

# *ECON2101*

Based on Intermediate Microeconomics: A  
Tool-Building Approach by Samiran Banerjee.

Notes by Harry Partridge

Term 1 2021

# Contents

<b>1</b>	<b>Markets</b>	<b>3</b>
1.1	Supply and demand . . . . .	3
1.2	Equilibrium . . . . .	3
1.3	Surplus . . . . .	3
1.4	Determinants of Supply and Demand . . . . .	3
1.5	Interventions . . . . .	4
1.6	Elasticities . . . . .	4
<b>2</b>	<b>Budgets</b>	<b>5</b>
2.1	Consumption Space . . . . .	5
2.2	Non competitive budgets . . . . .	6
<b>3</b>	<b>Preferences</b>	<b>6</b>
3.1	Binary Relations . . . . .	6
3.2	Utility . . . . .	6
3.3	Preferences . . . . .	7
<b>4</b>	<b>Individual Demands</b>	<b>7</b>
4.1	Preference Maximization . . . . .	7
4.2	Individual Demands . . . . .	8
<b>5</b>	<b>Consumer Comparative Statics</b>	<b>8</b>
5.1	Price and Income Consumption Curves . . . . .	8
5.2	Decomposing Price Effects . . . . .	9
<b>6</b>	<b>Exchange Economics</b>	<b>10</b>
6.1	Allocations . . . . .	10
6.2	Rational allocations . . . . .	10
6.3	Walras Equilibrium . . . . .	11
<b>7</b>	<b>Technology</b>	<b>11</b>
7.1	Production . . . . .	11
7.2	Types of Technologies . . . . .	12
7.3	Returns to Scale . . . . .	12
7.4	Production possibility frontier . . . . .	12
<b>8</b>	<b>Costs</b>	<b>13</b>
8.1	Cost functions . . . . .	13
8.2	Cost concepts . . . . .	13
<b>9</b>	<b>Competitive Firms</b>	<b>14</b>
9.1	Profits . . . . .	14
9.2	Short Run Profit Maximization . . . . .	14
9.3	Shifts in a Firm's Supply . . . . .	15
9.4	Perfect Competition in the Long Run . . . . .	15

<b>10 Monopoly</b>	<b>15</b>
10.1 Uniform pricing . . . . .	15
10.2 Differential Pricing . . . . .	16

# 1 Markets

## 1.1 Supply and demand

- A **market demand** function for a particular good expresses the quantity demanded  $Q^d$  in terms of the price  $p$  of that good. The **inverse market demand** function expresses  $p$  in terms of  $Q^d$ , representing the maximum price a customer is prepared to pay for a quantity  $Q^d$ .
- The **Law of Demand** states that  $\frac{dQ^d}{dp}$  is negative.
- In a system with multiple markets, the **aggregate demand** at a given price is the sum of the demanded quantities at that price:  $Q^d(p) = \sum Q_i^d(p)$ . This will often be piecewise linear.
- **Market supply**  $Q^s$  is also a function of  $p$ . The **inverse world supply** is the inverse of this function.

## 1.2 Equilibrium

- The **equilibrium price**  $p^*$  and **equilibrium quantity**  $Q^*$  are the price and quantity such that  $Q^* = Q^d(p^*) = Q^s(p^*)$ .
- If a market has an equilibrium price, it is said to be in **equilibrium**.
- An equilibrium is said to be stable when it is self correcting: any deviation from the equilibrium will lead to either **excess supply** or **excess demand**.

## 1.3 Surplus

- The integral of  $p(Q^d) - p^*$  from 0 to the equilibrium quantity is the **consumer surplus**. Similarly the integral of  $p^* - p(Q^s)$  from 0 to the equilibrium quantity is the **producer surplus**.
- **Total surplus** is the sum of producer and consumer surplus.

## 1.4 Determinants of Supply and Demand

- Factors other than price affect  $Q^d$ . Common such factors are:
  - Buyer income levels. Increased income levels  $\implies$  more demand for **normal goods** and less demand for **inferior goods**.
  - Prices of other goods (**substitutes** and **complements**). Increase in price of substitute  $\implies$  increased demand for good in question. Increase in price of complements  $\implies$  decreased demand for good in question.
  - Preferences of buyers
  - Number of buyers
- Factors other than price affect  $Q^s$ . Common such factors are:

- Price of inputs
- Technological factors
- Number of firms
- Changes in these other determinants can cause the supply and demand curves to shift.
- If the quantity demanded of a good increases with income levels, it is called a **normal good**. Otherwise it is known as an **inferior good**.

