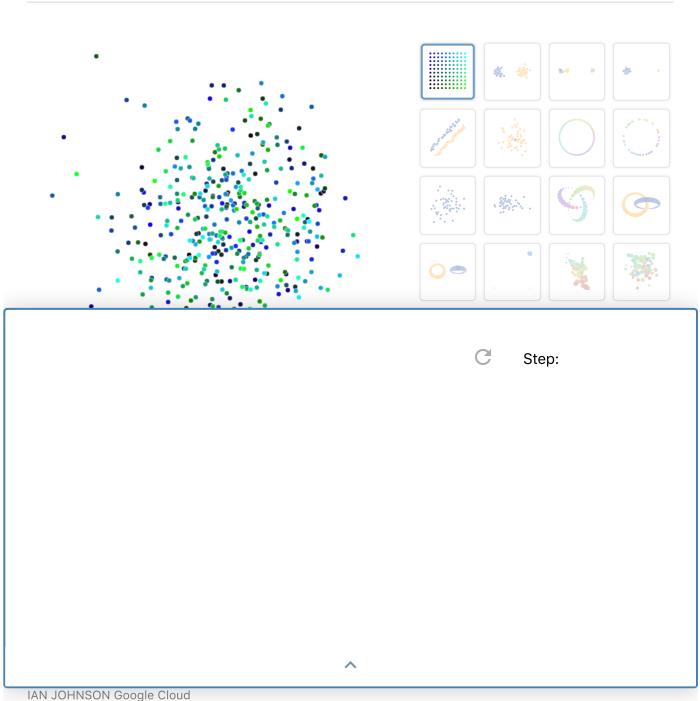
# How to Use t-SNE Effectively

Although extremely useful for visualizing high-dimensional data, t-SNE plots can sometimes be mysterious or misleading. By exploring how it behaves in simple cases, we can learn to use it more effectively.



Oct. 13 2016

Citation: Wattenberg, et al., 2016

A popular method for exploring high-dimensional data is something called t-SNE, introduced by van der Maaten and Hinton in 2008 [1]. The technique has become widespread in the field of machine learning, since it has an almost magical ability to create compelling two-dimensonal "maps" from data with hundreds or even thousands of dimensions. Although impressive, these images can be tempting to misread. The purpose of this note is to prevent some common misreadings.

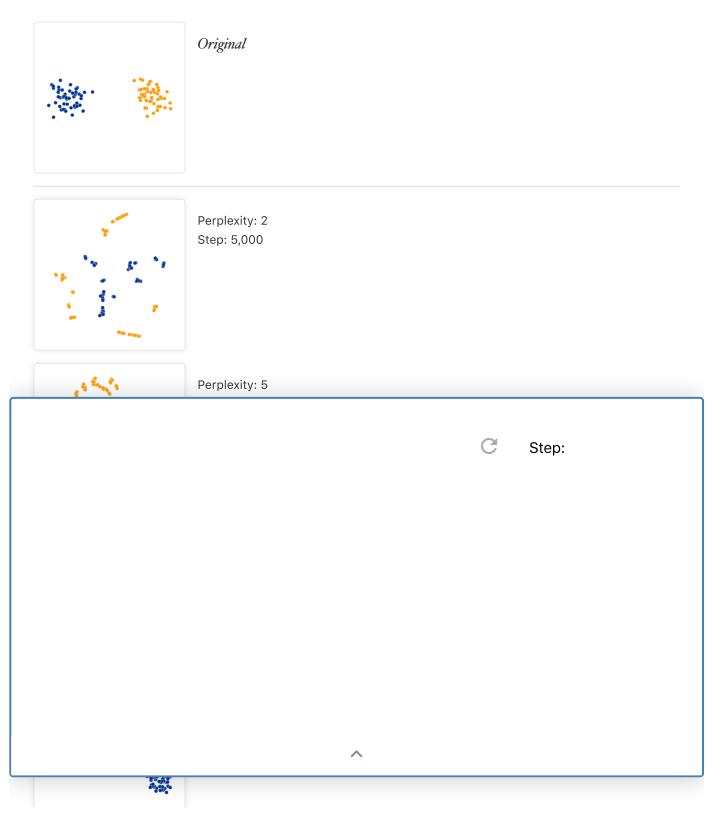
We'll walk through a series of simple examples to illustrate what t-SNE diagrams can and cannot show. The t-SNE technique really is useful—but only if you know how to interpret it.

