

$$\begin{aligned}
T(n) &= 4T\left(\frac{n}{2}\right) + n^2 \log n \\
&= 4\left[4T\left(\frac{n}{2^2}\right) + \frac{n^2 \log n}{2}\right] + n^2 \log n \\
&= 4^2 T\left(\frac{n}{2^2}\right) + \frac{4n^2 \log n}{2} + n^2 \log n \\
&= 4^2 \left[4T\left(\frac{n}{2^3}\right) + \frac{n^2 \log n}{2^2}\right] + \frac{4n^2 \log n}{2} + n^2 \log n \\
&= 4^3 T\left(\frac{n}{2^3}\right) + \frac{4^2 n^2 \log n}{2^2} + \frac{4n^2 \log n}{2} + n^2 \log n
\end{aligned}$$

$$\begin{aligned}
&+ (4 + 2 + 1) n^2 \log n \\
&+ (2^2 + 2^1 + 2^0) n^2 \log n \\
&+ \left(\sum_{i=0}^{K-1} 2^i\right) n^2 \log n
\end{aligned}$$

$$= 4^K T\left(\frac{n}{2^K}\right) + (2^K - 1) n^2 \log n$$

$$\frac{n}{2^K} = 1 \Rightarrow n = 2^K \Rightarrow \log_2 n = \log_2 2^K \Rightarrow \log_2 n = K$$

$$= 4^{\log_2 n} T(1) + (2^{\log_2 n} - 1) n^2 \log n$$

$$= n^{\log_2 4} T(1) + (n^{\log_2 2} - 1) n^2 \log n$$

$$= n^2 T(1) + (n - 1) n^2 \log n$$

$$\therefore O(n^2 \log n)$$