### 1.5 Interventions

- A **price ceiling** is an imposed maximum price. This causes the supplied quantity to reduce, creating **excess demand**. Sellers will be forced to engage in **rationing**. Even if the rationing is efficient, there will be **deadweight loss**, which indicates a **market inefficiency**.
- A **price floor** is an imposed minimum price, leading to **excess supply**. There will again be rationing (this time by the buyers) and deadweight loss.
- A **quota** is a specified quantity that must be produced. This quantity must be less than the equilibrium quantity, or else some suppliers will be forced to produce at a loss which will cause them to go out of business. Therefore a **quota** can also be defined as a maximum quantity limit. Quotas will also create deadweight loss and inefficiencies.
- A **tax** on production effectively increases the cost of production, shifting the supply curve up. Correspondingly, a tax on buyers decreases the demand, shifting the curve down. The new equilibrium price will be the same regardless of the party on which the tax is imposed.
- The **incidence** of the tax on the buyers is the amount by which their surplus is reduced by the tax, and similarly for the sellers. The total tax revenue is equal to the sum of the incidence of the tax on the buyers and the sellers. The **incidence** on both buyers and sellers will be the same regardless of which party the tax is imposed on.
- **Subsidies** are negative taxes. Both taxes and subsidies result in deadweight loss.

### 1.6 Elasticities

- The **price elasticity of demand**,  $\varepsilon$  is the percentage change in demand for a given percentage change in price. i.e.

$$\varepsilon = \frac{dQ^d/Q^d}{dp/p} = \frac{dQ^d}{dp} \frac{p}{Q^d}$$

- perfect elasticity is when  $|\varepsilon| = \infty$  and perfect inelasticity is when  $|\varepsilon| = 0$ . If  $|\varepsilon| > 1$  then demand is elastic, if  $|\varepsilon| < 1$  then demand is inelastic and otherwise it is unit elastic.

- If revenue for a firm is  $R = PQ$ , then  $R' = Q + PQ' = Q + \varepsilon Q = (1 + \varepsilon)Q$ . Hence when demand is elastic, increasing price will decrease revenue, but when demand is inelastic, increasing price will increase revenue.
- The **income elasticity of demand**,  $\eta$  replaces price with consumer income with the determiner of demand. Hence  $\eta = \frac{\partial Q^d}{\partial m} \frac{m}{Q^d}$  where  $m$  is consumer income. Normal goods have positive income elasticity.
- The **cross price elasticity of demand** on good 1 by good 2 is the impact of the change in price of good 2 on good 1:

$$\varepsilon_{12} = \frac{\partial Q_1^d}{\partial p_2} \frac{p_2}{Q_1^d}$$

- The various elasticities of supply can be defined in a similar way.

## 2 Budgets

### 2.1 Consumption Space

- The **consumption space** is the combination of goods that a consumer can potentially purchase. A point in the commodity space is called a **consumption bundle**. For  $n$  goods, the commodity space is the volume  $\mathbb{R}_+^n$ .
- The consumer's **budget constraint** or **budget set** is given by

$$\{\mathbf{x} \in \mathbb{R}_+^n : \mathbf{p} \cdot \mathbf{x} \leq m\},$$

where  $\mathbf{p}$  is the vector of prices for the goods,  $\mathbf{x}$  is the vector of quantities demanded and  $m$  is the consumer's income. The **budget surface** is the boundary of this set.

- A budget is **competitive** when the prices vector is constant as a function of  $\mathbf{x}$ .
- If an individual begins with a **consumption bundle** instead of an income, then this is called the **individual's endowment**,  $\omega$  with value  $\omega \cdot \mathbf{x}$ .
- In a situation with two goods, changing the price of one good alters the slope and one intercept, and changing the income alters the intercepts. If the individual begins with an endowment, then changing prices pivot the budget surface around  $\omega$ .
- Scaling  $\mathbf{p}$  and  $m$  by the same amount does not affect  $\mathbf{x}$ , so  $\mathbf{p}$  can be normalised by choosing one element (the **numeraire**) to have a price of 1.

