

# *Morphology and Finite-State Transducers*

# *Why this chapter?*

- *Hunting for singular or plural of the word 'woodchunks' was easy, isn't it?*
- *Lets consider words like*
  - *Fox*
  - *Goose*
  - *Fish*
  - *etc*
- *What is their plural form?*

# *Knowledge required*

- *Two kinds of knowledge is required to search for singulars and plurals of these forms*
- *Spelling rules*
  - *Words that end with 'y' changes to 'i+es' in the plural form*
- *Morphological rules*
  - *Fish has null plural and the plural of goose is formed by changing the vowel*

# *Morphological parsing.*

- *The problem of recognizing that foxes breaks down into the two morphemes fox and -es is called **morphological parsing**.*
- ***Parsing** means taking an input and producing some sort of structure for it*
- *Similar problem of mapping foxes into fox in the information retrieval domain: **stemming***

# *Morphological parsing contd...*

- *Applied to many affixes other than plurals*
  - *Takes verb form ending in -ing( going,talking...)*
  - *Parse it into verbal stem + -ing morpheme*
- *Given the **surface** or **input form** going, we might want to produce the parsed form: VERB-go + GERUND-ing*

# *In this chapter*

- *Morphology*
- *Finite-State Transducers*
- *Finite-state transducers?*
- *The main component of an important algorithm for morphological parsing*

# *Morphological parsing contd...*

- *It is quite inefficient to list all forms of noun and verb in the dictionary because the productivity of the forms.*
  - *Productive suffix*
  - *Applies to every verb*
  - *Example –ing*
- *Morphological parsing is necessary more than just IR, but also*
  - *Machine translation*
  - *Spelling checking*

# *Survey of English Morphology*

- *Morphology is the study of the way words are built up from smaller meaning-bearing units, **morphemes**.*
- *Two broad classes of morphemes:*
  - ***The stems:** the “main” morpheme of the word, supplying the main meaning*
  - ***The affixes:** add “additional” meaning of various kinds.*



# Affixes

- *Affixes are further divided into **prefixes**, **suffixes**, **infixes**, and **circumfixes**.*
  - *Suffix: eat-s*
  - *Prefix: un-buckle*
  - *Circumfix: ge-sag-t (said) (in German)*
  - *Infix:*
    - *hingi (borrow) + affix 'um' = humingi (in Philippine language )*

# *Another classification of morphology*

- *Prefixes and suffixes are often called **concatenative morphology**.*
  - *A word is composed of a number of morphemes concatenated together*
- *A number of languages have extensive **non-concatenative morphology***
  - *Morphemes are combined in a more complex way*
    - *The Tagalog infixation example*
  - *Another kind of non-concatenative morphology*
    - *Templatic morphology or root-and-pattern morphology*
    - *Common in Arabic, Hebrew, and other Semitic languages*

# *Ways to form words from morphemes*

- *Two broad classes*
- ***Inflection:***
  - *the combination of a word stem with a grammatical morpheme usually resulting in a word of the same class as the original stem*
- ***Derivation:***
  - *the combination of a word stem with a grammatical morpheme usually resulting in a word of a different class, often with a meaning hard to predict exactly*

# *Inflectional Morphology -NOUN*

- *In English,*
  - *only nouns, verbs, and sometimes adjectives can be inflected*
  - *the number of affixes is quite small.*
- *Inflections of nouns in English:*
  - *An affix marking **plural**,*
    - *cat(-s)*
    - *ibis(-es),*
    - *thrush(-es)*
    - *waltz(-es), finch(-es), box(-es)*
    - *butterfly(-lies)*
    - *ox (oxen), mouse (mice) [irregular nouns]*

## *An affix marking **possessive***

- *Regular singular noun- llama's*
- *Plural noun not ending in 's '-children's*
- *Regular plural noun -llamas'*
- *Names ending in 's' or 'z' - Euripides' comedies*

# *Inflectional Morphology- VERB*

- *Verbal inflection is more complicated than nominal inflection.*
- *English has three kinds of verbs:*
  - *Main verbs, eat, sleep, impeach*
  - *Modal verbs, can will, should*
  - *Primary verbs, be, have, do*
- *Of these verbs a large class are regular*
- *All verbs of this class have the same endings marking the same functions.*

# *Morphological forms of regular verbs*

- *Have four morphological form*
- *Just by knowing the stem we can predict the other forms*
  - *By adding one of the three predictable endings*
  - *Making some regular spelling changes*
- *These regular verbs and forms are significant in the morphology of English because of their majority and being productive.*

stem	walk	merge	try	map
-s form	walks	merges	tries	maps
-ing principle	walking	merging	trying	mapping
Past form or –ed participle	walked	merged	tried	mapped

# *Morphological forms of irregular verbs*

- *Have five different forms*
- *But can have as many as eight (verb 'be')*
- *Or as few as three (verb 'cut' )*

stem	eat	catch	cut
-s form	eats	catches	cuts
-ing principle	eating	catching	cutting
Past form	ate	caught	cut
-ed participle	eaten	caught	cut

the simple form: be

the -ing participle form: being

the past participle: been

the first person singular present tense form: am

the third person present tense (-s) form: is

the plural present tense form: are

the singular past tense form: was

the plural past tense form: were



# Derivational Morphology

- **Nominalization in English:**
  - *The formation of new nouns, often from verbs or adjectives*

Suffix	Base Verb/Adjective	Derived Noun
-ation	computerize (V)	computerization
-ee	appoint (V)	appointee
-er	kill (V)	killer
-ness	fuzzy (A)	fuzziness

