## hw4

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# 1 COMPSCI-589 HW4: Neural Network

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```
[]: from evaluationmatrix import *
from utils import *
from neuralnetwork import *
from stratified import *
from run import *
import matplotlib.pyplot as plt
```

```
[]: housedata, housecategory = importhousedata()
  winedata, winecategory = importwinedata()
  cancerdata, cancercategory = importcancerdata()
  cmcdata,cmccategory = importcmcdata()
```

### 1.0.1 EXAMPLES

place holder for new page.

```
[]: #
      #
       #
       #
       #
       #
       #
       #
       #
       #
       #
       #
       #
       #
      #
      #
```

#

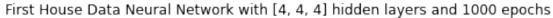
### 1.1 EXPERIMENTS & ANALYSES

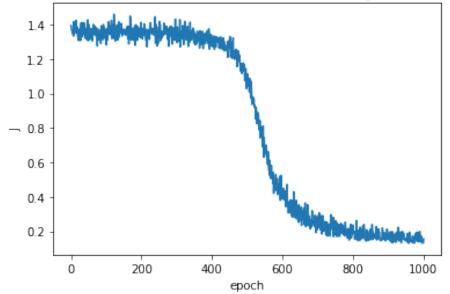
#### 1.1.1 House Data

Trained with MiniBatch, vectorized neural network, divided to 3 group, (batchsize = 435/3 = 145) (I named the minibatchk to the batches I want to divided to.)

```
[]: hiddenlayerparemeter = [4,4,4]
    epoch = 1000
[]: listoflistofoutputs, acc, listofjlist = kfoldcrossvalidneuralnetwork(housedata,
      housecategory, hiddenlayerparemeter, k = 5, minibatchk = 3, lambda_reg = 0.
      41, learning rate = 0.1, epsilon 0 = 0.0001, softstop = epoch, printq = False)
    fold 1 training in progress
    fold 1 training completed, accuracy = 0.9204545454545454
    fold 2 training in progress
    fold 2 training completed, accuracy = 0.9318181818181818
    fold 3 training in progress
    fold 3 training completed, accuracy = 0.9425287356321839
    fold 4 training in progress
    fold 4 training completed, accuracy = 0.9883720930232558
    fold 5 training in progress
    fold 5 training completed, accuracy = 0.9767441860465116
[]: accuarcy_, precision_, recall_, fscore_house_1=_
     meanevaluation(listoflistofoutputs,1)
    print("First House Data Neural Network with " + str(hiddenlayerparemeter) + "__
      ⇔hidden layers and " + str(epoch) + " epochs")
    print("accuracy:", acc)
    print("fscore:", fscore house 1)
    plt.plot(range(epoch+1), listofjlist[1])
    plt.xlabel("epoch")
    plt.ylabel("J")
    plt.title("First House Data Neural Network with " + str(hiddenlayerparemeter) + ∪
     →" hidden layers and " + str(epoch) + " epochs")
    plt.show()
```

First House Data Neural Network with [4, 4, 4] hidden layers and 1000 epochs accuracy: 0.9519835483949357 fscore: 0.9385771973545435

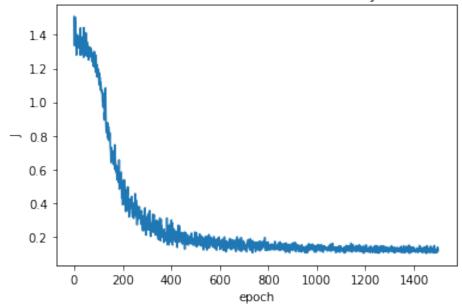




```
[]: hiddenlayerparemeter = [4,4]
    epoch = 1500
    listoflistofoutputs1_2, acc1_2, listofjlist1_2 = __
     ⇒kfoldcrossvalidneuralnetwork(housedata, housecategory, hiddenlayerparemeter,
     ⇔0001, softstop = epoch, printq = False)
    fold 1 training in progress
    fold 1 training completed, accuracy = 1.0
    fold 2 training in progress
    fold 2 training completed, accuracy = 0.9090909090909091
    fold 3 training in progress
    fold 3 training completed, accuracy = 0.9772727272727273
    fold 4 training in progress
    fold 4 training completed, accuracy = 0.9545454545454546
    fold 5 training in progress
    fold 5 training completed, accuracy = 0.9318181818181818
    fold 6 training in progress
    fold 6 training completed, accuracy = 0.9772727272727273
    fold 7 training in progress
    fold 7 training completed, accuracy = 0.9772727272727273
    fold 8 training in progress
    fold 8 training completed, accuracy = 1.0
    fold 9 training in progress
    fold 9 training completed, accuracy = 0.9285714285714286
    fold 10 training in progress
    fold 10 training completed, accuracy = 0.9761904761904762
```

First House Data Neural Network with [4, 4] hidden layers and 1500 epochs accuracy: 0.9632034632034632 fscore: 0.9513545046562125

First House Data Neural Network with [4, 4] hidden layers and 1500 epochs

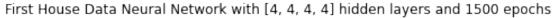


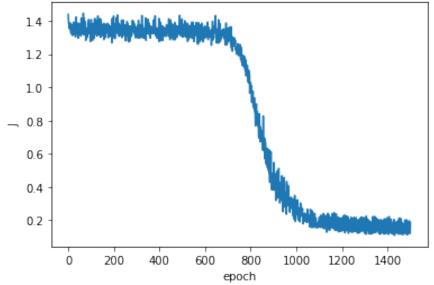
fold 1 training in progress
fold 1 training completed, accuracy = 0.97727272727272727

```
fold 2 training in progress
    fold 2 training completed, accuracy = 0.9545454545454546
    fold 3 training in progress
    fold 3 training completed, accuracy = 0.8409090909090909
    fold 4 training in progress
    fold 4 training completed, accuracy = 0.6136363636363636
    fold 5 training in progress
    fold 5 training completed, accuracy = 0.6136363636363636
    fold 6 training in progress
    fold 6 training completed, accuracy = 0.6136363636363636
    fold 7 training in progress
    fold 7 training completed, accuracy = 0.6136363636363636
    fold 8 training in progress
    fold 8 training completed, accuracy = 0.9767441860465116
    fold 9 training in progress
    fold 9 training completed, accuracy = 0.6190476190476191
    fold 10 training in progress
    fold 10 training completed, accuracy = 0.9285714285714286
[]: accuarcy1_3, precision1_3, recall1_3, fscore_house1_3=__
     meanevaluation(listoflistofoutputs1_3,1)
    print("First House Data Neural Network with " + str(hiddenlayerparemeter) + "
      ⇔hidden layers and " + str(epoch) + " epochs")
    print("accuracy:", acc1_3)
    print("fscore:", fscore_house1_3)
    plt.plot(range(epoch+1), listofjlist1_3[1])
    plt.xlabel("epoch")
    plt.ylabel("J")
    plt.title("First House Data Neural Network with " + str(hiddenlayerparemeter) +
     →" hidden layers and " + str(epoch) + " epochs")
    plt.show()
```

First House Data Neural Network with [4, 4, 4, 4] hidden layers and 1500 epochs accuracy: 0.7751635960938288

fscore: 0.45981240981240984





```
fold 1 training in progress
fold 1 training completed, accuracy = 1.0
fold 2 training in progress
fold 2 training completed, accuracy = 0.9318181818181818
fold 3 training in progress
fold 3 training completed, accuracy = 0.9545454545454546
fold 4 training in progress
fold 4 training completed, accuracy = 0.9772727272727273
fold 5 training in progress
fold 5 training completed, accuracy = 0.9318181818181818
fold 6 training in progress
fold 6 training completed, accuracy = 0.9772727272727273
fold 7 training in progress
fold 7 training completed, accuracy = 0.9318181818181818
fold 8 training in progress
fold 8 training completed, accuracy = 0.9302325581395349
fold 9 training in progress
fold 9 training completed, accuracy = 1.0
fold 10 training in progress
fold 10 training completed, accuracy = 0.9761904761904762
```

```
[]: accuarcy1_4, precision1_4, recall1_4, fscore_house1_4=_

→meanevaluation(listoflistofoutputs1_4,1)

print("First House Data Neural Network with " + str(hiddenlayerparemeter) + "__

→hidden layers and " + str(epoch) + " epochs")

print("accuracy:", acc1_4)

print("fscore:", fscore_house1_4)

plt.plot(range(epoch+1), listofjlist1_4[1])

plt.xlabel("epoch")

plt.ylabel("J")

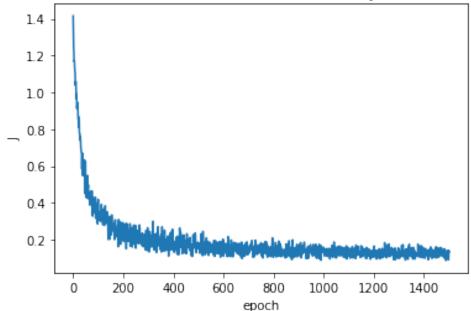
plt.title("First House Data Neural Network with " + str(hiddenlayerparemeter) +__

→" hidden layers and " + str(epoch) + " epochs")

plt.show()
```

First House Data Neural Network with [4] hidden layers and 1500 epochs accuracy: 0.9610968488875467 fscore: 0.9490942256668063

First House Data Neural Network with [4] hidden layers and 1500 epochs

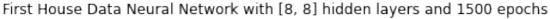


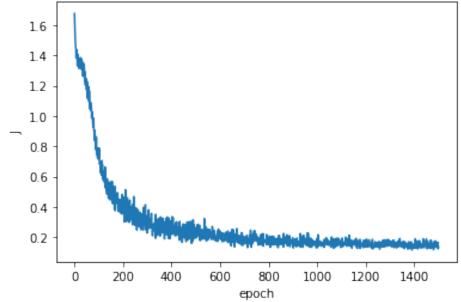
fold 1 training in progress
fold 1 training completed, accuracy = 0.97727272727272727

```
fold 2 training in progress
    fold 2 training completed, accuracy = 1.0
    fold 3 training in progress
    fold 3 training completed, accuracy = 0.8636363636363636
    fold 4 training in progress
    fold 4 training completed, accuracy = 0.8636363636363636
    fold 5 training in progress
    fold 5 training completed, accuracy = 0.9545454545454546
    fold 6 training in progress
    fold 6 training completed, accuracy = 0.9772727272727273
    fold 7 training in progress
    fold 7 training completed, accuracy = 0.9318181818181818
    fold 8 training in progress
    fold 8 training completed, accuracy = 0.9767441860465116
    fold 9 training in progress
    fold 9 training completed, accuracy = 1.0
    fold 10 training in progress
    fold 10 training completed, accuracy = 1.0
[]: accuarcy1_5, precision1_5, recall1_5, fscore_house1_5=_
     →meanevaluation(listoflistofoutputs1_5,1)
    print("First House Data Neural Network with " + str(hiddenlayerparemeter) + "
      ⇔hidden layers and " + str(epoch) + " epochs")
    print("accuracy:", acc1_5)
    print("fscore:", fscore_house1_5)
    plt.plot(range(epoch+1), listofjlist1_5[1])
    plt.xlabel("epoch")
    plt.ylabel("J")
    plt.title("First House Data Neural Network with " + str(hiddenlayerparemeter) + ⊔
     →" hidden layers and " + str(epoch) + " epochs")
    plt.show()
```

First House Data Neural Network with [8, 8] hidden layers and 1500 epochs

accuracy: 0.954492600422833 fscore: 0.9424683812919106





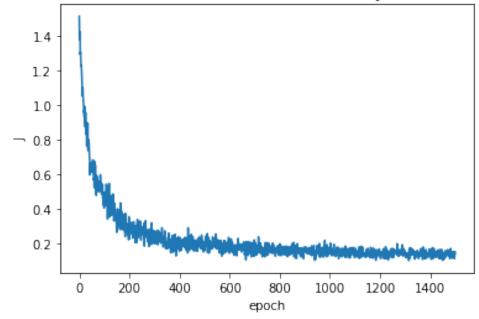
```
fold 1 training in progress
fold 1 training completed, accuracy = 1.0
fold 2 training in progress
fold 2 training completed, accuracy = 0.9545454545454546
fold 3 training in progress
fold 3 training completed, accuracy = 0.9772727272727273
fold 4 training in progress
fold 4 training completed, accuracy = 0.93181818181818
fold 5 training in progress
fold 5 training completed, accuracy = 0.9772727272727273
fold 6 training in progress
fold 6 training completed, accuracy = 0.9772727272727273
fold 7 training in progress
fold 7 training completed, accuracy = 0.8863636363636364
fold 8 training in progress
fold 8 training completed, accuracy = 0.9534883720930233
fold 9 training in progress
fold 9 training completed, accuracy = 0.9523809523809523
fold 10 training in progress
```

fold 10 training completed, accuracy = 1.0

First House Data Neural Network with [8] hidden layers and 1500 epochs

accuracy: 0.961041477901943 fscore: 0.9477564986287096

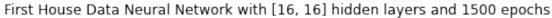
### First House Data Neural Network with [8] hidden layers and 1500 epochs

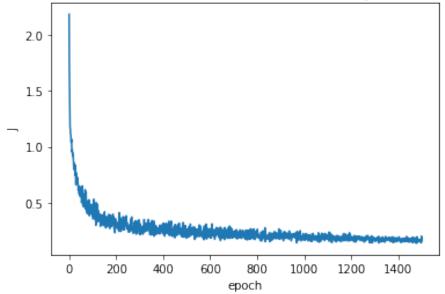


```
fold 1 training in progress
    fold 1 training completed, accuracy = 0.9545454545454546
    fold 2 training in progress
    fold 2 training completed, accuracy = 0.9318181818181818
    fold 3 training in progress
    fold 3 training completed, accuracy = 0.9545454545454546
    fold 4 training in progress
    fold 4 training completed, accuracy = 0.9772727272727273
    fold 5 training in progress
    fold 5 training completed, accuracy = 0.9090909090909091
    fold 6 training in progress
    fold 6 training completed, accuracy = 0.9772727272727273
    fold 7 training in progress
    fold 7 training completed, accuracy = 1.0
    fold 8 training in progress
    fold 8 training completed, accuracy = 0.9302325581395349
    fold 9 training in progress
    fold 9 training completed, accuracy = 0.9523809523809523
    fold 10 training in progress
    fold 10 training completed, accuracy = 1.0
[]: accuarcy1_7, precision1_7, recall1_7, fscore_house1_7=_
     meanevaluation(listoflistofoutputs1_7,1)
    print("First House Data Neural Network with " + str(hiddenlayerparemeter) + " |
     ⇔hidden layers and " + str(epoch) + " epochs")
    print("accuracy:", acc1_7)
    print("fscore:", fscore_house1_7)
    plt.plot(range(epoch+1), listofjlist1 7[1])
    plt.xlabel("epoch")
    plt.ylabel("J")
    plt.title("First House Data Neural Network with " + str(hiddenlayerparemeter) + ⊔
     plt.show()
```

First House Data Neural Network with [16, 16] hidden layers and 1500 epochs accuracy: 0.9587158965065943

fscore: 0.9472877623612916

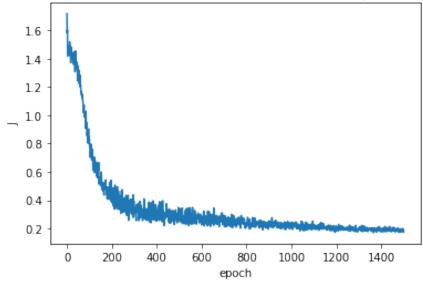




