

$$\theta = [5,3]$$

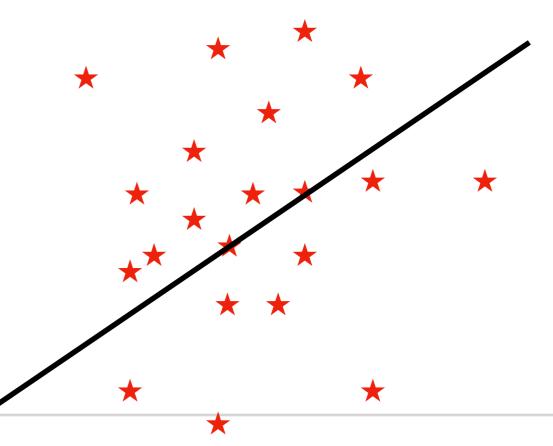
$$\hat{y}^{(j)} = sign(\theta x^{(j)})$$
or
$$\hat{y}^{(j)} = sign(\theta_1 x_1^{(j)} + \theta_2 x_2^{(j)})$$

$$\star \qquad \star \qquad \star \qquad \star$$

$$\star \qquad$$

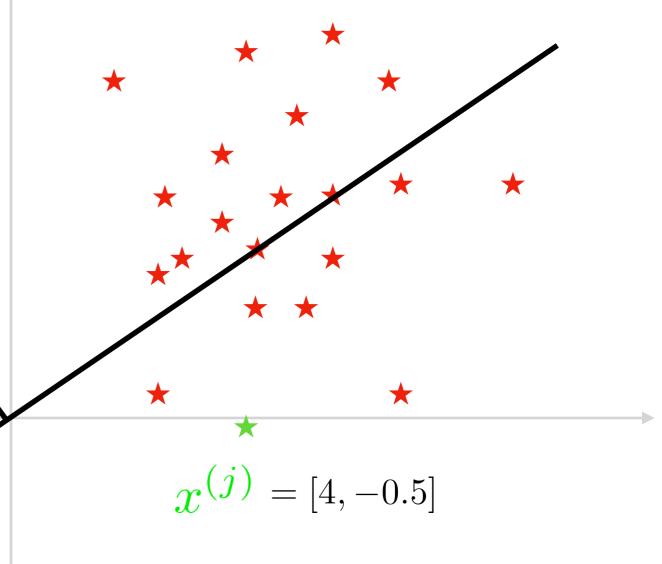
$$\Theta = [-1, 1]$$

$$\hat{y}^{(j)} = sign(\theta x^{(j)})$$
or
$$\hat{y}^{(j)} = sign(\theta_1 x_1^{(j)} + \theta_2 x_2^{(j)})$$



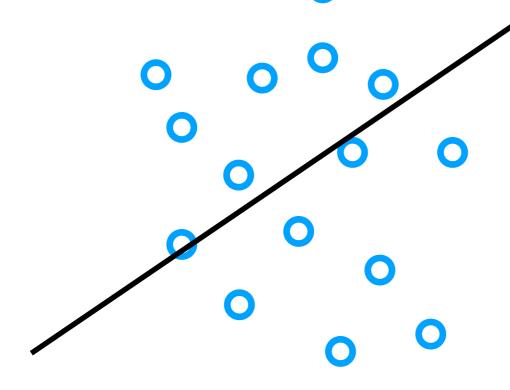
$$\Theta = [-3, 3]$$

$$\hat{y}^{(j)} = sign(\theta x^{(j)})$$
or
$$\hat{y}^{(j)} = sign(\theta_1 x_1^{(j)} + \theta_2 x_2^{(j)})$$

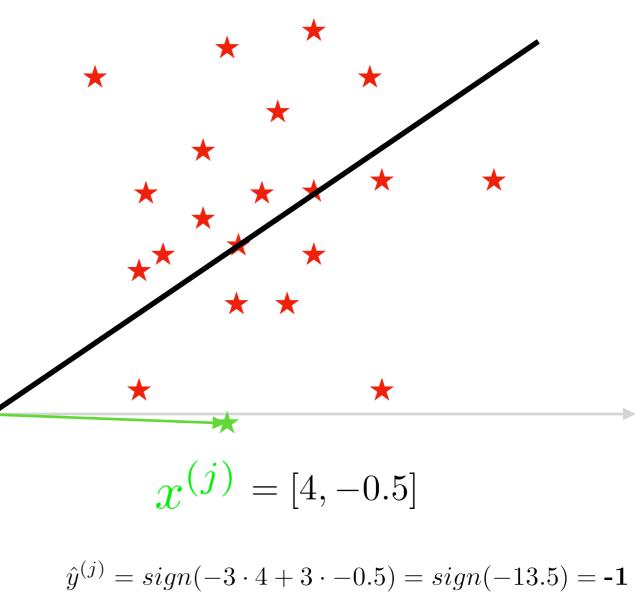


Wrong!