## 2.2 Non competitive budgets

- A budget can be made non competitive from many sources:
  - Price discounts on incremental purchases: will make a budget line concave.
  - Price discounts with bulk purchases: applies to all the purchased goods, not just incremental ones - creates a discontinuity in the budget line.
  - If an individual starts with an endowment (e.g. food stamps or currency), often those goods cannot be sold for their full value. This will result in a convex budget line.
  - Coupons may only become valuable after a certain amount is purchased. This will create a discontinuity in the middle of the budget line/surface.

## 3 Preferences

### 3.1 Binary Relations

- Preferences are represented by binary relations between consumption bundles. A **regular binary relation**  $\succsim$  is a total ordering on a set  $S$ . Total ordering satisfy
  1. **reflexivity**:  $(\forall x \in S) x \succsim x$
  2. **totality**:  $(\forall x, y \in S) x \succsim y$  or  $y \succsim x$
  3. **transitivity**:  $(\forall x, y, z \in S) x \succsim y$  and  $y \succsim z$  implies  $x \succsim z$
- Often, **monotonicity** is also required: if  $x \in S$  has every entry greater than or equal to  $y \in S$ , then  $x \succsim y$ . If at least one entry in  $x$  is greater than the corresponding entry in  $y$ , then **weak monotonicity** implies  $x \succsim y$  and **strong monotonicity** implies  $x \succ y$ .
- A binary relation is **convex** if for  $x, y \in S$  with  $x \succsim y$ , when  $z$  lies on the line segment joining  $x$  and  $y$ , then  $z \succsim y$ .

### 3.2 Utility

- A **utility function** assigns a real number to every consumption bundle. A regular binary relation can then be defined through the total ordering on the reals.
- An **indifference curve** is a level curve of the utility function.
- The **marginal rate of substitution** (MRS) of good 1 for good 2 is  $\frac{MU_1}{MU_2}$  where  $MU_i = \frac{\partial u}{\partial x_i}$ . If only two goods are being considered, it is the negative of the slope of the indifference curve.

- Utility is **ordinal** not **cardinal** because only the resulting binary relation on consumption bundles matters - the absolute value of the utility is irrelevant. This means that if  $v = f(u)$  with  $f' > 0$  for all  $u > 0$  ( $f$  monotonic increasing), the same preferences will be generated. Furthermore, the marginal rate of substitution on a given indifference curve will be the same if the utility function undergoes such a transformation.

### 3.3 Preferences

- **Linear preferences** can be represented by a utility function of the form  $u(\mathbf{x}) = \beta \cdot \mathbf{x}$ , where  $\beta$  is a vector of coefficients. The commodities which have negative coefficients are called the '**bads**'. A good with a coefficient of 0 is called **neutral**.
- If the marginal rate of substitution is constant at any point on the utility curve between two goods, then they are called **perfect substitutes**.
- A consumption bundle that is a local maximum of the utility function is called a **bliss point** or a point of **satisfaction**.
- **Leontief preferences** are those in which goods are **perfect complements** of consumption (e.g. 4 wheels in a car). This corresponds to the case where no substitution is possible between the goods - the utility function is the minimum function with appropriate coefficients:  $u(\mathbf{x}) = \min \beta_i x_i$ .
- **Quasilinear preferences** are those of the form  $u(x_1, x_2) = f(x_1) + x_2$  where  $f$  is concave down. The indifference curves for these preferences are always vertically parallel and concave up.
- **Cobb-Douglas preferences** are of the form  $u(\mathbf{x}) = Ax_1^{a_1} x_2^{a_2} \dots x_n^{a_n}$ . The marginal rate of substitution of  $x_i$  for  $x_j$  is  $\frac{a_i x_j}{a_j x_i}$ .
- There is a **diminishing marginal rate of substitution** for both quasilinear preferences and Cobb-Douglas preferences.
- All of these utility functions generate regular binary relations. They are all monotonic, but not all are strongly monotonic. All four preferences are convex.

## 4 Individual Demands

### 4.1 Preference Maximization

- An **interior solution** to the maximization problem is one in which the amount consumed of every good is positive.
- At the point of maximum utility, the indifference curve must be tangent to the budget line. The slope of the budget line is the ratio of the prices of the goods, and the slope of the indifference curve is the marginal rate of substitution of the two goods. Hence the maximum arises when  $MRS(x_1, x_2) = \frac{p_1}{p_2}$ .