```
[]: hiddenlayerparemeter = [16,16,16]
    epoch = 1500
    listoflistofoutputs1_8, acc1_8, listofjlist1_8 = __
     ⇒kfoldcrossvalidneuralnetwork(housedata, housecategory, hiddenlayerparemeter,
      ⇒k = 10, minibatchk = 3, lambda_reg = 0.1, learning_rate = 0.09, epsilon_0 =
      ⇔0.0001, softstop = epoch, printq = False)
    fold 1 training in progress
    fold 1 training completed, accuracy = 0.9318181818181818
    fold 2 training in progress
    fold 2 training completed, accuracy = 0.9545454545454546
    fold 3 training in progress
    fold 3 training completed, accuracy = 1.0
    fold 4 training in progress
    fold 4 training completed, accuracy = 0.9545454545454546
    fold 5 training in progress
    fold 5 training completed, accuracy = 0.9545454545454546
    fold 6 training in progress
    fold 6 training completed, accuracy = 0.9318181818181818
    fold 7 training in progress
    fold 7 training completed, accuracy = 0.9090909090909091
    fold 8 training in progress
    fold 8 training completed, accuracy = 0.9767441860465116
    fold 9 training in progress
    fold 9 training completed, accuracy = 0.9761904761904762
    fold 10 training in progress
    fold 10 training completed, accuracy = 0.9761904761904762
```

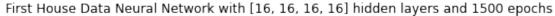
First House Data Neural Network with [16, 16, 16] hidden layers and 1500 epochs accuracy: 0.9565488774791101 fscore: 0.9442298869694508

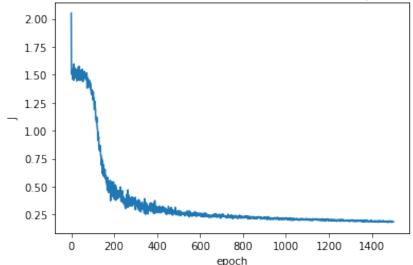
First House Data Neural Network with [16, 16, 16] hidden layers and 1500 epochs



```
fold 3 training in progress
    fold 3 training completed, accuracy = 1.0
    fold 4 training in progress
    fold 4 training completed, accuracy = 0.9545454545454546
    fold 5 training in progress
    fold 5 training completed, accuracy = 0.9545454545454546
    fold 6 training in progress
    fold 6 training completed, accuracy = 0.9318181818181818
    fold 7 training in progress
    fold 7 training completed, accuracy = 0.9318181818181818
    fold 8 training in progress
    fold 8 training completed, accuracy = 1.0
    fold 9 training in progress
    fold 9 training completed, accuracy = 0.9523809523809523
    fold 10 training in progress
    fold 10 training completed, accuracy = 0.9523809523809523
[]: accuracy1_9, precision1_9, recall1_9, fscore_house1_9=_
     →meanevaluation(listoflistofoutputs1_9,1)
    print("First House Data Neural Network with " + str(hiddenlayerparemeter) + "__
      ⇔hidden layers and " + str(epoch) + " epochs")
    print("accuracy:", acc1_9)
    print("fscore:", fscore_house1_9)
    plt.plot(range(epoch+1), listofjlist1_9[1])
    plt.xlabel("epoch")
    plt.ylabel("J")
    plt.title("First House Data Neural Network with " + str(hiddenlayerparemeter) +
     →" hidden layers and " + str(epoch) + " epochs")
    plt.show()
    First House Data Neural Network with [16, 16, 16, 16] hidden layers and 1500
```

accuracy: 0.9541125541125541 fscore: 0.9410304727951788





```
epoch = 1500
listoflistofoutputs1_10, acc1_10, listofjlist1_10 =
 ⇔kfoldcrossvalidneuralnetwork(housedata, housecategory, hiddenlayerparemeter, ⊔
 ⇒k = 10, minibatchk = 3, lambda_reg = 0.1, learning_rate = 0.1, epsilon_0 = 0.
 ⇔0001, softstop = epoch, printq = False)
fold 1 training in progress
fold 1 training completed, accuracy = 0.9545454545454546
fold 2 training in progress
fold 2 training completed, accuracy = 1.0
fold 3 training in progress
fold 3 training completed, accuracy = 1.0
fold 4 training in progress
fold 4 training completed, accuracy = 0.9545454545454546
fold 5 training in progress
fold 5 training completed, accuracy = 0.9545454545454546
fold 6 training in progress
fold 6 training completed, accuracy = 0.9545454545454546
fold 7 training in progress
fold 7 training completed, accuracy = 0.9772727272727273
```

fold 8 training completed, accuracy = 0.9069767441860465

fold 9 training completed, accuracy = 0.9523809523809523

fold 10 training completed, accuracy = 0.9285714285714286

[]: hiddenlayerparemeter = [2]

fold 8 training in progress

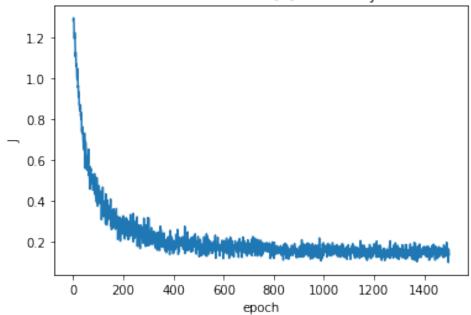
fold 9 training in progress

fold 10 training in progress

First House Data Neural Network with [2] hidden layers and 1500 epochs accuracy: 0.9583383670592973

fscore: 0.9472742127153891

## First House Data Neural Network with [2] hidden layers and 1500 epochs



House Data | Hidden Layers | (2) | (4) | (4,4) | (4,4,4) | (4,4,4) | (8) | (8,8) | (16,16) | (16,16,16) | (16,16,16) | | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | | Epoch | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500 | 1500

the learning rate of them are 0.09 and 0.1. (The only two 0.09 are the (16,16) and (16,16,16))

### Analysis of House Data

Discuss (on a high level) what contributed the most to improving performance: changing the regularization parameter; adding more layers; having deeper networks with many layers but few neurons per layer? designing networks with few layers but many neurons per layer? Discuss any patterns that you may have encountered. Also, discuss whether there is a point where constructing and training more "sophisticated"/complex networks—i.e., larger networks—no longer improves performance (or worsens performance).

Based on the analyses above, discuss which neural network architecture you would select if you had to deploy such a classifier in real life. Explain your reasoning.

**ANSWER - House Vote:** From this House Voting Data, most of them Have an accuracy around 0.9, except for the hidden layer [4,4,4,4] one. So that actually means the for this certain data, the increase in layer doesn't improve the accuracy, so this would means, the classification would be boundary could be easily with few neurons.

If we check on the table, we could find out that the best performance is from model with 2 hidden layers [4,4], with accuracy 0.9632 and F-score 0.9513, which also tell us, for this dataset, increasing the # of neurons per layer also doesn't increase the improvements a lot.

Indeed my assumption is that the data might even work well with logistic regression (that is, empty hidden layer[], directly calulate the output from input).

As for the graph, there are some interesting points. We can see that when the # of layer are at 1 or 2, the j graph is more 'smooth', that means it converge to a final weight without reaching and get stuck at some local minimum or so. (Heuristic might solve it but I didn't implement that)

Take a look of [16,16,16,16],[4,4,4,4],[16,16,16], we can see they've all been get to some local minimum stage, while others didn't or they escape from the local minimum very quick.

In real life, I will just use the [4,4] hidden layer, but maybe I will train using slightly smaller learning rate and more epochs so it converges better.

### 1.1.2 WINE Data

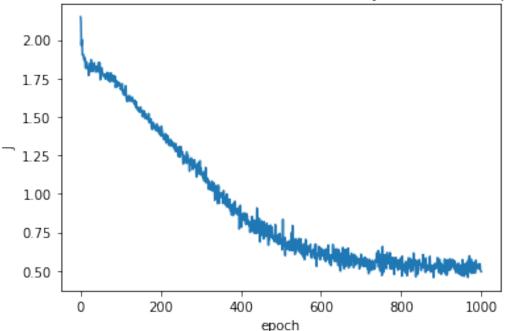
Trained with MiniBatch, vectorized neural network, divided to 3 group, (batchsize around 60)

```
fold 5 training in progress
   fold 5 training completed, accuracy = 1.0
   fold 6 training in progress
   fold 7 training in progress
   fold 7 training completed, accuracy = 1.0
   fold 8 training in progress
   fold 8 training completed, accuracy = 1.0
   fold 9 training in progress
   fold 9 training completed, accuracy = 0.9411764705882353
   fold 10 training in progress
   fold 10 training completed, accuracy = 1.0
[]: accuracy2_1, precision2_1, recall2_1, fscore_wine2_1=_
     →meanevaluation(listoflistofoutputs2_1,1)
    print("Wine Data Neural Network with " + str(hiddenlayerparemeter) + " hidden_u
     →layers and " + str(epoch) + " epochs")
    print("accuracy:", float("{0:.4f}". format(acc2 1)))
    print("fscore:", float("{0:.4f}". format(fscore_wine2_1)))
    plt.plot(range(epoch+1), listofjlist2_1[1])
    plt.xlabel("epoch")
    plt.ylabel("J")
    plt.title("Wine Data Neural Network with " + str(hiddenlayerparemeter) + "__
     ⇔hidden layers and " + str(epoch) + " epochs")
    plt.show()
```

Wine Data Neural Network with [2] hidden layers and 1000 epochs

accuracy: 0.983 fscore: 0.9818

# Wine Data Neural Network with [2] hidden layers and 1000 epochs

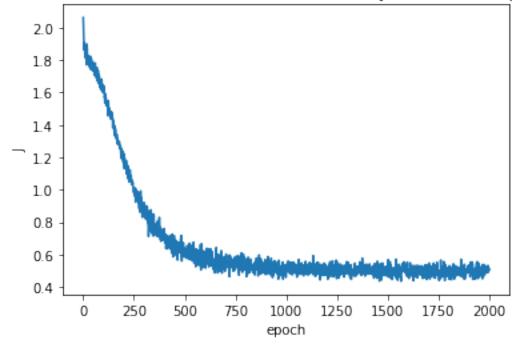


```
[]: hiddenlayerparemeter = [2]
    epoch = 2000
    listoflistofoutputs2_2, acc2_2, listofjlist2_2 =_
     ⇔kfoldcrossvalidneuralnetwork(winedata, winecategory, hiddenlayerparemeter, k⊔
     ⇒= 10, minibatchk = 3, lambda_reg = 0.1, learning_rate = 0.1, epsilon_0 = 0.
     ⇔0001, softstop = epoch, printq = False)
   fold 1 training in progress
   fold 1 training completed, accuracy = 0.9473684210526315
   fold 2 training in progress
   fold 2 training completed, accuracy = 1.0
   fold 3 training in progress
   fold 3 training completed, accuracy = 1.0
   fold 4 training in progress
   fold 5 training in progress
   fold 6 training in progress
   fold 6 training completed, accuracy = 1.0
   fold 7 training in progress
   fold 7 training completed, accuracy = 1.0
   fold 8 training in progress
   fold 8 training completed, accuracy = 1.0
   fold 9 training in progress
```

Wine Data Neural Network with [2] hidden layers and 2000 epochs

accuracy: 0.9836 fscore: 0.9818

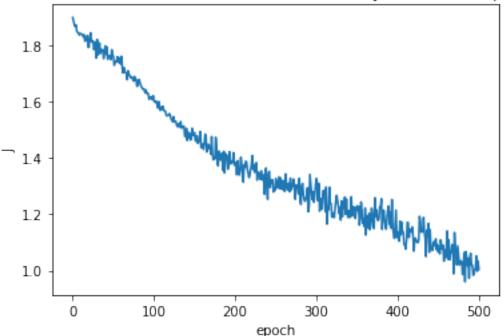
## Wine Data Neural Network with [2] hidden layers and 2000 epochs



```
[]: hiddenlayerparemeter = [2] epoch = 500
```

```
listoflistofoutputs2_3, acc2_3, listofjlist2_3 =__
     ⇒kfoldcrossvalidneuralnetwork(winedata, winecategory, hiddenlayerparemeter, k⊔
     = 10, minibatchk = 3, lambda reg = 0.1, learning rate = 0.1, epsilon_0 = 0.
     ⇔0001, softstop = epoch, printq = False)
   fold 1 training in progress
   fold 1 training completed, accuracy = 0.9473684210526315
   fold 2 training in progress
   fold 3 training in progress
   fold 4 training in progress
   fold 4 training completed, accuracy = 1.0
   fold 5 training in progress
   fold 6 training in progress
   fold 6 training completed, accuracy = 1.0
   fold 7 training in progress
   fold 7 training completed, accuracy = 1.0
   fold 8 training in progress
   fold 9 training in progress
   fold 9 training completed, accuracy = 0.9411764705882353
   fold 10 training in progress
   fold 10 training completed, accuracy = 1.0
[]: accuracy2_3, precision2_3, recall2_3, fscore_wine2_3=_
    →meanevaluation(listoflistofoutputs2_3,1)
    print("Wine Data Neural Network with " + str(hiddenlayerparemeter) + " hidden_⊔
     ⇔layers and " + str(epoch) + " epochs")
    print("accuracy:", float("{0:.4f}". format(acc2 3)))
    print("fscore:", float("{0:.4f}". format(fscore_wine2_3)))
    plt.plot(range(epoch+1), listofjlist2_3[1])
    plt.xlabel("epoch")
    plt.ylabel("J")
    plt.title("Wine Data Neural Network with " + str(hiddenlayerparemeter) + "__
     ⇔hidden layers and " + str(epoch) + " epochs")
    plt.show()
   Wine Data Neural Network with [2] hidden layers and 500 epochs
   accuracy: 0.9555
   fscore: 0.939
```

# Wine Data Neural Network with [2] hidden layers and 500 epochs



```
[]: hiddenlayerparemeter = [4,4]
    epoch = 1000
    listoflistofoutputs2_4, acc2_4, listofjlist2_4 = __
     ⊸kfoldcrossvalidneuralnetwork(winedata, winecategory, hiddenlayerparemeter, k<sub>□</sub>
    == 10, minibatchk = 3, lambda_reg = 0.1, learning_rate = 0.1, epsilon_0 = 0.
     ⇔0001, softstop = epoch, printq = False)
   fold 1 training in progress
   fold 1 training completed, accuracy = 1.0
   fold 2 training in progress
   fold 2 training completed, accuracy = 1.0
   fold 3 training in progress
   fold 4 training in progress
   fold 5 training in progress
   fold 5 training completed, accuracy = 0.722222222222222
   fold 6 training in progress
   fold 6 training completed, accuracy = 1.0
   fold 7 training in progress
   fold 8 training in progress
```

fold 8 training completed, accuracy = 1.0

fold 9 training in progress

Wine Data Neural Network with [4, 4] hidden layers and 1000 epochs

⇔hidden layers and " + str(epoch) + " epochs")

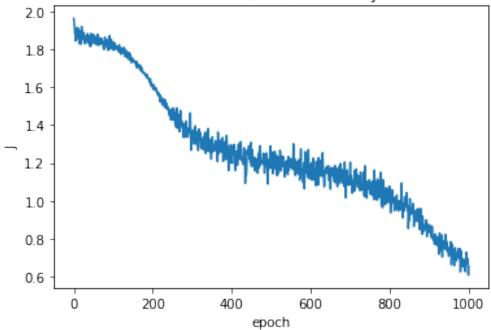
accuracy: 0.95 fscore: 0.979

plt.show()

plt.xlabel("epoch")
plt.ylabel("J")

Wine Data Neural Network with [4, 4] hidden layers and 1000 epochs

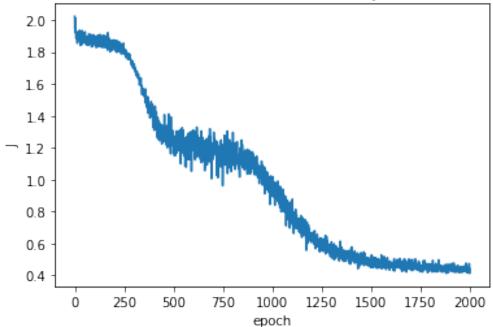
plt.title("Wine Data Neural Network with " + str(hiddenlayerparemeter) + "\_\_