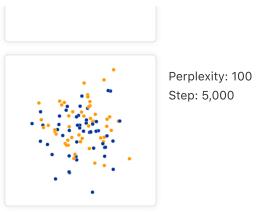
Before diving in: if you haven't encountered t-SNE before, here's what you need to know about the math behind it. The goal is to take a set of points in a high-dimensional space and find a faithful representation of those points in a lower-dimensional space, typically the 2D plane. The algorithm is non-linear and adapts to the underlying data, performing different transformations on different regions. Those differences can be a major source of confusion.

| A second feature of t-SNE is a tuneable parameter, "perplexity," which says (loosely) |  |  |
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| how to balance attention between local and global aspects of your data. The parameter |  |  |
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## 1. Those hyperparameters really matter

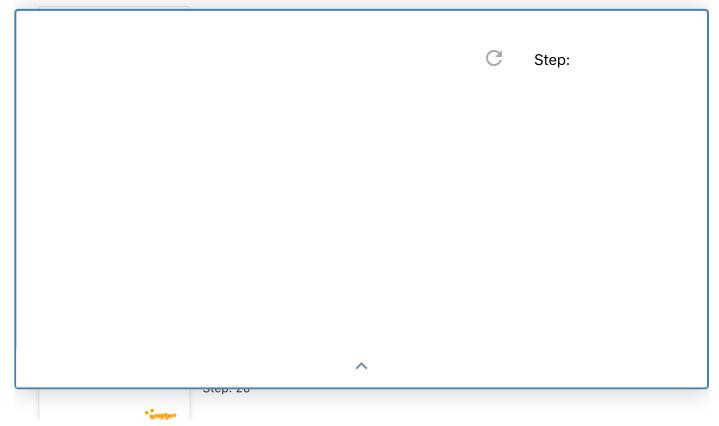
Let's start with the "hello world" of t-SNE: a data set of two widely separated clusters. To make things as simple as possible, we'll consider clusters in a 2D plane, as shown in the lefthand diagram. (For clarity, the two clusters are color coded.) The diagrams at right show t-SNE plots for five different perplexity values.