- Adjectives derived from nouns or verbs

Suffix	Base Noun/Verb	Derived Adjective
-al	computation (N)	computational
-able	embrace (V)	embraceable
-less	clue (A)	clueless

# *Derivational Morphology*

- *Derivation in English is more complex than inflection because*
  - *It is generally less productive*
    - *A nominalizing affix like –ation can not be added to absolutely every verb. eatation(\*)*
  - *There are subtle and complex meaning differences among nominalizing suffixes.*
    - *For example, sincerity has a subtle difference in meaning from sincereness.*

# Finite-State Morphological Parsing

- *The problem of parsing English morphology*
- *Aim is to take input forms in the first column and produce output forms in the second column*

Input	Morphological parsed output
cats	cat +N +PL
cat	cat +N +SG
cities	city +N +PL
geese	goose +N +PL
goose	(goose +N +SG) or (goose +V)
gooses	goose +V +3SG
merging	merge +V +PRES-PART
caught	(caught +V +PAST-PART) or (catch +V +PAST)

*Input form*

*Stems and morphological features*

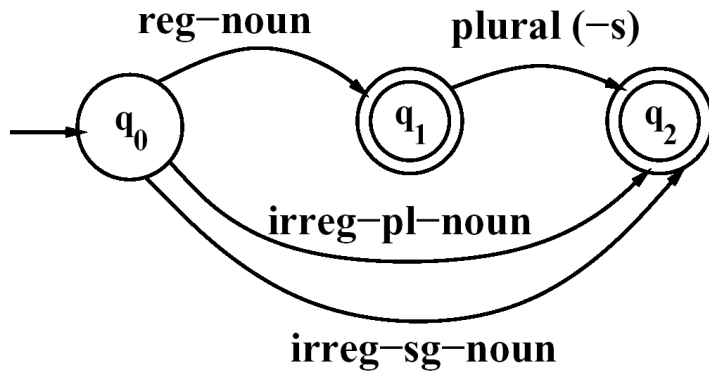
# *To build a morphological parser:*

- 1. *Lexicon:*** *the list of stems and affixes, together with basic information about them*
  - *E.g., Noun stem or Verb stem, etc.*
- 2. *Morphotactics:*** *the model of morpheme ordering that explains which classes of morphemes can follow other classes of morphemes inside a word.*
  - *E.g., the rule that English plural morpheme follows the noun rather than preceding it.*
- 3. *Orthographic rules:*** *these **spelling rules** are used to model the changes that occur in a word, usually when two morphemes combine*
  - *E.g., the  $y \rightarrow ie$  spelling rule changes city + -s to cities.*

# *The Lexicon and Morphotactics*

- *A lexicon is a repository for words.*
  - *The simplest one would consist of an explicit list of every word of the language.*
    - *Inconvenient or impossible!*
- *Computational lexicons are usually structured with*
  - *a list of each of the stems and*
  - *Affixes of the language together with a representation of morphotactics telling us how they can fit together.*
- *The most common way of modeling morphotactics is the finite-state automaton.*

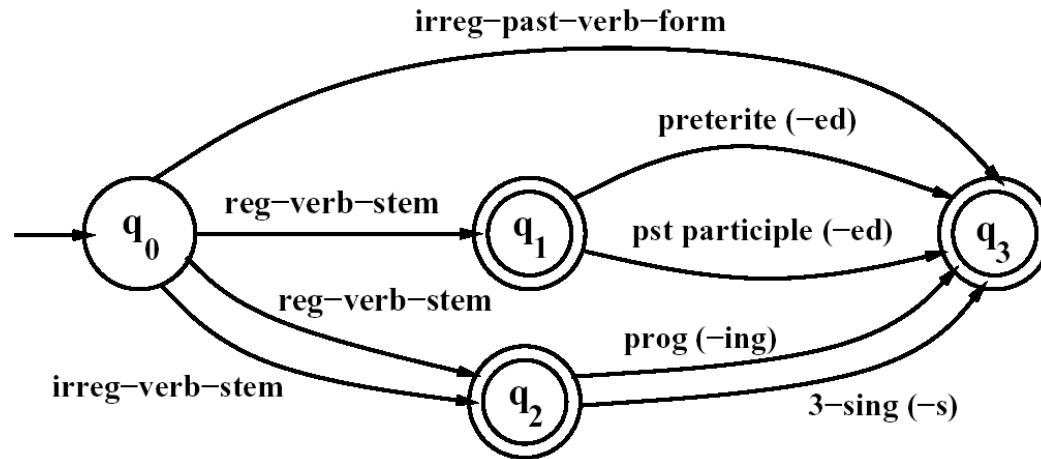
# *An FSA for English nominal inflection*



<b>Reg-noun</b>	<b>Irreg-pl-noun</b>	<b>Irreg-sg-noun</b>	<b>plural</b>
fox	geese	goose	-s
fat	sheep	sheep	
fog	Mice	mouse	
fardvark			