```
[]: hiddenlayerparemeter = [4,4] epoch = 2000
```

```
listoflistofoutputs2_5, acc2_5, listofjlist2_5 =__
     ⇒kfoldcrossvalidneuralnetwork(winedata, winecategory, hiddenlayerparemeter, k⊔
     = 10, minibatchk = 3, lambda reg = 0.1, learning rate = 0.1, epsilon_0 = 0.
     ⇔0001, softstop = epoch, printq = False)
   fold 1 training in progress
   fold 1 training completed, accuracy = 1.0
   fold 2 training in progress
   fold 3 training in progress
   fold 3 training completed, accuracy = 1.0
   fold 4 training in progress
   fold 4 training completed, accuracy = 1.0
   fold 5 training in progress
   fold 5 training completed, accuracy = 1.0
   fold 6 training in progress
   fold 7 training in progress
   fold 8 training in progress
   fold 8 training completed, accuracy = 1.0
   fold 9 training in progress
   fold 9 training completed, accuracy = 1.0
   fold 10 training in progress
   fold 10 training completed, accuracy = 1.0
[]: accuracy2_5, precision2_5, recall2_5, fscore_wine2_5=_
     →meanevaluation(listoflistofoutputs2_5,1)
    print("Wine Data Neural Network with " + str(hiddenlayerparemeter) + " hidden_⊔
     slayers and " + str(epoch) + " epochs")
    print("accuracy:", float("{0:.4f}". format(acc2 5)))
    print("fscore:", float("{0:.4f}". format(fscore_wine2_5)))
    plt.plot(range(epoch+1), listofjlist2_5[1])
    plt.xlabel("epoch")
    plt.ylabel("J")
    plt.title("Wine Data Neural Network with " + str(hiddenlayerparemeter) + "__
     ⇔hidden layers and " + str(epoch) + " epochs")
    plt.show()
   Wine Data Neural Network with [4, 4] hidden layers and 2000 epochs
   accuracy: 0.9833
   fscore: 0.9779
```

## Wine Data Neural Network with [4, 4] hidden layers and 2000 epochs



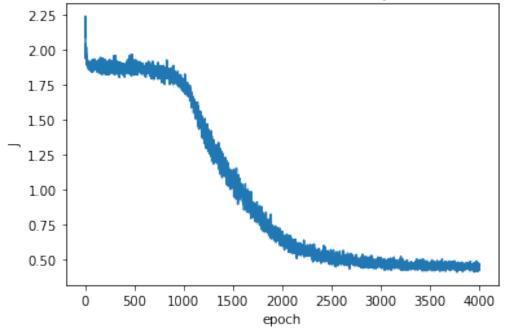
```
[]: hiddenlayerparemeter = [4,4]
    epoch = 4000
    listoflistofoutputs2_6, acc2_6, listofjlist2_6 = __
      \hookrightarrowkfoldcrossvalidneuralnetwork(winedata, winecategory, hiddenlayerparemeter, k<sub>\substack-1</sub>
      →= 10, minibatchk = 3, lambda_reg = 0.1, learning_rate = 0.05, epsilon_0 = 0.
      ⇒0001, softstop = epoch, printg = False)
    fold 1 training in progress
    fold 1 training completed, accuracy = 1.0
    fold 2 training in progress
    fold 2 training completed, accuracy = 1.0
    fold 3 training in progress
    fold 4 training in progress
    fold 4 training completed, accuracy =
    fold 5 training in progress
    fold 5 training completed, accuracy = 1.0
    fold 6 training in progress
    fold 6 training completed, accuracy = 1.0
    fold 7 training in progress
    fold 7 training completed, accuracy = 1.0
    fold 8 training in progress
    fold 8 training completed, accuracy = 1.0
    fold 9 training in progress
```

```
fold 9 training completed, accuracy = 0.9411764705882353
fold 10 training in progress
fold 10 training completed, accuracy = 1.0
```

Wine Data Neural Network with [4, 4] hidden layers and 4000 epochs

accuracy: 0.9886 fscore: 0.9856

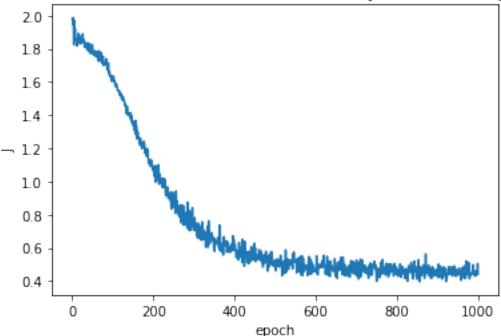
## Wine Data Neural Network with [4, 4] hidden layers and 4000 epochs



```
[]: hiddenlayerparemeter = [4] epoch = 1000
```

```
listoflistofoutputs2_7, acc2_7, listofjlist2_7 =__
     ⇒kfoldcrossvalidneuralnetwork(winedata, winecategory, hiddenlayerparemeter, k⊔
     = 10, minibatchk = 3, lambda reg = 0.1, learning rate = 0.1, epsilon_0 = 0.
     ⇔0001, softstop = epoch, printq = False)
    fold 1 training in progress
    fold 1 training completed, accuracy = 1.0
    fold 2 training in progress
    fold 2 training completed, accuracy = 1.0
    fold 3 training in progress
    fold 3 training completed, accuracy = 1.0
    fold 4 training in progress
    fold 5 training in progress
    fold 5 training completed, accuracy = 1.0
    fold 6 training in progress
    fold 6 training completed, accuracy = 1.0
    fold 7 training in progress
    fold 7 training completed, accuracy = 1.0
    fold 8 training in progress
    fold 8 training completed, accuracy = 1.0
    fold 9 training in progress
    fold 9 training completed, accuracy = 0.9411764705882353
    fold 10 training in progress
    fold 10 training completed, accuracy = 0.9375
[]: accuracy2_7, precision2_7, recall2_7, fscore_wine2_7=_
     →meanevaluation(listoflistofoutputs2_7,1)
    print("Wine Data Neural Network with " + str(hiddenlayerparemeter) + " hidden_⊔
     slayers and " + str(epoch) + " epochs")
    print("accuracy:", float("{0:.4f}". format(acc2 7)))
    print("fscore:", float("{0:.4f}". format(fscore_wine2_7)))
    plt.plot(range(epoch+1), listofjlist2_7[1])
    plt.xlabel("epoch")
    plt.ylabel("J")
    plt.title("Wine Data Neural Network with " + str(hiddenlayerparemeter) + "__
      ⇔hidden layers and " + str(epoch) + " epochs")
    plt.show()
    Wine Data Neural Network with [4] hidden layers and 1000 epochs
    accuracy: 0.9823
    fscore: 0.9779
```

# Wine Data Neural Network with [4] hidden layers and 1000 epochs

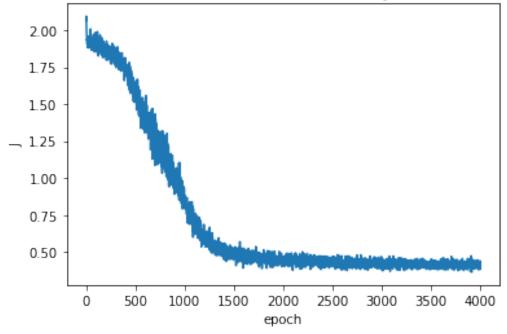


```
fold 1 training completed, accuracy = 0.9473684210526315
fold 2 training in progress
fold 2 training completed, accuracy = 1.0
fold 3 training in progress
fold 4 training in progress
fold 5 training in progress
fold 5 training completed, accuracy = 1.0
fold 6 training in progress
fold 6 training completed, accuracy = 1.0
fold 7 training in progress
fold 7 training completed, accuracy = 1.0
fold 8 training in progress
fold 8 training completed, accuracy = 1.0
fold 9 training in progress
```

Wine Data Neural Network with [8, 8] hidden layers and 4000 epochs

accuracy: 0.9836 fscore: 0.979

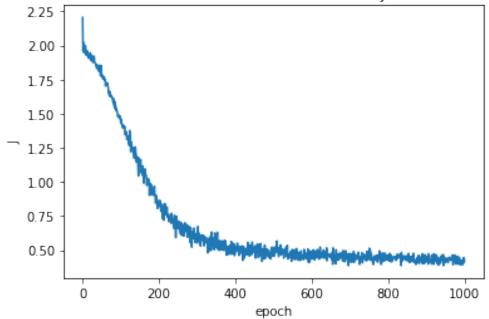
## Wine Data Neural Network with [8, 8] hidden layers and 4000 epochs



```
[]: hiddenlayerparemeter = [16,16] epoch = 1000
```

```
listoflistofoutputs2_9, acc2_9, listofjlist2_9 =__
             ⇒kfoldcrossvalidneuralnetwork(winedata, winecategory, hiddenlayerparemeter, k⊔
            = 10, minibatchk = 3, lambda reg = 0.1, learning rate = 0.1, epsilon_0 = 0.
             ⇔0001, softstop = epoch, printq = False)
         fold 1 training in progress
         fold 1 training completed, accuracy = 0.9473684210526315
         fold 2 training in progress
         fold 2 training completed, accuracy = 1.0
         fold 3 training in progress
         fold 4 training in progress
         fold 4 training completed, accuracy = 1.0
         fold 5 training in progress
         fold 5 training completed, accuracy = 1.0
         fold 6 training in progress
         fold 7 training in progress
         fold 7 training completed, accuracy = 1.0
         fold 8 training in progress
         fold 8 training completed, accuracy = 1.0
         fold 9 training in progress
         fold 9 training completed, accuracy = 1.0
         fold 10 training in progress
         fold 10 training completed, accuracy = 1.0
[]: accuracy2_9, precision2_9, recall2_9, fscore_wine2_9=_
            →meanevaluation(listoflistofoutputs2_9,1)
          print("Wine Data Neural Network with " + str(hiddenlayerparemeter) + " hidden | hid
             ⇔layers and " + str(epoch) + " epochs")
          print("accuracy:", float("{0:.4f}". format(acc2_9)))
          print("fscore:", float("{0:.4f}". format(fscore_wine2_9)))
          plt.plot(range(epoch+1), listofjlist2_9[1])
          plt.xlabel("epoch")
          plt.ylabel("J")
          plt.title("Wine Data Neural Network with " + str(hiddenlayerparemeter) + "__
             ⇔hidden layers and " + str(epoch) + " epochs")
          plt.show()
         Wine Data Neural Network with [16, 16] hidden layers and 1000 epochs
         accuracy: 0.9781
         fscore: 0.9698
```

## Wine Data Neural Network with [16, 16] hidden layers and 1000 epochs

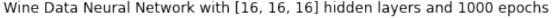


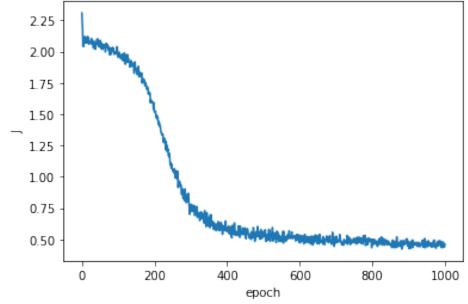
```
[]: hiddenlayerparemeter = [16,16,16]
    epoch = 1000
    listoflistofoutputs2_10, acc2_10, listofjlist2_10 =__
     →kfoldcrossvalidneuralnetwork(winedata, winecategory, hiddenlayerparemeter, k_
     ⇒= 10, minibatchk = 3, lambda_reg = 0.1, learning_rate = 0.1, epsilon_0 = 0.
     ⇔0001, softstop = epoch, printq = False)
   fold 1 training in progress
   fold 1 training completed, accuracy = 1.0
   fold 2 training in progress
   fold 2 training completed, accuracy = 1.0
   fold 3 training in progress
   fold 3 training completed, accuracy = 1.0
   fold 4 training in progress
   fold 4 training completed, accuracy = 1.0
   fold 5 training in progress
   fold 6 training in progress
   fold 6 training completed, accuracy = 1.0
   fold 7 training in progress
   fold 7 training completed, accuracy = 1.0
   fold 8 training in progress
   fold 9 training in progress
   fold 9 training completed, accuracy = 1.0
```

```
fold 10 training in progress
fold 10 training completed, accuracy = 1.0
```

Wine Data Neural Network with [16, 16, 16] hidden layers and 1000 epochs

accuracy: 0.9778 fscore: 0.9667





WINE Data | Hidden Layers | (2) | (2) | (2) | (4) | (4,4) | (4,4) | (4,4) | LR=0.05 | (8,8) LR=0.05 | (16,16) | (16,16,16) | | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- |

the learning rate of them are 0.05 and 0.1. (The two 0.05 have the label 'LR=0.5')

### Analysis of WINE Data

Discuss (on a high level) what contributed the most to improving performance: changing the regularization parameter; adding more layers; having deeper networks with many layers but few neurons per layer? designing networks with few layers but many neurons per layer? Discuss any patterns that you may have encountered. Also, discuss whether there is a point where constructing and training more "sophisticated"/complex networks—i.e., larger networks—no longer improves performance (or worsens performance).

Based on the analyses above, discuss which neural network architecture you would select if you had to deploy such a classifier in real life. Explain your reasoning.

**ANSWER:** The performance of the neural network for wine dataset are generally really good, with around 0.98 accuracy and f-score. For these group of tests, I am and trying to change the epoch, learning rate and layer data to see what are the contributions of them to the performance of the network.

For the first three (columns), I tested them with same single hidden layer [2] with different epochs. As we see from the value, with epoch = 500, the performance is around 0.95, and when epoch=1000, accuracy is around 0.983, and when epoch=2000, accuracy is about 0.9836, what demonstrate that with higher e, the j function converge to it's smallest value. As shown in the plot figures, we can see how j converge for all the [2] hidden layers neural network.

Then, I tried to change the # of layers to see what's the difference are, so, for [4] and [4,4], with both 1000 epochs, we can see that [4] have better performance than [4,4]. My reasoning is that with more layers and neurons, there will be more weights, so that would the model more epochs to converge to a minimum value, but we set both to 1000, so it still hasn't converged to a nice value vet.

Then I decided to modify the learning rate of the data, with modifyine the learning rate of [4,4] from 0.1 to 0.05, I doubled the epoch because intuitively, I think the learning rate will make the gradient descent process slower, so we need more epoch to converge. And it turns out that the performance get even better, accuracy improved from 0.983 to 0.989, and f-score improved from 0.978 to 0.986.

Then, I changed to [4,4] to [8,8], holding other parameter unchanged. And the performance didn't improve. So that shows us the max performance is around [4,4] with one or two layers.

In real world, I might just use the [4] with 1000 epochs, since the performance 0.982 is already good enough,

considering it take less time to train than the [4,4] 2000-epochs network.

### 1.2 EXTRA CREDITS

#### 1.2.1 EXTRA I: vectorized form of backpropagation

I Implemented backpropagation using vectors.

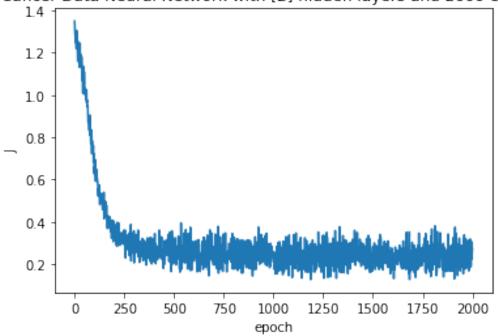
### 1.2.2 EXTRA II: CANCER Data

Trained with MiniBatch, vectorized neural network, divided to 5 group, (batchsize around 130-140)

