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等值演算
逻辑推理
命题证明方法

证明集合相等

知道求和公式

排序、查找、贪心
看一下

求最大公约(欧几里德)
欧几里德数
中国剩余定理

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必看: 数学归纳法 / 强归纳 (大题)

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关系运算
新: 偏序

不看关系图

生成函数

怎样求线性齐次
递归方程: (非齐次不看)

考分治算法

包含排斥

只考二元

等价, 偏序

自反对称传递

自反对称传递

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☆度, 有向无向
关联, 连接矩阵
同构(小题)
路径矩阵

概念
先遍历

1. 文法
2. 有限自动机
(状态图/表)

语言识别