## 3.2 Finite-State Morphological Parsing

### *The Lexicon and Morphotactics*

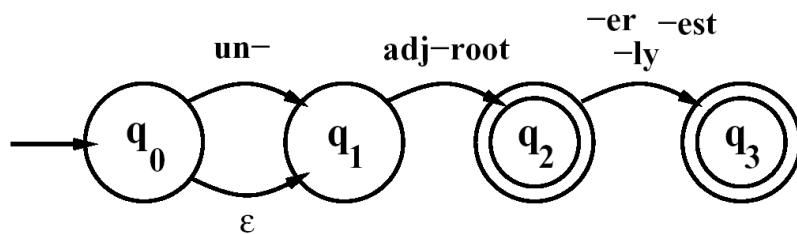


*An FSA for English verbal inflection*

Reg-verb-stem	Irreg-verb-stem	Irreg-past-verb	past	Past-part	Pres-part	3sg
walk fry talk impeach	cut speak sing sang spoken	caught ate eaten	-ed	-ed	-ing	-s

# The Lexicon and Morphotactics

- *English derivational morphology is more complex than English inflectional morphology, and so automata of modeling English derivation tends to be quite complex.*
  - *Some even based on CFG*
- *A small part of morphosyntactics of English adjectives*



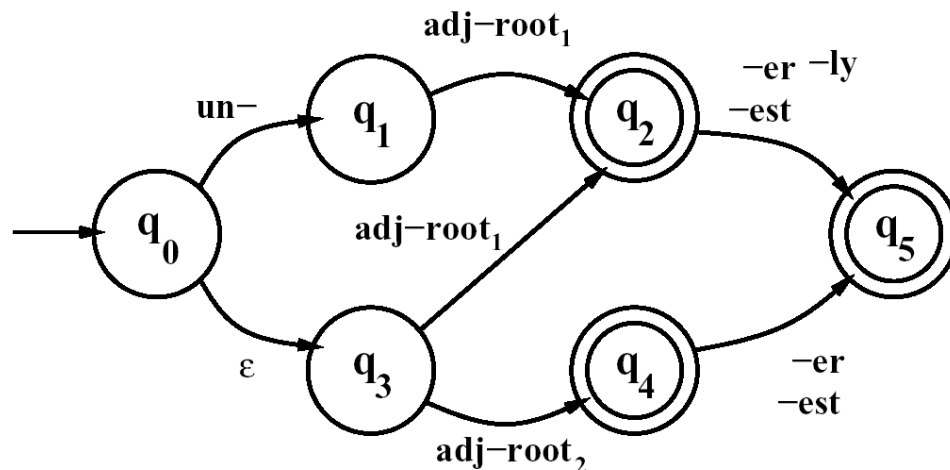
*An FSA for a fragment of English adjective Morphology #1*

big, bigger, biggest  
cool, cooler, coolest, coolly  
red, redder, reddest  
clear, clearer, clearest, clearly, unclear, unclearly  
happy, happier, happiest, happily  
unhappy, unhappier, unhappiest, unhappily  
real, unreal, really



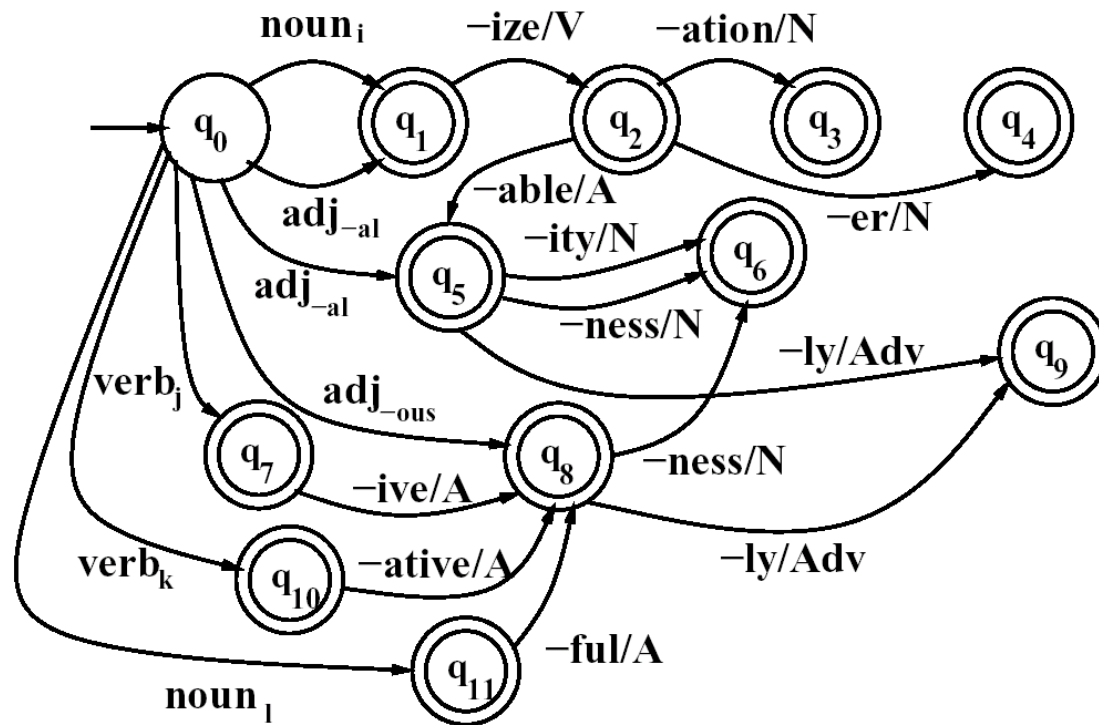
# Finite-State Morphological Parsing

- The FSA#1 recognizes all the listed adjectives, and ungrammatical forms like *unbig*, *redly*, and *realest*.
- Thus #1 is revised to become #2.
- The complexity is expected from English derivation.