```
[]: hiddenlayerparemeter = [2]
     epoch = 2000
     listoflistofoutputs3_1, acc3_1, listofjlist3_1 =__
      ⇔kfoldcrossvalidneuralnetwork(cancerdata, cancercategory, □
      ⇒hiddenlayerparemeter, k = 10, minibatchk = 3, lambda_reg = 0.1, ⊔
      →learning_rate = 0.1, epsilon_0 = 0.0001, softstop = epoch, printq = False)
    fold 1 training in progress
    fold 1 training completed, accuracy = 1.0
    fold 2 training in progress
    fold 2 training completed, accuracy = 0.9857142857142858
    fold 3 training in progress
    fold 3 training completed, accuracy = 0.9285714285714286
    fold 4 training in progress
    fold 4 training completed, accuracy = 0.9571428571428572
    fold 5 training in progress
    fold 5 training completed, accuracy = 0.9714285714285714
    fold 6 training in progress
    fold 6 training completed, accuracy = 0.9714285714285714
    fold 7 training in progress
    fold 7 training completed, accuracy = 0.9428571428571428
    fold 8 training in progress
    fold 8 training completed, accuracy = 0.9714285714285714
    fold 9 training in progress
    fold 9 training completed, accuracy = 0.927536231884058
    fold 10 training in progress
    fold 10 training completed, accuracy = 0.9710144927536232
[]: accuracy3_1, precision3_1, recall3_1, fscore_cancer3_1=__
      →meanevaluation(listoflistofoutputs3_1,1)
     print("Cancer Data Neural Network with " + str(hiddenlayerparemeter) + " hidden
      →layers and " + str(epoch) + " epochs")
     print("accuracy:", float("{0:.4f}". format(acc3 1)))
     print("fscore:", float("{0:.4f}". format(fscore_cancer3_1)))
     plt.plot(range(epoch+1), listofjlist3_1[1])
     plt.xlabel("epoch")
     plt.ylabel("J")
     plt.title("Cancer Data Neural Network with " + str(hiddenlayerparemeter) + "__
      ⇔hidden layers and " + str(epoch) + " epochs")
     plt.show()
```

Cancer Data Neural Network with [2] hidden layers and 2000 epochs accuracy: 0.9627 fscore: 0.9469





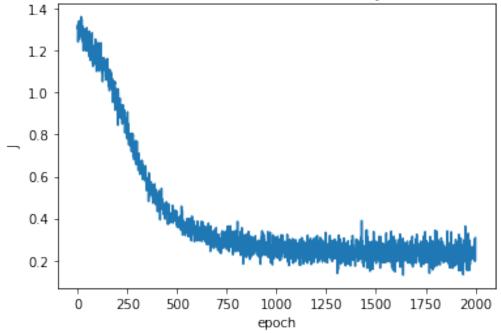
```
[]: hiddenlayerparemeter = [2]
     epoch = 2000
     listoflistofoutputs3_2, acc3_2, listofjlist3_2 =_
      ⇔kfoldcrossvalidneuralnetwork(cancerdata, cancercategory, □
      ⇔hiddenlayerparemeter, k = 10, minibatchk = 3, lambda_reg = 0.1, ⊔
      -learning rate = 0.05, epsilon 0 = 0.0001, softstop = epoch, printq = False)
    fold 1 training in progress
    fold 1 training completed, accuracy = 0.9436619718309859
    fold 2 training in progress
    fold 2 training completed, accuracy = 0.9571428571428572
    fold 3 training in progress
    fold 3 training completed, accuracy = 0.9857142857142858
    fold 4 training in progress
    fold 4 training completed, accuracy = 0.9857142857142858
    fold 5 training in progress
    fold 5 training completed, accuracy = 0.9857142857142858
    fold 6 training in progress
    fold 6 training completed, accuracy = 0.9571428571428572
    fold 7 training in progress
    fold 7 training completed, accuracy = 0.9
    fold 8 training in progress
    fold 8 training completed, accuracy = 0.9714285714285714
    fold 9 training in progress
```

```
fold 9 training completed, accuracy = 0.9420289855072463
fold 10 training in progress
fold 10 training completed, accuracy = 0.9855072463768116
```

Cancer Data Neural Network with [2] hidden layers and 2000 epochs

accuracy: 0.9614 fscore: 0.9447

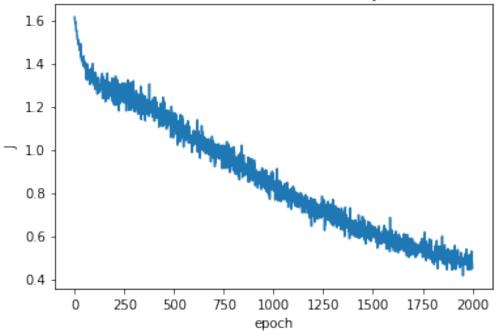
## Cancer Data Neural Network with [2] hidden layers and 2000 epochs



```
[]: hiddenlayerparemeter = [2]
epoch = 2000
```

```
listoflistofoutputs3_3, acc3_3, listofjlist3_3 =__
      ⇔kfoldcrossvalidneuralnetwork(cancerdata, cancercategory, ∟
      hiddenlayerparemeter, k = 10, minibatchk = 3, lambda_reg = 0.1,
      elearning rate = 0.01, epsilon 0 = 0.0001, softstop = epoch, printq = False)
    fold 1 training in progress
    fold 1 training completed, accuracy = 0.971830985915493
    fold 2 training in progress
    fold 2 training completed, accuracy = 0.9714285714285714
    fold 3 training in progress
    fold 3 training completed, accuracy = 0.9571428571428572
    fold 4 training in progress
    fold 4 training completed, accuracy = 0.9857142857142858
    fold 5 training in progress
    fold 5 training completed, accuracy = 0.9571428571428572
    fold 6 training in progress
    fold 6 training completed, accuracy = 0.9571428571428572
    fold 7 training in progress
    fold 7 training completed, accuracy = 0.9285714285714286
    fold 8 training in progress
    fold 8 training completed, accuracy = 0.9285714285714286
    fold 9 training in progress
    fold 9 training completed, accuracy = 0.9420289855072463
    fold 10 training in progress
    fold 10 training completed, accuracy = 0.9710144927536232
[]: accuracy3_3, precision3_3, recall3_3, fscore_cancer3_3=_
     →meanevaluation(listoflistofoutputs3_3,1)
     print("Cancer Data Neural Network with " + str(hiddenlayerparemeter) + " hidden
      ⇔layers and " + str(epoch) + " epochs")
     print("accuracy:", float("{0:.4f}". format(acc3 3)))
     print("fscore:", float("{0:.4f}". format(fscore_cancer3_3)))
     plt.plot(range(epoch+1), listofjlist3_3[1])
     plt.xlabel("epoch")
     plt.ylabel("J")
     plt.title("Cancer Data Neural Network with " + str(hiddenlayerparemeter) + "__
      ⇔hidden layers and " + str(epoch) + " epochs")
    plt.show()
    Cancer Data Neural Network with [2] hidden layers and 2000 epochs
    accuracy: 0.9571
    fscore: 0.9365
```

## Cancer Data Neural Network with [2] hidden layers and 2000 epochs



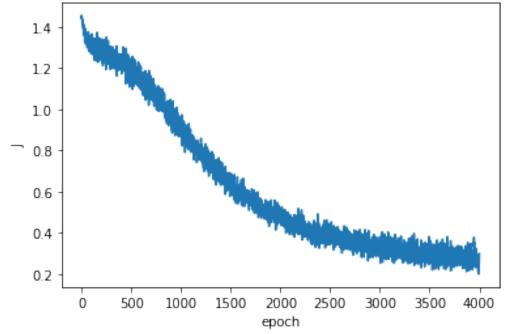
```
[]: hiddenlayerparemeter = [2]
    epoch = 4000
    listoflistofoutputs3_4, acc3_4, listofjlist3_4 =_
      ⇔kfoldcrossvalidneuralnetwork(cancerdata, cancercategory, ⊔
      ⇔hiddenlayerparemeter, k = 10, minibatchk = 3, lambda_reg = 0.1,⊔
      Glearning_rate = 0.01, epsilon_0 = 0.0001, softstop = epoch, printq = False)
    fold 1 training in progress
    fold 1 training completed, accuracy = 0.971830985915493
    fold 2 training in progress
    fold 2 training completed, accuracy = 0.9285714285714286
    fold 3 training in progress
    fold 3 training completed, accuracy = 0.9857142857142858
    fold 4 training in progress
    fold 4 training completed, accuracy = 0.9285714285714286
    fold 5 training in progress
    fold 5 training completed, accuracy = 0.9714285714285714
    fold 6 training in progress
    fold 6 training completed, accuracy = 0.9285714285714286
    fold 7 training in progress
    fold 7 training completed, accuracy = 0.9857142857142858
    fold 8 training in progress
    fold 8 training completed, accuracy = 0.9714285714285714
    fold 9 training in progress
```

```
fold 9 training completed, accuracy = 0.9855072463768116
fold 10 training in progress
fold 10 training completed, accuracy = 0.9710144927536232
```

Cancer Data Neural Network with [2] hidden layers and 4000 epochs

accuracy: 0.9628 fscore: 0.9462

# Cancer Data Neural Network with [2] hidden layers and 4000 epochs

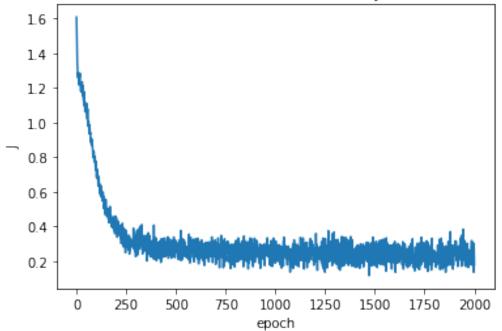


```
[]: hiddenlayerparemeter = [4]
     epoch = 2000
     listoflistofoutputs3_5, acc3_5, listofjlist3_5 =_
      →kfoldcrossvalidneuralnetwork(cancerdata, cancercategory,
      ⇒hiddenlayerparemeter, k = 10, minibatchk = 3, lambda_reg = 0.1, ⊔
      →learning_rate = 0.1, epsilon_0 = 0.0001, softstop = epoch, printq = False)
    fold 1 training in progress
    fold 1 training completed, accuracy = 0.9014084507042254
    fold 2 training in progress
    fold 2 training completed, accuracy = 1.0
    fold 3 training in progress
    fold 3 training completed, accuracy = 0.9714285714285714
    fold 4 training in progress
    fold 4 training completed, accuracy = 0.9714285714285714
    fold 5 training in progress
    fold 5 training completed, accuracy = 0.9714285714285714
    fold 6 training in progress
    fold 6 training completed, accuracy = 0.9285714285714286
    fold 7 training in progress
    fold 7 training completed, accuracy = 0.9571428571428572
    fold 8 training in progress
    fold 8 training completed, accuracy = 1.0
    fold 9 training in progress
    fold 9 training completed, accuracy = 0.9855072463768116
    fold 10 training in progress
    fold 10 training completed, accuracy = 0.9420289855072463
[]: epoch = 2000
     hiddenlayerparemeter = [4]
     accuracy3_5, precision3_5, recall3_5, fscore_cancer3_5=_
      →meanevaluation(listoflistofoutputs3_5,1)
     print("Cancer Data Neural Network with " + str(hiddenlayerparemeter) + " hidden ∪
      ⇔layers and " + str(epoch) + " epochs")
     print("accuracy:", float("{0:.4f}". format(acc3 5)))
     print("fscore:", float("{0:.4f}". format(fscore_cancer3_5)))
     plt.plot(range(epoch+1), listofjlist3_5[1])
     plt.xlabel("epoch")
     plt.ylabel("J")
     plt.title("Cancer Data Neural Network with " + str(hiddenlayerparemeter) + "__
      ⇔hidden layers and " + str(epoch) + " epochs")
    plt.show()
```

Cancer Data Neural Network with [4] hidden layers and 2000 epochs accuracy: 0.9629 fscore: 0.9472

.....

# Cancer Data Neural Network with [4] hidden layers and 2000 epochs



```
[]: hiddenlayerparemeter = [4,4]
    epoch = 2000
    listoflistofoutputs3_6, acc3_6, listofjlist3_6 =_
      ⇔kfoldcrossvalidneuralnetwork(cancerdata, cancercategory, □
      ⇔hiddenlayerparemeter, k = 10, minibatchk = 3, lambda_reg = 0.1,⊔
      →learning_rate = 0.1, epsilon_0 = 0.0001, softstop = epoch, printq = False)
    fold 1 training in progress
    fold 1 training completed, accuracy = 0.9436619718309859
    fold 2 training in progress
    fold 2 training completed, accuracy = 0.9714285714285714
    fold 3 training in progress
    fold 3 training completed, accuracy = 0.9857142857142858
    fold 4 training in progress
    fold 4 training completed, accuracy = 0.9714285714285714
    fold 5 training in progress
    fold 5 training completed, accuracy = 0.9714285714285714
    fold 6 training in progress
    fold 6 training completed, accuracy = 0.9714285714285714
    fold 7 training in progress
    fold 7 training completed, accuracy = 0.9285714285714286
    fold 8 training in progress
    fold 8 training completed, accuracy = 0.9571428571428572
    fold 9 training in progress
```

```
fold 9 training completed, accuracy = 0.9710144927536232
fold 10 training in progress
fold 10 training completed, accuracy = 0.9420289855072463
```

```
[]: accuracy3_6, precision3_6, recall3_6, fscore_cancer3_6=_

→meanevaluation(listoflistofoutputs3_6,1)

print("Cancer Data Neural Network with " + str(hiddenlayerparemeter) + " hidden_

→layers and " + str(epoch) + " epochs")

print("accuracy:", float("{0:.4f}". format(acc3_6)))

print("fscore:", float("{0:.4f}". format(fscore_cancer3_6)))

plt.plot(range(epoch+1), listofjlist3_6[1])

plt.xlabel("epoch")

plt.ylabel("J")

plt.title("Cancer Data Neural Network with " + str(hiddenlayerparemeter) + "