$$\Theta$$
 = [-3, 3] 
$$\hat{y}^{(j)} = sign(\theta x^{(j)})$$
 or 
$$\hat{y}^{(j)} = sign(\theta_1 x_1^{(j)} + \theta_2 x_2^{(j)})$$



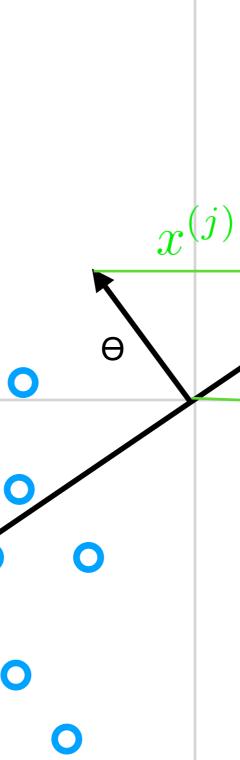
θ

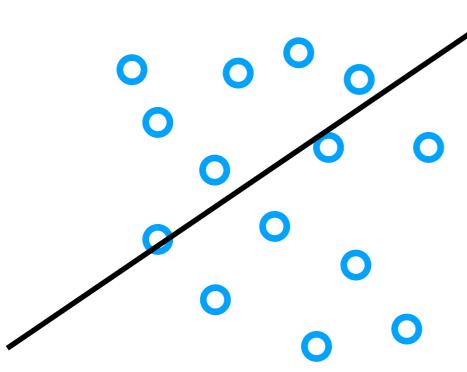


$$\hat{y}^{(j)} = sign(-3 \cdot 4 + 3 \cdot -0.5) = sign(-13.5) = -1$$

Wrong!

$$\Theta$$
 = [-3, 3]  $\hat{y}^{(j)} = sign(\theta x^{(j)})$  or  $\hat{y}^{(j)} = sign(\theta_1 x_1^{(j)} + \theta_2 x_2^{(j)})$ 



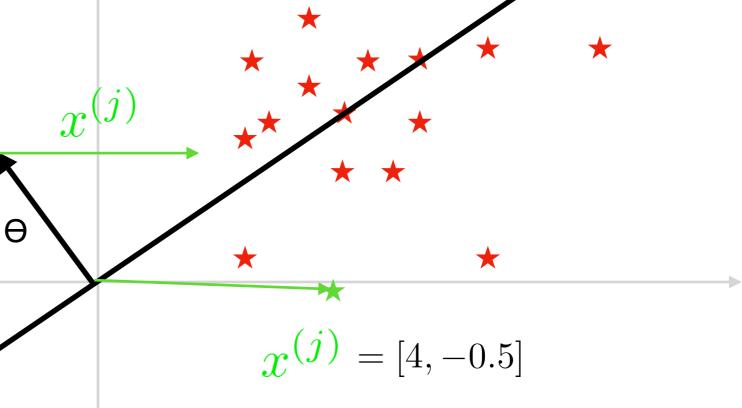


$$x^{(j)} = [4, -0.5]$$

$$\hat{y}^{(j)} = sign(-3 \cdot 4 + 3 \cdot -0.5) = sign(-13.5) = -1$$

$$\theta \leftarrow \theta + \alpha (y^{(j)} - \hat{y}^{(j)}) x^{(j)}$$

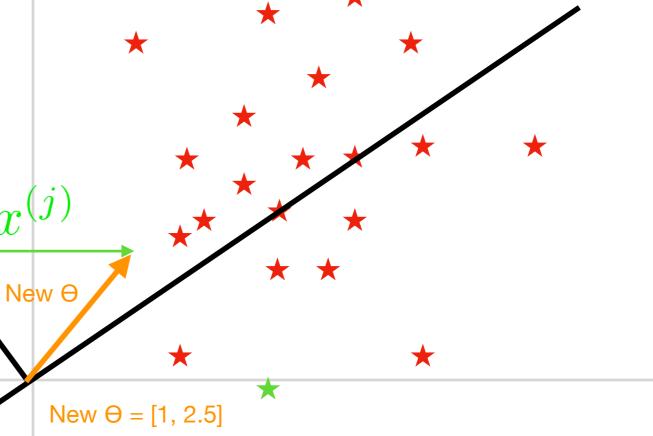
$$\Theta = [-3, 3]$$
 
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$$\hat{y}^{(j)} = sign(\theta_1 x_1^{(j)} + \theta_2 x_2^{(j)})$$