*An FSA for a fragment of English adjective Morphology #2*

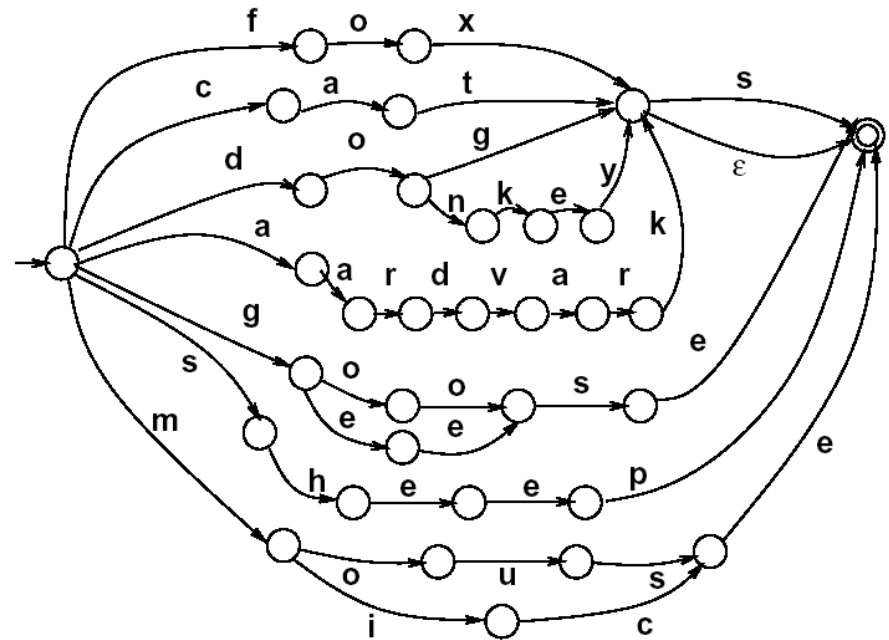
# Finite-State Morphological Parsing



*An FSA for another fragment of English derivational morphology*

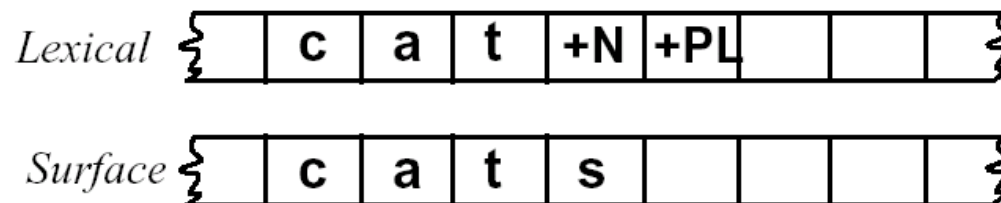
# Finite-State Morphological Parsing

- We can now use these FSAs to solve the problem of **morphological recognition**:
  - Determining whether an input string of letters makes up a legitimate English word or not
  - We do this by taking the morphotactic FSAs, and plugging in each “sub-lexicon” into the FSA.
  - The resulting FSA can then be defined as the level of the individual letter.



# Morphological Parsing with FST

- Given the input, for example, *cats*, we would like to produce *cat +N +PL*.
- Two-level morphology, by Koskenniemi (1983)
  - Representing a word as a correspondence between a *lexical level*
    - Representing a simple concatenation of morphemes making up a word, and
  - The *surface level*
    - Representing the actual spelling of the final word.
- Morphological parsing is implemented by building mapping rules that maps letter sequences like *cats* on the surface level into morpheme and features sequence like *cat +N +PL* on the lexical level.



# *Morphological Parsing with FST*

- *The automaton we use for performing the mapping between these two levels is the **finite-state transducer** or **FST**.*
  - *A transducer maps between one set of symbols and another;*
  - *An FST does this via a finite automaton.*
- *Thus an FST can be seen as a two-tape automaton which **recognizes** or **generates pairs** of strings.*
- *The FST has a more general function than an FSA:*
  - *An FSA defines a formal language*
  - *An FST defines a relation between sets of strings.*
- *Another view of an FST:*
  - *A machine reads one string and generates another.*

# *Morphological Parsing with FST*

- ***FST as recognizer:***
  - *a transducer that takes a pair of strings as input and output accept if the string-pair is in the string-pair language, and a reject if it is not.*
- ***FST as generator:***
  - *a machine that outputs pairs of strings of the language. Thus the output is a yes or no, and a pair of output strings.*
- ***FST as transducer:***
  - *A machine that reads a string and outputs another string.*
- ***FST as set relater:***
  - *A machine that computes relation between sets.*

# *Morphological Parsing with FST*

- *A formal definition of FST (based on the **Mealy machine** extension to a simple FSA):*
  - *$Q$ : a finite set of  $N$  states  $q_0, q_1, \dots, q_N$*
  - *$\Sigma$ : a finite alphabet of complex symbols. Each complex symbol is composed of an input-output pair  $i : o$ ; one symbol  $I$  from an input alphabet  $I$ , and one symbol  $o$  from an output alphabet  $O$ , thus  $\Sigma \subseteq I \times O$ .  $I$  and  $O$  may each also include the epsilon symbol  $\epsilon$ .*
  - *$q_0$ : the start state*
  - *$F$ : the set of final states,  $F \subseteq Q$*
  - *$\delta(q, i:o)$ : the transition function or transition matrix between states. Given a state  $q \in Q$  and complex symbol  $i:o \in \Sigma$ ,  $\delta(q, i:o)$  returns a new state  $q' \in Q$ .  $\delta$  is thus a relation from  $Q \times \Sigma$  to  $Q$ .*