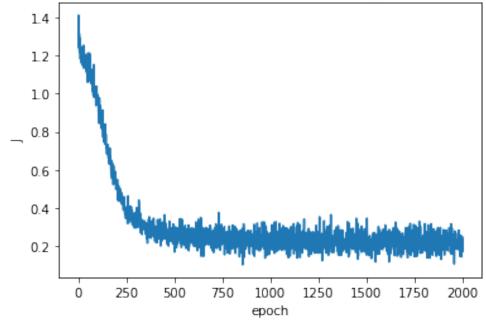
→hidden layers and " + str(epoch) + " epochs")

plt.show()
```

Cancer Data Neural Network with [4, 4] hidden layers and 2000 epochs

accuracy: 0.9614 fscore: 0.9448

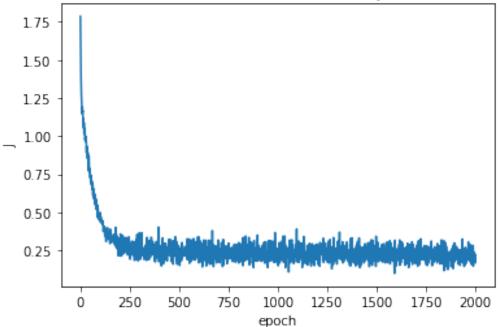
## Cancer Data Neural Network with [4, 4] hidden layers and 2000 epochs



```
[]: hiddenlayerparemeter = [8] epoch = 2000
```

```
listoflistofoutputs3_7, acc3_7, listofjlist3_7 =__
      ⇔kfoldcrossvalidneuralnetwork(cancerdata, cancercategory, □
      ⇒hiddenlayerparemeter, k = 10, minibatchk = 3, lambda_reg = 0.1, ⊔
      Glearning rate = 0.1, epsilon_0 = 0.0001, softstop = epoch, printq = False)
    fold 1 training in progress
    fold 1 training completed, accuracy = 0.9859154929577465
    fold 2 training in progress
    fold 2 training completed, accuracy = 0.9571428571428572
    fold 3 training in progress
    fold 3 training completed, accuracy = 0.9
    fold 4 training in progress
    fold 4 training completed, accuracy = 0.9857142857142858
    fold 5 training in progress
    fold 5 training completed, accuracy = 0.9714285714285714
    fold 6 training in progress
    fold 6 training completed, accuracy = 0.9428571428571428
    fold 7 training in progress
    fold 7 training completed, accuracy = 0.9571428571428572
    fold 8 training in progress
    fold 8 training completed, accuracy = 0.9857142857142858
    fold 9 training in progress
    fold 9 training completed, accuracy = 0.9855072463768116
    fold 10 training in progress
    fold 10 training completed, accuracy = 0.9710144927536232
[]: hiddenlayerparemeter = [8]
     accuracy3_7, precision3_7, recall3_7, fscore_cancer3_7=_
      →meanevaluation(listoflistofoutputs3_7,1)
     print("Cancer Data Neural Network with " + str(hiddenlayerparemeter) + " hidden_
      ⇔layers and " + str(epoch) + " epochs")
     print("accuracy:", float("{0:.4f}". format(acc3_7)))
     print("fscore:", float("{0:.4f}". format(fscore cancer3 7)))
     plt.plot(range(epoch+1), listofjlist3_7[1])
     plt.xlabel("epoch")
     plt.ylabel("J")
    plt.title("Cancer Data Neural Network with " + str(hiddenlayerparemeter) + "__
      ⇔hidden layers and " + str(epoch) + " epochs")
    plt.show()
    Cancer Data Neural Network with [8] hidden layers and 2000 epochs
    accuracy: 0.9642
    fscore: 0.9489
```

## Cancer Data Neural Network with [8] hidden layers and 2000 epochs



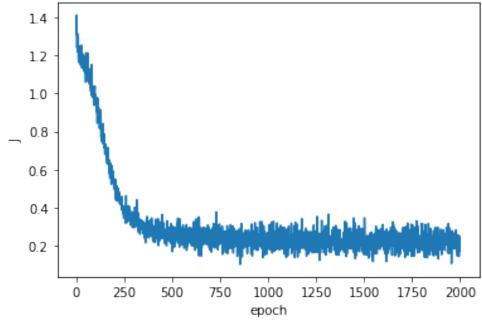
```
[]: hiddenlayerparemeter = [8,8]
    epoch = 2000
    listoflistofoutputs3_8, acc3_8, listofjlist3_8 =_
      ⇔kfoldcrossvalidneuralnetwork(cancerdata, cancercategory,
      ⇔hiddenlayerparemeter, k = 10, minibatchk = 3, lambda_reg = 0.1,⊔
      -learning rate = 0.1, epsilon 0 = 0.0001, softstop = epoch, printq = False)
    fold 1 training in progress
    fold 1 training completed, accuracy = 0.971830985915493
    fold 2 training in progress
    fold 2 training completed, accuracy = 0.9714285714285714
    fold 3 training in progress
    fold 3 training completed, accuracy = 0.9285714285714286
    fold 4 training in progress
    fold 4 training completed, accuracy = 0.9857142857142858
    fold 5 training in progress
    fold 5 training completed, accuracy = 0.9571428571428572
    fold 6 training in progress
    fold 6 training completed, accuracy = 0.9857142857142858
    fold 7 training in progress
    fold 7 training completed, accuracy = 0.9714285714285714
    fold 8 training in progress
    fold 8 training completed, accuracy = 0.9285714285714286
    fold 9 training in progress
```

```
fold 9 training completed, accuracy = 0.9710144927536232
fold 10 training in progress
fold 10 training completed, accuracy = 0.9710144927536232
```

Cancer Data Neural Network with [8, 8] hidden layers and 2000 epochs

accuracy: 0.9642 fscore: 0.9448

## Cancer Data Neural Network with [8, 8] hidden layers and 2000 epochs



#### Analysis of CANCER Data

Discuss (on a high level) what contributed the most to improving performance: changing the regularization parameter; adding more layers; having deeper networks with many layers but few neurons per layer? designing networks with few layers but many neurons per layer? Discuss any patterns that you may have encountered. Also, discuss whether there is a point where constructing and training more "sophisticated"/complex networks—i.e., larger networks—no longer improves performance (or worsens performance).

Based on the analyses above, discuss which neural network architecture you would select if you had to deploy such a classifier in real life. Explain your reasoning.

**ANSWER:** The overall performance is also pretty nice for this data set. What I've notice while plotting them is that I find out that once the j get smaller, it becomes very noisy, so here I am trying to reduce the noise by changing the learning rate for them.

What we can see here is that smaller learning rate did decrease the noise, but there are sill many left. Maybe heuristic is a solotion to it.

Also, it verified what I wrote in the Wine Data Analysis: The smaller learning rate requires more epochs to converge.

In real world, I think I will just use the [2], LR=1, 2000-epochs model, considering that cancer might have learning relation between the input to the output.

It's also a choice to analyze this using the ROC because in cancer, we want to find all real positive/actual positive.

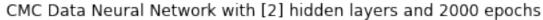
### 1.2.3 EXTRA III: CMC Data

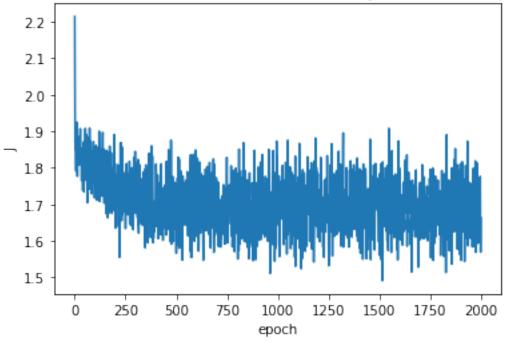
Trained with MiniBatch, vectorized neural network, divided to minibatchk group,

(I might modify the minibatchk(mbk), I will start with mbk = 15, that is batch size about 90 to 100.)

```
fold 5 training completed, accuracy = 0.5306122448979592
    fold 6 training in progress
    fold 6 training completed, accuracy = 0.5170068027210885
    fold 7 training in progress
    fold 7 training completed, accuracy = 0.5170068027210885
    fold 8 training in progress
    fold 8 training completed, accuracy = 0.5102040816326531
    fold 9 training in progress
    fold 9 training completed, accuracy = 0.4965986394557823
    fold 10 training in progress
    fold 10 training completed, accuracy = 0.5068493150684932
[]: accuracy4_1, precision4_1, recall4_1, fscore_cmc4_1=__
     →meanevaluation(listoflistofoutputs4_1,1)
    print("CMC Data Neural Network with " + str(hiddenlayerparemeter4_1) + " hidden_
     ⇔layers and " + str(epoch4_1) + " epochs")
    print("accuracy:", float("{0:.4f}". format(acc4_1)))
    print("fscore:", float("{0:.4f}". format(fscore_cmc4_1)))
    plt.plot(range(epoch4_1+1), listofjlist4_1[-3])
    plt.xlabel("epoch")
    plt.ylabel("J")
    plt.title("CMC Data Neural Network with " + str(hiddenlayerparemeter4_1) + "__
      chidden layers and " + str(epoch4_1) + " epochs")
    plt.show()
    CMC Data Neural Network with [2] hidden layers and 2000 epochs
    accuracy: 0.5118
```

fscore: 0.4092





The performance is about 0.5, which is the least want output. (even 0.1 would be better). Besides, this Doesn't converge to a good spot. I'd assume this is a local minimum.

The problem might be the learning rate: too low?

Also try different mbk for batchsize and more neuron.

```
fold 1 training in progress
fold 1 training completed, accuracy = 0.5838926174496645
fold 2 training in progress
fold 2 training completed, accuracy = 0.5202702702702703
fold 3 training in progress
fold 3 training completed, accuracy = 0.5067567567567568
fold 4 training in progress
fold 4 training completed, accuracy = 0.5578231292517006
fold 5 training in progress
fold 5 training completed, accuracy = 0.5102040816326531
fold 6 training in progress
```

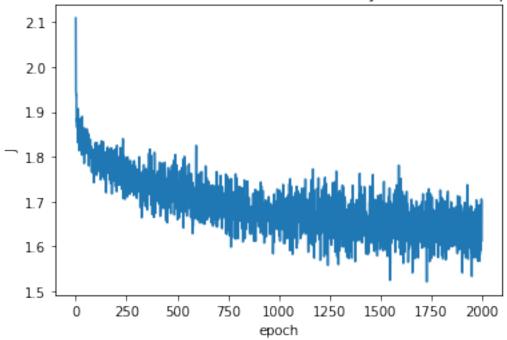
```
fold 6 training completed, accuracy = 0.5306122448979592
    fold 7 training in progress
    fold 7 training completed, accuracy = 0.5034013605442177
    fold 8 training in progress
    fold 8 training completed, accuracy = 0.5170068027210885
    fold 9 training in progress
    fold 9 training completed, accuracy = 0.5034013605442177
    fold 10 training in progress
    fold 10 training completed, accuracy = 0.541095890410959
[]: accuracy4_2, precision4_2, recall4_2, fscore_cmc4_2=_
     →meanevaluation(listoflistofoutputs4_2,1)
     print("CMC Data Neural Network with " + str(hiddenlayerparemeter4 2) + " hidden_u
      slayers and " + str(epoch4_2) + " epochs")
     print("accuracy:", float("{0:.4f}". format(acc4 2)))
     print("fscore:", float("{0:.4f}". format(fscore_cmc4_2)))
     plt.plot(range(epoch4_2+1), listofjlist4_2[0])
     plt.xlabel("epoch")
     plt.ylabel("J")
     plt.title("CMC Data Neural Network with " + str(hiddenlayerparemeter4_2) + "__
      ⇔hidden layers and " + str(epoch4_2) + " epochs")
```

CMC Data Neural Network with [4] hidden layers and 2000 epochs

accuracy: 0.5274 fscore: 0.4278

plt.show()

## CMC Data Neural Network with [4] hidden layers and 2000 epochs

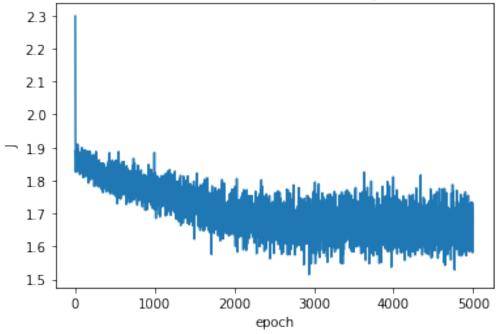


Sadly, there's only small improvements. Both network kind of stuck around j=1.7, maybe I will run the next network with more epochs, and try out more layers. I will use kfold k=5 instead of 10 so it won't take forever

But maybe, from the graph, I'd guess it's just the minimum around 1.6?

```
[]: hiddenlayerparemeter4_3 = [4,4]
     epoch4_3 = 5000
     listoflistofoutputs4_3, acc4_3, listofjlist4_3 =__
      ⊸kfoldcrossvalidneuralnetwork(cmcdata, cmccategory, hiddenlayerparemeter4_3, ⊔
      ⇒k = 5, minibatchk = 5, lambda_reg = 0.1, learning_rate = 0.1, epsilon_0 = 0.
      ⇔00001, softstop = epoch4_3, printq = False)
    fold 1 training in progress
    fold 1 training completed, accuracy = 0.543918918918919
    fold 2 training in progress
    fold 2 training completed, accuracy = 0.576271186440678
    fold 3 training in progress
    fold 3 training completed, accuracy = 0.5389830508474577
    fold 4 training in progress
    fold 4 training completed, accuracy = 0.5238095238095238
    fold 5 training in progress
    fold 5 training completed, accuracy = 0.4812286689419795
[]: accuracy4_3, precision4_3, recall4_3, fscore_cmc4_3=_
      meanevaluation(listoflistofoutputs4_3,1)
     print("CMC Data Neural Network with " + str(hiddenlayerparemeter4 3) + " hidden_u
      slayers and " + str(epoch4_3) + " epochs")
     print("accuracy:", float("{0:.4f}". format(acc4_3)))
     print("fscore:", float("{0:.4f}". format(fscore_cmc4_3)))
     plt.plot(range(epoch4_3+1), listofjlist4_3[0])
     plt.xlabel("epoch")
     plt.ylabel("J")
     plt.title("CMC Data Neural Network with " + str(hiddenlayerparemeter4_3) + "__
      ⇔hidden layers and " + str(epoch4_3) + " epochs")
     plt.show()
    CMC Data Neural Network with [4, 4] hidden layers and 5000 epochs
    accuracy: 0.5328
    fscore: 0.4197
```

# CMC Data Neural Network with [4, 4] hidden layers and 5000 epochs



Still Not a lot of changes.

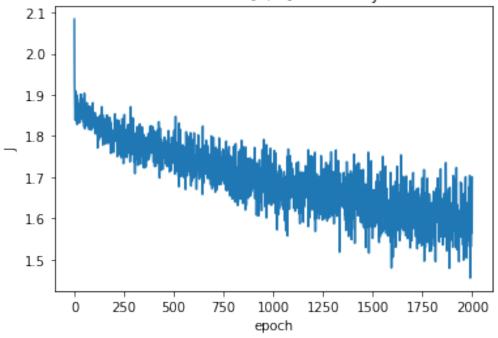
- (1) Try Higher learning rate (0.2)
- (2) Try More layers [4,4,4],[8,8,8,8]

```
fold 1 training in progress
fold 1 training completed, accuracy = 0.5777027027027027
fold 2 training in progress
fold 2 training completed, accuracy = 0.5796610169491525
fold 3 training in progress
fold 3 training completed, accuracy = 0.5898305084745763
fold 4 training in progress
fold 4 training completed, accuracy = 0.4897959183673469
fold 5 training in progress
fold 5 training completed, accuracy = 0.5290102389078498
```

CMC Data Neural Network with  $[4,\ 4]$  hidden layers and 2000 epochs

accuracy: 0.5532 fscore: 0.4284

# CMC Data Neural Network with [4, 4] hidden layers and 2000 epochs

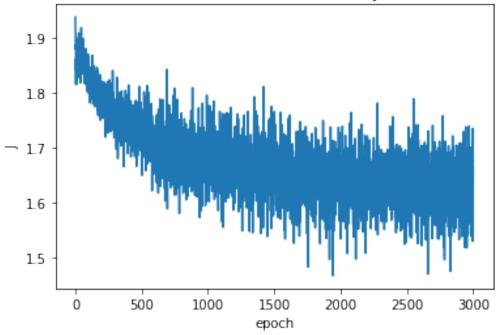


The sign of convergance! Try larger epoch