$$\theta \leftarrow \theta + \alpha (y^{(j)} - \hat{y}^{(j)}) x^{(j)}$$
 $\theta_1 \leftarrow -3 + 0.5(1 - (-1))4 = 1$ 
 $\theta_2 \leftarrow 3 + 0.5(1 - (-1))(-0.5) = \mathbf{2.5}$ 

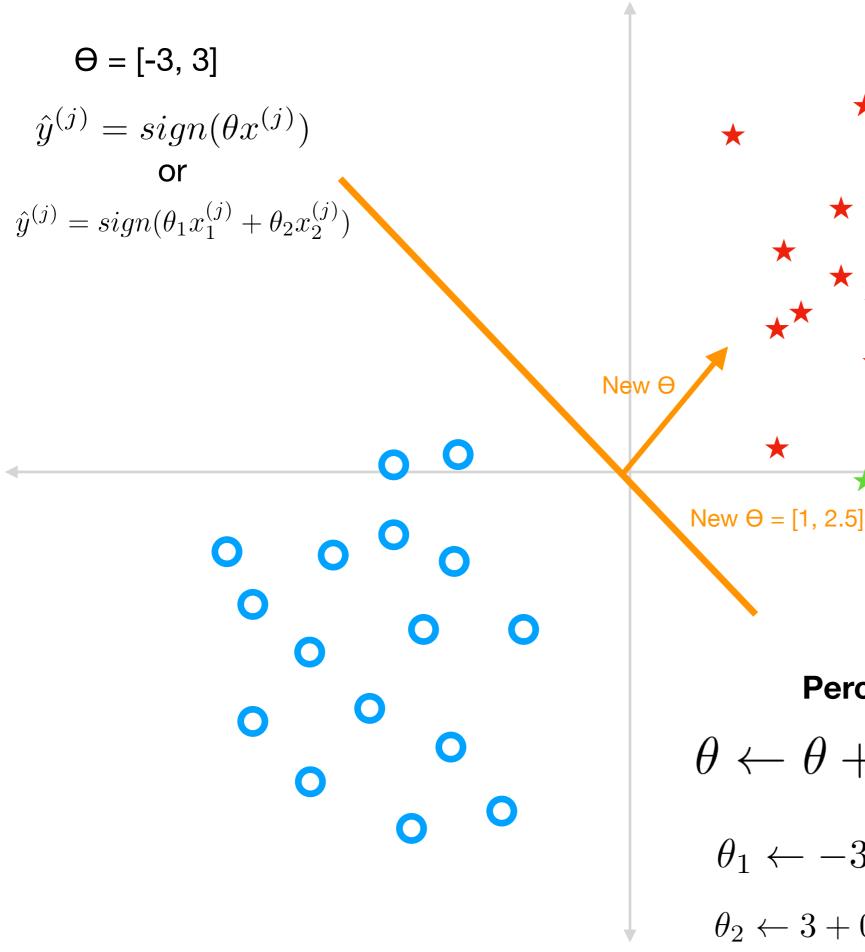
$$\Theta = [-3, 3]$$

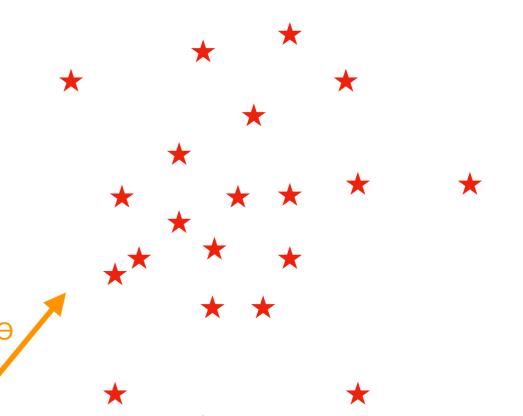
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 $x^{(j)} = [4, -0.5]$ 

$$\theta \leftarrow \theta + \alpha (y^{(j)} - \hat{y}^{(j)}) x^{(j)}$$
 $\theta_1 \leftarrow -3 + 0.5(1 - (-1))4 = \mathbf{1}$ 
 $\theta_2 \leftarrow 3 + 0.5(1 - (-1))(-0.5) = \mathbf{2.5}$ 