# *Morphological Parsing with FST*

- *FSAs are isomorphic to regular languages, FSTs are isomorphic to **regular relations**.*
  - *Regular relations are sets of pairs of strings, a natural extension of the regular language, which are sets of strings.*
- *FSTs are closed under union, but generally they are not closed under difference, complementation, and intersection.*
- *Two useful closure properties of FSTs:*
  - **Inversion:** *If  $T$  maps from  $I$  to  $O$ , then the inverse of  $T$ ,  $T^{-1}$  maps from  $O$  to  $I$ .*
  - **Composition:** *If  $T_1$  is a transducer from  $I_1$  to  $O_1$  and  $T_2$  a transducer from  $I_2$  to  $O_2$ , then  $T_1 \circ T_2$  maps from  $I_1$  to  $O_2$*



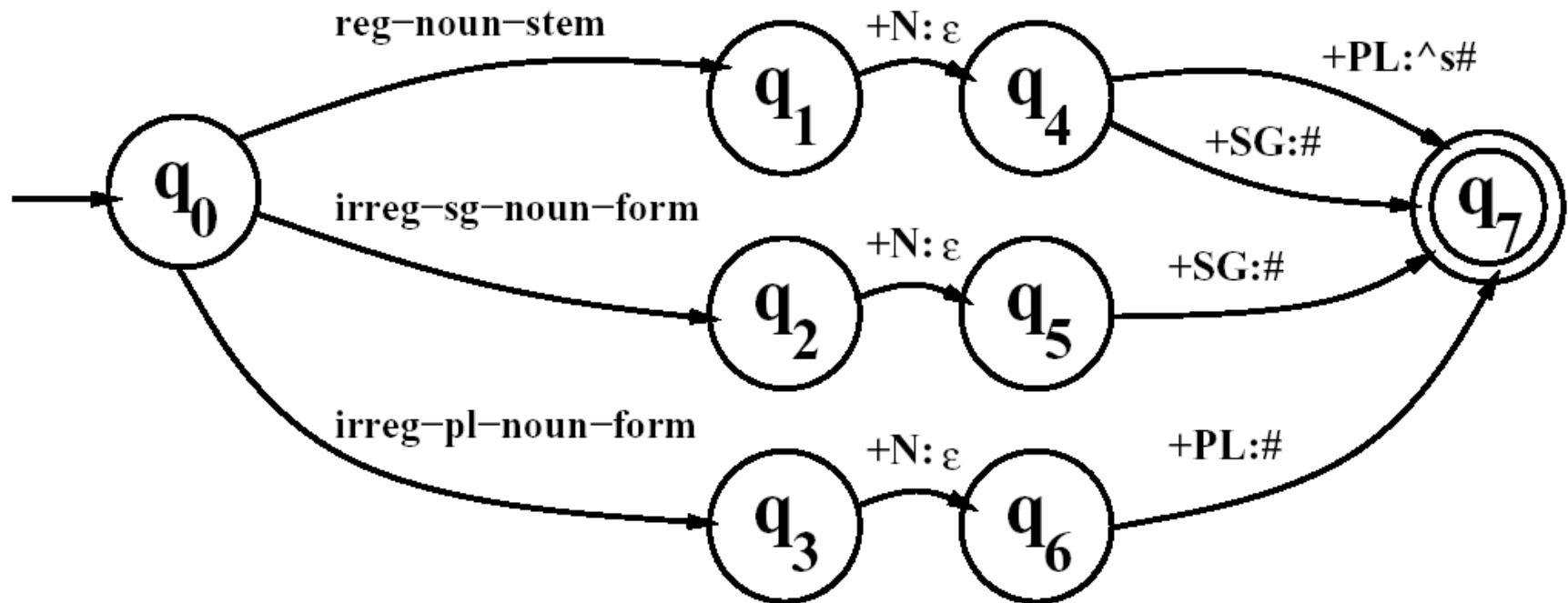
# *Morphological Parsing with FST*

- *Inversion is useful because it makes it easy to convert a FST-as-parser into an FST-as-generator.*
- *Composition is useful because it allows us to take two transducers than run in series and replace them with one complex transducer.*
  - $T_1 \circ T_2(S) = T_2(T_1(S))$

