

### Key Points to Remember:

1. A **polynomial** is a function of a variable ( $x$ , say), which is built just from addition, subtraction, multiplication, and raising  $x$  to positive whole-number powers. For instance,  $8x^3 - 7x^2 + 3$  is a polynomial, but  $\sin(x) + x^3$  is not, because of the  $\sin$  term.
2. The **degree** of a polynomial is the largest power of the variable appearing. For instance, the degree of  $-x^3 + 4x^2 - 2x$  is 3.
3. A **root** of a polynomial  $f(x)$  is a number  $a$  such that  $f(a) = 0$  - *i.e.*, substituting  $a$  in place of  $x$  gives 0.
4. A polynomial  $f(x)$  is a **factor** of another polynomial  $g(x)$  if  $f(x)$  can be multiplied by a polynomial to make  $g(x)$  - just like a whole number  $f$  is a factor of another whole number  $g$  if  $f$  can be multiplied by some other number to make  $g$ .
5. Any degree- $n$  polynomial can be divided by a degree-1 polynomial to give a degree- $(n - 1)$  polynomial and a constant remainder.
6. To divide one polynomial by another, use long division, starting with the largest power and working down.
7. The **Polynomial Factor Theorem** says that a number  $a$  is a **root** of a polynomial if and only if  $(x - a)$  is a **factor** of that polynomial.