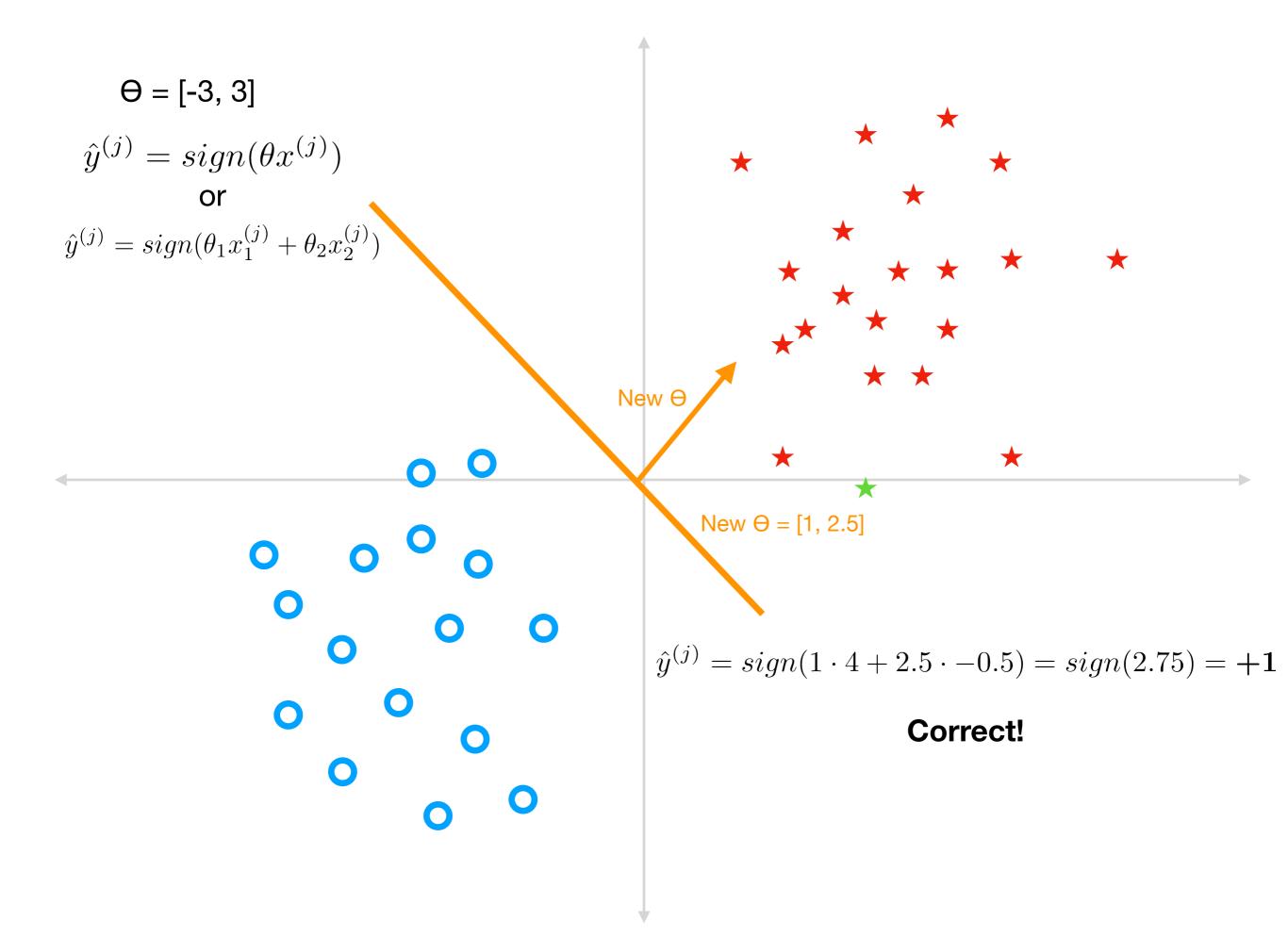


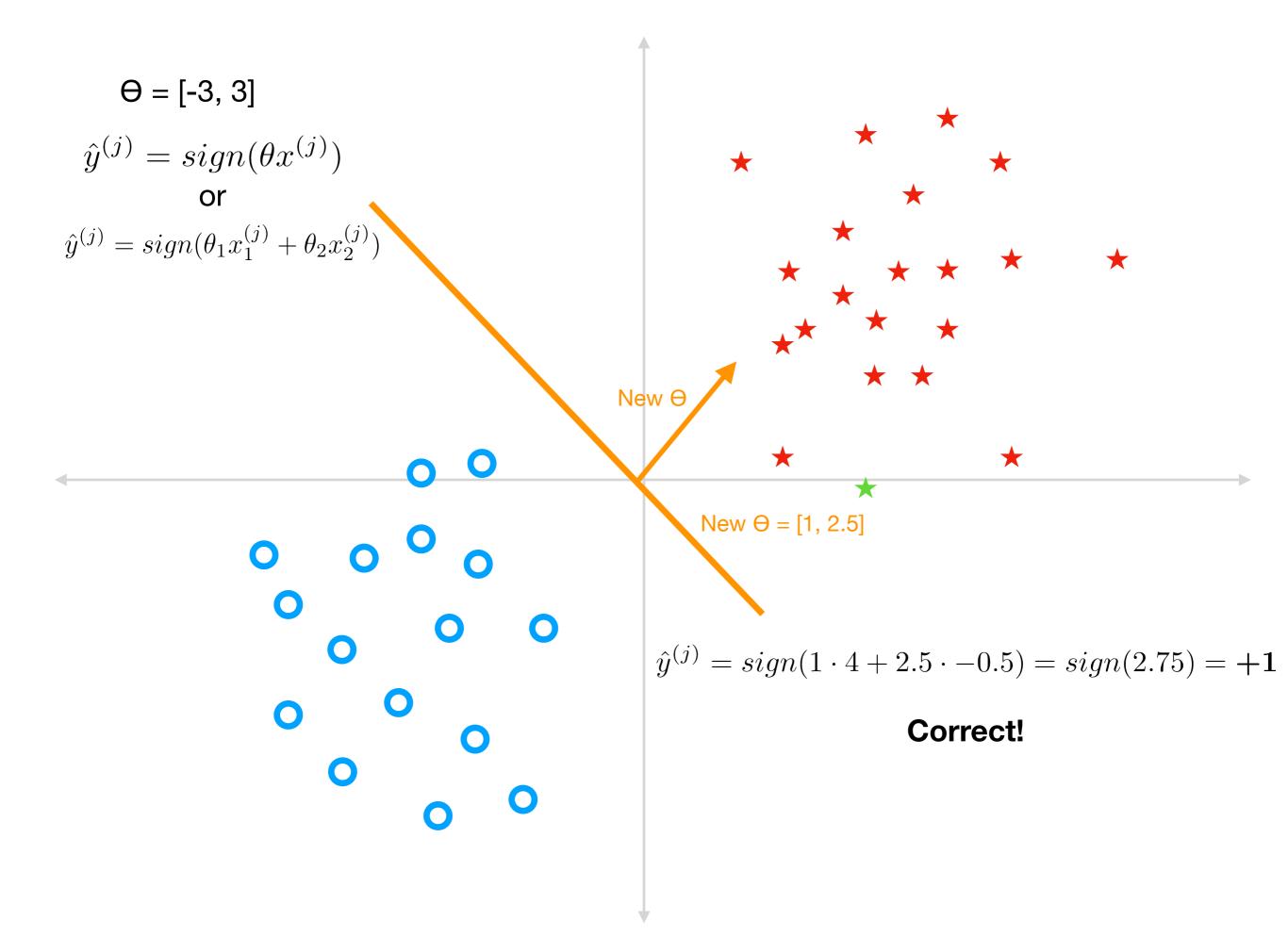