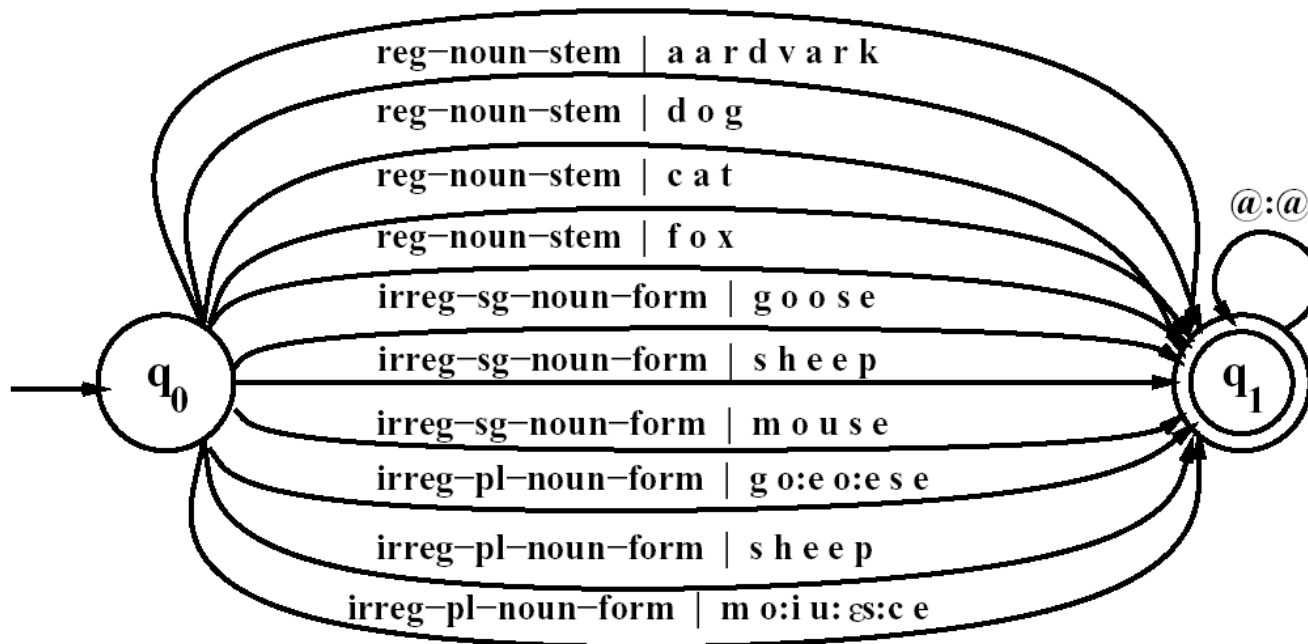
Reg-noun	Irreg-pl-noun	Irreg-sg-noun
fox	g o:e o:e s e	goose
fat	sheep	sheep
fog	m o:i u:es:c e	mouse
aardvark		