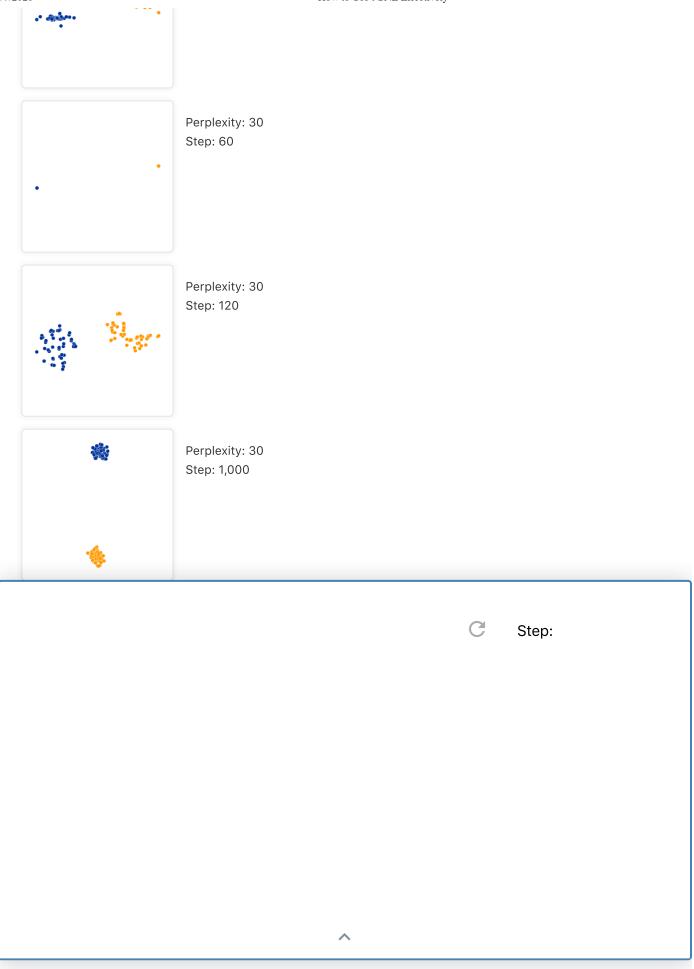




With perplexity values in the range (5 - 50) suggested by van der Maaten & Hinton, the diagrams do show these clusters, although with very different shapes. Outside that range, things get a little weird. With perplexity 2, local variations dominate. The image for perplexity 100, with merged clusters, illustrates a pitfall: for the algorithm to operate properly, the perplexity really should be smaller than the number of points. Implementations can give unexpected behavior otherwise.

Each of the plots above was made with 5,000 iterations with a learning rate (often called "epsilon") of 10, and had reached a point of stability by step 5,000. How much of a difference do those values make? In our experience, the most important thing is to iterate until reaching a stable configuration.

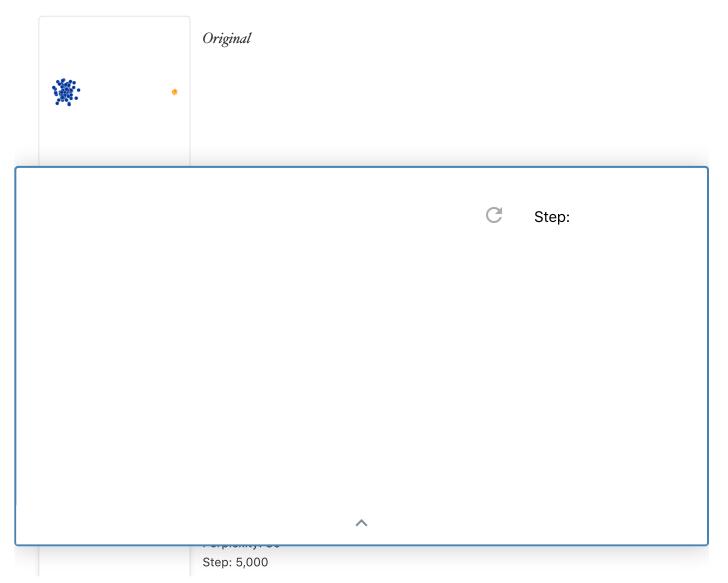


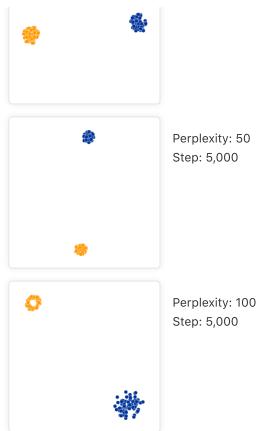


From now on, unless otherwise stated, we'll show results from 5,000 iterations. That's generally enough for convergence in the (relatively small) examples in this essay. We'll keep showing a range of perplexities, however, since that seems to make a big difference in every case.