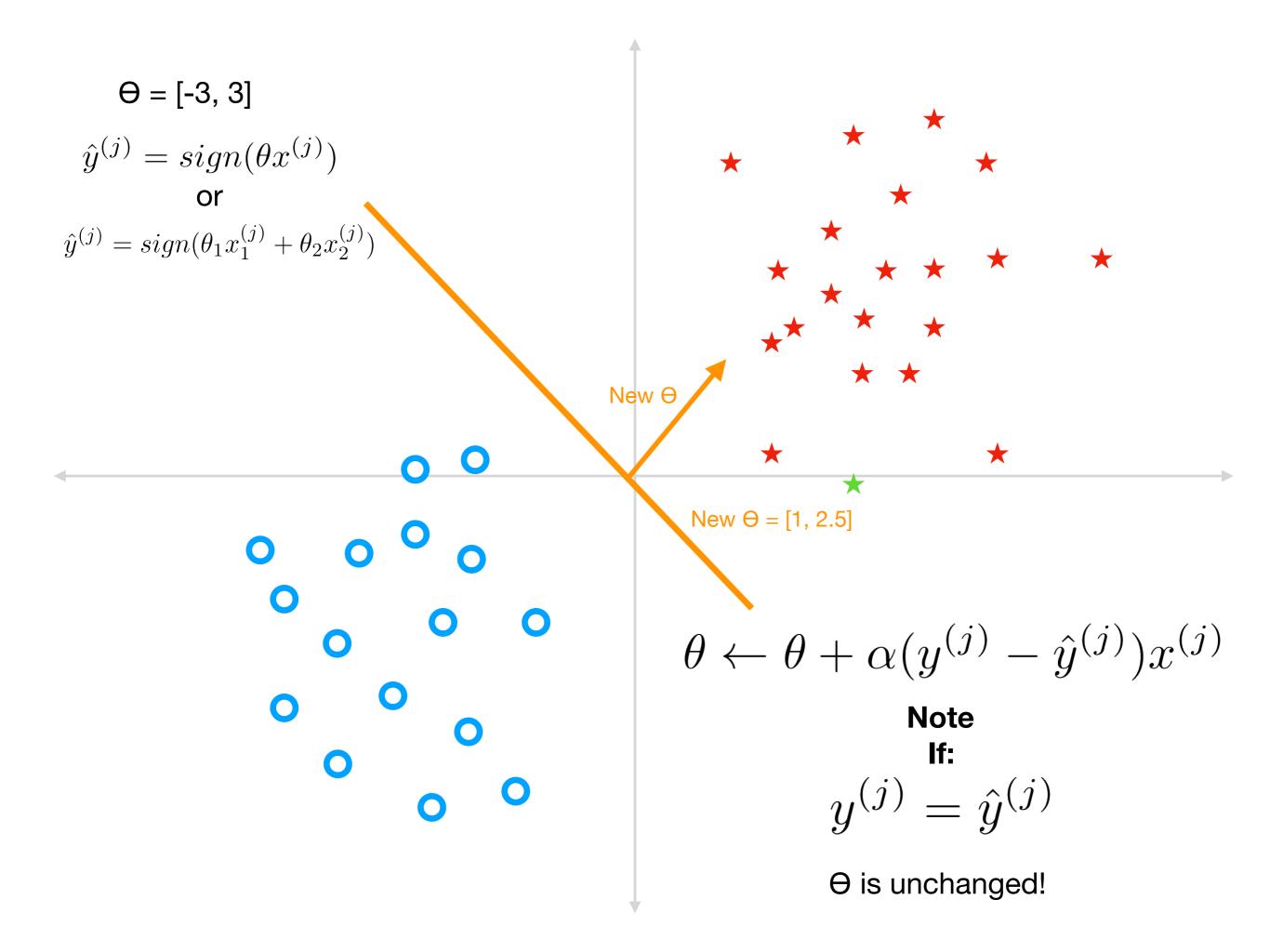
$$\theta \leftarrow \theta + \alpha (y^{(j)} - \hat{y}^{(j)}) x^{(j)}$$

