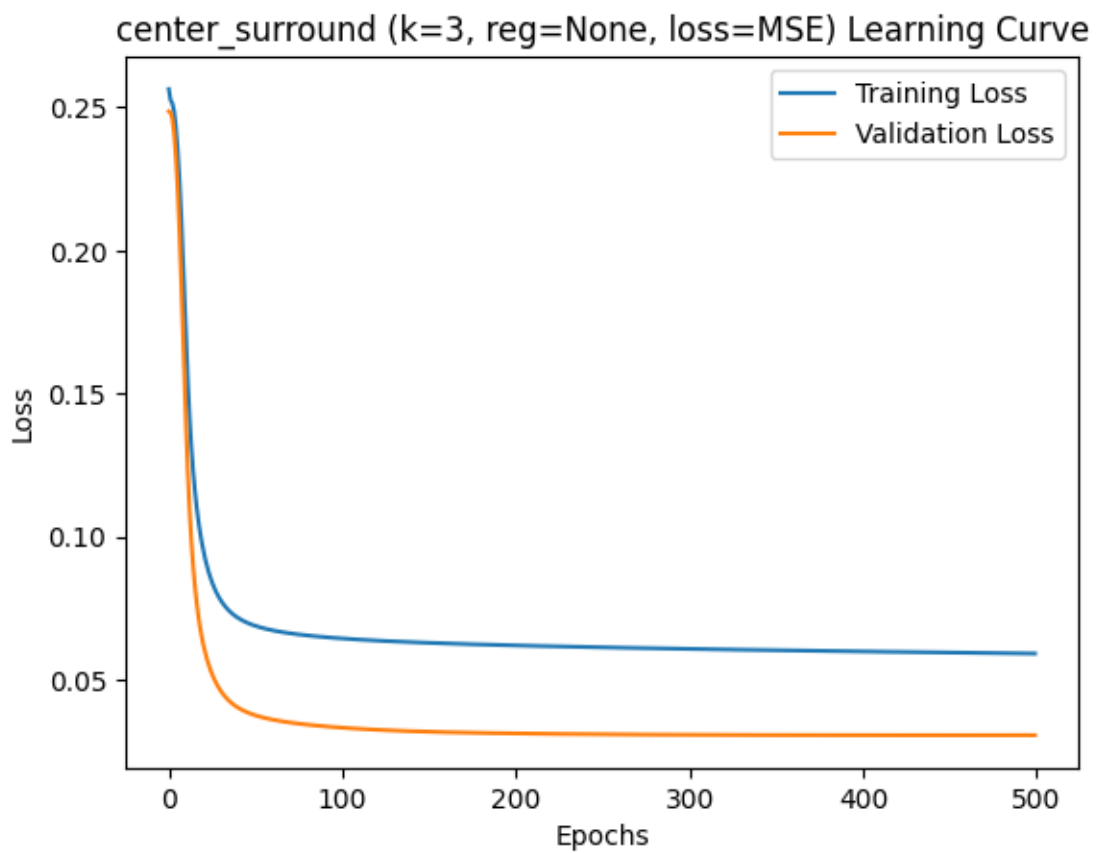
=====

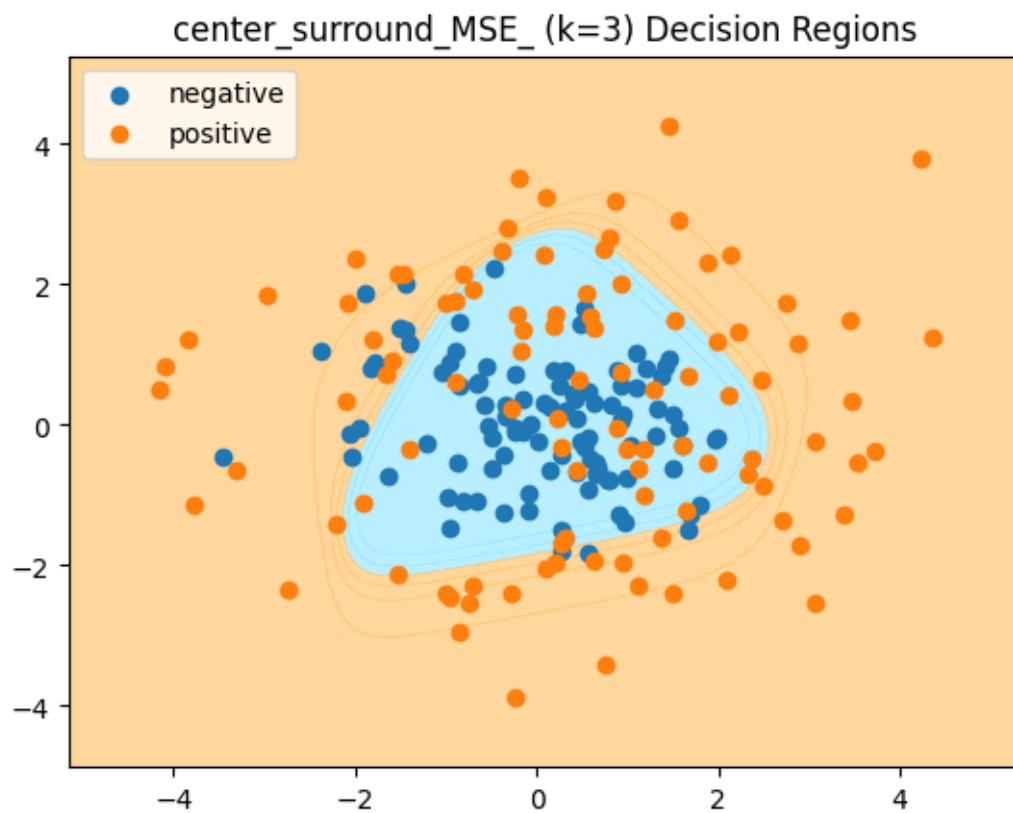
Drawing Decision Region for two_gaussians_MSE_orthogonal

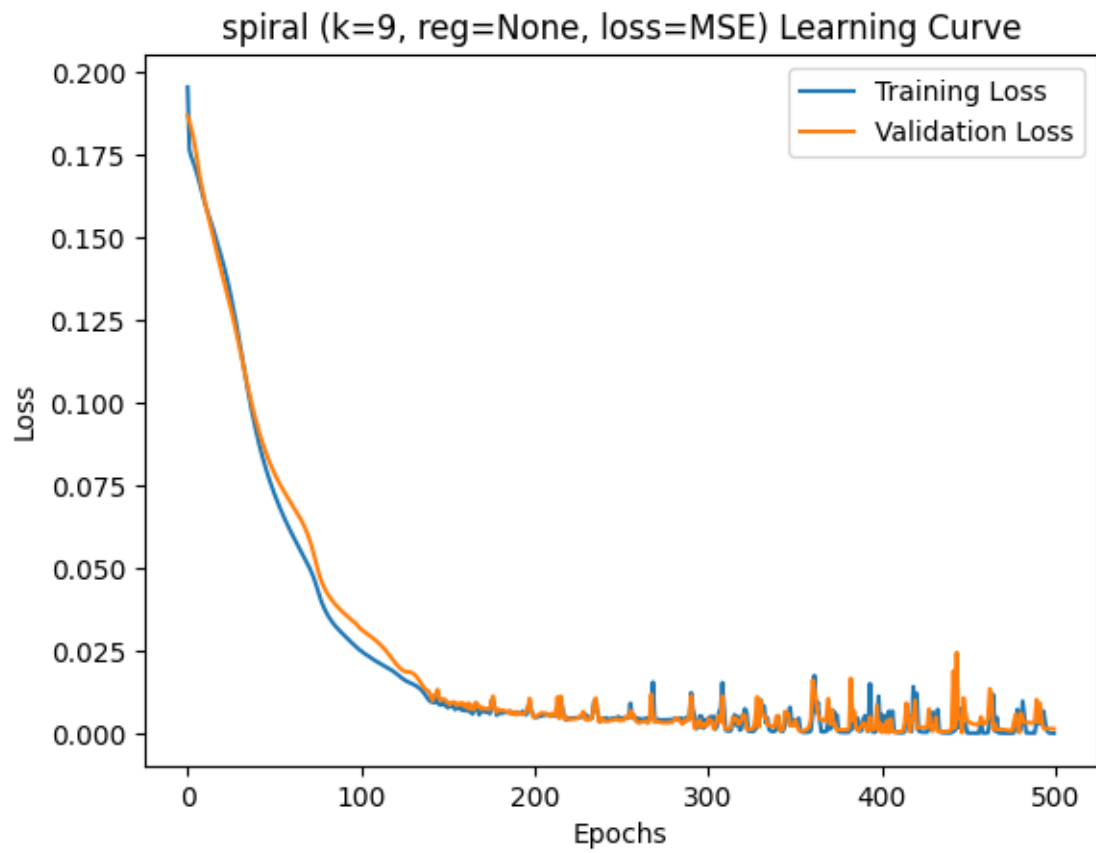
===== Finished training and evaluating models =====