- If one of the maximising quantities is zero, then the solution is called a **corner solution**. A corner solution requires that the price ratio of is either always more than the marginal rate of substitution or always less than the marginal rate of substitution.

## 4.2 Individual Demands

- An individual's demand  $h(p_1, p_2, m) = (h_1, h_2)$  for two goods  $h_1$  and  $h_2$  is the quantity (or set of possible quantities) of each good the individual demands at the specified  $(p_1, p_2, m)$ .
- Each of the different utility functions generate different demand functions:
  - Linear utility  $u(x_1, x_2) = ax_1 + bx_2$  generates

$$h(p_1, p_2, m) = \begin{cases} (0, m/p_2) & \text{if } p_1/p_2 > a/b \\ \{(x_1, x_2) : p_1x_1 + p_2x_2 = m\} & \text{if } p_1/p_2 = a/b \\ (m/p_1, 0) & \text{if } p_1/p_2 < a/b \end{cases}.$$

- Leontief preferences  $u(x_1, x_2) = \min(ax_1, bx_2)$  generates

$$h(p_1, p_2, m) = \left( \frac{mb}{p_1b + p_2a}, \frac{ma}{p_1b + p_2a} \right).$$

- The demand generated by quasilinear preferences  $u(x_1, x_2) = f(x_1) + x_2$  are found when  $f'(x_1) = p_1/p_2$ . A central feature of quasilinear preferences is that the demand for one of the goods does not depend on the income at an interior solution.
- Cobb-Douglas utility  $u(x_1, x_2) = Ax_1^a x_2^b$  generates

$$h(p_1, p_2, m) = \left( \frac{m}{p_1} \frac{a}{(a+b)}, \frac{m}{p_2} \frac{b}{(a+b)} \right).$$

If  $a = b$ , note that the demand lies at the midpoint of the budget line.

- When a consumer's preferences are strictly monotonic, they will always be maximized on the budget line. We then say that the consumer's demand satisfies **budget exhaustion**.
- Demand functions are homogeneous of degree zero in prices and income:

$$h(tp_1, tp_2, tm) = h(p_1, p_2, m).$$

## 5 Consumer Comparative Statics

### 5.1 Price and Income Consumption Curves

- A **price consumption curve** (PPC) is the curve that the preference maximising bundle traces out as one of the prices changes. Similarly, the **income consumption curve** (ICC) results when the consumer's income changes.

- In the language of consumption curves, the Law of Demand states that the PPC has a positive slope. A negative slope occurs when one of the goods is a **Giffen good**.
- For Leontief preferences  $u(x_1, x_2) = \min(ax_1, bx_2)$ , the PPC will be a straight line along  $ax_1 = bx_2$ . For Cobb-Douglas preferences, it will be either a horizontal or vertical line depending on which price is changed.
- The ICC for Cobb-Douglas preferences will be a straight line along  $p_2ax_2 = p_1bx_1$ . Quasilinear preferences will result in a vertical ICC.
- A positively sloping ICC indicates that both goods are normal (or both inferior), whereas a negatively sloping ICC demonstrates that one of the goods is inferior. A vertical ICC shows that the good on the horizontal axis has no income effect (and visa-versa for a horizontal ICC).

## 5.2 Decomposing Price Effects

- When the price of one good changes while the income and other prices remain fixed, the quantity demanded for that good will change. This is a **price effect**.
- A price effect is broken down into a **substitution effect**, which describes how the consumer purchases more or less due to the change in **relative** price, and an **income effect**, which describes how the consumer purchases more or less due to a change in their effective purchasing power. The two main such decompositions are **Hicks-Allen** and **Slutsky**.
- Starting at a preference maximising bundle A, the **Hicks-Allen** decomposition first finds the point B by holding utility constant and adjusting the price ratio. Contrastingly, the **Slutsky** approach finds point B by considering the individual's new endowment at A to be their income, and then finding the preference maximising bundle.
- If C denotes the preference maximising bundle with the old income and new price structure, then the substitution effect is the difference in quantities between A and B, and the income effect is the difference in quantities between B and C.
- The effective change in income is the difference between the individual's endowment at B and their true income.
- For infinitesimal price changes, the substitution and income effects will be the same for the **Hicks-Allen** and **Slutsky** models.
- For inferior goods (i.e. something like fast food), the income effect works in the opposite direction to the substitution effect. The income effect is typically smaller than the substitution effect, but in the case where it is not (if a consumer spends a large percentage of their income on a commodity like rice this may be the case), then the good will not obey the law of demand and is called a Giffen good.