### 2. Cluster sizes in a t-SNE plot mean nothing

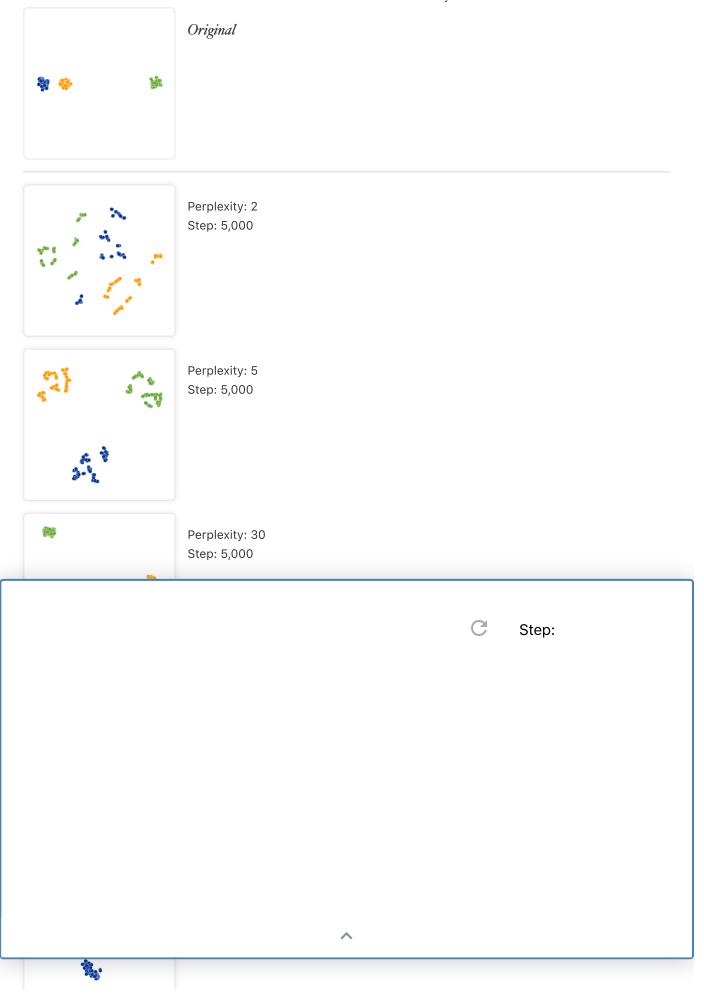
So far, so good. But what if the two clusters have different standard deviations, and so different sizes? (By size we mean bounding box measurements, not number of points.) Below are t-SNE plots for a mixture of Gaussians in plane, where one is 10 times as dispersed as the other.





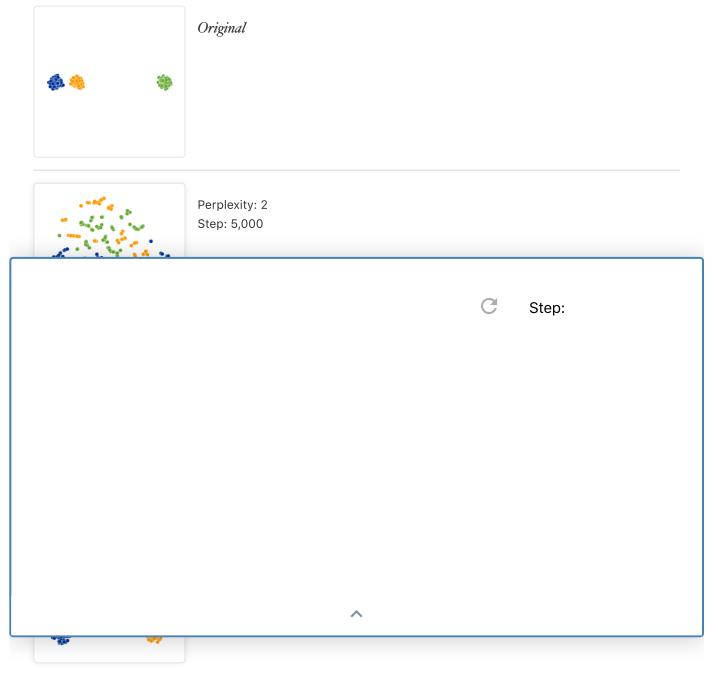
Surprisingly, the two clusters look about same size in the t-SNE plots. What's going on? The t-SNE algorithm adapts its notion of "distance" to regional density variations in the data set. As a result, it naturally expands dense clusters, and contracts sparse ones, evening out cluster sizes. To be clear, this is a different effect than the run-of-

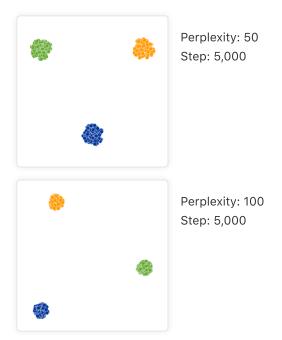
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At perplexity 50, the diagram gives a good sense of the global geometry. For lower perplexity values the clusters look equidistant. When the perplexity is 100, we see the global geometry fine, but one of the cluster appears, falsely, much smaller than the others. Since perplexity 50 gave us a good picture in this example, can we always set perplexity to 50 if we want to see global geometry?

