CS 61A Fall 2024

Structure and Interpretation of Computer Programs

MIDTERM 2

INSTRUCTIONS

This is your exam. Complete it either at exam.cs61a.org or, if that doesn't work, by emailing course staff with your solutions before the exam deadline.

This exam is intended for the student with email address <EMAILADDRESS>. If this is not your email address, notify course staff immediately, as each exam is different. Do not distribute this exam PDF even after the exam ends, as some students may be taking the exam in a different time zone.

For questions with circular bubbles, you should select exactly one choice.

You must choose either this option
Or this one, but not both!

For questions with square checkboxes, you may select multiple choices.

You could select this choice.

You could select this one too!

You may start your exam now. Your exam is due at <DEADLINE> Pacific Time. Go to the next page to begin.

Preliminaries

(a)	What is your full name?
(b)	What is your student ID number?

You can complete and submit these questions before the exam starts.

(c)	What is your @berkeley.edu email address?

` '	Sign (or type) your name to confirm that all work on this exam will be your own. The penalty misconduct on an exam is an F in the course.	for academic

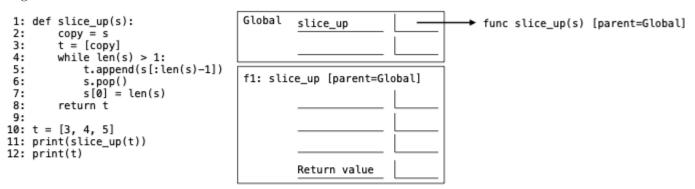
1. (5.0 points) What Would Python Display?

Assume the following code has been executed. The Tree class appears on the midterm 2 study guide (page 2, left side).

```
scare = Tree(0, [Tree(4), Tree(5, [Tree(10)]), Tree(2)])
crow = Tree(9, [scare, Tree(7, [Tree(6)])])
def climb(t, f):
    if t.is_leaf():
        return [t.label]
    return [t.label] + climb(max(t.branches, key=f), f)
def run(t):
    if t.is_leaf():
        return t.label
    else:
        return max(map(run, t.branches))
def hide(t):
    return t.label
jump = \{(2 * x - 1): x for x in range(50)\}
Write the value of each expression below or Error if an error occurs.
(a) (1.0 pt) crow.branches[0].label
(b) (1.0 pt) [hide(b) for b in scare.branches]
(c) (1.0 pt) climb(crow, hide)
(d) (1.0 pt) climb(crow, run)
(e) (1.0 pt) jump[jump[13]]
```

2. (5.0 points) Pizza by the Slice

Answer the questions about the code below. You are encouraged to draw an environment diagram, but the diagram itself will not be scored.



(a)	(3.0 pt) What would be printed by the expression print(slice_up(t)) on line 11?	I
(b)	(1.0 pt) What would be printed by the expression print(t) on line 12?	
	O [1]	
	○ [2]	
	○ [3]	
	○ [1, 4]	
	○ [2, 4]	
	○ [3, 4]	
	○ [1, 4, 5]	
	○ [2, 4, 5]	

(c) (1.0 pt) What is the order of growth of the time it takes to evaluate list(list(q)) for a list of numbers q in terms of the length of q. Assume that creating a list with one element takes constant time, and making a copy of a list takes linear time in the length of the list.

\bigcirc	exponential
\bigcirc	quadratic
\bigcirc	linear
\bigcirc	logarithmic
\bigcirc	constant

 \bigcirc [3, 4, 5]

3. (6.0 points) CS 61A Software Store

A Store instance has a list of branches, and each branch is also a Store instance, forming a tree of stores. Each Store instance also has a list of programs (strings) called its inventory. For a Store:

- The copies(s) method returns the number of times s appears in the inventories of all nodes in its tree of stores.
- The add_to(k) method returns a function that takes a string and appends it to the inventory of its kth branch. Assume that k is non-negative and less than the number of branches.

```
class Store:
    \hbox{\tt """A} Store selling programs has branches forming a tree of Stores.
    >>> north, south = Store(['Cats', 'Ants']), Store(['Cats', 'Cats', 'Hog'])
    >>> east, west = Store(['Cats', 'Hog', 'Hog'], [north, south]), Store(['Cats', 'Cats', 'Ants'])
    >>> main = Store(['Ants', 'Ants', 'Hog'], [east, west])
    >>> east.copies('Cats') # 1 in north, 2 in south, 1 in east
    4
   >>> main.copies('Ants') # 2 in main, 1 in north, 1 in west
   >>> main.add_to(1)('Ants') # Add 'Ants' to the inventory of west, the branch of main at index 1
    >>> [main.copies('Ants'), west.copies('Ants')] # increased copies in both main and west
    [5, 2]
    11 11 11
    def __init__(self, programs, branches=[]):
        assert all([isinstance(b, Store) for b in branches])
        self.branches = branches
        self.inventory = programs
    def copies(self, s):
        """Return the number of times s (string) appears in all inventories of this tree."""
        return sum([_____ for p in self.inventory if p == s] + [____ for b in self.branches])
                                                                      (b)
    def add_to(self, k):
        """Return a function that appends a string to the inventory of the branch at index k."""
        return _____
                 (c)
(a) (1.0 pt) Fill in blank (a).
    \bigcirc 1
    ( p
    ( ) len(p)
    len(self.inventory)
(b) (2.0 pt) Fill in blank (b).
```

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(c)	(3.0 pt) Fill in blank (c).

