

## A1 Analysis

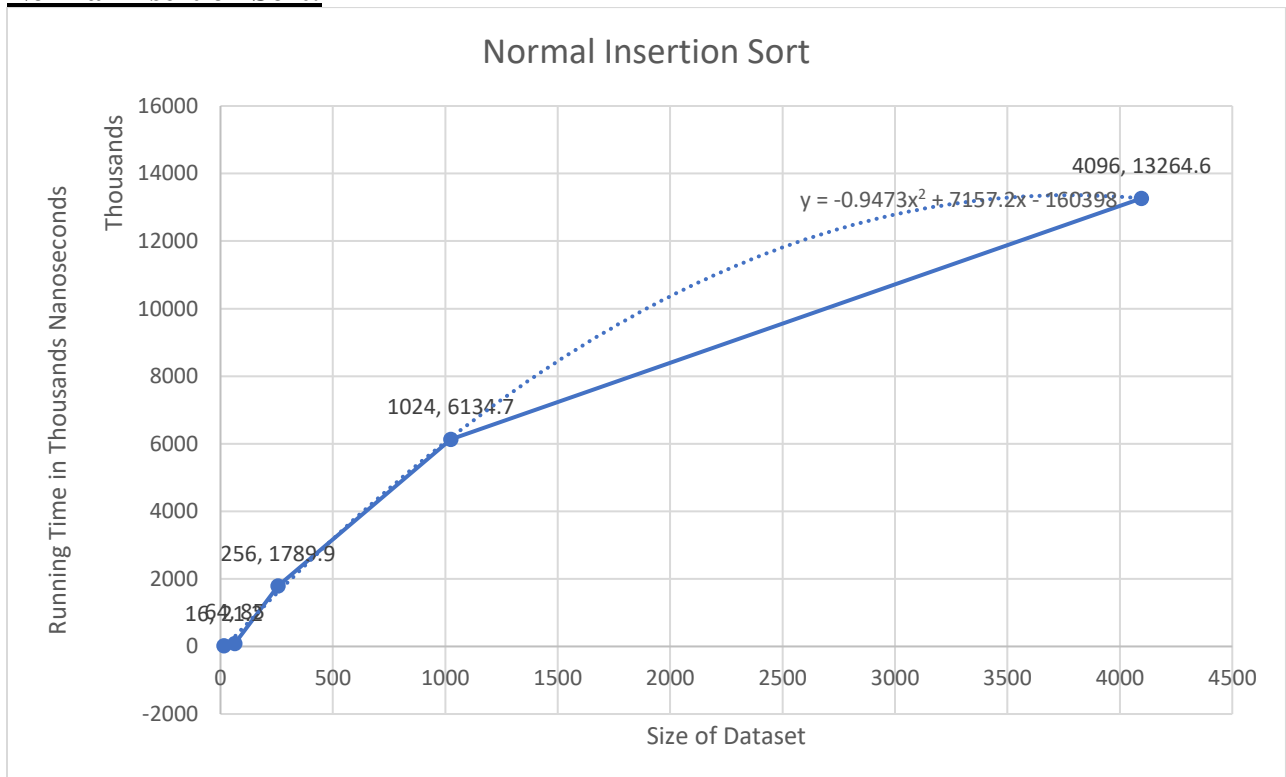
### Algorithms Running Time for Various Dataset Sizes:

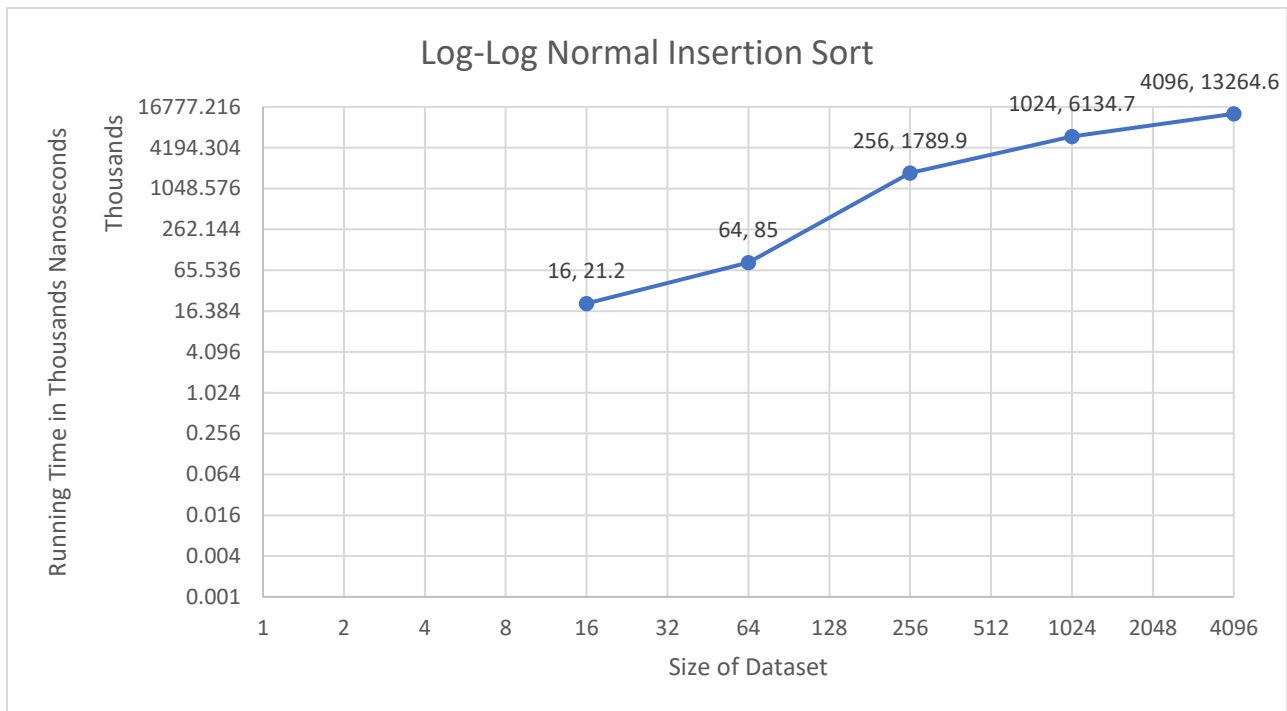
Size of Dataset	Execution Time of Sorting Algorithms (in nanoseconds)							
	Insertion			Merge		Quick		Heap
	Normal	Comparable	Binary	TD	BU	Normal/ Basic	Median Three Partition	Normal
$2^4$	21200	9100	27800	7500	10600	11700	71800	14700
$2^6$	85000	49700	459500	17000	85600	41100	116400	69000
$2^8$	1789900	761600	1409200	87100	569000	156600	395000	258000
$2^{10}$	6134700	4619000	16369400	691600	2964100	635000	1106500	478600
$2^{12}$	13264600	31440400	85867800	9477600	46785500	2131100	1478000	1427600