Sadly, no. If we add more points to each cluster, the perplexity has to increase to compensate. Here are the t-SNE diagrams for three Gaussian clusters with 200 points each, instead of 50. Now none of the trial perplexity values gives a good result.

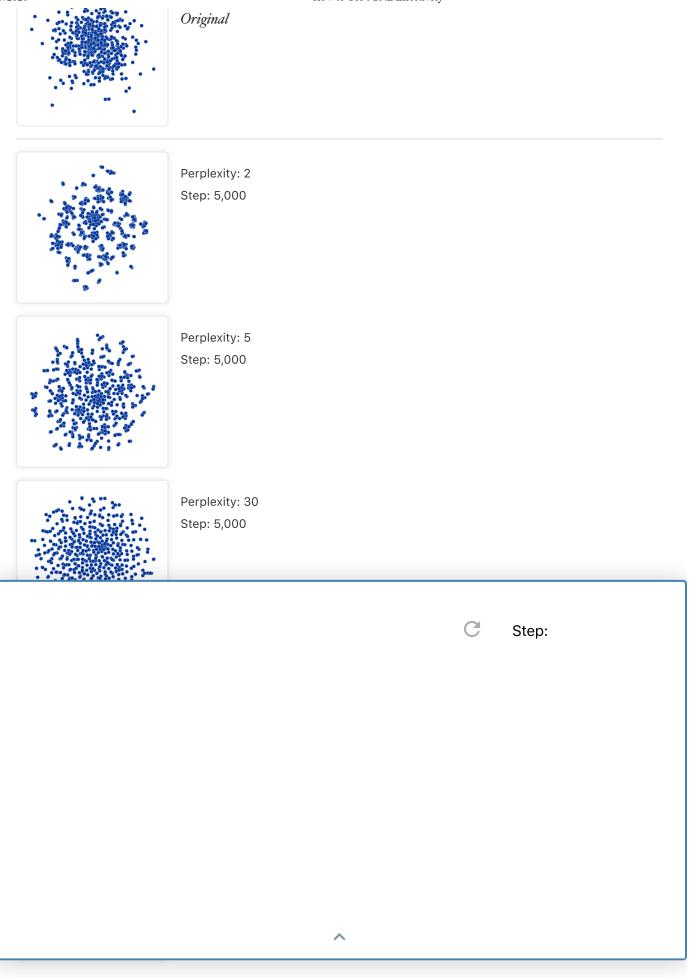




It's bad news that seeing global geometry requires fine-tuning perplexity. Real-world data would probably have multiple clusters with different numbers of elements. There may not be one perplexity value that will capture distances across all clusters—and sadly perplexity is a global parameter. Fixing this problem might be an interesting area for future research.

The basic message is that distances between well-separated clusters in a t-SNE plot





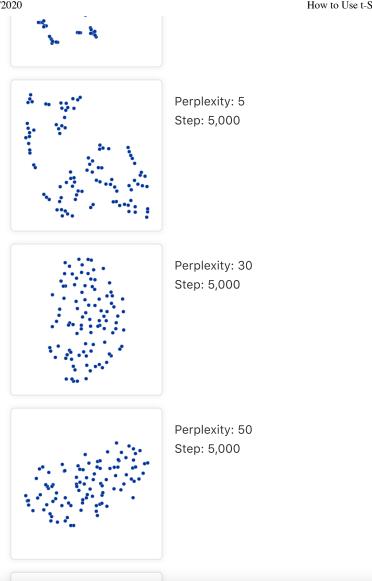
The plot with perplexity 2 seems to show dramatic clusters. If you were tuning perplexity to bring out structure in the data, you might think you'd hit the jackpot.