4. (18.0 points) Almost a Perfect Question

Definition. A proper divisor of an integer n is an integer d less than n that evenly divides n, and so n divided by d has no remainder. A semiperfect number is a positive integer that is the sum of some (or all) of its proper divisors. For example, 24 = 2 + 4 + 6 + 12 and so it is semiperfect. The sum of divisors cannot contain repeated numbers.

(a) (6.0 points)

Implement semiperfect, which takes a positive integer n. It returns True if n is semiperfect and False otherwise.

```
def semiperfect(n):
    """Return whether positive integer n is a sum of some (or all) of its proper divisors.
    >>> [k for k in range(1, 40) if semiperfect(k)]
    [6, 12, 18, 20, 24, 28, 30, 36]
    11 11 11
    def f(s, d):
         if ____:
               (a)
             return True
         if d \ge n:
             return False
         if _____, and f(____, d + 1):
               (b)
                               (c)
             return True
         return _____
                   (d)
    return f(n, 1)
 i. (1.0 pt) Fill in blank (a).
    \bigcirc n == 0
    ○ s == 0
    \bigcirc s == d
    \bigcirc n == d
ii. (1.0 pt) Fill in blank (b).
    \bigcirc n % d == 0
    \bigcirc s % d == 0
    \bigcirc n % d > 0
    \bigcirc s % d > 0
iii. (2.0 pt) Fill in blank (c).
iv. (2.0 pt) Fill in blank (d).
```

(b) (6.0 points)

Implement subsums, a generator function that takes a list of **unique** (no repeats) positive integers s and a positive integer n. It yields all sublists of s that sum to n. A sublist of s is a list containing some of the elements of s in order. The subsums function should not yield the same list twice. The lists may appear in any order.

```
def subsums(s, n):
    """Yield all sublists of s that sum to n.
    >>> list(subsums([1, 2, 3, 6, 9], 18))
    [[1, 2, 6, 9], [3, 6, 9]]
    >>> list(subsums([1, 2, 3, 4, 6], 16))
    [[1, 2, 3, 4, 6]]
    >>> list(subsums([1, 2, 3, 4, 6, 8, 12], 12))
    [[1, 2, 3, 6], [1, 3, 8], [2, 4, 6], [4, 8], [12]]
    if s:
        if ____:
             (e)
            yield [n]
        for t in _____:
                    (f)
            yield _____
                     (g)
        yield from _____
 i. (1.0 pt) Fill in blank (e).
   \bigcirc n == s
   \bigcirc n == s[0]
   On in s
   \bigcirc [n] == s
ii. (3.0 pt) Fill in blank (f).
```

iii. (1.0 pt) Fill in blank (g).

```
() s + t
```

- \bigcirc [s] + t
- \bigcirc s[1:] + t
- \bigcirc s[:1] + t

- iv. (1.0 pt) Fill in blank (h).
 - O subsums(s, n)
 - \bigcirc subsums(s[1:], n)
 - O subsums(s, n 1)
 - O subsums(s[1:], n 1)

(c) (6.0 points)

Implement semisums,	, which takes a	a positive	integer n.	It returns	a list of al	l lists of	unique	(no i	repeats
proper divisors of n tl	hat sum to n.	You may	call semip	erfect an	d subsums				

PIO	for divisors of it that sum to it. For many can be important and bubblanc.
def	<pre>semisums(n): """Return a list of all lists (with no repeats) of proper divisors of n that sum to n.</pre>
	>>> semisums(22) # 22 is not semiperfect, so there are no sums. [] >>> semisums(30) # 30 is semiperfect. It has three different sums. [[1, 3, 5, 6, 15], [2, 3, 10, 15], [5, 10, 15]]
	return list(([k for k in range(1, n) if],))
i.	(1.0 pt) Fill in blank (i).
	\bigcirc map
	<pre>filter</pre>
	○ sorted
	O subsums
	<pre>Semiperfect</pre>
ii.	(1.0 pt) Fill in blank (j).
	<pre> semiperfect(n)</pre>
	<pre>Semiperfect(k)</pre>
	<pre> semiperfect(n) or semiperfect(k)</pre>
	On % k == 0
iii.	(1.0 pt) Fill in blank (k).
iv.	(3.0 pt) Fill in blank (l) of primitive_semiperfect, a function that takes a positive integer n. I returns True if n is semiperfect and no smaller semiperfect number is a divisor of n. Your answershould have two expressions separated by a comma.
	$\label{lem:continuous} \begin{array}{llllllllllllllllllllllllllllllllllll$
	>>> [k for k in range(1, 300) if primitive_semiperfect(k)] [6, 20, 28, 88, 104, 272]
	<pre>return semiperfect(n) and not any(map(semiperfect, filter()))</pre>

5. (11.0 points) How Long is this Exam?