## 6 Exchange Economics

### 6.1 Allocations

- An economy where there is no production but only exchange is called a **pure exchange economy**.
- An individual's **characteristic**  $e^i = (u^i, \omega^i)$  captures both their utility function  $u^i$  and their endowment  $\omega^i$ . An **economy**  $e$  is a collection of individuals  $(e^a, e^b, \dots)$ .
- The **aggregate endowment**  $\Omega$  is the sum of every individual's endowment.
- A list of consumption bundles for all of the consumers is called an **allocation**. An allocation is **feasible** when the sum of goods in the allocation is less than or equal to the aggregate endowment.
- The **Edgeworth box** is the set of feasible allocations. An exchange between two consumers corresponds to a movement from the **initial endowment** (the starting allocation) to another point in the Edgeworth box.

### 6.2 Rational allocations

- **Individual rationality** says that if two people trade voluntarily, that trade must leave both people at least as well off as before the trade. An allocation  $(x^1, x^2, \dots, x^n)$  is said to be **rational** if  $u^i(x^i) \geq u^i(\omega^i)$  for all  $i = 1 \dots n$ . The **individually rational** allocations are the set of rational allocations given a certain initial endowment.
- An allocation is said to be **Pareto superior** if it is rational and at least one consumer is strictly better off.
- A **Pareto efficient** allocation it is not possible to reallocate goods without hurting one of the consumers: the set of Pareto superior allocations is empty
- Given an initial endowment, a the Pareto efficient allocation is found by fixing one of the consumer's utilities, and using that indifference curve as the other consumer's budget line.
- As an interior Pareto efficient allocation, must occur where the indifference curves are tangent, the set of all Pareto efficient allocations is found by setting the marginal rate of substitution for each of the consumers to be equal.
- The set of all Pareto efficient allocations is called the **contract curve** and labeled PE.

### 6.3 Walras Equilibrium

- **Walras prices** are the unique prices (up to normalisation) such that when every individual attempts to maximise their utility at market prices, the aggregate demand is the aggregate endowment. This is equivalent to saying that at these prices, every individual's budget set is tangent to their indifference curve at the point where their budget set intersects the contract curve.
- The **Walras allocation** is the allocation that arises in a market with Walras prices. Equivalently, it is the Pareto efficient allocation  $\mathbf{x}$  such that the line from  $\mathbf{x}$  to the initial endowment is tangent to the individual's indifference curves.
- A **Walras equilibrium** is the set of Walras prices and the Walras allocation. Theoretically, a Walras equilibrium is reached through a **Walrasian auctioneer**, who proposes a price, and then adjusts it until the aggregate demand for each good is equal to the aggregate endowment for that good. At this point, the market for each good is said to **clear**.
- **Walras' law** states that in a system of  $n$  goods, if the market clears for  $n - 1$  goods, then it also clears for the remaining good. This is obvious because the total value supplied must be the total value demanded.
- The Walras allocation is the unique allocation that is both individually rational and Pareto efficient. This is known as the **First Welfare Theorem**.
- The **Second Welfare Theorem** states that any Pareto efficient allocation  $P$ , there is an initial endowment for which  $P$  is also the Walras allocation.

## 7 Technology

### 7.1 Production

- A **technology**  $f$  (also called a **production function**) is a black box which converts inputs into outputs:

$$(q_1, \dots, q_m) = f(x_1, \dots, x_n).$$

Specifically,  $f(x)$  describes the maximum possible output for input combination  $x$ . An input-output combination describes a **feasible plan** if it is possible to produce the output given the inputs. The collection of all feasible plans is the **production set**.

- The **short run** is the period of time over which some inputs are **fixed**. The **long run** is the period of time over which all inputs are **variable**.
- The **marginal product** of an input  $x$  is  $\partial \mathbf{q} / \partial x$ .
- The assumption of **diminishing marginal productivity** states that the marginal product of each input is decreasing. Equivalently,  $\partial^2 \mathbf{q} / \partial x^2 < 0$ .