# *A transducer for English nominal number inflection*

$T_{num}$

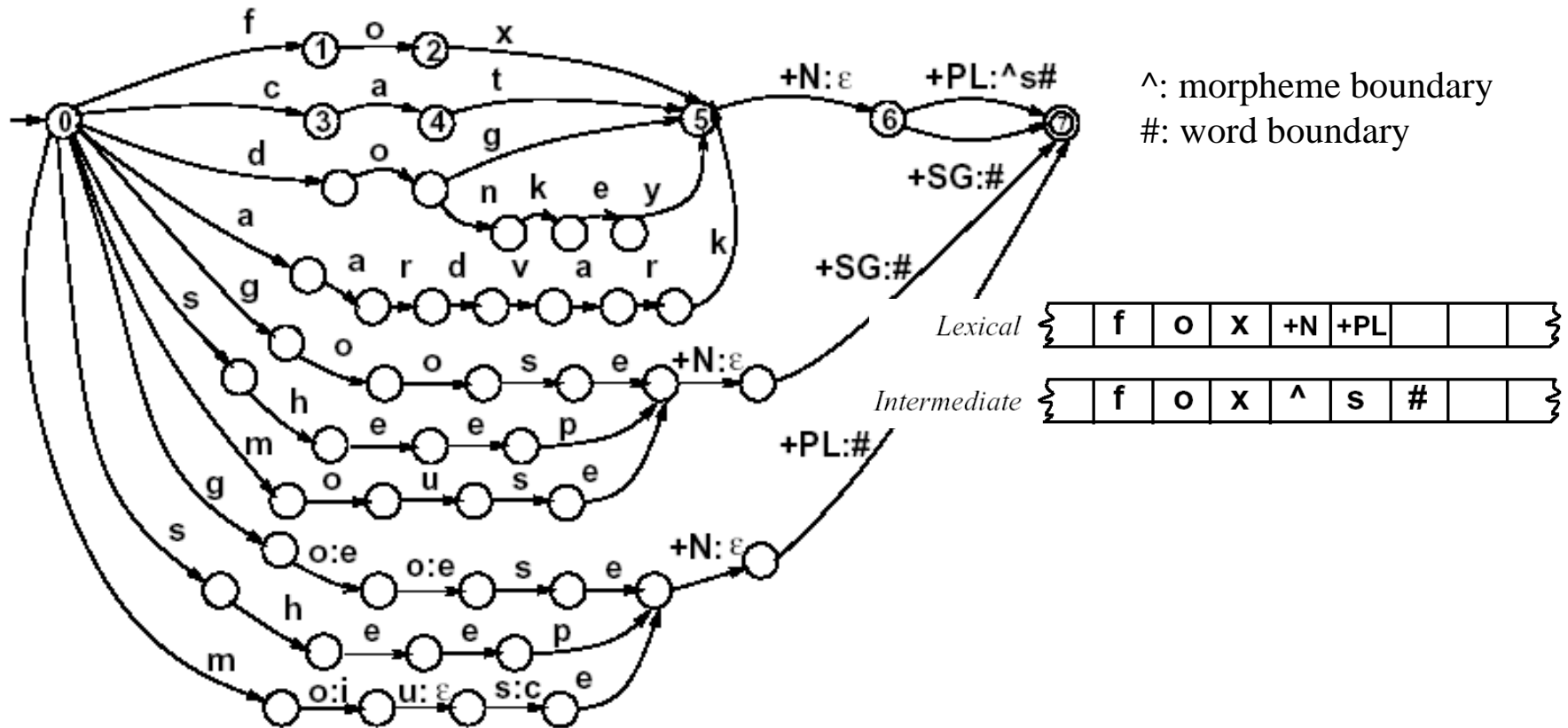


# Morphological Parsing with FST



The transducer  $T_{stems}$ , which maps roots to their root-class

# Morphological Parsing with FST



A fleshed-out English nominal inflection FST

$$T_{lex} = T_{num} \circ T_{stems}$$

# Orthographic Rules and FSTs

- *Spelling rules (or orthographic rules)*

Name	Description of Rule	Example
Consonant doubling	1-letter consonant doubled before <i>-ing/-ed</i>	beg/begging
E deletion	Silent e dropped before <i>-ing</i> and <i>-ed</i>	make/making
E insertion	e added after <i>-s, -z, -x, -ch, -sh</i> , before <i>-s</i>	watch/watches
Y replacement	<i>-y</i> changes to <i>-ie</i> before <i>-s, -i</i> before <i>-ed</i>	try/tries
K insertion	Verb ending with <i>vowel + -c</i> add <i>-k</i>	panic/panicked

- These spelling changes can be thought as taking as input a simple concatenation of morphemes and producing as output a slightly-modified concatenation of morphemes.

*Lexical*    { f | o | x | +N | +PL |   |   | }

*Intermediate*    { f | o | x | ^ | s | # |   | }

*Surface*    { f | o | x | e | s |   |   | }

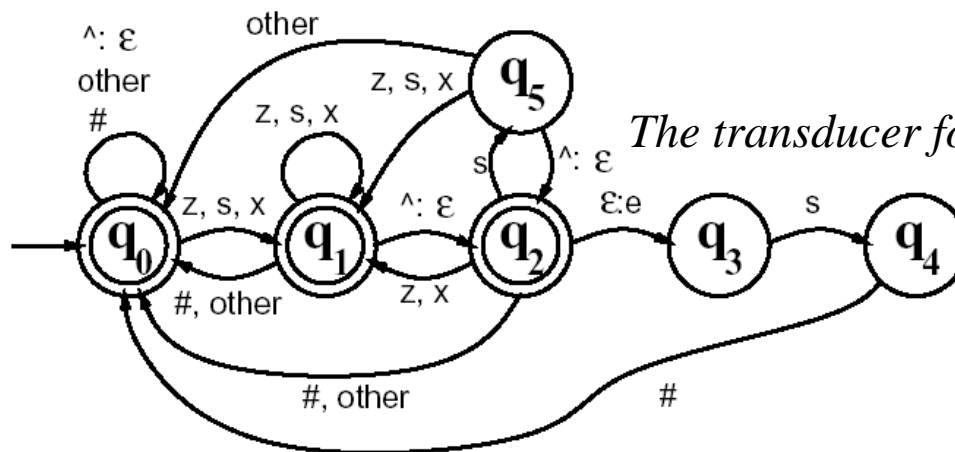
# Orthographic Rules and FSTs

- “insert an *e* on the surface tape just when the lexical tape has a morpheme ending in *x* (or *z*, etc) and the next morphemes is *-s*”

$$\varepsilon \rightarrow e / \left\{ \begin{array}{c} x \\ s \\ z \end{array} \right\} \_ \wedge s \#$$

- “rewrite *a* as *b* when it occurs between *c* and *d*”  
 $a \rightarrow b / c \_ d$