### 3.1.1 Normal and Log-Log Graphs of Sorting Algorithms

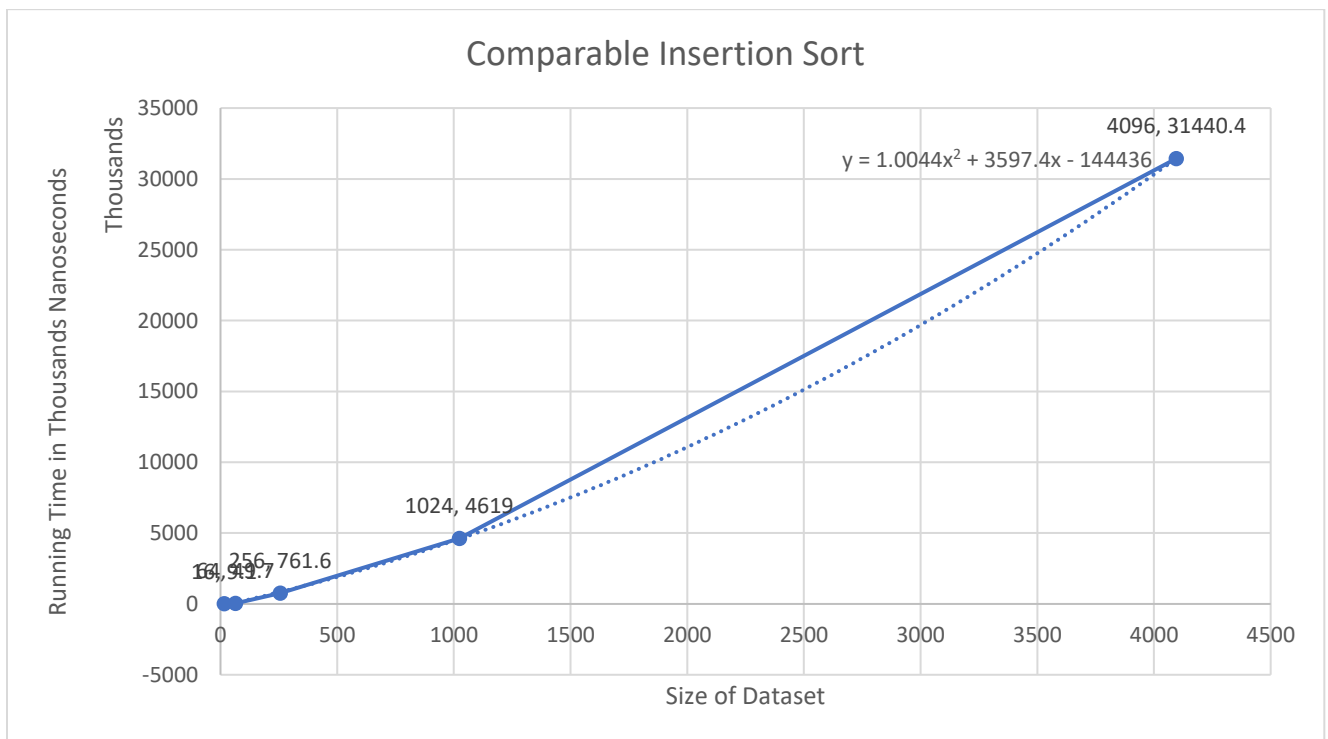
Note : Log base 2 used and scale for y-axis is in thousands nanoseconds to look cleaner

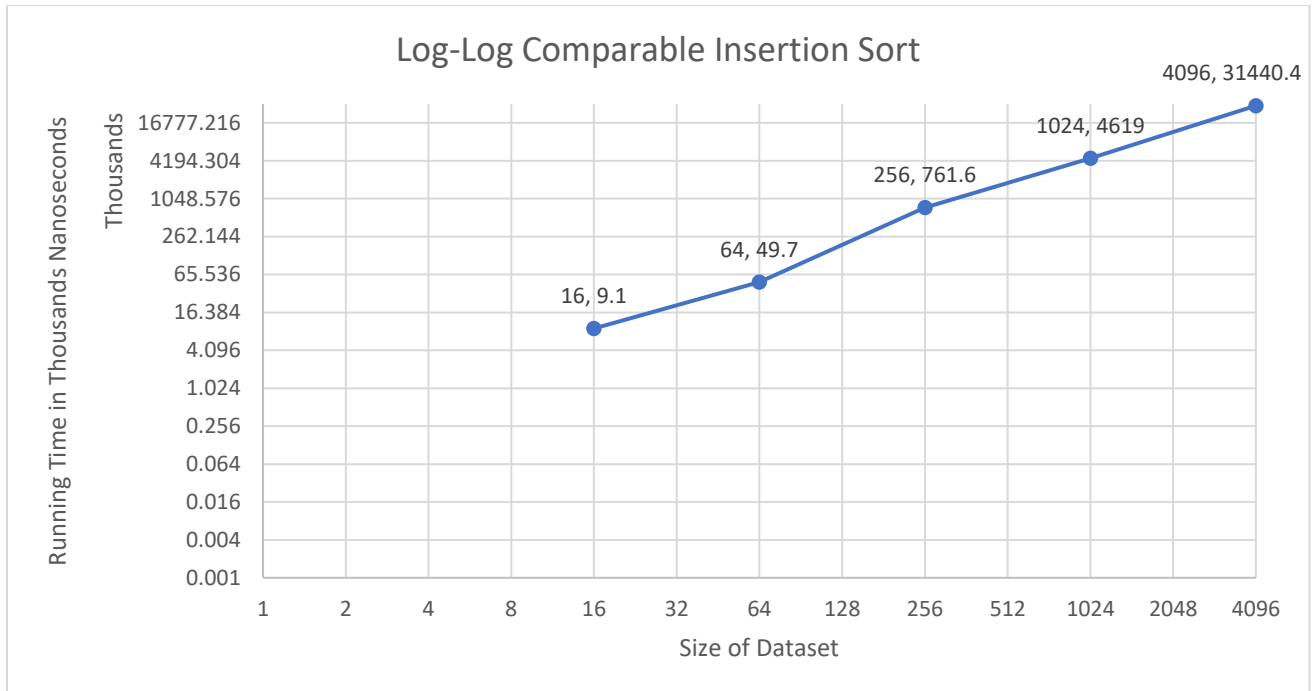
#### Normal Insertion Sort:



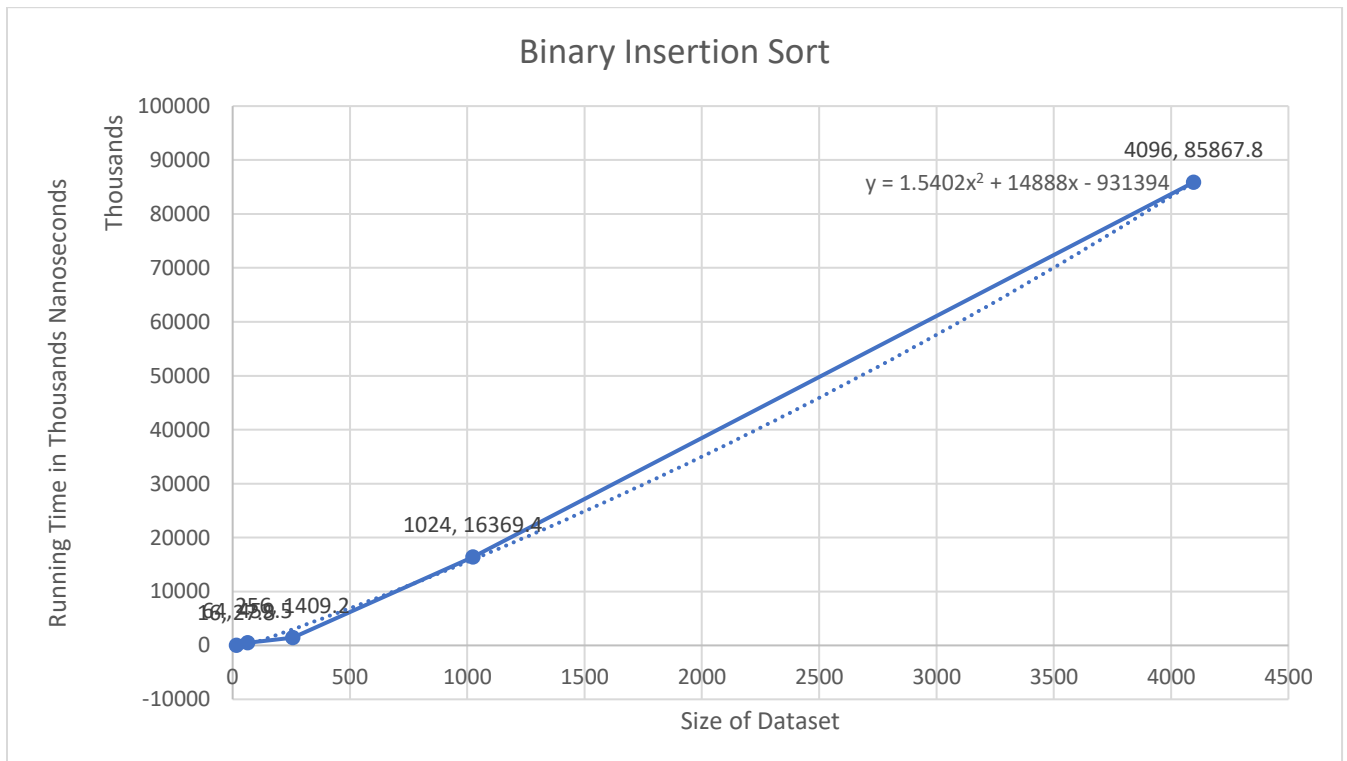


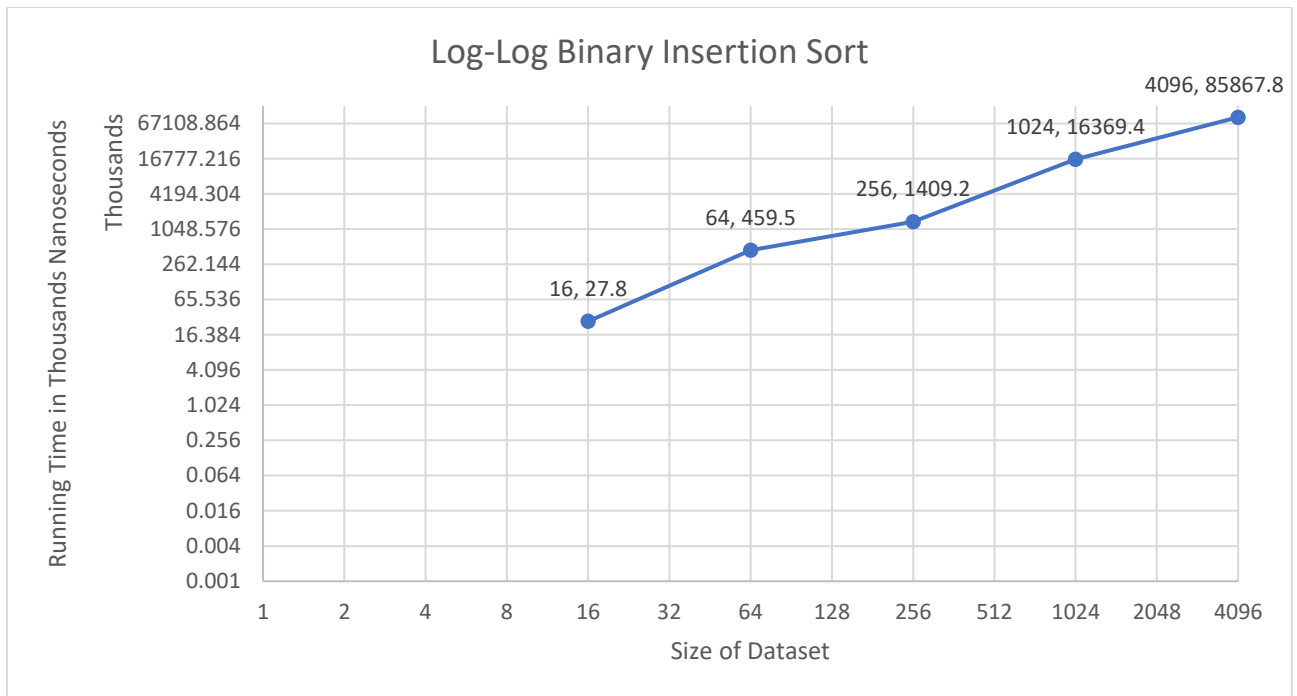
**Comparable Insertion Sort:**