```
[]: hiddenlayerparemeter4_5 = [4,4] epoch4_5 = 3000
```

```
listoflistofoutputs4_5, acc4_5, listofjlist4_5 = ___
      ⇔kfoldcrossvalidneuralnetwork(cmcdata, cmccategory, hiddenlayerparemeter4_5,__
      ⇒k = 5, minibatchk = 5, lambda reg = 0.1, learning rate = 0.22, epsilon_0 = 0.
      ⇔00001, softstop = epoch4_5, printq = False)
    fold 1 training in progress
    fold 1 training completed, accuracy = 0.5608108108108109
    fold 2 training in progress
    fold 2 training completed, accuracy = 0.5423728813559322
    fold 3 training in progress
    fold 3 training completed, accuracy = 0.5559322033898305
    fold 4 training in progress
    fold 4 training completed, accuracy = 0.5578231292517006
    fold 5 training in progress
    fold 5 training completed, accuracy = 0.5392491467576792
[]: accuracy4_5, precision4_5, recall4_5, fscore_cmc4_5=__
     →meanevaluation(listoflistofoutputs4_5,1)
     print("CMC Data Neural Network with " + str(hiddenlayerparemeter4_5) + " hidden_u
      ⇔layers and " + str(epoch4_5) + " epochs")
     print("accuracy:", float("{0:.4f}". format(acc4_5)))
     print("fscore:", float("{0:.4f}". format(fscore_cmc4_5)))
     plt.plot(range(epoch4_5+1), listofjlist4_5[0])
     plt.xlabel("epoch")
     plt.ylabel("J")
     plt.title("CMC Data Neural Network with " + str(hiddenlayerparemeter4_5) + "__
      shidden layers and " + str(epoch4_5) + " epochs")
    plt.show()
    CMC Data Neural Network with [4, 4] hidden layers and 3000 epochs
    accuracy: 0.5512
    fscore: 0.3968
```

# CMC Data Neural Network with [4, 4] hidden layers and 3000 epochs



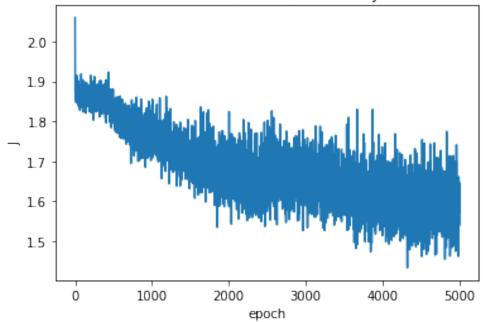
[]: hiddenlayerparemeter4 6 = [4,4,4]

```
epoch4_6 = 5000
    listoflistofoutputs4_6, acc4_6, listofjlist4_6 =
      ⇒kfoldcrossvalidneuralnetwork(cmcdata, cmccategory, hiddenlayerparemeter4 6, ⊔
      ⇒k = 5, minibatchk = 5, lambda_reg = 0.1, learning_rate = 0.2, epsilon_0 = 0.
      ⇔00001, softstop = epoch4_6, printq = False)
    fold 1 training in progress
    fold 1 training completed, accuracy = 0.5371621621621622
    fold 2 training in progress
    fold 2 training completed, accuracy = 0.5423728813559322
    fold 3 training in progress
    fold 3 training completed, accuracy = 0.5423728813559322
    fold 4 training in progress
    fold 4 training completed, accuracy = 0.5374149659863946
    fold 5 training in progress
    fold 5 training completed, accuracy = 0.5563139931740614
[]: accuracy4_6, precision4_6, recall4_6, fscore_cmc4_6=_
     →meanevaluation(listoflistofoutputs4_6,1)
    print("CMC Data Neural Network with " + str(hiddenlayerparemeter4 6) + " hidden,
     →layers and " + str(epoch4_6) + " epochs")
    print("accuracy:", float("{0:.4f}". format(acc4 6)))
    print("fscore:", float("{0:.4f}". format(fscore_cmc4_6)))
```

CMC Data Neural Network with  $[4,\ 4,\ 4]$  hidden layers and 5000 epochs

accuracy: 0.5431 fscore: 0.3392

## CMC Data Neural Network with [4, 4, 4] hidden layers and 5000 epochs



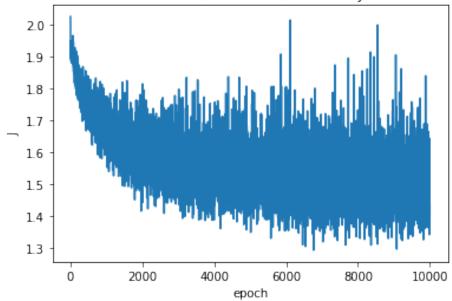
```
| hiddenlayerparemeter4_7 = [16,16,16] |
| epoch4_7 = 10000 |
| listoflistofoutputs4_7, acc4_7, listofjlist4_7 = |
| Akfoldcrossvalidneuralnetwork(cmcdata, cmccategory, hiddenlayerparemeter4_7, |
| Ak = 5, minibatchk = 5, lambda_reg = 0.1, learning_rate = 0.2, epsilon_0 = 0. |
| A00001, softstop = epoch4_7, printq = False) |
| fold 1 training in progress |
| fold 2 training completed, accuracy = 0.4797297297297297 |
| fold 2 training in progress |
| fold 3 training completed, accuracy = 0.511864406779661 |
| fold 3 training in progress |
| fold 4 training in progress |
| fold 6 training in progress |
| fold 9 training in progress
```

```
fold 4 training completed, accuracy = 0.5034013605442177
fold 5 training in progress
fold 5 training completed, accuracy = 0.5085324232081911
```

CMC Data Neural Network with [16, 16, 16] hidden layers and 10000 epochs

accuracy: 0.5017 fscore: 0.4065





So that seems to demonstrate we can have min j around 1.4, but I don't exactly know the tuning, maybe I will give up on find a better tuning for this data.

CMC Data | Hidden Layers | (2)LR=0.1 | (4)LR=0.1 | (4,4)LR=0.1 | (4,4)LR=0.2 | (4,4)LR=0.22 | (4,4,4)LR=0.2 | (16,16,16)LR=0.2 | | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- | :-- |

```
| 0.5532 | 0.5512 | 0.5431 | 0.5017 | | F-Score | 0.4092 | 0.4278 | 0.4197 | 0.4284 | 0.3968 | 0.3392 | 0.4065 |
```

#### 1.2.4 EXTRA IV: Numerical Check Gradient

I will not do this.

### 1.3 APPENDIX

#### 1.3.1 utils.py

```
[]: from sqlite3 import Row
     from evaluationmatrix import *
     from sklearn import datasets
     import sklearn.model_selection
     from sklearn.preprocessing import OneHotEncoder
     import random
     import numpy as np
     import csv
     import math
     import matplotlib.pyplot as plt
     from collections import Counter
     def importfile(name:str,delimit:str):
         # importfile('hw3\_wine.csv', '\t')
         file = open("datasets/"+name, encoding='utf-8-sig')
         reader = csv.reader(file, delimiter=delimit)
         dataset = []
         for row in reader:
             dataset.append(row)
         file.close()
         return dataset
     def onehotencoder(data, category):
         dataT=data.T.copy()
         enc = OneHotEncoder(sparse=False)
         i = 0
         appendeddict = {}
         for cat in category:
             if category[cat] == 'categorical':
                 hotneeded = dataT[i]
                 hotted = enc.fit_transform(hotneeded.reshape(-1,1))
                 for j in enc.categories_[0]:
                     newname = cat+'_'+str(j)
                     appendeddict[newname] = 'ohe numerical'
                 dataT = np.append(dataT,hotted.T,axis=0)
             if category[cat] == 'class':
                 hotneeded = dataT[i]
```

```
hotted = enc.fit_transform(hotneeded.reshape(-1,1))
            for class_ in enc.categories_[0]:
                newname = cat+'_'+str(class_)
                appendeddict[newname] = 'class_numerical'
            dataT = np.append(dataT,hotted.T,axis=0)
        i += 1
    category.update(appendeddict)
    categorycopy = category.copy()
    droplist = []
    for cat in category:
        if category[cat] == 'categorical' or category[cat] == 'class':
            droplist.append(i)
            categorycopy.pop(cat)
        i += 1
    dataT = np.delete(dataT,droplist,axis=0)
    return dataT.T, categorycopy
def normalizetrain(ohe_traindata, category): # input data in by row/by instance
    dataTC = ohe_traindata.T.copy()
    minmaxes = \Pi
    i = 0
    for oneattribute in category:
        if category[oneattribute] == 'numerical':
            colmin = np.min(dataTC[i])
            colmax = np.max(dataTC[i])
            singleminmax = [colmin,colmax]
            # normalize to 0 to 1
            for j in range(len(dataTC[i])):
                dataTC[i][j] = (dataTC[i][j] - colmin)/(colmax - colmin)
            minmaxes.append(singleminmax)
        else:
            minmaxes.append([0.0,1.0])
    return dataTC.T, minmaxes
def normalizeonetest(instance_data, category, minmaxes):
    i = 0
    for oneattribute in category:
        if category[oneattribute] == 'numerical':
            instance_data[i] = (instance_data[i] - minmaxes[i][0])/
 →(minmaxes[i][1] - minmaxes[i][0])
        i += 1
    return instance_data
def normalizealltest(ohe_testdata, category, minmaxes):
```

```
result = []
for i in ohe_testdata:
    n_ohe_test = normalizeonetest(i, category, minmaxes)
    result.append(n_ohe_test)
return np.array(result)

def g(x): # sigmoid function
    return 1/(1 + np.exp(-x))

def transposelistoflist(1):
    newlistoflist = []
    for i in range(len(1[0])):
        newlist = []
    for j in range(len(1)):
        newlist.append(1[j][i])
        newlistoflist.append(newlist)
    return newlistoflist
```

### 1.3.2 neuralnetwork.py

```
[]: from utils import *
     def initialize_weights(ohe_category,layer_parameter, biasterm=True):
         weight_matrix_list = []
         inputcategory, outputcategory = [],[]
         inputindex, outputindex = [],[]
         n = 0
         for i in ohe_category:
             if ohe category[i] != 'class numerical':
                 inputcategory.append(i) # name of the input category
                 inputindex.append(n) # index of the input category
             else:
                 outputcategory.append(i) # name of the output category
                 outputindex.append(n) # index of the output category
             n += 1
         b = 1 if biasterm == True else 0
         updatedlayerparameterwbias = [len(inputcategory)+b] + list(np.
      -array(layer_parameter)+b) + [len(outputcategory)] # [inputlayer, ]
      → layerparameters, outputlayer]
         for i in range(len(updatedlayerparameterwbias)-1):
             layernow = updatedlayerparameterwbias[i]
             layernext = updatedlayerparameterwbias[i+1]-1 if i !
      ⇒=len(updatedlayerparameterwbias)-2 else updatedlayerparameterwbias[i+1]
```

```
\# ^ for the last layer, the bias is not included, so don't need to \sqcup
 ⇔minus 1 1
        init_weight = np.random.rand(layernext, layernow) * 2 - 1 # initialize_
 → the weight with random number between -1 and 1
        weight_matrix_list.append(init_weight)
    return weight_matrix_list
def costfunction(expected_output, actual_output):
    j = -np.multiply(expected_output, np.log(actual_output)) - np.multiply((1 - <math>u
 →expected_output),np.log(1 - actual_output))
    return np.sum(j)
def sumofweights(listofweights, bias=True): # computes the square of all weights_
 →of the network and sum them up
    sum = 0
    for weight in listofweights:
        if bias:
            w = weight.copy()
            w[:, 0] = 0
            sum += np.sum(np.square(w))
        else:
            sum += np.sum(np.square(weight))
    return sum
def blame(predict_output, expected_output, weights_list, a_list, biasterm=True):
 → # This is to find out the delta function
    deltalist = []
    delta_layer_l = predict_output - expected_output
    deltalist.append(delta_layer_l)
    i = len(weights_list)-1
    current_delta = delta_layer_l
    while i > 0:
        delta_layer_now = np.multiply(np.multiply(np.dot(weights_list[i].

¬T, current_delta), a_list[i]), (1-a_list[i]))
        if biasterm:
            delta_layer_now[0] = 1 # the first attribute is the bias
            current_delta = delta_layer_now[1:] # the first attribute is the_
 ⇔bias
        else:
            current_delta = delta_layer_now
        deltalist.append(current_delta)
        i-=1
    deltalist.reverse()
```

```
return deltalist
def gradientD(weights list,deltalist,attributelist,biasterm=True):
    gradlist = []
    for i in range(len(weights_list)):
        attributenow = attributelist[i]
        deltanow = np.array([deltalist[i]]).T
        dotproduct = deltanow*attributenow
        # print('dotshape', dotproduct.shape)
        gradlist.append(dotproduct)
    return gradlist
# Forward propagation vectorized
def neural_network(normed_hotted_data,ohe_category,weights_list, minibatchk = __
 ⇒15, lambda_reg = 0.2, learning_rate = 0.01):
    biasterm=True
    normed_ohe_copy = normed_hotted_data.copy()
    if minibatchk > len(normed_hotted_data):
        minibatchk = len(normed hotted data)
    np.random.shuffle(normed_ohe_copy)
    # print('minibatchk', minibatchk)
    # print('shape of normed_ohe_copy',normed_ohe_copy.shape)
    splitted = np.array_split(normed_ohe_copy, minibatchk)
    inputcategory, outputcategory = [],[]
    inputindex, outputindex = [],[]
    n = 0
    for i in ohe_category:
        if ohe_category[i] != 'class_numerical':
            inputcategory.append(i) # name of the input category
            inputindex.append(n) # index of the input category
            outputcategory.append(i) # name of the output category
            outputindex.append(n) # index of the output category
        n += 1
    b = 1 if biasterm else 0
    for onebatch in splitted:
        onebatch = onebatch.T
        input_data = onebatch[inputindex].T
        output_data = onebatch[outputindex].T
        # input_data_mean = onebatch[inputindex].mean(axis=1)
        output_data = onebatch[outputindex].T
        # forward propagation
        instance index = 0
```