- The **average product** of an input is  $AP_x = f(x)/x$ .
- An **isoquant** is the set of inputs that can be used to produce a fixed level of output. This is equivalent to the notion of an indifference curve for a consumer.
- The **technical rate of substitution** (TRS) of good  $i$  for good  $j$  is the ratio of the marginal productivities of those goods.
- The **elasticity of substitution** between inputs  $i$  and  $j$  is the percentage change in **input intensity**  $x_i/x_j$  when there is a percentage change in the TRS along an isoquant:

$$\epsilon = \frac{dI/I}{dTRS/TRS} = ?$$

## 7.2 Types of Technologies

- A Linear technology has the form  $f(\mathbf{x}) = \beta \cdot \mathbf{x}$  for some set of coefficients  $\beta$ . This corresponds to the situation where the goods are perfect substitutes.
- A Leontief technology has the form  $f(\mathbf{x}) = \min \beta_i x_i$  for some set of coefficients  $\beta$ . This corresponds to the situation where inputs cannot be substituted and must be used in fixed proportions. If however a firm has multiple different Leontief technologies, then substitution possibilities do arise.
- Cobb-Douglas technologies are those with the form  $f(\mathbf{x}) = Ax_1^{a_1} x_2^{a_2} \dots x_n^{a_n}$ .
- **Constant elasticity of substitution** (CES) technologies have the form  $f(\mathbf{x}) = A(a_1 x_1^s + a_2 x_2^s \dots a_n x_n^s)^{\frac{1}{s}}$ , where  $s < 1$ . In this case, the elasticity of substitution is the constant  $\frac{1}{1-s}$ . When  $s = 1$ , CES technologies are linear, and as  $s \rightarrow -\infty$  CES technologies approach Leontief. Furthermore, when  $s = 0$  CES becomes equivalent to Cobb-Douglas.

## 7.3 Returns to Scale

- The production of a good shows **constant returns to scale** if the technology is homogenous of first degree:  $f(t\mathbf{x}) = tf(\mathbf{x})$ . If  $f(t\mathbf{x}) < tf(\mathbf{x})$ , it is said that there are **decreasing returns to scale**, and if  $f(t\mathbf{x}) > tf(\mathbf{x})$ , it is said that there are **increasing returns to scale**.

## 7.4 Production possibility frontier

- A **production possibility frontier** (PPF) (also called the **transformation frontier**) shows the maximum combinations of goods that can be produced for constrained inputs. It is often defined implicitly:  $T(q_1, q_2) = c$ , where  $T$  represents the total inputs required for the production of  $q_1$  and  $q_2$ .
  - This would correspond to the situation where goods (corresponding to inputs) are shared between two consumers, producing two different levels of utility (corresponding to  $q_1$  and  $q_2$ ).

- For a single input, the **opportunity cost** of producing good one in favour of good two is  $|dq_2/dq_1| = \frac{\partial T/\partial q_1}{\partial T/\partial q_2}$ , also called the **marginal rate of transformation** (MTF). This would be analogous to the situation where one consumer's utility is increased at the expense of the other's.
- When there are two inputs and two outputs, an **input Edgeworth box** is used to represent the combinations.
- An input allocation is **Lerner efficient** when there is no allocation which yields a higher output for either good without reducing the output of one of the goods. These allocations arise where the isoquants for the two outputs are tangent to each other.
  - This would correspond to the situation where neither consumer could increase their utility without reducing the other's - i.e. a Pareto Efficient solution.

## 8 Costs

### 8.1 Cost functions

- A **cost function** describes the minimum cost of producing a certain level of output as a function of the input prices.
- An **isocost** is the line which shows the input combinations which are just affordable for a firm. This is analogous to a budget line for a consumer.
- The cost minimising input combination arises when the isocost is tangent to the isoquant. This combination consists of the **conditional input demand functions**.
- For Leontief and linear technologies that are not smooth curves, the cost is found in the same way as demand function for a consumer.

### 8.2 Cost concepts

- The total cost is  $TC = c(w, q)$
- The **total fixed cost** is the cost incurred when nothing is produced:  $TFC = c(w, 0)$ .
- The **total variable cost** is the cost not included in the TFC:  $TVC = c(w, q) - c(w, 0)$ .
- The **average cost** is the cost of producing each unit when  $q$  units are produced:  $AC = c(w, q)/q$ .
- The **average fixed cost** is  $AFC = c(w, 0)/q$
- The **average variable cost** is  $AFC = TVC/q = AC - AFC$ .
- The **marginal cost** is the cost of producing another unit of output:  $MC = \partial c/\partial q$ .