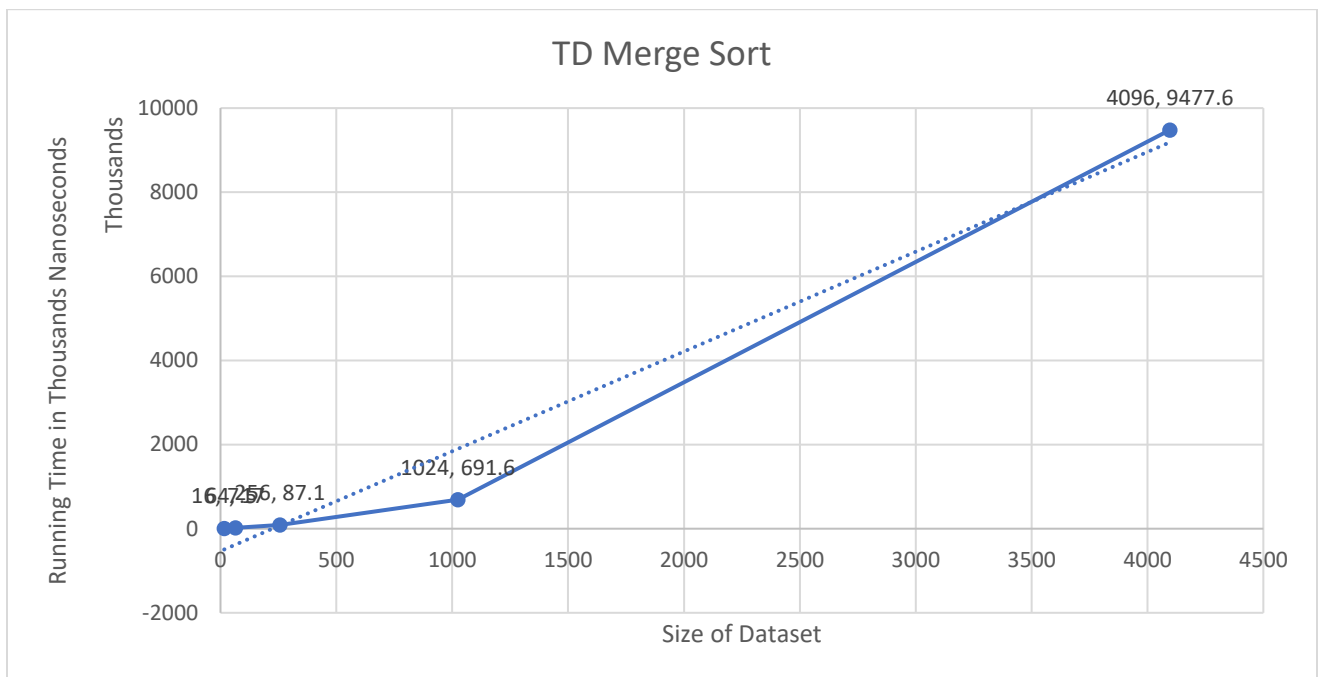


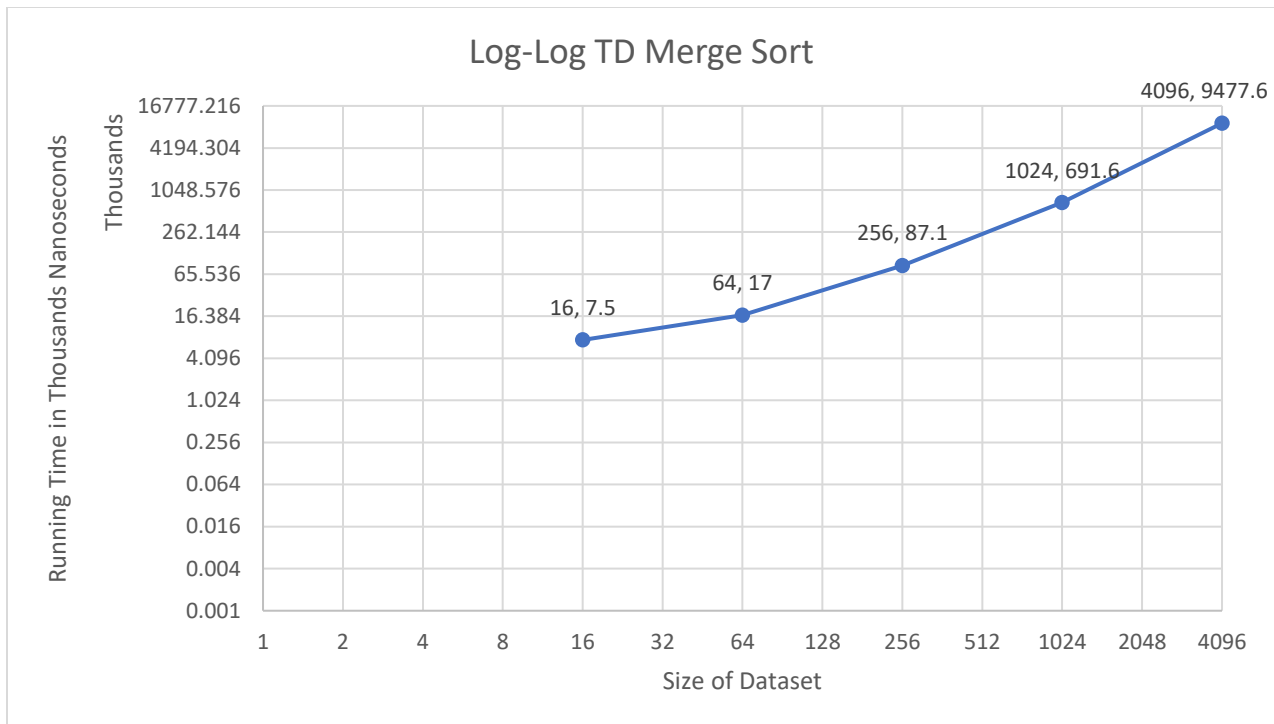
### Binary Insertion Sort:



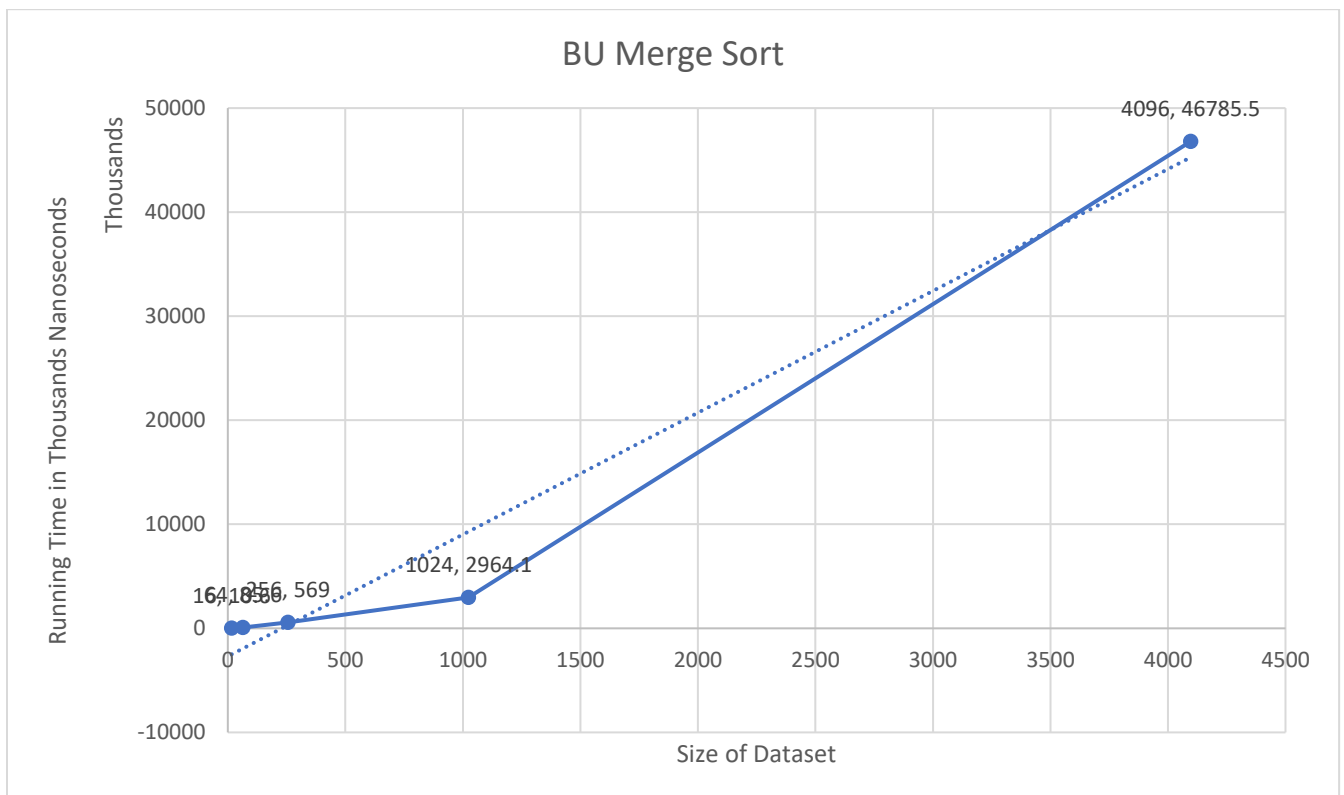


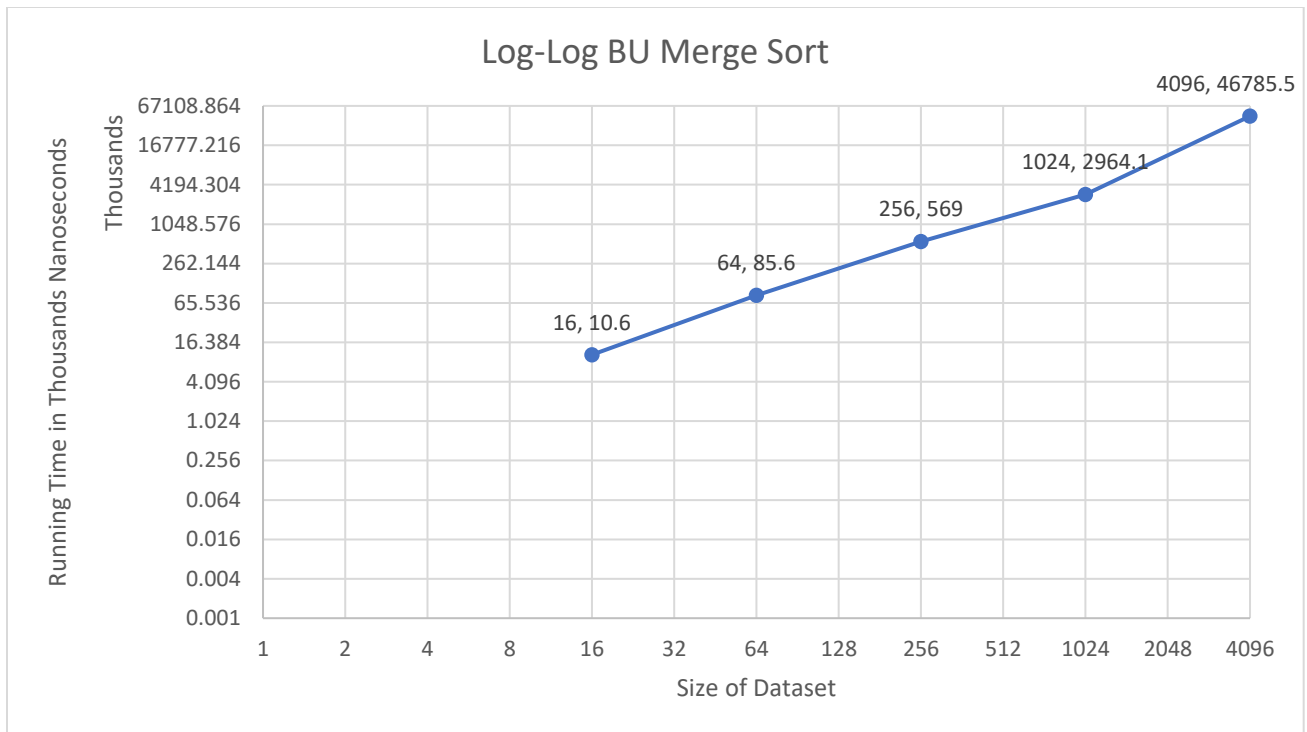
### TD Merge Sort:



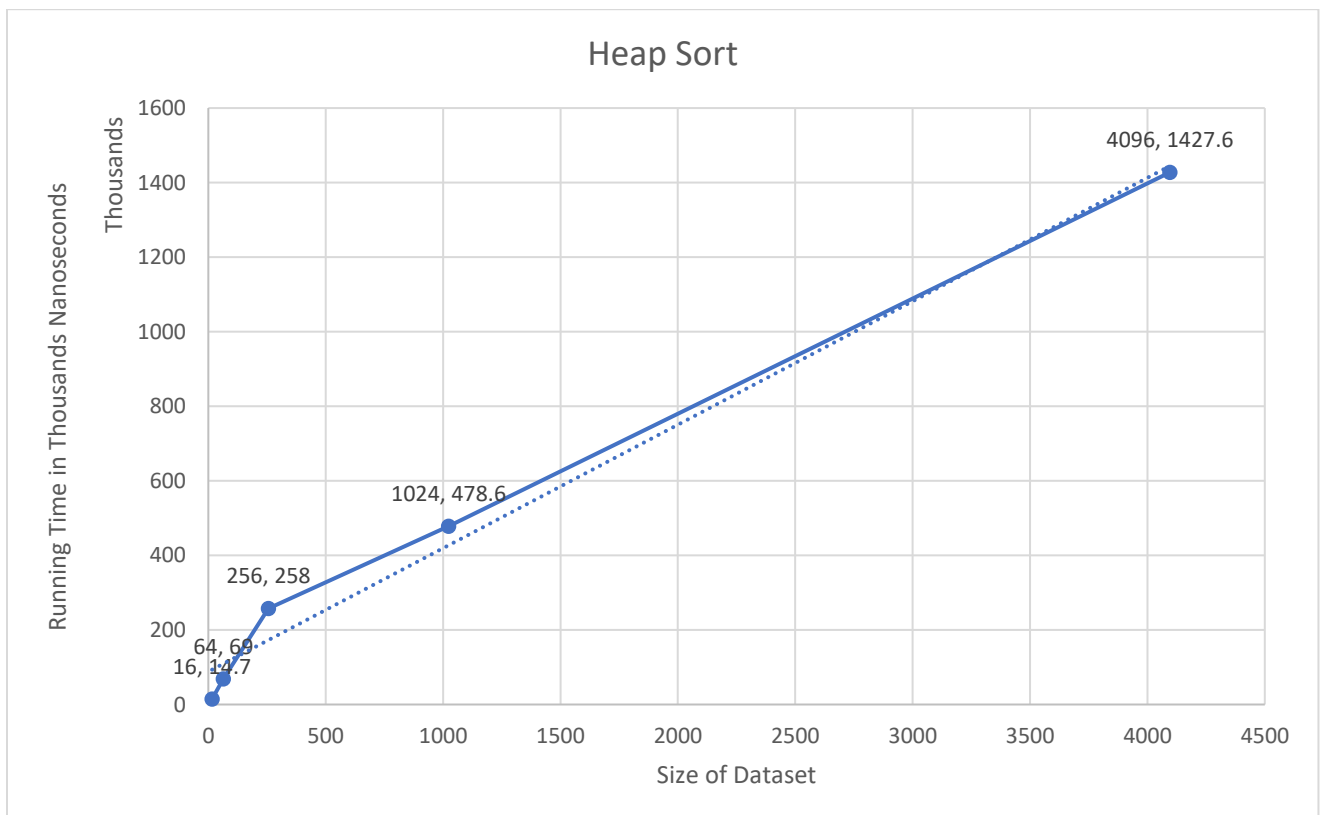


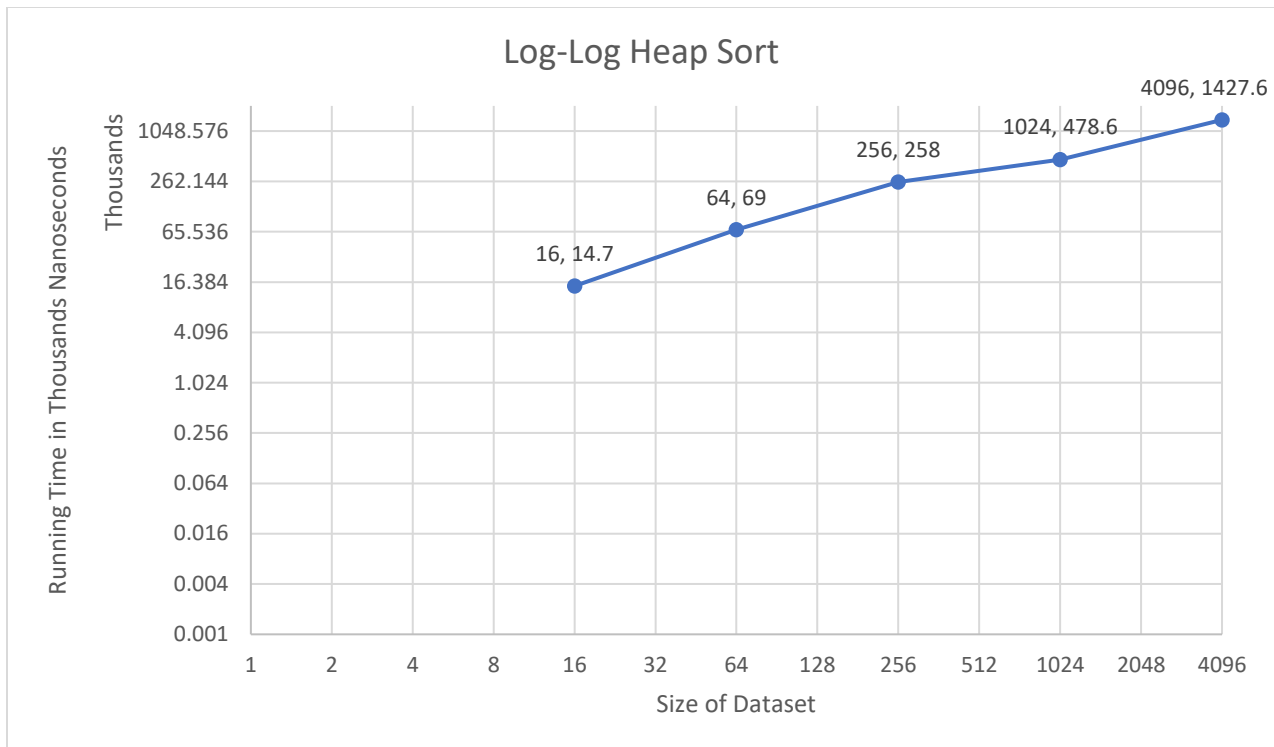
**BU Merge Sort:**