```
j = 0
      listofgradient = []
      for one_instance in input_data:
           current_layer_a = np.append(1,one_instance) if b == 1 else_
→one_instance
           # input layer is the current layer
           current layer index = 0
          output_expect = output_data[instance_index]
          attributesnobias = [one_instance]
          attributeswbias = [current_layer_a]
          for theta in weights_list:
              z = np.dot(theta,current_layer_a)
              a = g(z)
               current_layer_a = np.append(1,a) if (b == 1) and_
⇔(current_layer_index+1 != len(weights_list)) else a
              attributesnobias.append(a)
               attributeswbias.append(current_layer_a)
               current_layer_index += 1
          output_predict = current_layer_a # the last attribute is the output_
⇔for this batch.
          instance_index += 1
           j += costfunction(output expect,output predict)
           # calculate delta blame (back propagation)
          listofdelta = blame(output_predict,output_expect,weights_list,__
⇒attributeswbias)
          thisgradient =
→gradientD(weights_list,listofdelta,attributeswbias,biasterm)
          listofgradient.append(thisgradient)
      gradientP = [lambda_reg*t for t in weights_list]
       # first column in singleP in the np.array = 0
      for singleP in gradientP:
          singleP[:, 0] = 0
      grad_D_transpose = transposelistoflist(listofgradient)
      grad_D_sum = [np.sum(t,axis=0) for t in grad_D_transpose]
      gradients_batch = []
      for i in range(len(grad_D_sum)):
          gradients_batch.append((grad_D_sum[i] + gradientP[i])*(1/
→instance_index))
      j /= (instance_index+1)
      s = sumofweights(weights_list,bias=b)*lambda reg/(2*(instance_index+1))
      allj = j+s # total cose with regularization
```

```
# update weights
        for i in range(len(weights_list)):
            weights_list[i] -= learning_rate*gradients_batch[i]
    return weights_list, allj, j #j is j without regularization: only for
 \rightarrow testing
def train_neural_network(normed_ohetraining_data,ohe_category,layerparameter,u
 minibatchk = 15, lambda reg = 0.15, learning_rate = 0.01, epsilon_0 = 0.
 →00001, softstop = 8000, printq = False):
    init weight = initialize weights(ohe category,layerparameter)
    updated_weight, jsum, purej =__
 ⊸neural_network(normed_ohetraining_data,ohe_category,init_weight, minibatchk,_
 →lambda_reg, learning_rate)
    epsilon = epsilon_0 + 20
    currentj = jsum
    smallestj = jsum
    count = 0
    jlist = []
    jlist.append(currentj)
    while ((epsilon > epsilon_0) or (count < softstop) or (currentj >=_{\sqcup}
 ⇒smallestj)) and (count < (softstop)):
        if printq:
            print('currentj',currentj)
            print('count',count)
        count += 1
        updated_weight, jsum, purej = □
 -neural_network(normed_ohetraining_data,ohe_category,updated_weight,minibatchk,lambda_reg,le
        epsilon = jsum - currentj
        currentj = jsum
        jlist.append(currentj)
        if currentj < smallestj:</pre>
            smallestj = currentj
    return updated_weight, jlist
def predictoneinstance(inputdata, weightl): # inputdata here doesn't include the ⊔
 ⇔class and bias.
    current_layer_a = np.append(1,inputdata)
    current_layer_index = 0
    alist = []
    alist.append(current_layer_a)
    for theta in weightl:
        z = np.dot(theta,current_layer_a)
        a = g(z)
```

```
current_layer_a = np.append(1,a) if (current_layer_index+1 !=_
 ⇔len(weightl)) else a
        alist.append(current_layer_a)
        current layer index += 1
        raw_output = a
    predict_output = current_layer_a
    if len(predict_output) <=1:</pre>
        predict_output[0] = 0 if predict_output[0] <= 0.5 else 1</pre>
    else:
        predict_output[np.where(predict_output==np.max(predict_output))] = 1
        predict_output[np.where(predict_output!=1)] = 0
    return predict_output, raw_output
def predict_many_nn(testdatafull, ohecategory, weight):
    n = 0
    inputindex, outputindex = [],[]
    for i in ohecategory:
        if ohecategory[i] != 'class_numerical':
            inputindex.append(n)
        else:
            outputindex.append(n)
    predictvsexpectlist = [] # list of list of predict and expect/actual
    for instance in testdatafull:
        datainput = instance[inputindex]
        expect_output = instance[outputindex]
        predict_output, raw_output = predictoneinstance(datainput, weight)
        # process the index of value 1 in np.array
        processdexpect = np.where(expect_output==1)[0][0]
        processdpredict = np.where(predict_output==1)[0][0]
        predictvsexpectlist.append([processdpredict,processdexpect])
    correct = 0
    for outputtup in predictvsexpectlist:
        if outputtup[0] == outputtup[1]:
            correct += 1
    accuracy = correct/len(predictvsexpectlist)
    return predictvsexpectlist, accuracy
```

#### 1.3.3 example.py

```
[]: import numpy as np
     from utils import *
     from stratified import *
     from neuralnetwork import *
     def g(x): # sigmoid function
         return 1/(1 + np.exp(-x))
     # Theta 1
     # 0.40000 0.10000
     # 0.30000 0.20000
     theta1 = np.array([[0.4, 0.1], [0.3, 0.2]])
     # Theta 2
     # 0.70000 0.50000 0.60000
     theta2 = np.array([0.7,0.5,0.6])
     weightlist1= [theta1,theta2]
     # Training set
     #
               Training instance 1
     #
                       x: [0.13000]
                       y: [0.90000]
     #
               Training instance 2
                       x: [0.42000]
                       y: [0.23000]
     # Training instance 1
     trainingcategory = {'x1':'numerical', 'y':'class_numerical'}
     trainingdata1 = np.array([0.13,0.9])
     trainingdata2 = np.array([0.42,0.23])
     inputdata1 = np.append(1,trainingdata1[0])
     inputdata2 = np.append(1,trainingdata2[0])
     exceptout1 = trainingdata1[1]
     exceptout2 = trainingdata2[1]
     lambda1 = 0
     def costfunction(expected_output, actual_output):
         j = -np.multiply(expected_output,np.log(actual_output)) - np.multiply((1 -u
      ⇔expected_output),np.log(1 - actual_output))
         return np.sum(j)
     def forwardtest(inputdata, weightl, expectedout):
         current_layer_a = inputdata
         print('current_a at 1 is',current_layer_a)
         current_layer_index = 0
         alist = []
         alist.append(current_layer_a)
```

```
for theta in weightl:
        z = np.dot(theta,current_layer_a)
        a = g(z)
        current_layer_a = np.append(1,a) if (current_layer_index+1 !=_
 →len(weightl)) else a
        print('current a at',current layer index+2,'is',current layer a)
       alist.append(current_layer_a)
        current layer index += 1
   result = current_layer_a
   print('prediction is', result)
   print('exceptout is', expectedout)
   print('cost is', costfunction(expectedout,result))
   return result, costfunction(expectedout, result), alist
print('example 1 instance 1 forward test')
r1,j1,a1 = forwardtest(inputdata1,weightlist1,exceptout1)
# Computing the error/cost, J, of the network
         Processing training instance 1
         Forward propagating the input [0.13000]
#
#
                  a1: [1.00000 0.13000]
                  z2: [0.41300 0.32600]
                  a2: [1.00000 0.60181 0.58079]
                 z3: [1.34937]
#
                  a3: [0.79403]
#
                 f(x): [0.79403]
          Predicted output for instance 1: [0.79403]
          Expected output for instance 1: [0.90000]
          Cost, J, associated with instance 1: 0.366
print('\n')
print('example 1 instance 2 forward test')
r2, j2, a2 = forwardtest(inputdata2, weightlist1, exceptout2)
        # Processing training instance 2
        # Forward propagating the input [0.42000]
                  a1: [1.00000
                                0.42000]
        #
                 z2: [0.44200 0.38400]
        #
                 a2: [1.00000 0.60874 0.59484]
                 z3: [1.36127]
                 a3: [0.79597]
                  f(x): [0.79597]
```

```
# Predicted output for instance 2: [0.79597]
        # Expected output for instance 2: [0.23000]
        # Cost, J, associated with instance 2: 1.276
print('\n')
jlist1 = np.array([j1,j2])
number of instance 1 = 2
def overallcost(jlist,n,weightl,lambda_reg):
    s = sumofweights(weightl,bias=0)*lambda_reg/(2*n)
    jsum = np.sum(jlist)
    return jsum/n + s
print('example 1 overall cost')
print(overallcost(jlist1,numberofinstance1,weightlist1,lambda1))
# Final (regularized) cost, J, based on the complete training set: 0.82098
print('\n')
def delta(weightl,alist,expect,actual):
    delta_layer_n = actual-expect
    deltalist = []
    deltalist.append(delta_layer_n)
    i = len(weight1)-1
    current delta = delta layer n
    while i > 0:
        delta_layer_now = np.multiply(np.multiply(np.dot(weightl[i].
 →T, current_delta), alist[i]), (1-alist[i]))
        current_delta = delta_layer_now[1:]
        deltalist.append(current_delta)
        i -= 1
    deltalist.reverse()
    return deltalist
def gradientD(weights_list,delta_list,a_list,biasterm=True):
    gradlist = []
    for i in range(len(weights_list)):
        anow = a list[i]
        deltanow = np.array([delta_list[i]]).T
        dotproduct = deltanow*anow
        # print('dotshape',dotproduct.shape)
        gradlist.append(dotproduct)
    return gradlist
print('example 1 instance 1 theta value')
delta1_1 = delta(weightlist1,a1,exceptout1,r1)
        # Computing gradients based on training instance 1
                  delta3: [-0.10597]
```

```
delta2: [-0.01270 -0.01548]
print(delta1_1)
print('\n')
print('example 1 instance 1 gradient value')
                # Gradients of Theta2 based on training instance 1:
                         -0.10597 -0.06378 -0.06155
                # Gradients of Theta1 based on training instance 1:
                          -0.01270 -0.00165
                          -0.01548 -0.00201
gradd1_1 = gradientD(weightlist1,delta1_1,a1)
print(gradd1 1)
print('\n')
print('example 1 instance 2 theta value')
delta1_2 = delta(weightlist1,a2,exceptout2,r2)
        # Computing gradients based on training instance 2
                 delta3: [0.56597]
                 delta2: [0.06740 0.08184]
print(delta1_2)
print('\n')
print('example 1 instance 2 gradient value')
                # Gradients of Theta2 based on training instance 2:
                          0.56597 0.34452 0.33666
                # Gradients of Theta1 based on training instance 2:
                          0.06740 0.02831
                          0.08184 0.03437
gradd1_2 = gradientD(weightlist1,delta1_2,a2)
print(gradd1_2)
print('\n')
def transposelistoflist(1):
   newlistoflist = []
   for i in range(len(1[0])):
       newlist = []
       for j in range(len(1)):
           newlist.append(l[j][i])
       newlistoflist.append(newlist)
   return newlistoflist
listofgradient = [gradd1_1,gradd1_2]
gradientP1 = [lambda1*t for t in weightlist1]
grad_D_transpose = transposelistoflist(listofgradient)
grad_D_sum = [np.sum(t,axis=0) for t in grad_D_transpose]
```

```
update_gradients = []
for i in range(len(grad_D_sum)):
   update_gradients.append((grad_D_sum[i] + gradientP1[i])*(1/
 →numberofinstance1))
print('example 1 update gradient value')
print(update_gradients)
        # The entire training set has been processes. Computing the average,
 ⇔(regularized) gradients:
        #
                 Final regularized gradients of Theta1:
        #
                         0.02735 0.01333
                         0.03318 0.01618
        #
                 Final regularized gradients of Theta2:
                         0.23000 0.14037 0.13756
print('\n')
print('end of example 1')
print('\n')
print('\n')
print('start of example 2')
# Initial Theta1 (the weights of each neuron, including the bias weight, are
⇔stored in the rows):
         0.42000 0.15000 0.40000
         0.72000 0.10000 0.54000
         0.01000 0.19000 0.42000
         0.30000 0.35000 0.68000
# Initial Theta2 (the weights of each neuron, including the bias weight, are
⇔stored in the rows):
         0.21000 0.67000 0.14000 0.96000 0.87000
         0.87000 0.42000 0.20000 0.32000 0.89000
         0.03000 0.56000 0.80000 0.69000 0.09000
# Initial Theta3 (the weights of each neuron, including the bias weight, are
⇔stored in the rows):
         0.04000 0.87000 0.42000 0.53000
         0.17000 0.10000 0.95000 0.69000
e2theta1 = np.array([[0.42,0.15,0.4],[0.72,0.1,0.54],[0.01,0.19,0.42],[0.3,0.
<sup>4</sup>35,0.68]])
e2theta2 = np.array([[0.21,0.67,0.14,0.96,0.87],[0.87,0.42,0.2,0.32,0.89],[0.
403,0.56,0.8,0.69,0.09])
e2theta3 = np.array([[0.04, 0.87, 0.42, 0.53], [0.17, 0.1, 0.95, 0.69]])
e2weightlist = [e2theta1,e2theta2,e2theta3]
# Training set
```

```
Training instance 1
                 x: [0.32000 0.68000]
#
                 y: [0.75000
                               0.98000]
#
          Training instance 2
                 x: [0.83000
                               0.02000]
#
                 y: [0.75000
                               0.28000]
e2input1 = np.array([0.32, 0.68])
e2input2 = np.array([0.83,0.02])
e2exceptout1 = np.array([0.75,0.98])
e2exceptout2 = np.array([0.75,0.28])
e2input1 = np.append(1,e2input1)
e2input2 = np.append(1,e2input2)
e2lambda0 = 0.25
print('example 2 instance 1 forward propagation')
e2r1,e2j1,e2a1 = forwardtest(e2input1,e2weightlist,e2exceptout1)
       # Processing training instance 1
       # Forward propagating the input [0.32000 0.68000]
                 a1: [1.00000 0.32000 0.68000]
                 z2: [0.74000 1.11920 0.35640
                                                  0.87440]
                 a2: [1.00000
                              0.67700 0.75384
                                                  0.58817
                                                            0.705661
                 z3: [1.94769 2.12136 1.48154]
                 a3: [1.00000 0.87519 0.89296
                                                  0.81480]
       #
                 z4: [1.60831 1.66805]
                 a4: [0.83318 0.84132]
                 f(x): [0.83318 \quad 0.84132]
       # Predicted output for instance 1: [0.83318  0.84132]
       # Expected output for instance 1: [0.75000 0.98000]
       # Cost, J, associated with instance 1: 0.791
print('\n')
print('example 2 instance 2 forward propagation')
e2r2,e2j2,e2a2 = forwardtest(e2input2,e2weightlist,e2exceptout2)
       # Processing training instance 2
       # Forward propagating the input [0.83000 0.02000]
                 a1: [1.00000 0.83000 0.02000]
                 z2: [0.55250 0.81380 0.17610 0.60410]
                 a2: [1.00000
                              0.63472 0.69292
                                                 0.54391
                                                            0.64659]
                 z3: [1.81696
                               2.02468 1.37327]
```

```
a3: [1.00000 0.86020 0.88336 0.79791]
                 z4: [1.58228 1.64577]
                 a4: [0.82953 0.83832]
                 f(x): [0.82953 \quad 0.83832]
       # Expected output for instance 2: [0.75000 0.28000]
       # Cost, J, associated with instance 2: 1.944
print('\n')
e2jlist = np.array([e2j1,e2j2])
e2numberofinstance = 2
def sumofweights(listofweights, bias=True): # computes the square of all weights_
 ⇔of the network and sum them up
   sum = 0
   for weight in listofweights:
       if bias:
           w = weight.copy()
           w[:, 0] = 0
           sum += np.sum(np.square(w))
           sum += np.sum(np.square(weight))
   return sum
def overallcost(jlist,n,weightl,lambda_reg):
   s = sumofweights(weightl,bias=1)*lambda_reg/(2*n)
   jsum = np.sum(jlist)
   return jsum/n + s
print('example 2 overall cost')
print(overallcost(e2jlist,e2numberofinstance,e2weightlist,e2lambda0))
# Final (regularized) cost, J, based on the complete training set: 1.90351
print('\n')
print('example 2 backpropagation')
print('\n')
print('example 2 instance 1 delta')
e2delta1 = delta(e2weightlist,e2a1,e2exceptout1,e2r1)
# Running backpropagation
#
         Computing gradients based on training instance 1
#
                 delta4: [0.08318 -0.13868]
#
                 delta3: [0.00639 -0.00925 -0.00779]
                 delta2: [-0.00087 -0.00133 -0.00053 -0.00070]
print(e2delta1)
```