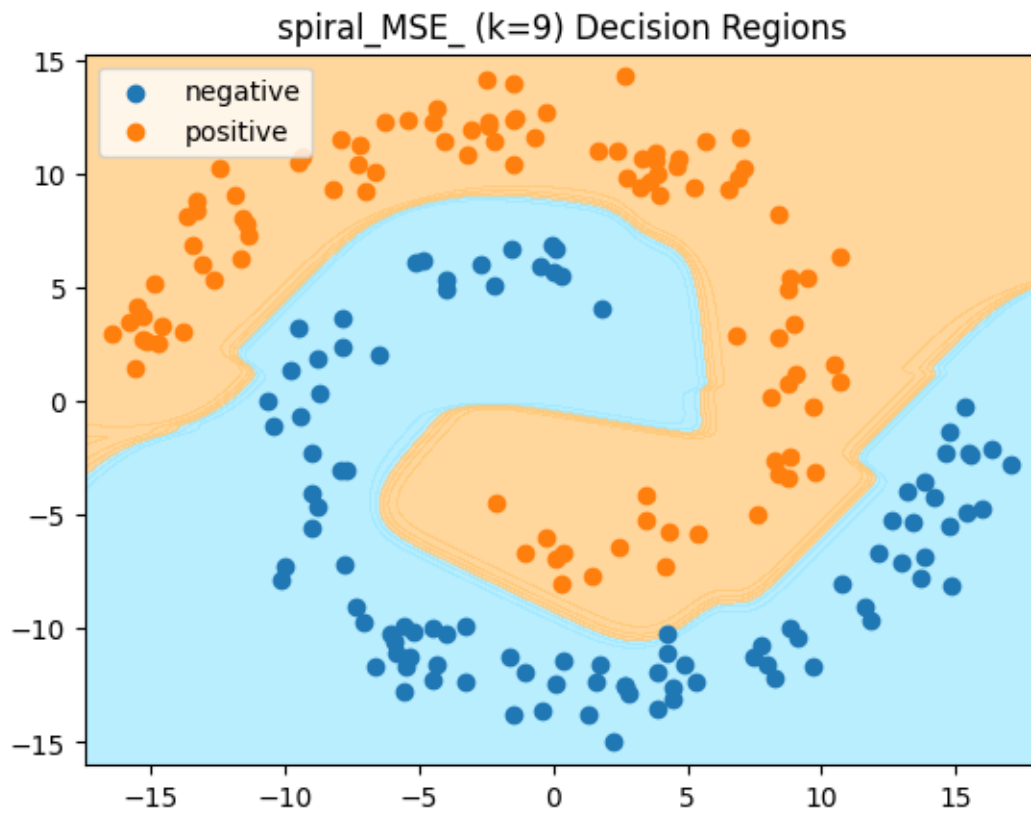


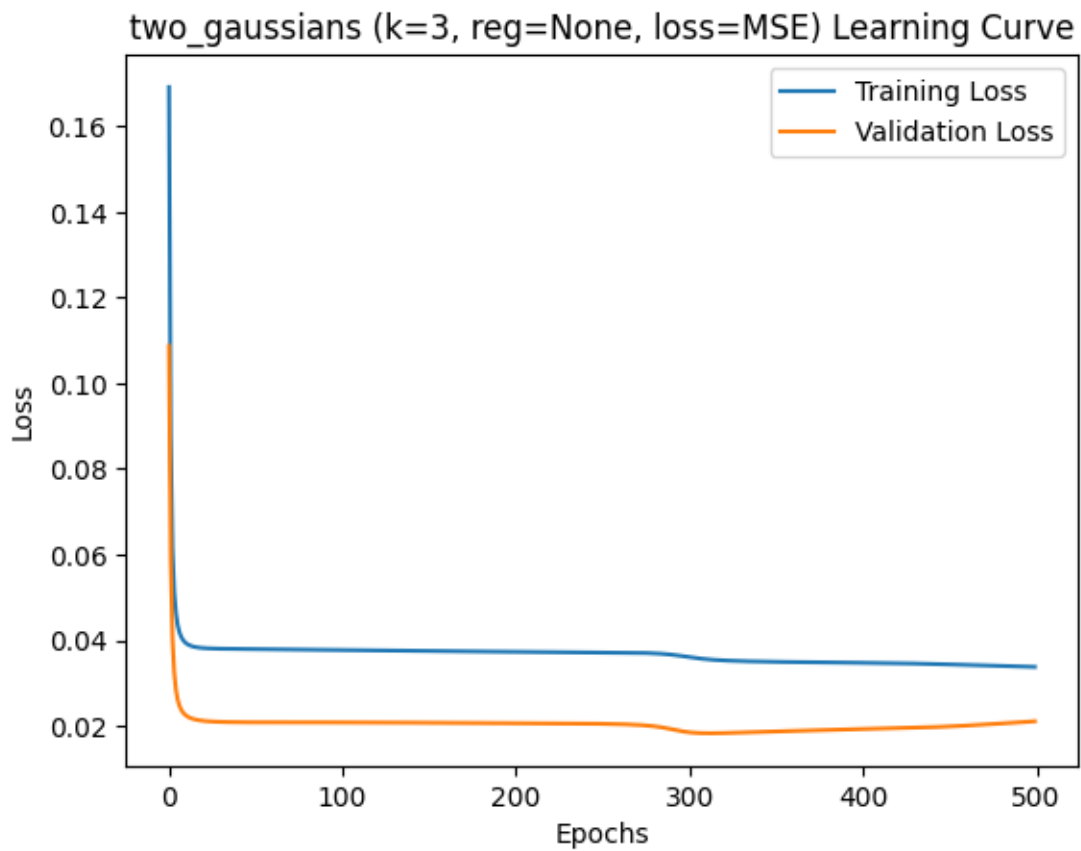


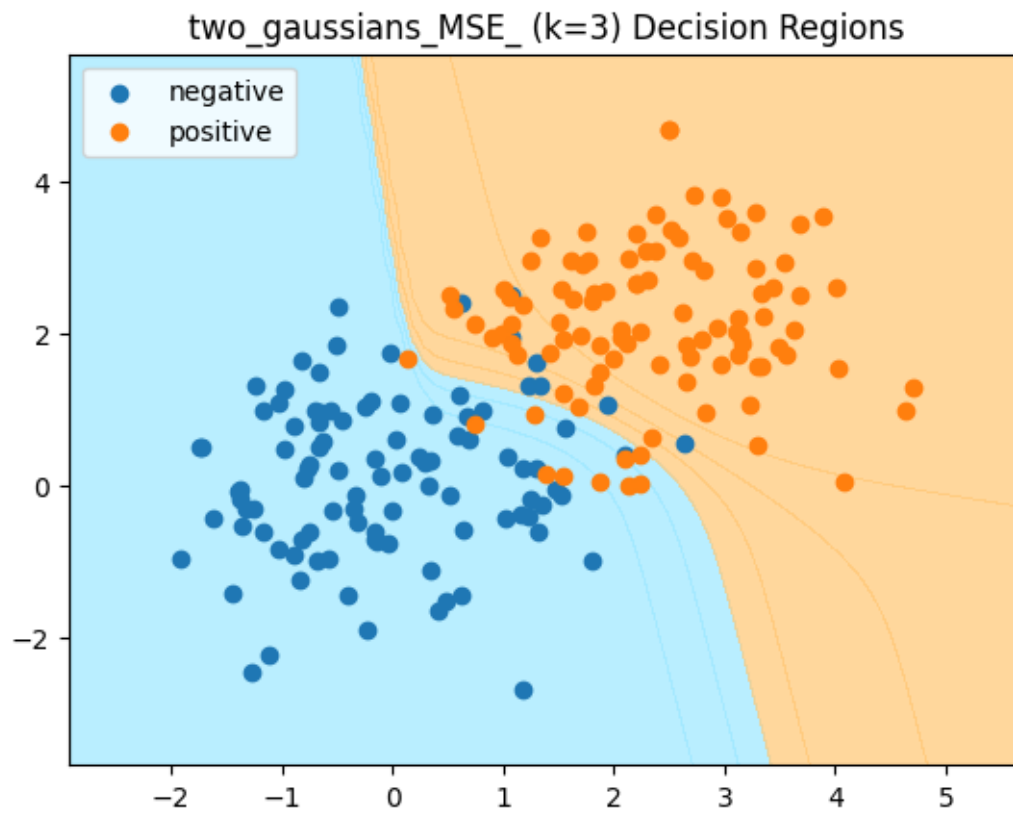


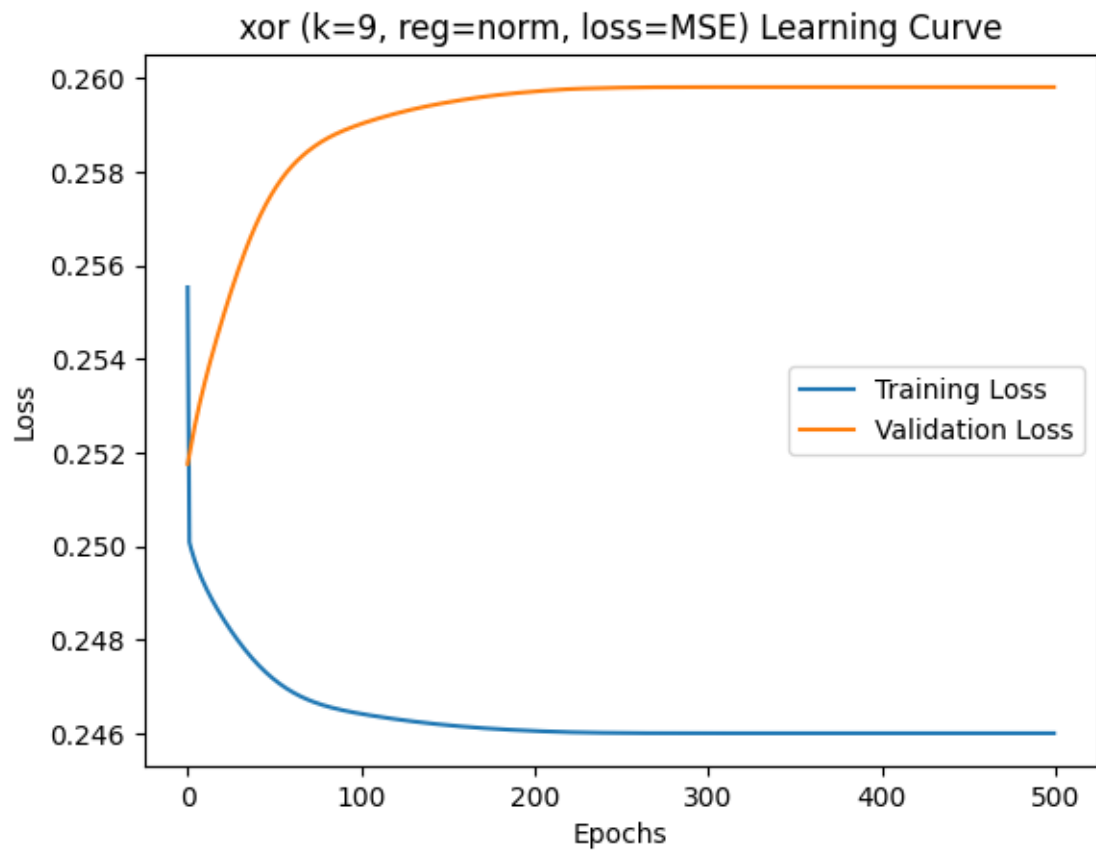


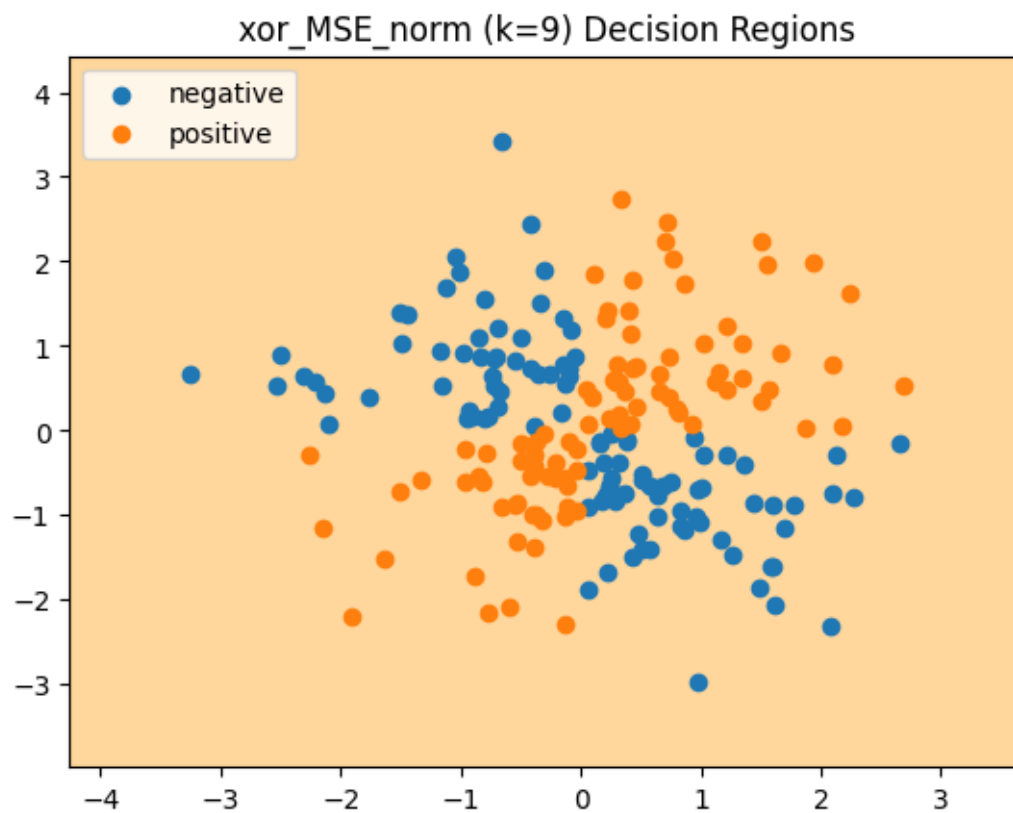


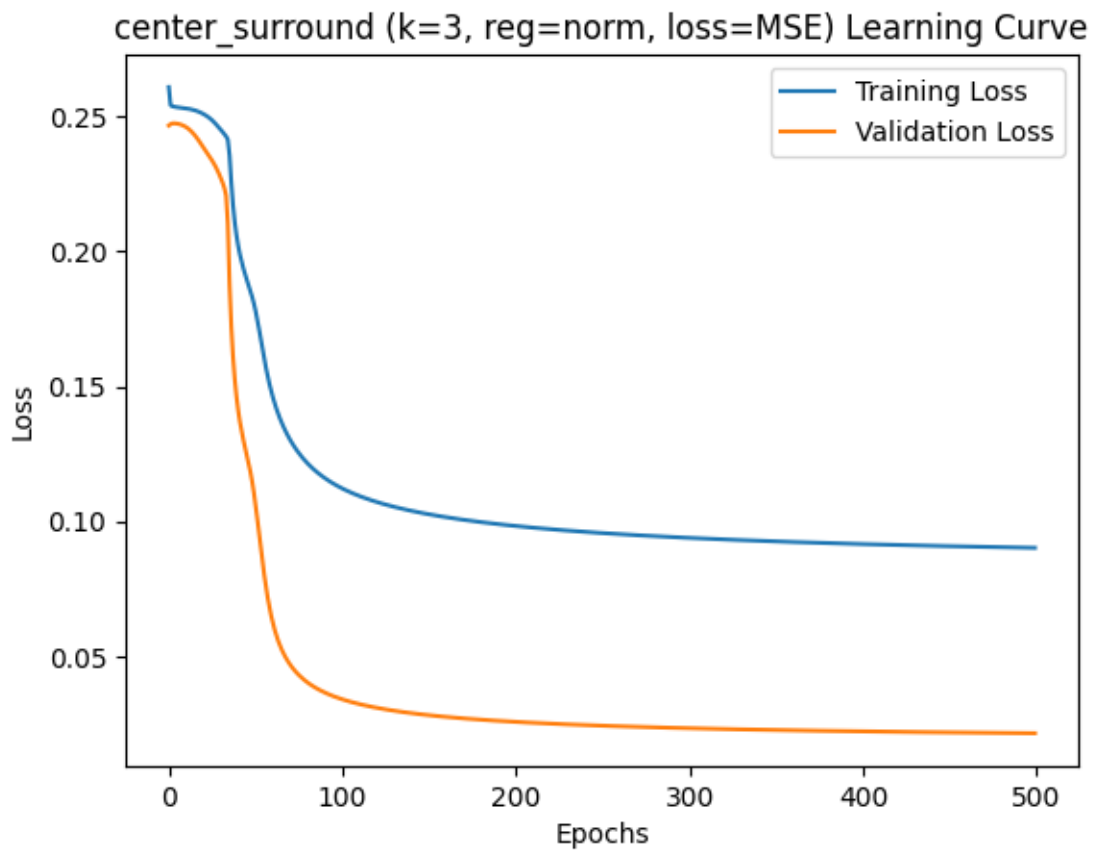


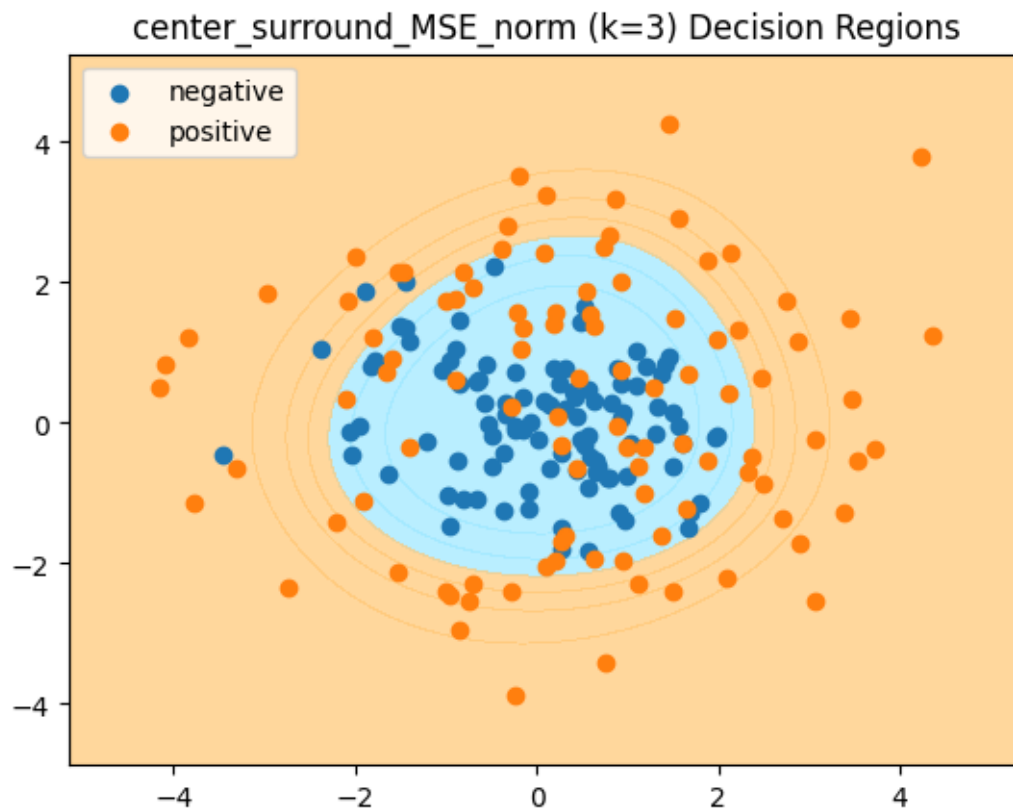


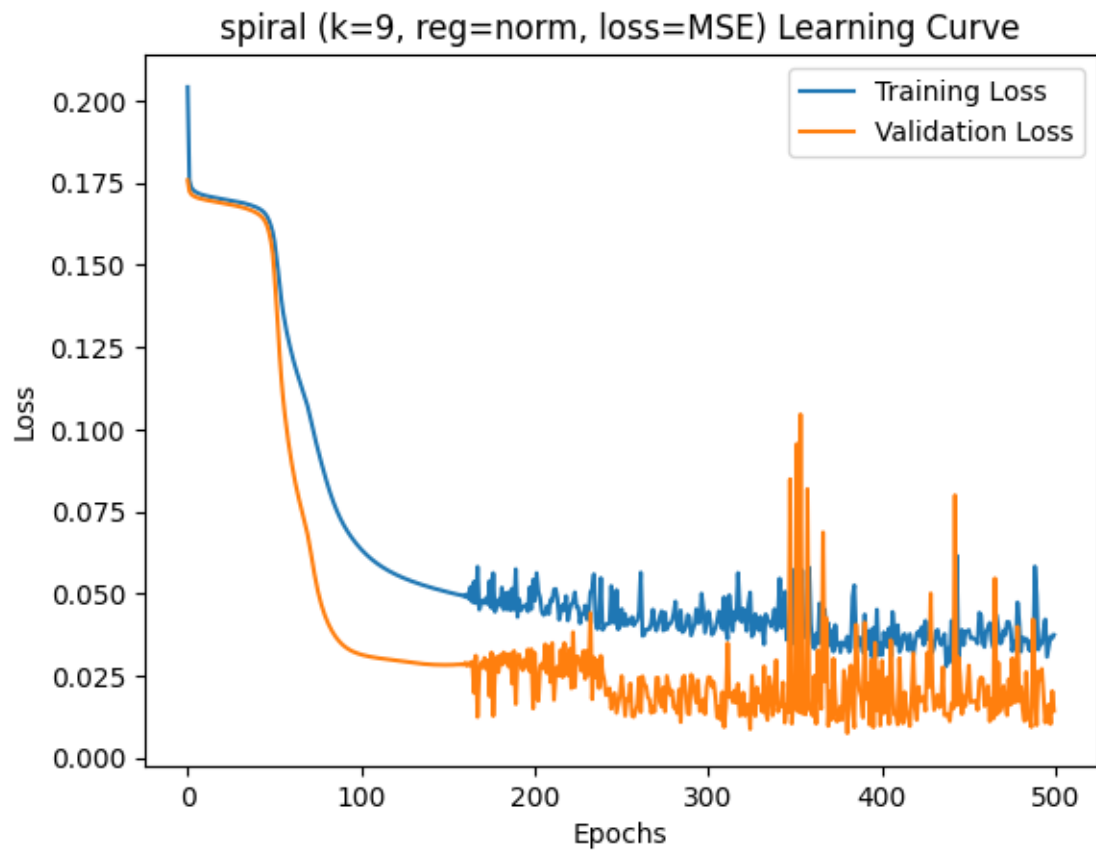


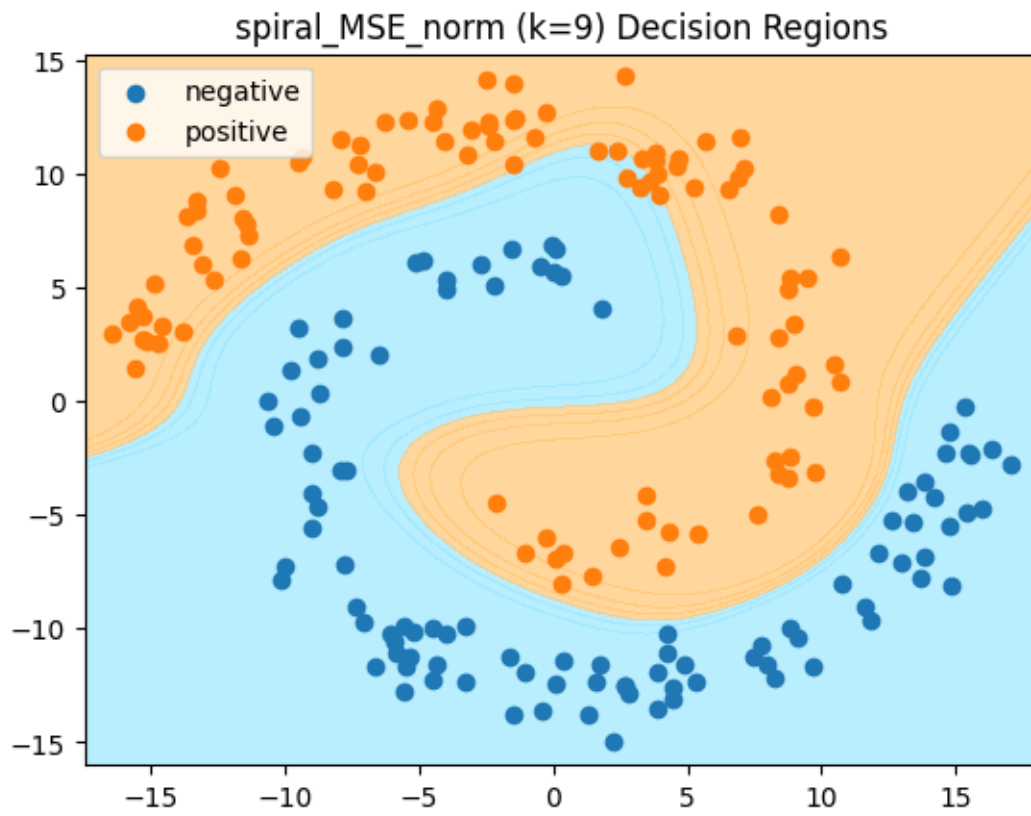


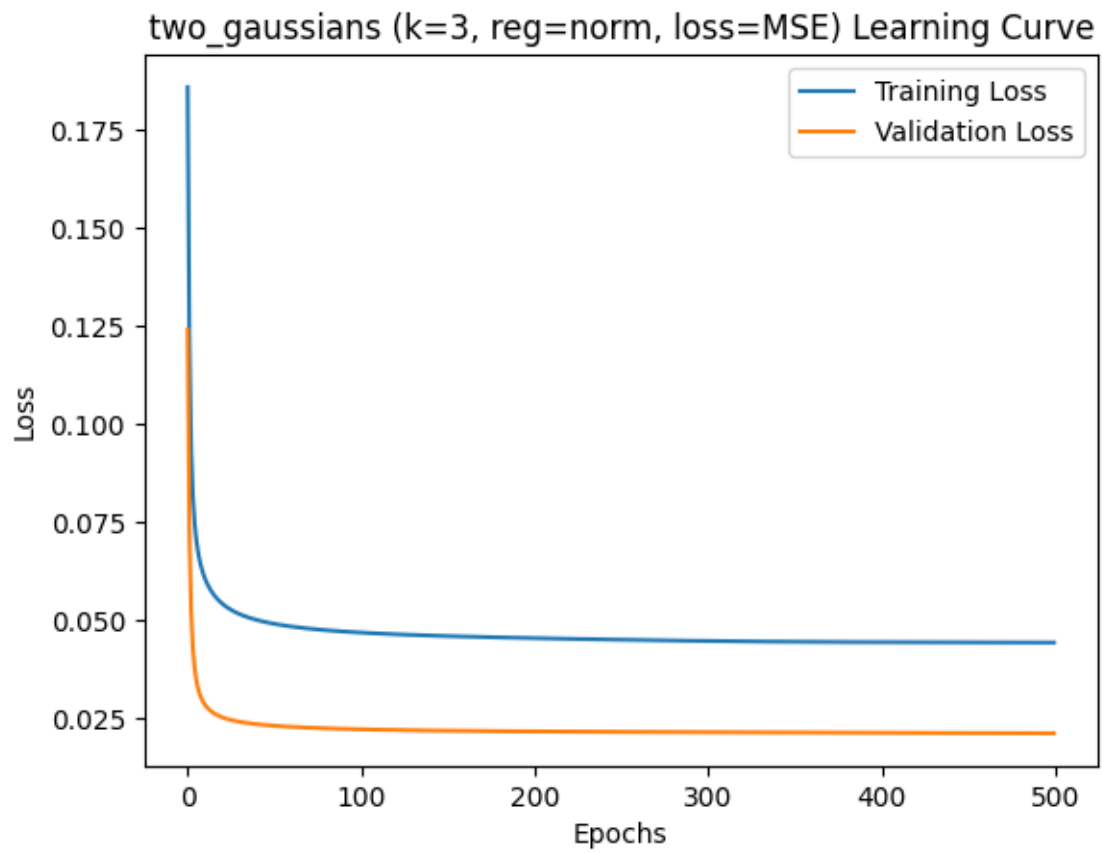


