

```
/*
 * For every possible move for the current board state, find the move that has
 * the highest evaluation from evaluate(). Has similar implementation to
 * maxValue(), however, it also has book keeping to record which move had the
 * highest evaluation.
 *
 * Computational complexity analysis:
 *
 *          Let moves.size() = n
 *          Let depth_ = m
 *          Complexity:  $O(n^m)$ 
 *
 * Explanation:
 * minimax() calls minValue which is indirectly recursive with maxValue()
 * for a total of m times. For each of these calls, moves are evaluated for
 * a total of n times. For example, if we assume that  $n = 3$ , and  $m = 2$ , then
 * we have 3 moves for every level of depth, for a total of 6 moves that
 * need to be processed:
 *
 * m_0: n_0, n_1, n_2
 * m_1: n_0, n_1, n_2
 *
 * which is  $3^2 = 6$ , or  $n^m$ 
 * Therefore, the computational complexity is  $O(n^m)$ 
 *
 * Pre-condition:
 * - The board is not full.
 *
 * Post-condition:
 * - The board is left unchanged from simulations.
 *
 * @return A valid move.
 */
```

```
Move HardComputer::minimax()
{
    map<float_t, Move> valueMoveMap;
    auto moves = gameAnalyzer_->findAllValidMoves(playerColor_);

    // For each move, record its evaluation.
    for (const auto& move : moves)
    {
        board_->setMove(move);
        auto value = minValue(depth_ - 1);
        valueMoveMap[value] = move;
        board_->undoMove();
    }

    // Return the move that had the highest evaluation.
    return valueMoveMap.rbegin()->second;
}
```

```
float_t HardComputer::maxValue(const uint32_t depth)
{
    // Base case: board is full or depth of search reaches 0.
    if (depth == 0 || board_>isBoardFull())
    {
        return evaluate(OCCUPANT_COUNT_DIFFERENCE);
    }

    // general case: there are board states to search.
    auto value = -INFINITY;
    auto moves = gameAnalyzer_>findAllValidMoves(playerColor_);
    for (const auto& move : moves)
    {
        board_>setMove(move);
        value = max(value, minValue(depth - 1));
        board_>undoMove();
    }
    return value;
}

float_t HardComputer::minValue(const uint32_t depth)
{
    // Base case: board is full or depth of search reaches 0.
    if (depth == 0 || board_>isBoardFull())
    {
        return evaluate(OCCUPANT_COUNT_DIFFERENCE);
    }

    // general case: there are board states to search.
    auto value = INFINITY;
    auto moves = gameAnalyzer_>findAllValidMoves(oppositionColor_);
    for (const auto& move : moves)
    {
        board_>setMove(move);
        value = min(value, maxValue(depth - 1));
        board_>undoMove();
    }
    return value;
}
```

```
float_t HardComputer::evaluate(const HeuristicMethod method) const
{
    const auto whiteCount
        = static_cast<float_t>(gameAnalyzer_>countCellsWithColor(WHITE));
    const auto blackCount
        = static_cast<float_t>(gameAnalyzer_>countCellsWithColor(BLACK));
    const auto winner = gameAnalyzer_>findWinnersColor();

    switch (method)
    {
    case OCCUPANT_COUNT_DIFFERENCE:

        // Counts the number of occupancies and returns a difference that is
        // maximized for the maxing player and minimized for the mining player.
        if (playerColor_ == WHITE)
        {
            return whiteCount - blackCount;
        }
        return blackCount - whiteCount;

    case GAME_RESULT_ENCODING:

        //Encodes the result of games with a 1 for a win or a - 1 for a loss.
        if (winner == playerColor_)
        {
            return 1.0;
        }
        if (winner == oppositionColor_)
        {
            return -1.0;
        }
    }
    return 0.0;
}
```