```
print('\n')
print('example 2 instance 2 gradient')
               # Gradients of Theta3 based on training instance 1:
                       0.08318 0.07280 0.07427 0.06777
                        -0.13868 -0.12138 -0.12384 -0.11300
               # Gradients of Theta2 based on training instance 1:
                        0.00639 0.00433 0.00482 0.00376 0.00451
                        -0.00925 -0.00626 -0.00698 -0.00544 -0.00653
                        -0.00779 -0.00527 -0.00587 -0.00458 -0.00550
               # Gradients of Theta1 based on training instance 1:
                       -0.00087 -0.00028 -0.00059
                        -0.00133 -0.00043 -0.00091
                        -0.00053 -0.00017 -0.00036
                        -0.00070 -0.00022 -0.00048
e2grad1 = gradientD(e2weightlist,e2delta1,e2a1)
print(e2grad1)
print('\n')
print('example 2 instance 2 delta')
e2delta2 = delta(e2weightlist,e2a2,e2exceptout2,e2r2)
       # Computing gradients based on training instance 2
                delta4: [0.07953 0.55832]
                delta3: [0.01503 0.05809 0.06892]
                 delta2: [0.01694 0.01465 0.01999 0.01622]
print(e2delta2)
print('\n')
print('example 2 instance 2 gradient')
               # Gradients of Theta3 based on training instance 2:
                       0.07953 0.06841 0.07025 0.06346
                        0.55832 0.48027 0.49320 0.44549
               # Gradients of Theta2 based on training instance 2:
                        0.01503 0.00954 0.01042 0.00818 0.00972
                        0.05809 0.03687 0.04025 0.03160 0.03756
                        0.06892 0.04374 0.04775 0.03748 0.04456
               # Gradients of Theta1 based on training instance 2:
                       0.01694 0.01406 0.00034
                        0.01465 0.01216 0.00029
                        0.01999 0.01659 0.00040
                        0.01622 0.01346 0.00032
e2grad2 = gradientD(e2weightlist,e2delta2,e2a2)
print(e2grad2)
```

```
print('\n')
e2listofgradient = [e2grad1,e2grad2]
gradientP2 = [e2lambda0*t for t in e2weightlist]
for singleP in gradientP2:
    singleP[:, 0] = 0
e2_grad_D_transpose = transposelistoflist(e2listofgradient)
e2_grad_D_sum = [np.sum(t,axis=0) for t in e2_grad_D_transpose]
e2 update gradients = []
for i in range(len(grad_D_sum)):
    e2_update_gradients.append((e2_grad_D_sum[i] + gradientP2[i])*(1/
→e2numberofinstance))
print('example 2 update gradients')
print(e2_update_gradients)
        # The entire training set has been processes. Computing the average_{\sqcup}
 → (regularized) gradients:
                 Final regularized gradients of Theta1:
                          0.00804 0.02564 0.04987
        #
                          0.00666 0.01837 0.06719
        #
                          0.00973 0.03196 0.05252
                          0.00776 0.05037 0.08492
        #
                Final regularized gradients of Theta2:
                          0.01071 0.09068 0.02512 0.12597 0.11586
        #
                          0.02442 0.06780 0.04164 0.05308 0.12677
        #
                          0.03056 0.08924 0.12094 0.10270 0.03078
        #
                Final regularized gradients of Theta3:
        #
                         0.08135 0.17935 0.12476 0.13186
                          0.20982 0.19195 0.30343 0.25249
print('\n')
print('end of example 2')
```

### 1.3.4 stratified.py

```
datacopy = np.copy(data).T
    classes = list(Counter(datacopy[classindex]).keys())
    nclass = len(classes) # number of classes
    listofclasses = []
    for oneclass in classes:
        index = [idx for idx, element in enumerate(datacopy[classindex]) if
 ⇔element == oneclass]
        oneclassdata = np.array(datacopy.T[index])
        np.random.shuffle(oneclassdata)
        listofclasses.append(oneclassdata)
    splitted = [np.array_split(i, k) for i in listofclasses]
    combined = []
    for j in range(k):
        ithterm = []
        for i in range(nclass):
            if len(ithterm) == 0:
                ithterm = splitted[i][j]
            else:
                ithterm = np.append(ithterm, splitted[i][j],0)
        combined.append(ithterm)
    return combined
def ohe_stratifiedkfold(ohed_data, categorydict, k = 10):
    ohed_c = np.copy(ohed_data)
    n = 0
    classindices = []
    for i in categorydict:
        if categorydict[i] == "class numerical":
            classindices.append(n)
        n += 1
    # nclass = len(classindices)
    listofclasses = []
    for index in classindices:
        ohed_copy = np.copy(ohed_c)
        # delete data with value !=1 at index
        ohed_copy = np.delete(ohed_copy, np.where((ohed_copy[:,index] == 0)),__
 ⇒axis=0)
        # shuffle data
        np.random.shuffle(ohed_copy)
        listofclasses.append(ohed_copy)
    splitted = [np.array_split(i, k) for i in listofclasses]
```

```
combined = []
    for j in range(k):
        ithterm = []
        for i in range(len(classindices)):
            if len(ithterm) == 0:
                ithterm = splitted[i][j]
            else:
                ithterm = np.append(ithterm,splitted[i][j],0)
        combined.append(ithterm)
    return combined
# def k foldcrossvalidneuralnetwork(raw_data, rawcategory, layerparameter, k = 1
 →10, minibatchk = 15, lambda_req = 0.15, learning_rate = 0.01, epsilon 0 = 0.
 \hookrightarrow00001, softstop = 6000, printq = False):
      folded = stratifiedkfold(raw_data, rawcategory, k)
#
      listofnd = []
#
      accuracylist = []
#
      listofilist = []
#
      for i in range(k):
#
          if printq:
#
              print('fold',i+1)
#
          rawtestdataset = folded[i].copy()
#
          rawfoldedcopy = folded.copy()
#
          rawfoldedcopy.pop(i)
          rawtraindataset = np.vstack(rawfoldedcopy)
#
          ohe_traindata, ohe_category = onehotencoder(rawtraindataset,_
 →rawcategory)
          ohe_testdata = onehotencoder(rawtestdataset, rawcategory)[0]
          n ohe train, minmax = normalizetrain(ohe traindata, ohe category)
#
          n_ohe_test = normalizealltest(ohe_testdata, ohe_category, minmax)
          finalweight, jlist = train neural network(n ohe train, ohe category,
 →layerparameter, minibatchk, lambda req, learning rate, epsilon 0, softstop, u
 ⇔printq)
          predictvsexpect, singleaccuracy = predict_many_nn(n_ohe_test,__
 ⇔ohe category, finalweight)
          listofnd.append(predictusexpect)
#
          accuracylist.append(singleaccuracy)
          listofjlist.append(jlist)
      acc = np.mean(accuracylist)
      return listofnd, acc, listofilist
def kfoldcrossvalidneuralnetwork(raw_data, rawcategory, layerparameter, k = 10, u
 minibatchk = 15, lambda_reg = 0.15, learning_rate = 0.01, epsilon_0 = 0.
 ⇔00001, softstop = 6000, printq = False):
```

```
ohe_data,ohe_category = onehotencoder(raw_data, rawcategory)
  folded = ohe_stratifiedkfold(ohe_data, ohe_category, k)
  listofnd = []
  accuracylist = []
  listofjlist = []
  for i in range(k):
      print('fold',i+1,'training in progress')
      if printq:
          print('fold',i+1)
      ohe_test = folded[i].copy()
      ohe_copy = folded.copy()
      ohe_copy.pop(i)
      ohe_train = np.vstack(ohe_copy)
      n_ohe_train,minmax = normalizetrain(ohe_train, ohe_category)
      n_ohe_test = normalizealltest(ohe_test, ohe_category, minmax)
      finalweight, jlist = train_neural_network(n_ohe_train, ohe_category,__
-layerparameter, minibatchk, lambda_reg, learning_rate, epsilon_0, softstop,__
→printq)
      predictvsexpect, singleaccuracy = predict_many_nn(n_ohe_test,__
⇔ohe_category, finalweight)
      print('fold',i+1,'training completed, accuracy = ',singleaccuracy)
      listofnd.append(predictvsexpect)
      accuracylist.append(singleaccuracy)
      listofjlist.append(jlist)
  acc = np.mean(accuracylist)
  return listofnd, acc, listofjlist
```

#### 1.3.5 run.py

```
[]: from utils import *
  from stratified import *
  from neuralnetwork import *

def importhousedata():
    house = importfile('hw3_house_votes_84.csv', ',')
    housecategory = {}
    for i in house[0]:
        housecategory[i] = 'categorical'
    housecategory["class"] = 'class'
    housedata = np.array(house[1:]).astype(float)
    return housedata, housecategory

def importwinedata():
    wine = importfile('hw3_wine.csv', '\t')
    winecategory = {}
    for i in wine[0]:
```

```
winecategory[i] = 'numerical'
    winecategory["# class"] = 'class'
    winedata = np.array(wine[1:]).astype(float)
    return winedata, winecategory
def importcancerdata():
    cancer = importfile('hw3_cancer.csv', '\t')
    cancercategory = {}
    for i in cancer[0]:
        cancercategory[i] = 'numerical'
    cancercategory["Class"] = 'class'
    cancerdata = np.array(cancer[1:]).astype(float)
    return cancerdata, cancercategory
def importcmcdata():
    cmc = importfile('cmc.data', ',')
    cmccategory = {"Wife's age":"numerical","Wife's education":"categorical",
    "Husband's education": "categorical", "Number of children ever born":

¬"numerical",
    "Wife's religion": "binary", "Wife's now working?": "binary",
    "Husband's occupation": "categorical", "Standard-of-living index":

¬"categorical",
    "Media exposure": "binary", "Contraceptive method used": "class"}
    cmcdata = np.array(cmc).astype(int)
    return cmcdata, cmccategory
if __name__=="__main__":
    housedata, housecategory = importhousedata()
    winedata, winecategory = importwinedata()
    cancerdata, cancercategory = importcancerdata()
    cmcdata,cmccategory = importcmcdata()
    hiddenlayerparameter = [3,2]
    listoflistofoutputs, acc, listofjlist = ____
 →kfoldcrossvalidneuralnetwork(housedata, housecategory, hiddenlayerparameter, ⊔
 -k = 5, minibatchk = 3, lambda_reg = 0.1, learning_rate = 0.1, epsilon_0 = 0.
 ⇒0001, softstop = 2000, printq = False)
    print(acc)
```

### 1.3.6 evaluationmatrix.py

```
[]: import math
  import numpy as np
  import matplotlib.pyplot as plt
  from IPython.display import display, Markdown

# I reused the code from my last assignment.
```

```
def accuracy(truePosi, trueNega, falsePosi, falseNega): # Count of all four
        return (truePosi+trueNega)/(truePosi+trueNega+falsePosi)
def precision(truePosi, trueNega, falsePosi, falseNega):
        if (truePosi+falsePosi) == 0:
                return 0
       preposi = truePosi/(truePosi+falsePosi)
        # prenega = trueNega/(trueNega+falseNega)
       return preposi
def recall(truePosi, trueNega, falsePosi, falseNega):
        if (truePosi+falseNega)== 0:
                return ()
       recposi = truePosi/(truePosi+falseNega)
        # recnega = trueNega/(trueNega+falsePosi)
       return recposi
def fscore(truePosi, trueNega, falsePosi, falseNega, beta: 1):
       pre = precision(truePosi, trueNega, falsePosi, falseNega)
       rec = recall(truePosi, trueNega, falsePosi, falseNega)
        if (pre*(beta**2)+rec) == 0:
                return 0
        f = (1+beta**2)*((pre*rec)/(pre*(beta**2)+rec))
        return f
def evaluate(listsofoutput, positivelabel, beta=1):
    # list is list of [predicted, actual]
   listoftptnfpfn = []
   accuarcylists = []
   precisionlists = []
   recalllists = []
   fscorelists = []
   for output in listsofoutput:
        tp, tn, fp, fn, = 0, 0, 0, 0
       for i in range(len(output)):
            if output[i][0] == positivelabel and output[i][1] == positivelabel:
            elif output[i][0] != positivelabel and output[i][0] == output[i][1]:
            elif output[i][0] == positivelabel and output[i][1] !=_
 →positivelabel:
            elif output[i][0] != positivelabel and output[i][1] ==__
 →positivelabel:
                fn += 1
        tptnfpfn = [tp, tn, fp, fn]
```

```
listoftptnfpfn.append(tptnfpfn)
        accuarcylists.append(accuracy(tp, tn, fp, fn))
        precisionlists.append(precision(tp, tn, fp, fn))
        recalllists.append(recall(tp, tn, fp, fn))
        fscorelists.append(fscore(tp, tn, fp, fn, beta))
    return accuarcylists, precisionlists, recalllists, fscorelists,
 \hookrightarrowlistoftptnfpfn
def meanevaluation(listsofoutput, positivelabel, beta=1):
    accuarcylists, precisionlists, recalllists, fscorelists, notused = __
 ⇔evaluate(listsofoutput, positivelabel, beta)
    return sum(accuarcylists)/len(accuarcylists), sum(precisionlists)/
 Gen(precisionlists), sum(recalllists)/len(recalllists), sum(fscorelists)/
 →len(fscorelists)
def markdownaprf(acc,pre,rec,fsc,beta,nvalue,title):
    acc, pre, rec, fsc = round(acc,3), round(pre,3), round(rec,3), round(fsc,3)
    display(Markdown(rf"""
        Result/Stat of {nvalue} trees random forest of {title}:
    | **Accuracy** | **Precision** | **Recall** | **F-Score, Beta={beta}** |
    | :---: | :---: | :---: |
    |{acc} | {pre} | {rec} | {fsc} |
    """))
def markdownmatrix(tptnfpfn,title):
    tp, tn, fp, fn = tptnfpfn[0], tptnfpfn[1], tptnfpfn[2], tptnfpfn[3]
    display(Markdown(rf"""
    Confusion Matrix: {title}
    | | **Predicted +** | **Predicted-** |
    | :--- | :--- | :--- |
    | **Actual +** | {tp} | {fp} |
    | **Actual -** | {fn} | {tn} |
    """))
def confusionmatrix(truePosi, trueNega, falsePosi, falseNega, title=""):
        fig = plt.figure()
        plt.title(title)
        col labels = ['Predict:+', 'Predict:-']
        row_labels = ['Real:+', 'Real:-']
        table_vals = [[truePosi, falseNega], [falsePosi, trueNega]]
        the_table = plt.table(cellText=table_vals,
                      colWidths=[0.1] * 3,
                      rowLabels=row_labels,
                      colLabels=col labels,
                      loc='center')
        the_table.auto_set_font_size(False)
        the_table.set_fontsize(24)
```

```
the_table.scale(4, 4)

plt.tick_params(axis='x', which='both', bottom=False, top=False, u

labelbottom=False)

plt.tick_params(axis='y', which='both', right=False, left=False, u

labelleft=False)

for pos in ['right', 'top', 'bottom', 'left']:

plt.gca().spines[pos].set_visible(False)

plt.show()

return
```