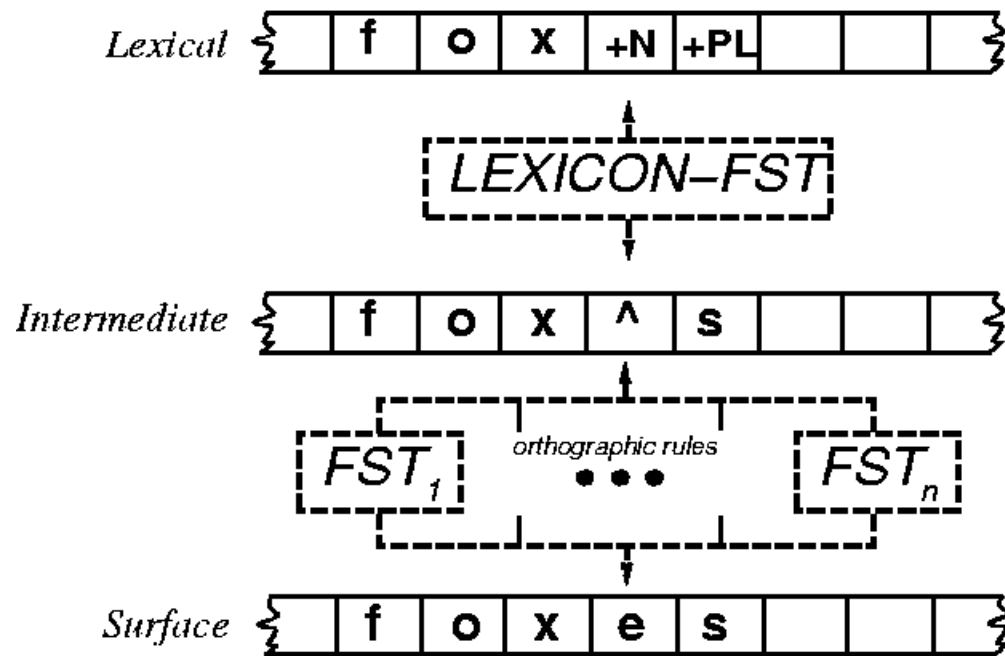
# Orthographic Rules and FSTs



*The transducer for the E-insertion rule*

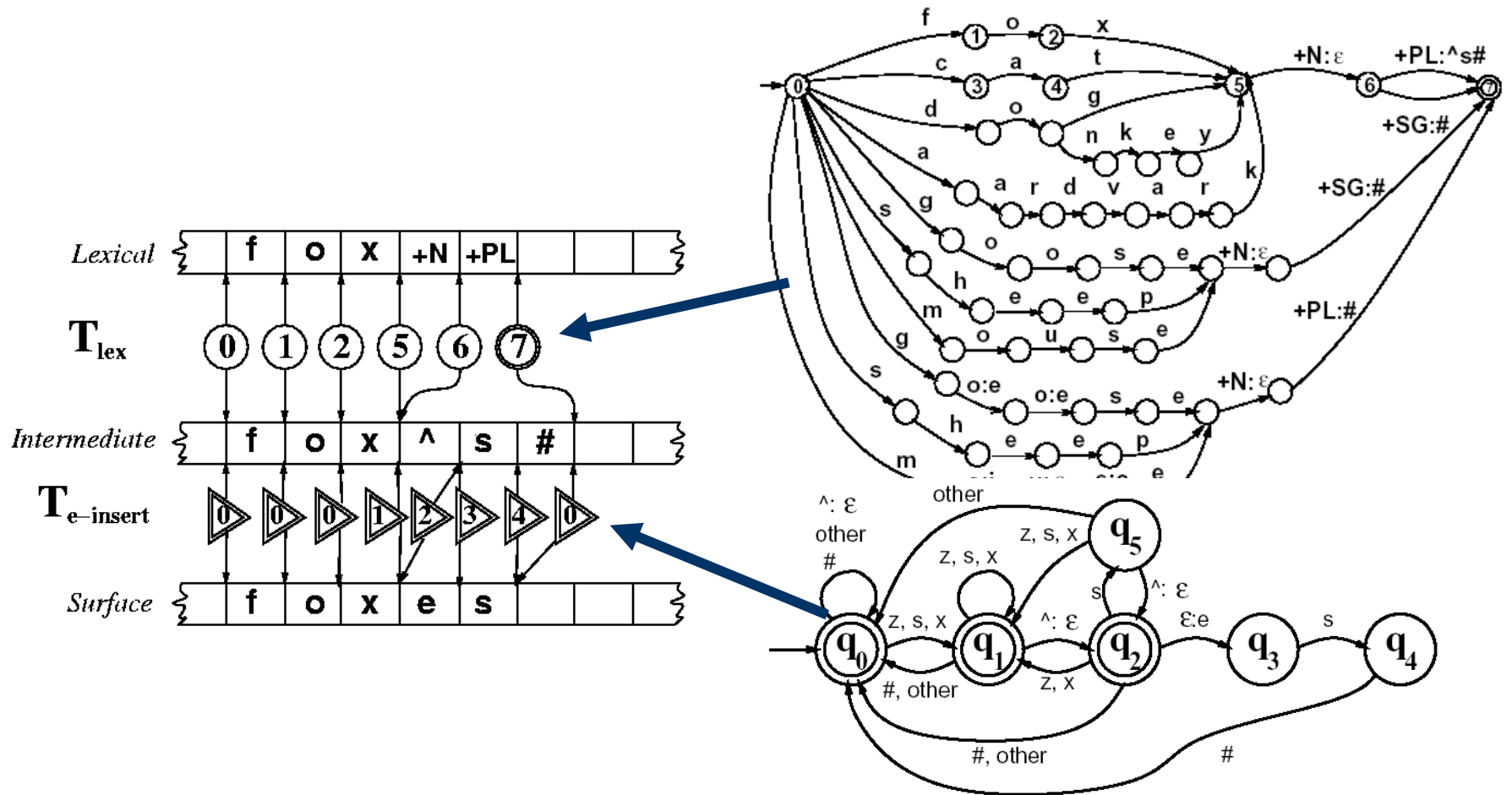
State \ Input	s : s	x : x	z : z	^: ε	ε: e	#	other
$q_0$ :	1	1	1	0	-	0	0
$q_1$ :	1	1	1	2	-	0	0
$q_2$ :	5	1	1	0	3	0	0
$q_3$ :	4	-	-	-	-	-	-
$q_4$ :	-	-	-	-	-	0	-
$q_5$ :	1	1	1	2	-	-	0

# Combining FST Lexicon and Rules





# Combining FST Lexicon and Rules



# *Combining FST Lexicon and Rules*

- *The power of FSTs is that the exact same cascade with the same state sequences is used*
  - *when machine is generating the surface form from the lexical tape, or*
  - *When it is parsing the lexical tape from the surface tape.*
- *Parsing can be slightly more complicated than generation, because of the problem of **ambiguity**.*
  - *For example, foxes could be fox +V +3SG as well as fox +N +PL*

# *Lexicon-Free FSTs: the Porter Stemmer*

- *Information retrieval*
- *One of the mostly widely used **stemming** algorithms is the simple and efficient Porter (1980) algorithm, which is based on a series of simple cascaded rewrite rules.*
  - *ATIONAL → ATE (e.g., relational → relate)*
  - *ING →  $\epsilon$ if stem contains vowel (e.g., motoring → motor)*
- *Problem:*
  - *Not perfect: error of commision, omission*
- *Experiments have been made*
  - *Some improvement with smaller documents*
  - *Any improvement is quite small*