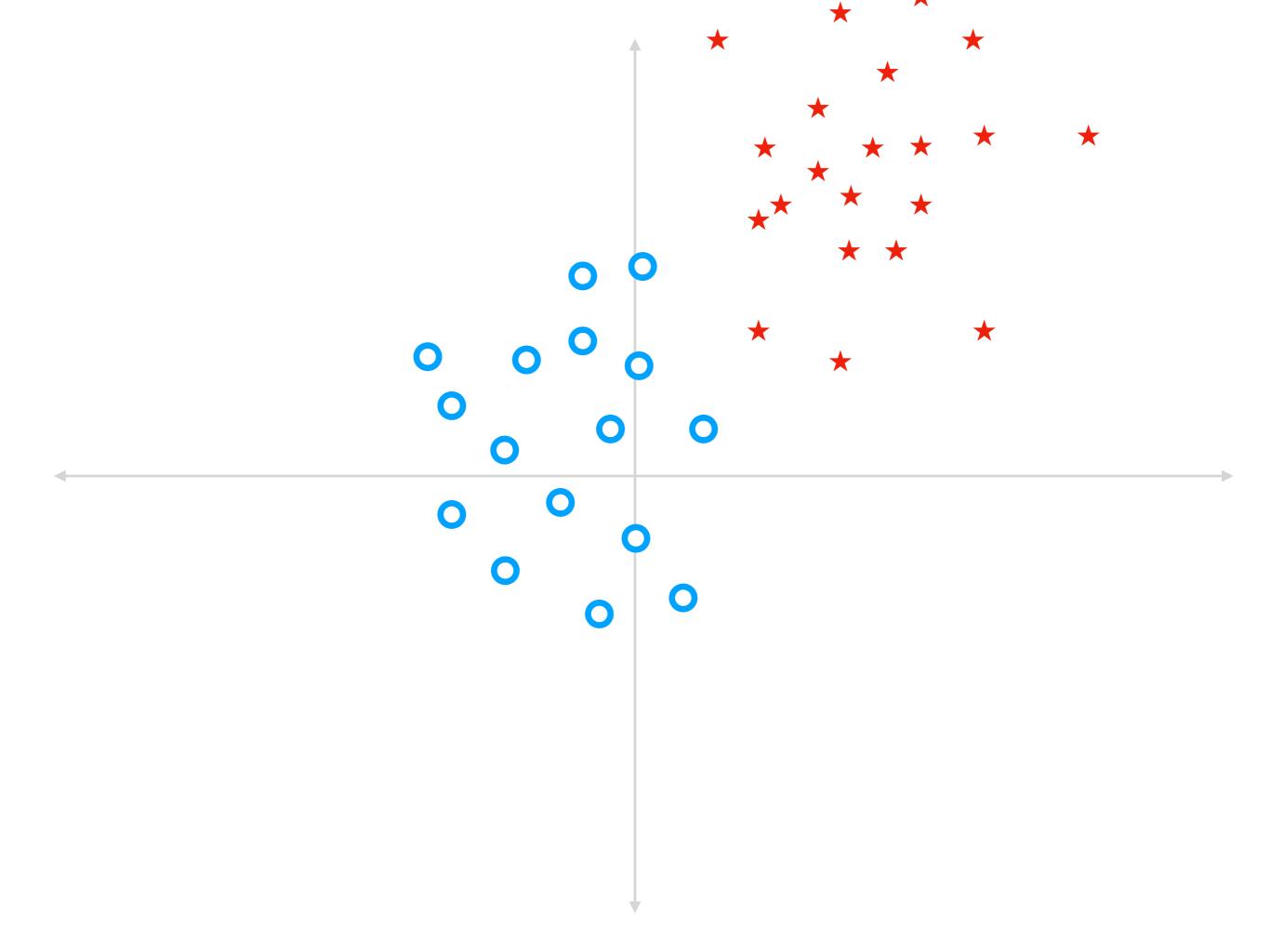
$$\theta_1 \leftarrow -3 + 0.5(1 - (-1))4 = \mathbf{1}$$