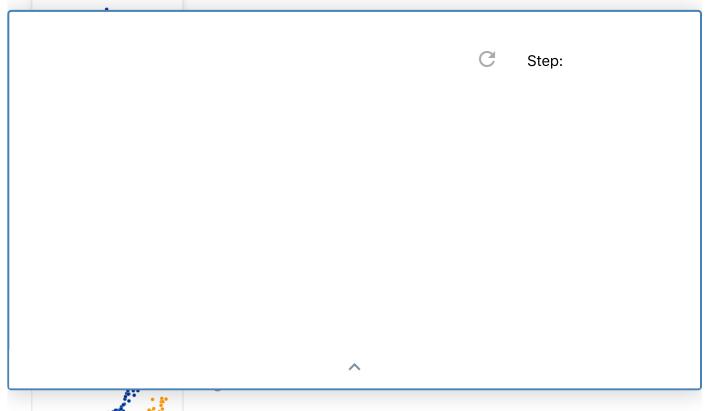
Of course, since we know the cloud of points was generated randomly, it has no statistically interesting clusters: those "clumps" aren't meaningful. If you look back at previous examples, low perplexity values often lead to this kind of distribution. Recognizing these clumps as random noise is an important part of reading t-SNE plots.

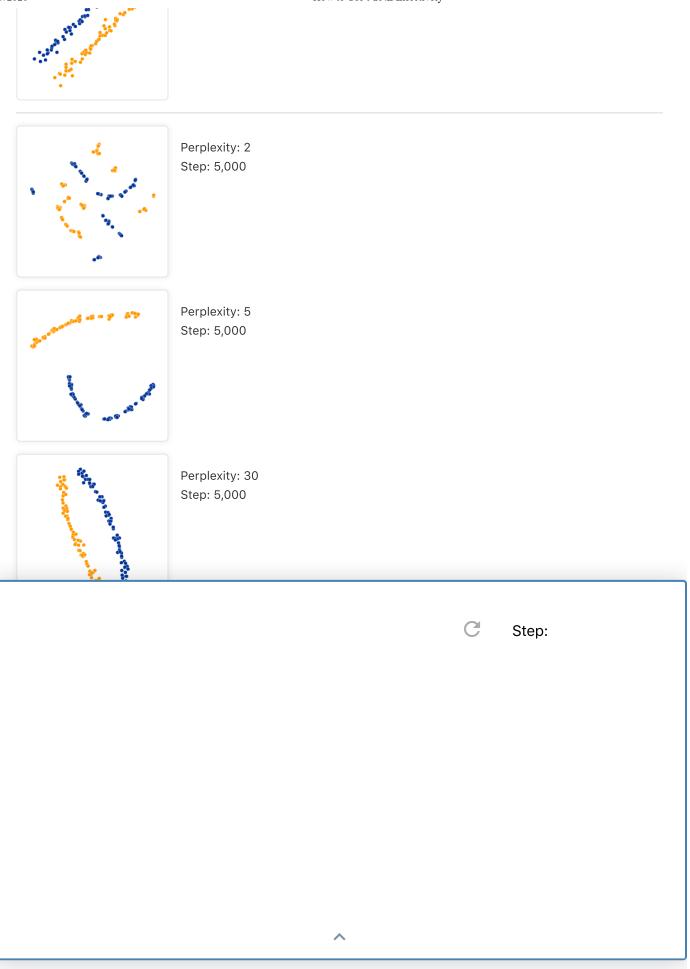
There's something else interesting, though, which may be a win for t-SNE. At first the perplexity 30 plot doesn't look like a Gaussian distribution at all: there's only a slight density difference across different regions of the cloud, and the points seem suspiciously evenly distributed. In fact, these features are saying useful things about high-dimensional normal distributions, which are very close to uniform distributions on a sphere: evenly distributed, with roughly equal spaces between points. Seen in this light, the t-SNE plot is more accurate than any linear projection could be.