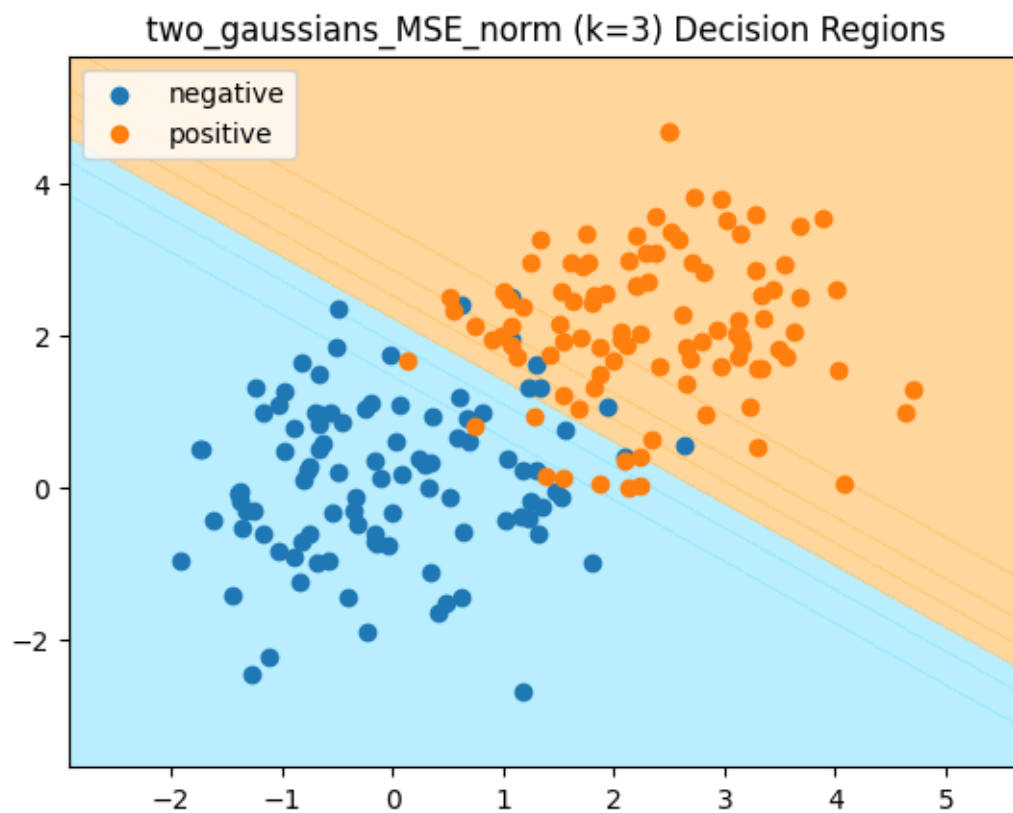


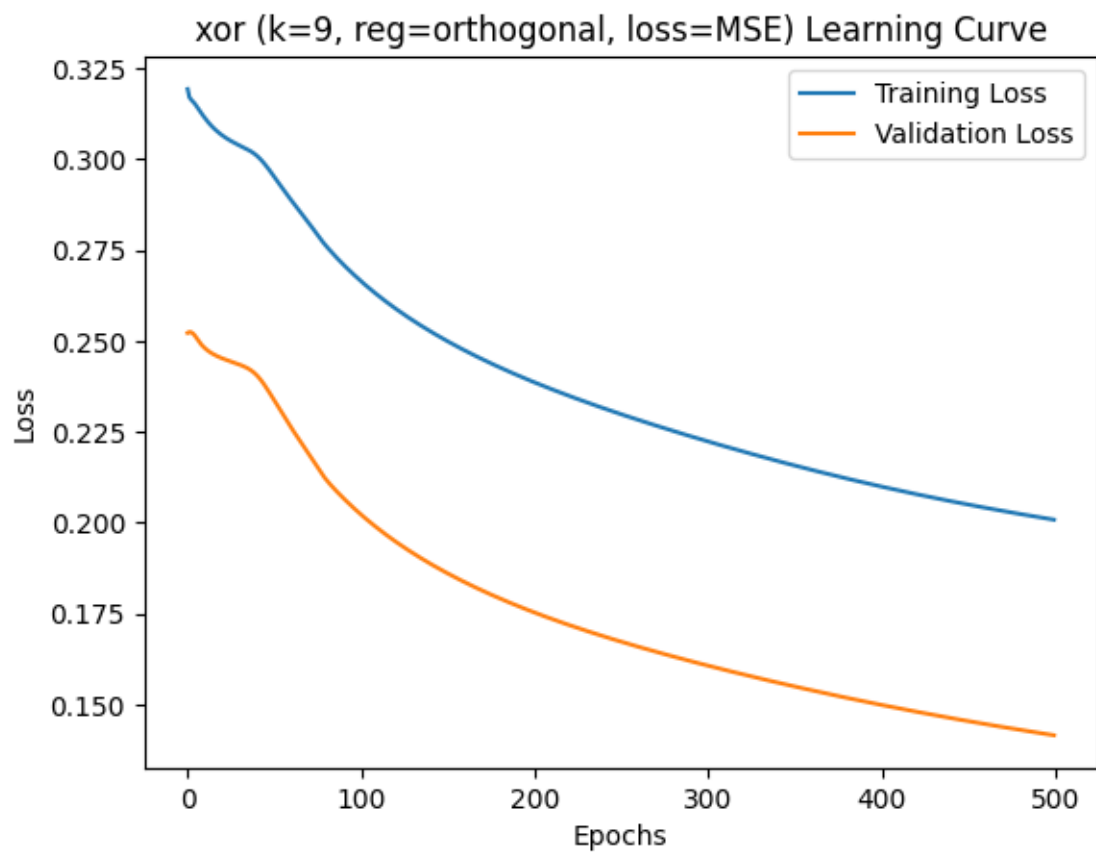


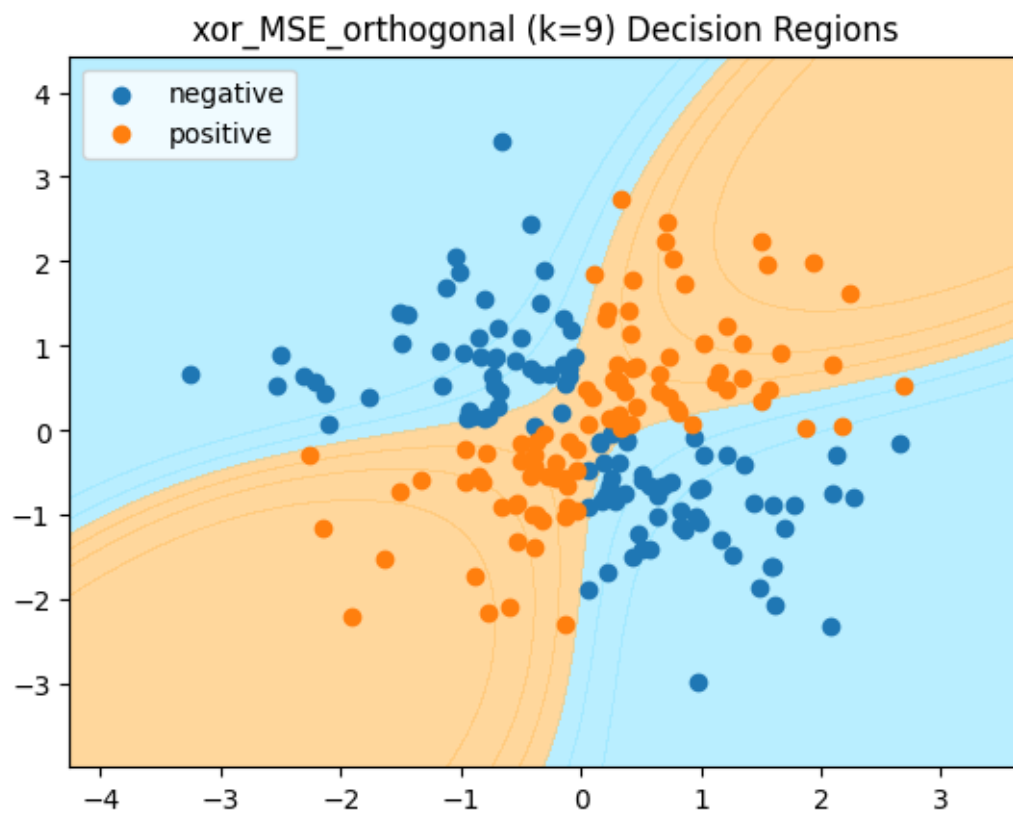


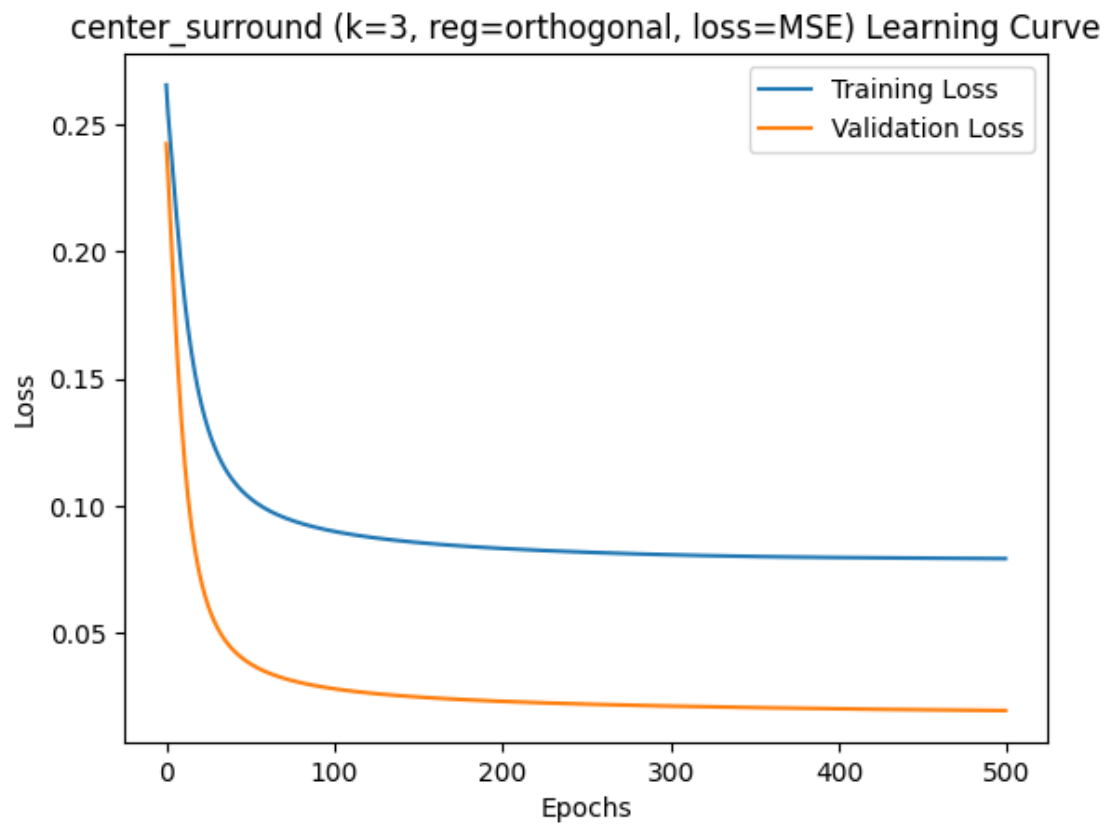


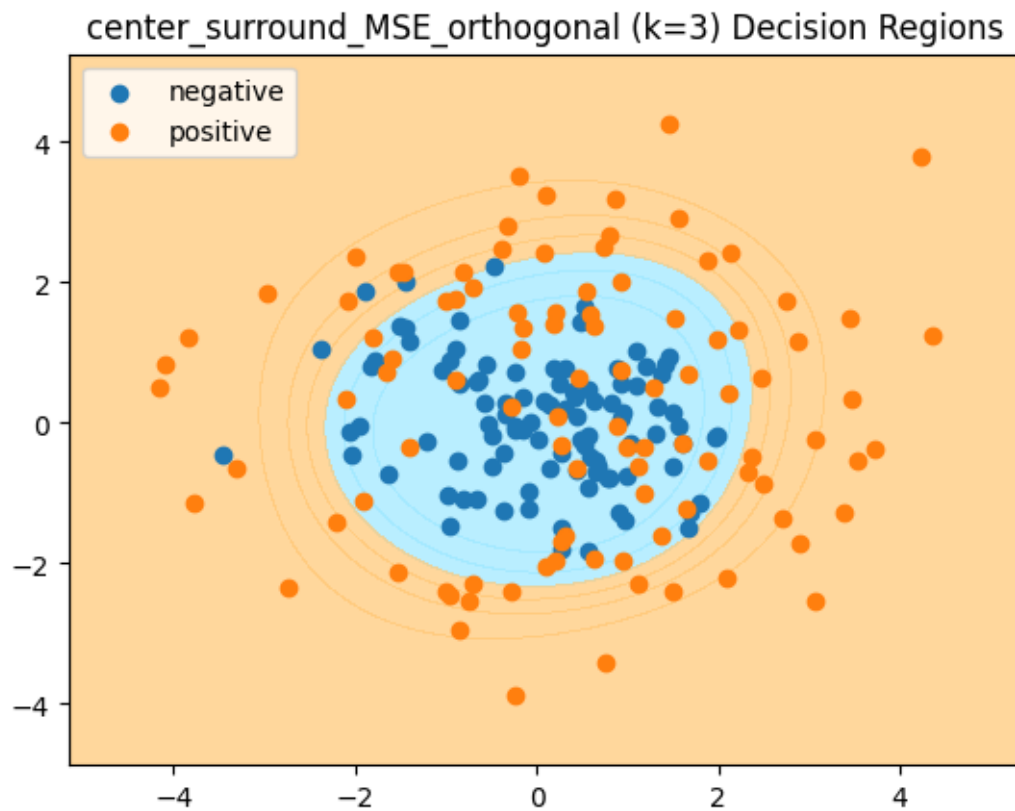


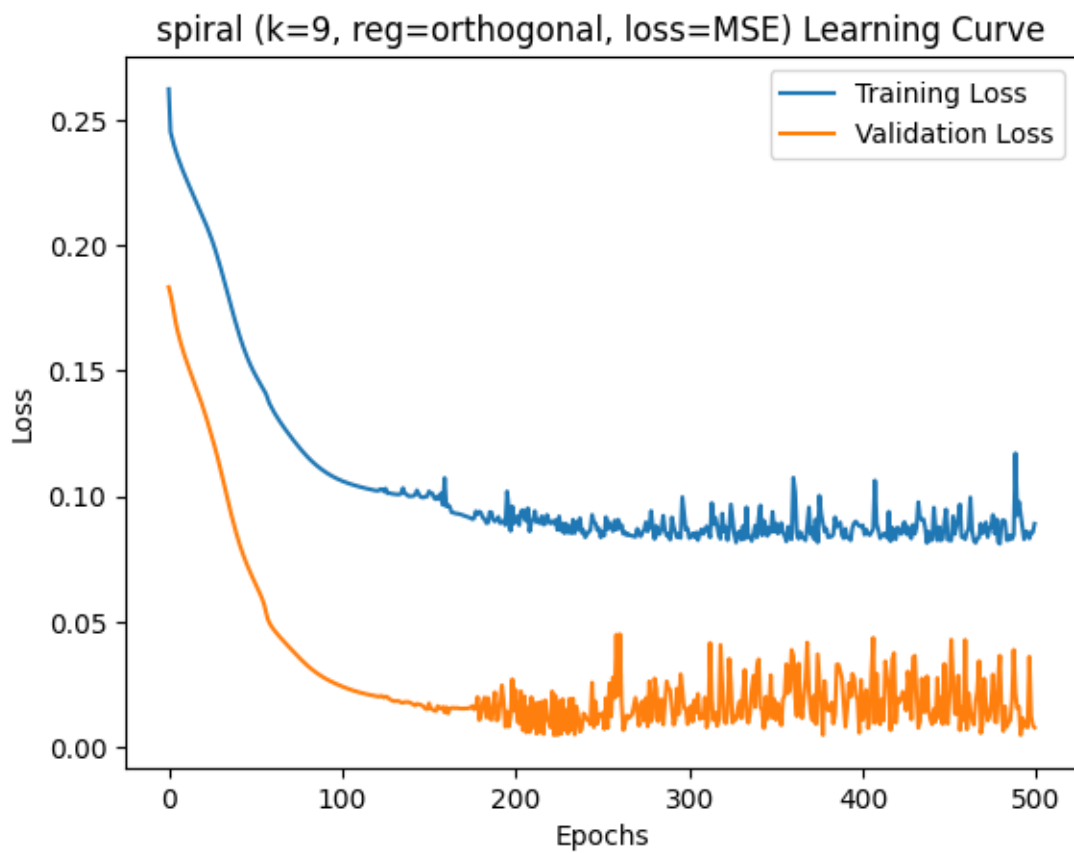


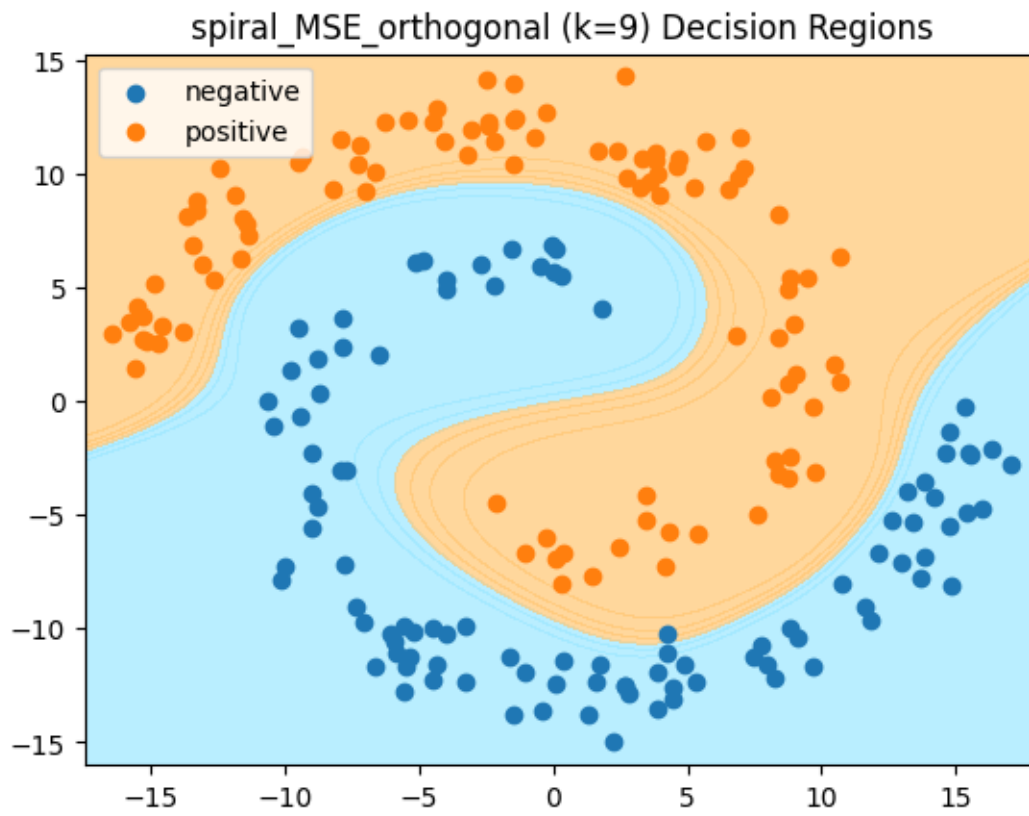


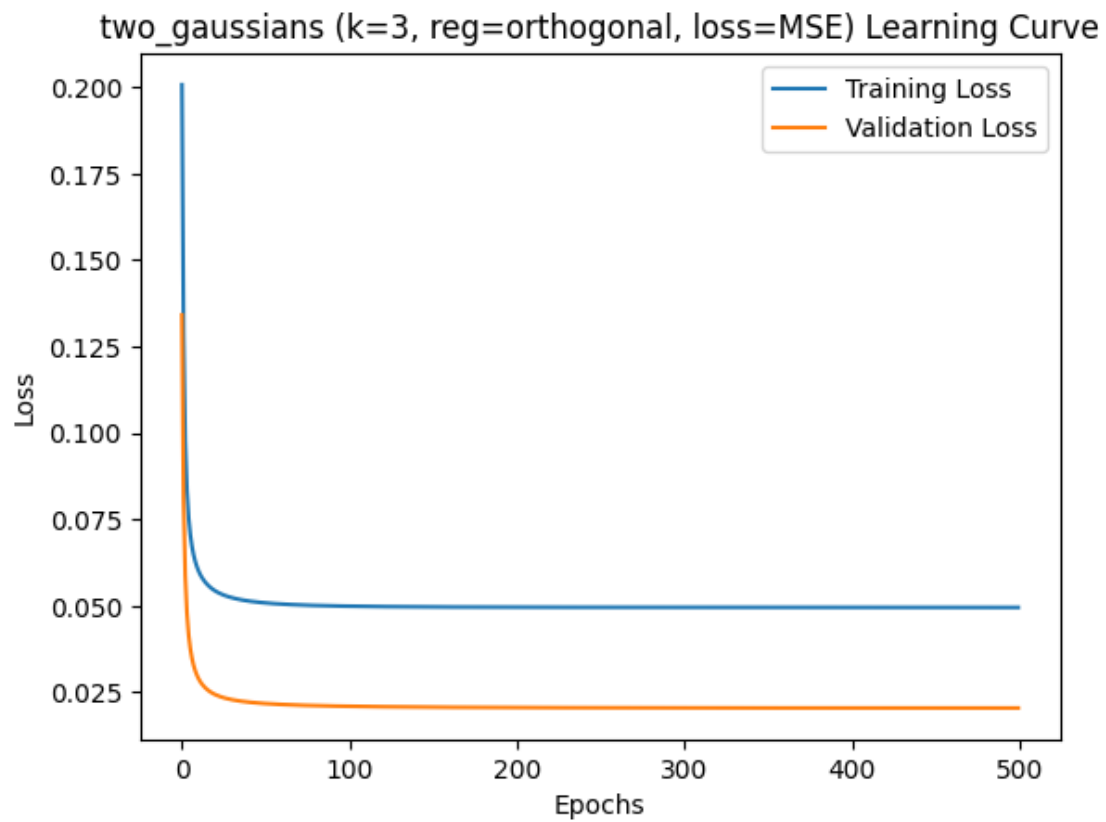


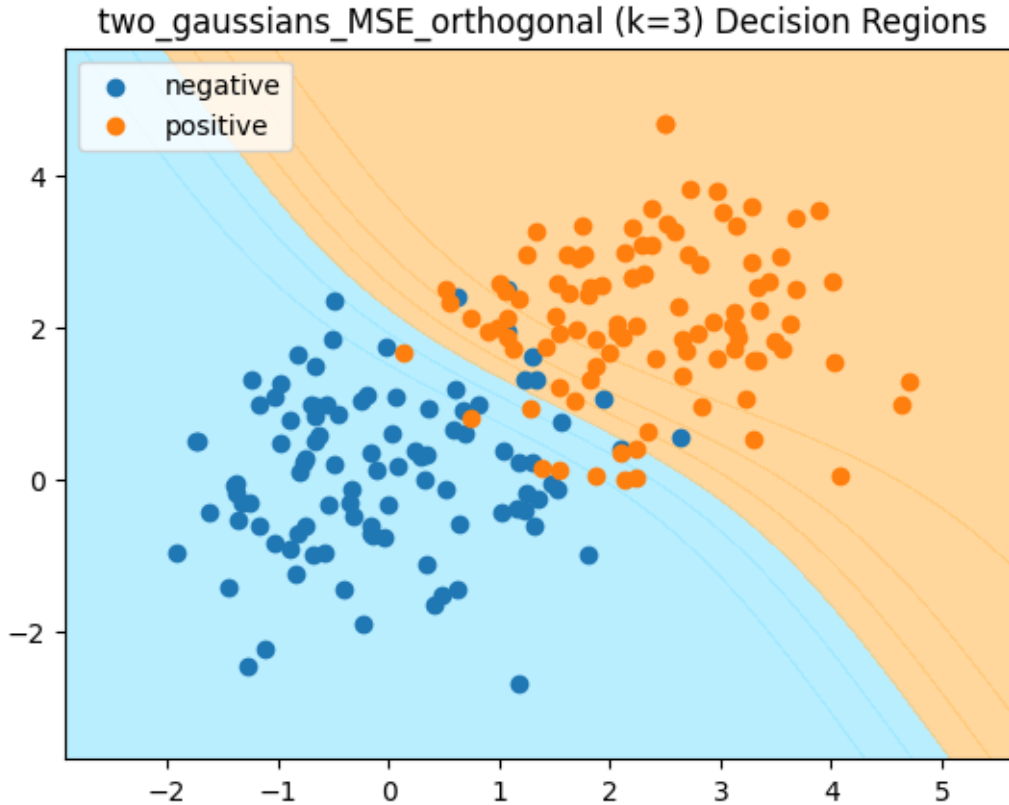