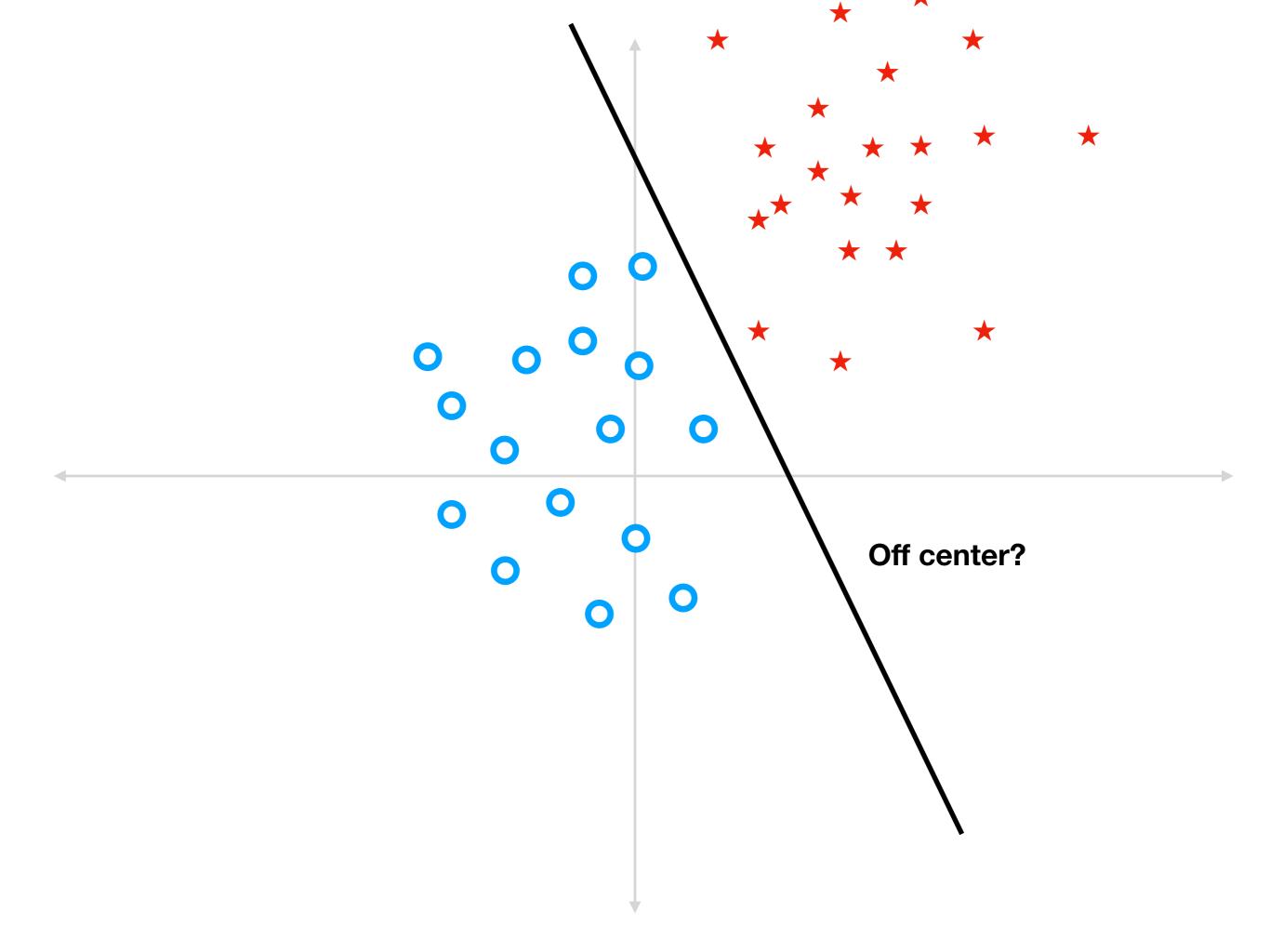
$$\theta_2 \leftarrow 3 + 0.5(1 - (-1))(-0.5) = \mathbf{2.5}$$







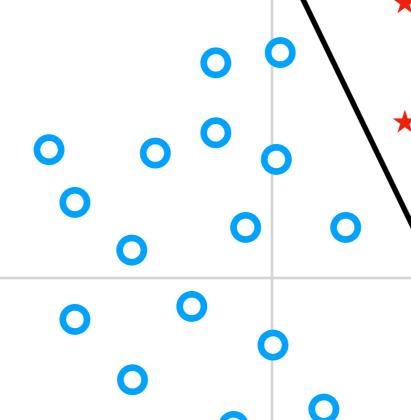




# Add bias to decision rule $\hat{y}^{(j)} = sign(\theta_0 + \theta_1 x_1^{(j)} + \theta_2 x_2^{(j)})$ **Boundary:** $0 = \theta_0 + \theta_1 x_1^{(j)} + \theta_2 x_2^{(j)}$ $x_2^{(j)} = -\frac{\theta_0}{\theta_2} + -\frac{\theta_0}{\theta_1} x_1^{(j)}$

# Add bias to decision rule

$$\hat{y}^{(j)} = sign(\theta_0 + \theta_1 x_1^{(j)} + \theta_2 x_2^{(j)})$$



#### Trick:

$$\hat{y}^{(j)} = sign(\theta_0(1) + \theta_1 x_1^{(j)} + \theta_2 x_2^{(j)})$$

#### So let:

$$x^{(j)} = [x_1^{(j)}, x_2^{(j)}] \to x^{(j)} = [1, x_1^{(j)}, x_2^{(j)}]$$

#### Then:

$$\hat{y}^{(j)} = sign(\theta x^{(j)})$$

# **Boundary:**

$$0 = \theta_0 + \theta_1 x_1^{(j)} + \theta_2 x_2^{(j)}$$

$$0 = \theta_0 + \theta_1 x_1^{(j)} + \theta_2 x_2^{(j)}$$
$$x_2^{(j)} = -\frac{\theta_0}{\theta_2} + -\frac{\theta_0}{\theta_1} x_1^{(j)}$$