- For the average (variable or fixed) cost to be increasing/decreasing, the marginal cost must be more/less than the average cost. Hence, when graphed, the marginal cost passes through the minimum of AC and AVC.

## 9 Competitive Firms

### 9.1 Profits

- **Perfect competition** arises when a market has many sellers and many buyers, all with perfect information and no barriers to entry.
- A trader under perfect competition is said to be a **price-taker**, in that they cannot influence the price through their own actions.
- The **profit** for a firm is defined as the difference between total revenue and total cost:  $\pi(q) = pq - c(q)$ . When  $\pi > 0$ ,  $\pi = 0$  or  $\pi < 0$ , we say that the firm makes **supernormal profits**, **normal profits** or **losses** respectively.
  - Profit doesn't have a good analogue for consumers, because the value of a consumer's utility cannot be converted into a monetary value. (because consumers do not have absolute utility but only ordinal preferences)
- Normal profits arise when the average cost of producing an output is the price of that output.

### 9.2 Short Run Profit Maximization

- The **isoprofit line** is the set of combinations of input and output quantities that produce the same profit. In general, it has the form  $\pi = pq - \beta\mathbf{x}$ , implicitly relating the output requirement  $q$  and the inputs  $\mathbf{x}$ .
  - The profit is maximised when the isoprofit line is tangent to the technology frontier.
  - This corresponds to the point at which the marginal cost of production is equal to the value of the marginal product.
- Profit maximisation is possible only with a production function that eventually has decreasing returns to scale.
- Another way of calculating a supply curve is to decompose the action of the firms into two parts.
  - First of all the firm will ensure that if they are producing a quantity  $q$ , then it will be produced at the minimum cost.
  - Secondly, the firm will ensure that they produce the profit maximising quantity of goods.
  - The firm's profits are then a function of only the output level alone, allowing for maximisation. This maximum will occur when the price is equal to the marginal cost, and the marginal cost is rising (when the second derivative of the costs is greater than zero).

- Even if the maximum profit is negative, a firm should continue operation when the total variable cost is less than the total revenue. This can occur when the price is greater than the minimum average variable cost. The **shutdown price** is therefore the minimum of the firm's average variable cost.
- The **shutdown quantity** is the quantity the firm will produce at the shutdown price. This can be found when the marginal cost is equal to the average variable cost.

### 9.3 Shifts in a Firm's Supply

- An increase in **productivity** will shift the supply curve down.
- An increase in input prices has the opposite effect of an increase in productivity
- A tax changes the cost of production

### 9.4 Perfect Competition in the Long Run

- If firms in a market are not making zero profit, then others will either enter or exit over the long run, thereby ensuring that profits will eventually be zero.
- A firm will make normal profits when the price is the minimum of the average cost. This is also where the marginal cost equals the average cost. Therefore, in the long run, if all firms are identical, then the equilibrium price will be this minimum.

## 10 Monopoly

### 10.1 Uniform pricing

- A monopoly is by definition able to set prices for the goods it produces. If  $D(Q)$  is the price demand for their goods at the quantity  $Q$ , then  $\pi(Q) = D(Q)Q - c(Q)$ , where  $c(Q)$  represents the minimum cost of producing at quantity  $Q$ . The task of the firm is then to maximize this profit. This occurs when marginal revenue is equal to marginal cost, which can also be expressed as

$$p(1 + \frac{1}{\varepsilon}) = c'(Q).$$

- The **absolute mark-up** is the difference between the monopoly's optimal price and their marginal cost at that price.
- The **relative mark-up** is the absolute markup divided by the equilibrium price. This gives a measure of market power that is called the **Lerner**



**Index.** The equation relating the monopoly's profit maximising price and quantity can also be written as

$$\frac{p - c'(Q)}{p} = -\frac{1}{\varepsilon},$$

showing that the Lerner Index is equal to the reciprocal of the elasticity.

- Due to the fact that the Monopoly's marginal revenue does not coincide with the economy's demand function, the monopoly will not produce at a price where their marginal cost is equal to the price. This will lead to Pareto inefficiency and deadweight loss.

## 10.2 Differential Pricing

-