6 Design Choices

6.0.1 Design and Impact on Performance

We experimented with varying hidden layer sizes, datasets and learning rates to understand model complexity and convergence speed. For loss functions, we used Mean Squared Error (MSE) and Cross-Entropy Loss (MCE) to address regression and classification tasks. And for regularization techniques, we used L2 norm-based and orthogonal, to prevent overfitting.

We used a grid search to try out all combinations of regularizers, loss functions, hidden layer sizes and validation datasets, and logged the hyper-parameters and accuracies. And used it to find the optimal hyperparameter values for each case. These datasets were not complex, so one hidden layer introduced enough complexity for the model to learn.

By using our search, we narrowed down the hyperparameters that were best suited for each dataset. This increased performance across the board, yielding high accuracies and quick training times (also due to the small dataset).

6.0.2 Observation:

- For xor dataset, decision regions result is pretty accurate for orthogonal » none » norm regularizer.

- For spiral dataset, decision regions formed is almost same for all the regularisers. The learning curve for this dataset is pretty unstable for all reg options.
- For two__gaussian dataset (k=3), not using it is slightly better than other two.
- For centre__surround dataset (k=3), decision regions formed is almost same for all the regularisers. The learning curve observed for all is pretty stable, plots suggest fastest in case of orthogonal.

We observed that for every dataset, all regulariser got the best result with the same hyperparameter(no. of hidden layer) value. And we can clearly observe that the training set's losses in the case of every dataset's regularized result is less than not regularized one, while having the reverse pattern for validation losses. As we would have expected in theory as well. Thus, we can conclude, that regularizers were able to generalise the model, leading to better fitted for an unseen dataset.