

# ECE 235: Introduction to Solid State Electronics

## Discussion

### Week 8

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## Carrier Statistics

$$n = N_c e^{-(E_c - E_F)/kT} \quad \text{where} \quad N_c = 2 \left( \frac{2\pi m^* kT}{h^2} \right)^{3/2}$$

$$p = N_v e^{-(E_F - E_v)/kT} \quad \text{where} \quad N_v = 2 \left( \frac{2\pi m^* kT}{h^2} \right)^{3/2}$$

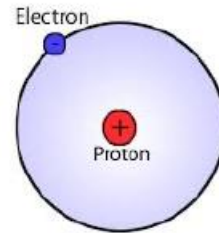
$$E_i = \frac{E_c + E_v}{2} + \frac{3kT}{4} \ln\left(\frac{m_p^*}{m_n^*}\right) \cong \frac{E_c + E_v}{2}$$

$$n_i = \sqrt{N_c N_v} e^{-E_G/2kT}$$

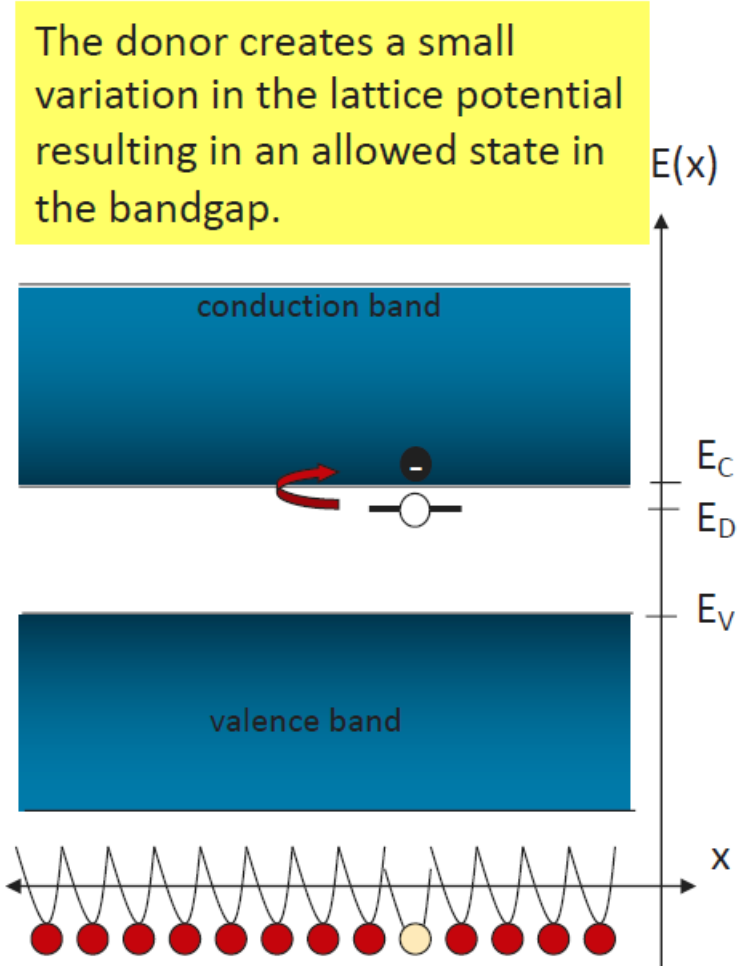
# Donor Energy

5 B	6 C	7 N
13 Al	14 Si	15 P
31 Ga	32 Ge	33 As
49 In	50 Sn	51 Sb

$$E_b = -\frac{m_e e^4}{8\epsilon_0^2 h^2} = -13.6 \text{ eV}$$



$$E_b^{As} = E_b \frac{m_e^*}{m_e} \frac{1}{\epsilon_r^2} = -0.032 \text{ eV}$$



# Electron and Hole Concentration

$$np = n_i^2$$

Intrinsic  
semiconductor

$$n = p = n_i$$

N-type material

$$n \approx N_D$$

$$p \approx \frac{n_i^2}{N_D}$$

P-type material

$$p \approx N_A$$

$$n \approx \frac{n_i^2}{N_A}$$

## Drift and Diffusion Current

$$J_e(\text{drift}) = n e \mu_e E$$

$$J_h(\text{drift}) = p e \mu_h E$$

$$J_e(\text{diffusion}) = e D_e \frac{dn}{dx}$$

$$J_h(\text{diffusion}) = -e D_h \frac{dp}{dx}$$

$$J(\text{diffusion}) = J_e(\text{diffusion}) + J_h(\text{diffusion})$$

## Practice Problem 1

Given that the density of states related effective masses of electrons and holes in Si are approximately  $1.08m_e$ , and  $0.60m_e$ , respectively, and the electron and hole drift mobilities at room temperature are  $1350$  and  $450 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$ , respectively, calculate the intrinsic concentration and intrinsic resistivity of Si. Si bandgap is  $1.10 \text{ eV}$ .

## Practice Problem 2

Find the resistance of a  $1\text{ cm} \times 1\text{ cm} \times 1\text{ cm}$  pure silicon crystal. What is the resistance when the crystal is doped with arsenic if the doping is 1 part per billion (ppb)? Given data: Atomic concentration in silicon is  $5 \times 10^{22}\text{ cm}^{-3}$ ,  $n_i = 1.0 \times 10^{10}\text{ cm}^{-3}$ , the electron and hole drift mobilities at room temperature are  $1350$  and  $450\text{ cm}^2\text{ V}^{-1}\text{ s}^{-1}$ , respectively.

## Practice Problem 3

An n-type Si semiconductor containing  $10^{16}$  phosphorus (donor) atoms  $\text{cm}^{-3}$  has been doped with  $10^{17}$  boron (acceptor) atoms  $\text{cm}^{-3}$ . Calculate the electron and hole concentrations in this semiconductor. Given that  $n_i = 1.0 \times 10^{10} \text{ cm}^{-3}$



## Practice Problem 4

An n-type Si wafer has been doped uniformly with  $10^{16}$  antimony (Sb) atoms  $\text{cm}^{-3}$ . Calculate the position of the Fermi energy with respect to the Fermi energy  $E_{Fi}$  in intrinsic Si. The above n-type Si sample is further doped with  $2 \times 10^{17}$  boron atoms  $\text{cm}^{-3}$ . Calculate the position of the Fermi energy with respect to the Fermi energy  $E_{Fi}$  in intrinsic Si. Given that  $n_i = 1.0 \times 10^{10} \text{ cm}^{-3}$  (Assume that  $T = 300 \text{ K}$ ).