### 5. You can see some shapes, sometimes

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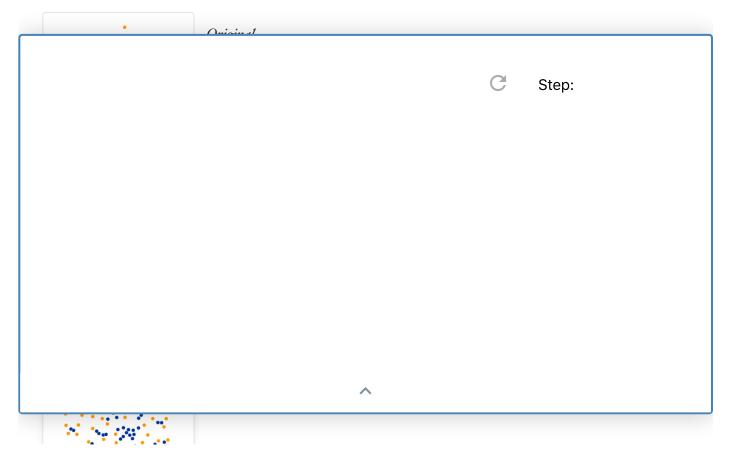


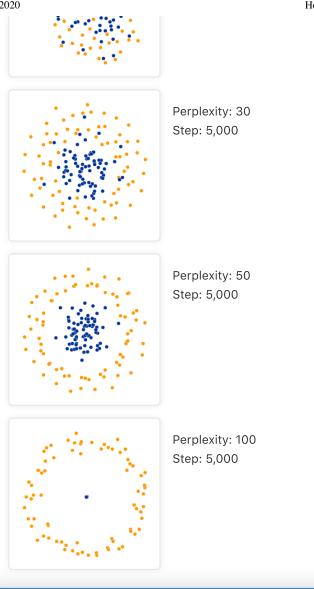
For a certain range of perplexity the long clusters look close to correct, which is reassuring.

Even in the best cases, though, there's a subtle distortion: the lines are slightly curved outwards in the t-SNE diagram. The reason is that, as usual, t-SNE tends to expand denser regions of data. Since the middles of the clusters have less empty space around them than the ends, the algorithm magnifies them.

### 6. For topology, you may need more than one plot

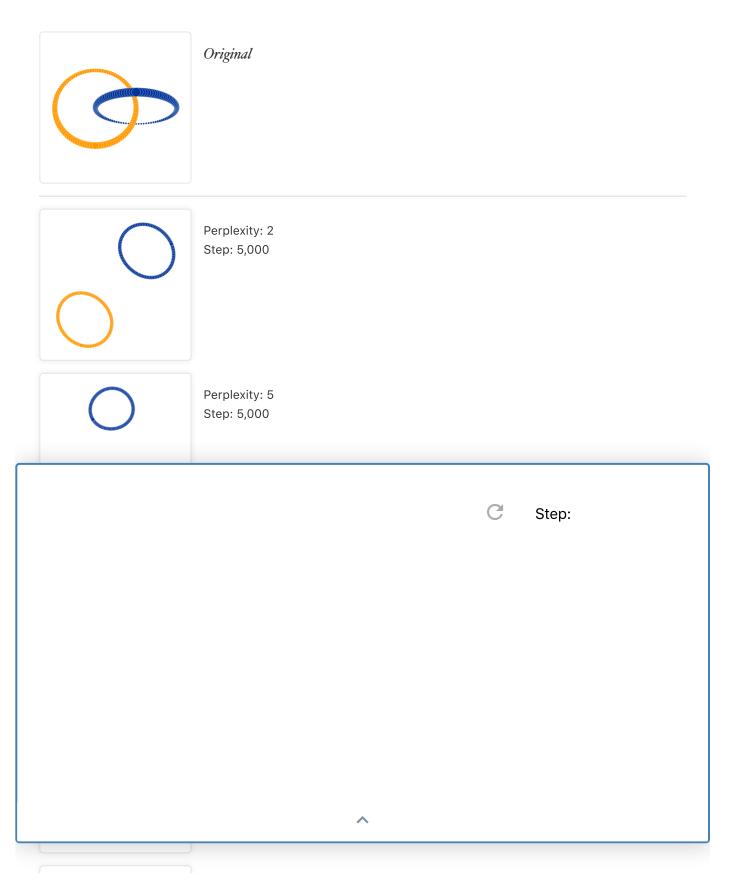
Sometimes you can read topological information off a t-SNE plot, but that typically requires views at multiple perplexities. One of the simplest topological properties is containment. The plots below show two groups of 75 points in 50 dimensional space. Both are sampled from symmetric Gaussian distributions centered at the origin, but one is 50 times more tightly dispersed than the other. The "small" distribution is in effect contained in the large one.