(a) (5.0 points)

Implement longer, which takes two linked lists of numbers s and t. It returns the longer of the two. If they have the same length, it returns s.

A linked list is either a Link instance or Link.empty. The Link class is on page 2 of the midterm 2 study guide.

```
def longer(s, t):
    """Return the longer linked list, s or t. (Same length? return s.)
    >>> longer(Link(2, Link(3)), Link.empty)
    Link(2, Link(3))
    >>> longer(Link(2, Link(3)), Link(4, Link(5)))
    Link(2, Link(3))
    >>> longer(Link(2, Link(3)), Link(4, Link(5, Link(6, Link(7)))))
    Link(4, Link(5, Link(6, Link(7))))
    >>> longer(Link.empty, Link.empty) is Link.empty
    True
    11 11 11
    a, b = s, t
    while b is not Link.empty:
        if ____:
             (a)
            return _____
                      (b)
          (c)
    return _____
             (d)
 i. (2.0 pt) Fill in blank (a).
ii. (1.0 pt) Fill in blank (b).
   ○ a
   ○ b
   () s
   \bigcirc t
   Olonger(a, b)
   O longer(s, t)
```

iii.	(1.	0 pt) Fill in blank (c).
	\bigcirc	a = a.rest
	\bigcirc	a = s.rest
	\bigcirc	b = b.rest
	\bigcirc	b = t.rest
	\bigcirc	a, b = a.rest, b.rest
	\bigcirc	a, b = s.rest, t.rest
	/-	0 () Fill 11 1 (1)
iv.	(1.	0 pt) Fill in blank (d).
iv.	(1.	
iv.	_	a
iv.	0	a b
iv.		a b s
iv.	0	a b s
iv.		a b s

(b) (6.0 points)

Implement longest, which takes a linked list of postive integers s and a positive integer n. It returns the longest sublist of s with elements that sum to a number less than or equal to n. Do not mutate s. In case of a tie, return any of the longest sublists whose sum is n or less. Assume longer is implemented correctly.

A sublist of a linked list **s** is a linked list with some (or none or all) of the elements of **s** in order.

Assume the sum of the elements of Link.empty is 0. Link.empty is a sublist of any linked list.

```
def longest(s, n):
    """Return the longest sublist of s that sums to n or less.
    >>> longest(Link(5, Link(1, Link(3, Link(4, Link(2, Link(7))))), 7)
    Link(1, Link(3, Link(2)))
    >>> longest(Link(5, Link(1, Link(3, Link(4, Link(2, Link(7)))))), 70)
    Link(5, Link(1, Link(3, Link(4, Link(2, Link(7)))))
    >>> longest(Link(3, Link(4, Link(5))), 2) is Link.empty
    True
    if s is Link.empty:
        return s
          (e)
    if ____:
         (f)
        return longer( _____ , t)
                          (g)
    else:
        return t
 i. (1.0 pt) Fill in blank (e).
   O longest(s, n)
   O longest(s, n - s.first)
   O longest(s.rest, n)
   O longest(s.rest, n - s.first)
ii. (2.0 pt) Fill in blank (f).
iii. (3.0 pt) Fill in blank (g).
```

6. (0.0 points) Nice Path!

This A+ question is not worth any points. It can only affect your course grade if you have a high A and might receive an A+. Finish the rest of the exam first!

(a) (0.0 pt) Fill in the blank of max_path, which takes a Tree of integers t and a function g. It returns a list s containing the labels along the path from the root of t to a leaf for which g(s) is as large or larger than for any other path. In case of a tie, return any path with a maximum g(s) value.

```
def climb(t, f):
    if t.is_leaf():
        return [t.label]
   return [t.label] + climb(max(t.branches, key=f), f)
def max_path(t, g):
    """Return the path s from the root of t to a leaf for which g(s) is largest.
   >>> scare = Tree(0, [Tree(4), Tree(5, [Tree(10)]), Tree(2)])
   >>> crow = Tree(4, [Tree(5), Tree(9, [scare, Tree(7, [Tree(6)])]), Tree(8)])
   >>> max_path(crow, lambda p: -p[-1])
                                                    # The path to the smallest leaf
    [4, 9, 0, 2]
   >>> max_path(crow, len)
                                                    # The longest path
    [4, 9, 0, 5, 10]
   >>> \max_{path(crow, lambda p: -abs(p[0]-p[-1]))} # To the leaf closest in value to the root
    [4, 9, 0, 4]
   x = [t.label] # You can use x instead of [t.label] to shorten your answer!
   return climb(t, lambda b: _____)
```

No more questions.