Consider a set of points that trace a link or a knot in three dimensions. Once again, looking at multiple perplexity values gives the most complete picture. Low perplexity values give two completely separate loops; high ones show a kind of global connectivity.





Perplexity: 100 Step: 5,000



Original

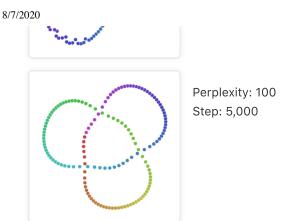


Perplexity: 2 Step: 5,000

Perplexity: 5

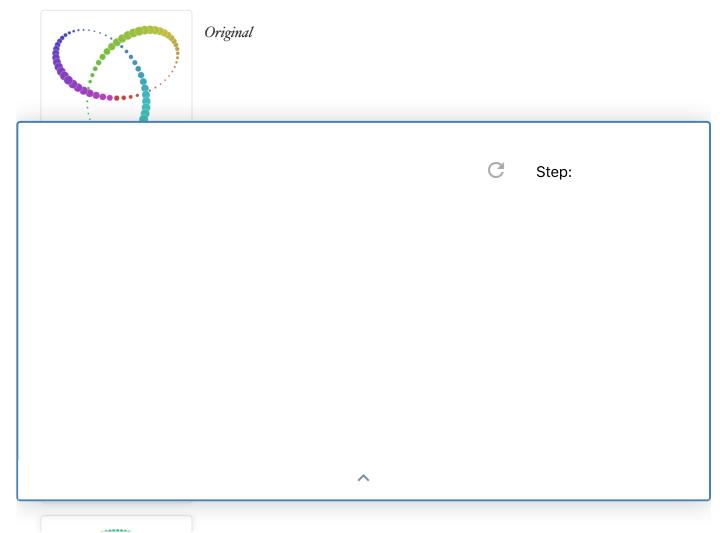
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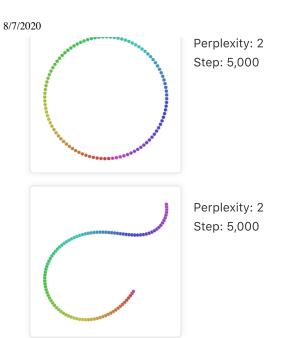
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The trefoil knot is an interesting example of how multiple runs affect the outcome of t-SNE. Below are five runs of the perplexity-2 view.

The algorithm settles twice on a circle, which at least preserves the intrinsic topology. But in three of the runs it ends up with three different solutions which introduce artificial breaks. Using the dot color as a guide, you can see that the first and third runs are far from each other.





Step: 5,000

Perplexity: 2

Five runs at perplexity 50, however, give results that (up to symmetry) are visually identical. Evidently some problems are easier than others to optimize.







Perplexity: 50 Step: 5,000

Step:

an intuition for what's going on.

#### Acknowledgments

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This work was made possible by the support of the Google Brain team.

Edited on Oct. 18, 2016 to describe and correct issues when perplexity is defined to be larger than the number of points. Thanks to Laurens van der Maaten for pointing this out.

#### References

1. Visualizing data using t-SNE [PDF]

Maaten, L.v.d. and Hinton, G., 2008. Journal of Machine Learning Research, Vol 9(Nov), pp. 2579-2605.

#### **Updates and Corrections**

| View all changes to this article since it was first published. If you see a mis | stake or want to suggest a |
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