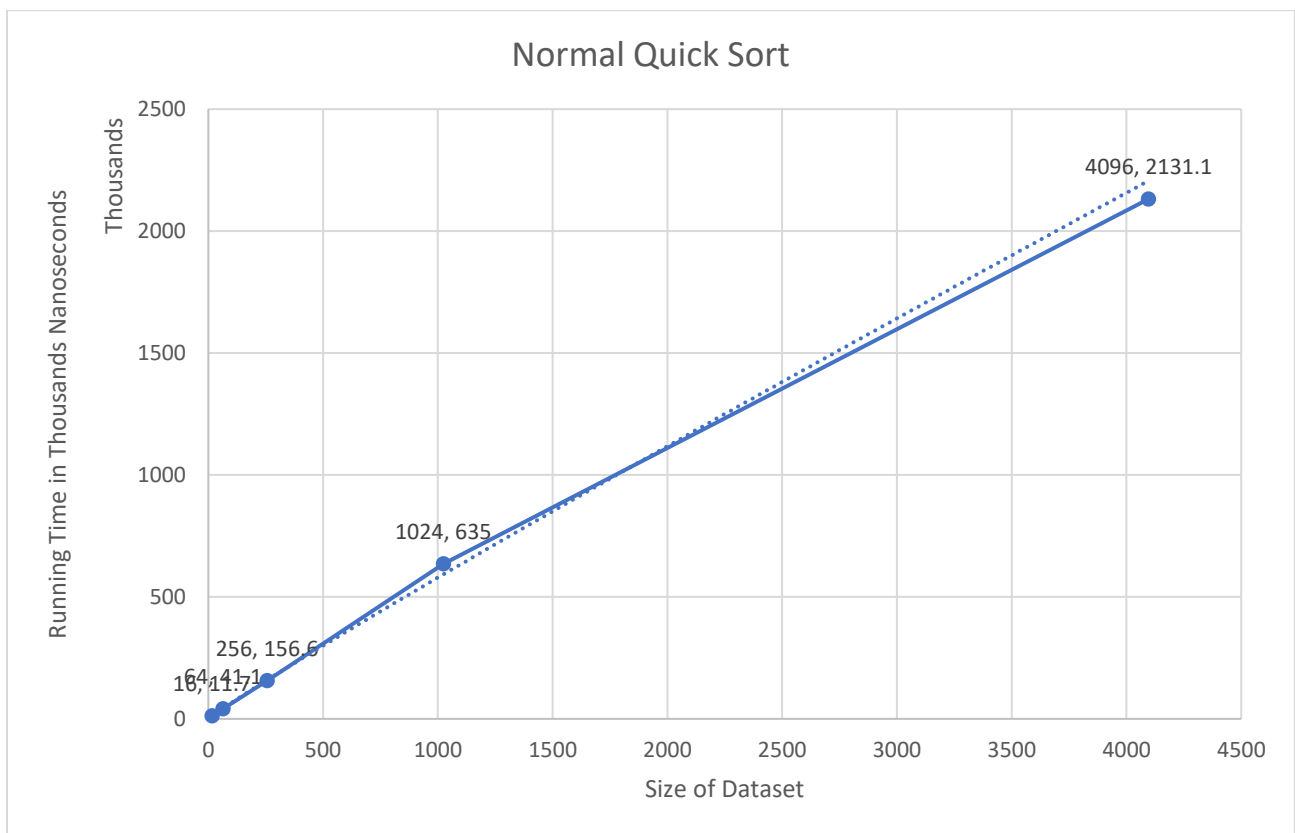


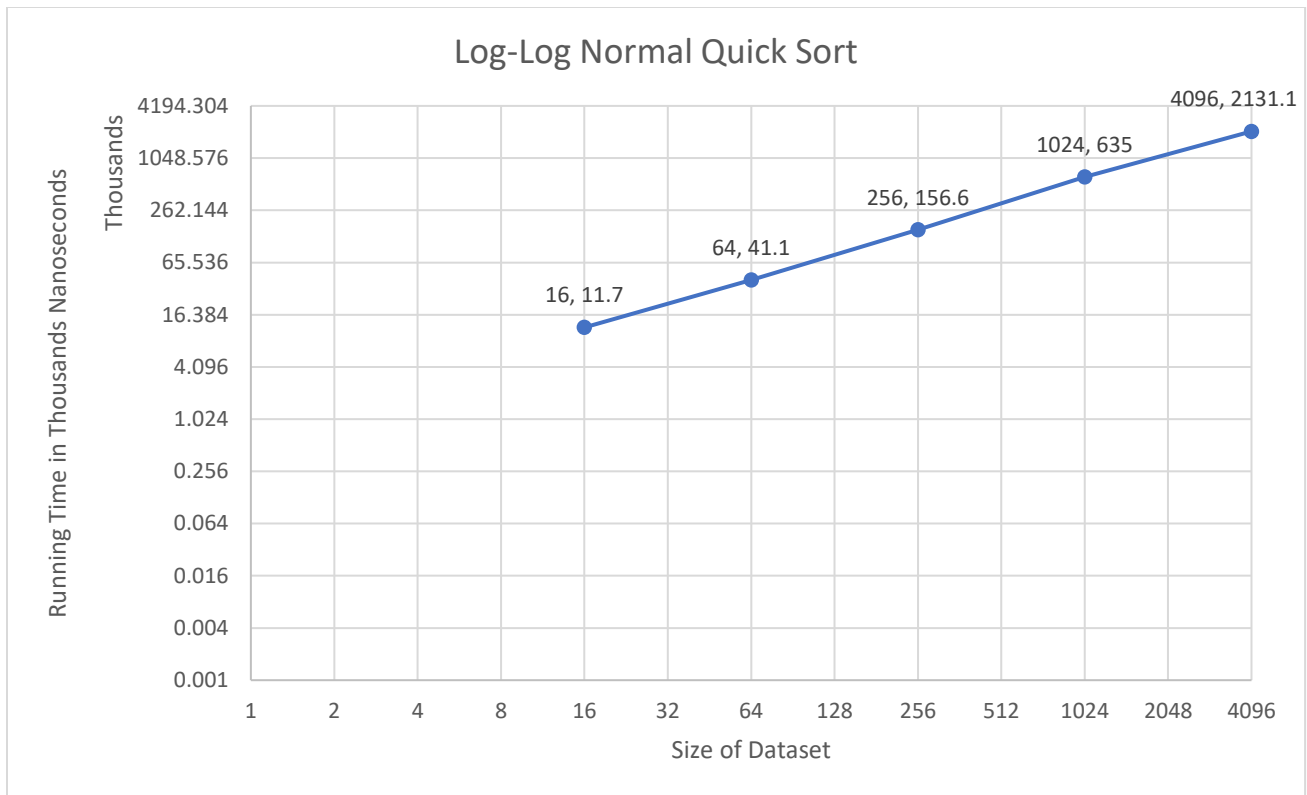
### Heap Sort:



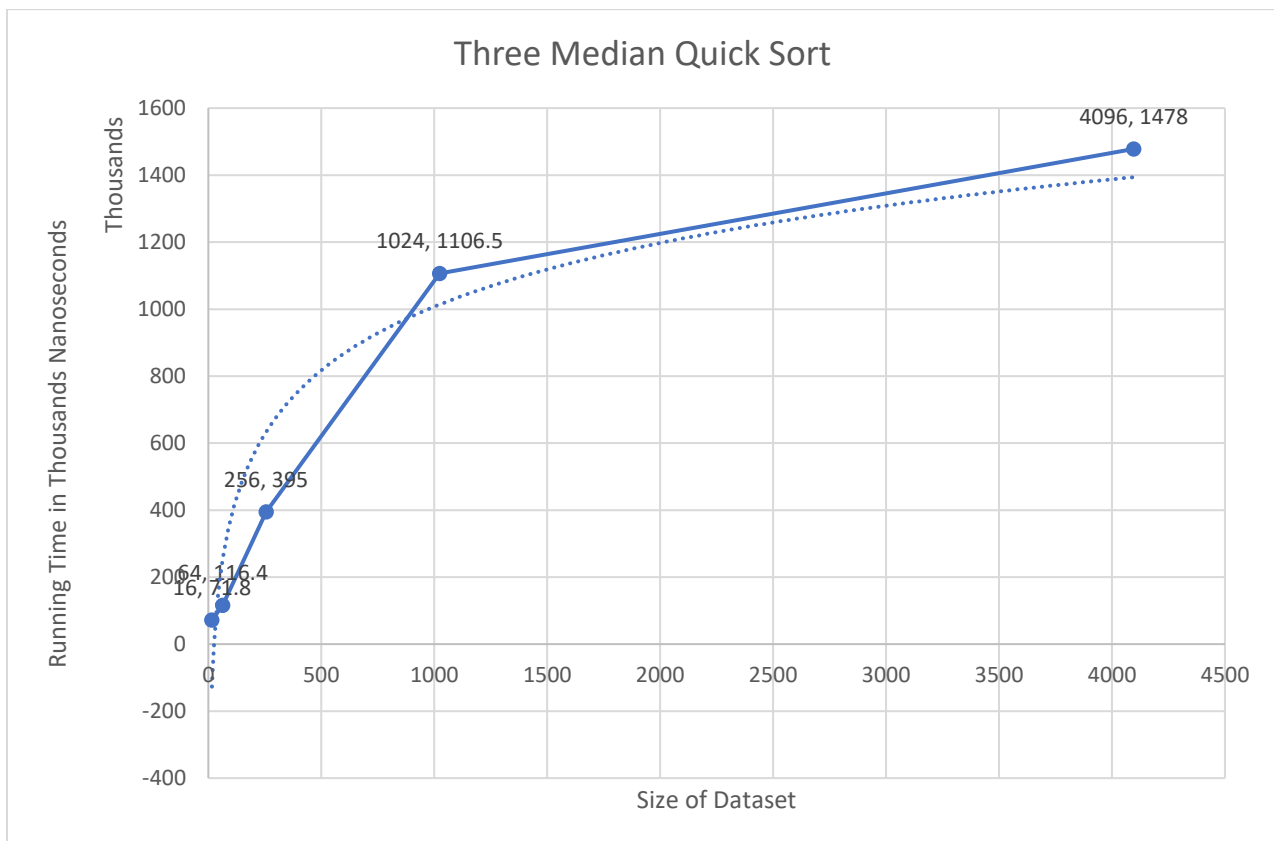


### Basic Quick Sort:

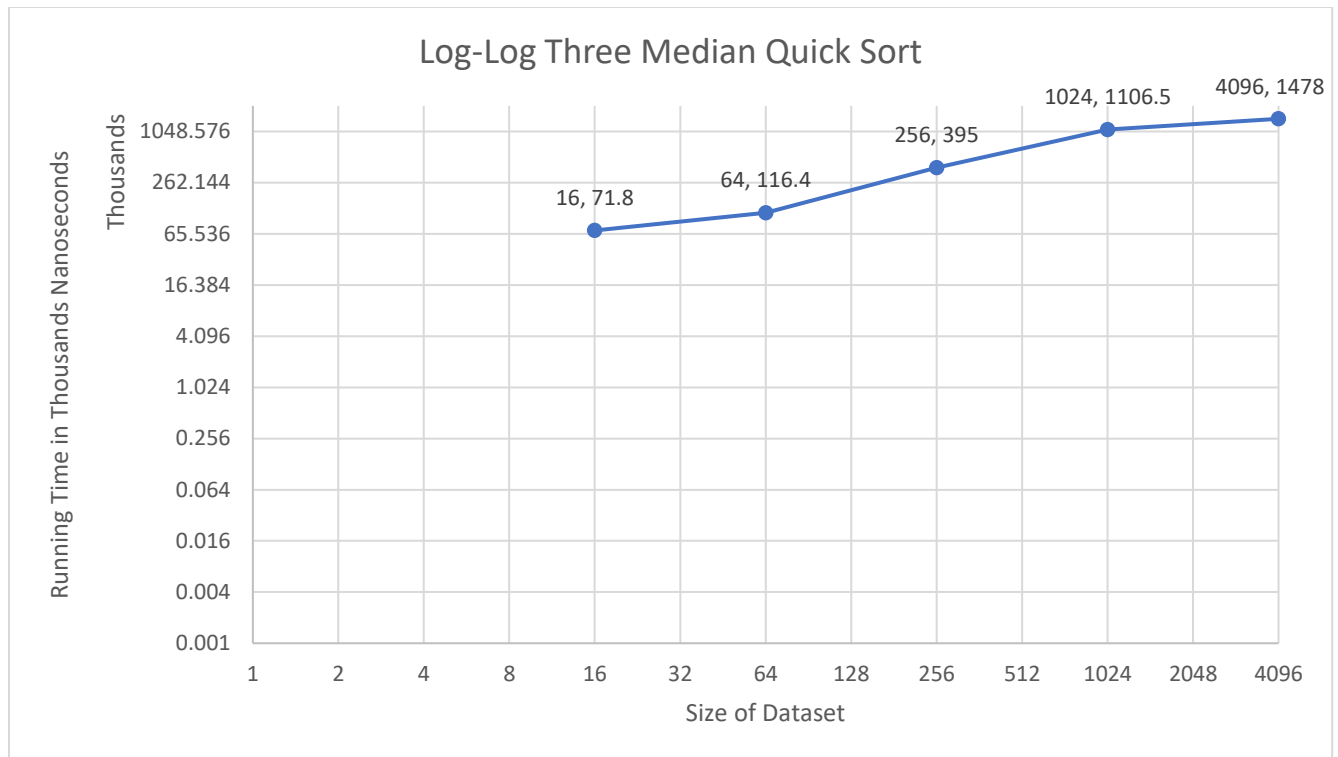




### Median of Three Quick Sort:







### **3.1.2 Running Time of Four Types of Sorting Algorithms**

#### **Insertion Sort:**

The trend line that best matches the curve of points for the three insertions sort algorithms running time graph is a polynomial of base 2. The equation of the graph shows that the trend of the data points correlates to that of a quadratic. Therefore, the running time complexity of insertion sort is  $O(N^2)$ .

#### **Merge Sort:**

The line graph of the points for both types of merge correspond to a function of equation  $N\log(N)$ . Therefore, the running time complexity of merge sort is  $O(N\log(N))$ .

#### **Quick Sort:**

The line graph of the points for both types of Quick sort correspond to a function of equation  $N\log(N)$ . Therefore, the running time complexity of Quick sort is  $O(N\log(N))$ .

#### **Heap Sort:**

The line graph of the points for both types of heap correspond to a function of equation  $N\log(N)$ . Therefore, the running time complexity of heap sort is  $O(N\log(N))$ .

### 3.1.3 Predicted Execution time for $2^{14}$ & $2^{16}$ :

Size of Dataset	PREDICTED Execution Time of Sorting Algorithms (in nanoseconds)							
	Insertion			Merge		Quick		Heap
	Normal	Comparable	Binary	TD	BU	Normal/ Basic	Median Three Partition	Normal
$2^{14}$	132646100	97319200	731938400	13172930	572147200	45813200	4613700	3627200
$2^{16}$	1326460900	9832015300	83092946000	3725299000	31824278200	152567200	68213300	53278200

### 3.1.4 Running Time on array sizes $2^{14}$ & $2^{16}$ :

Size of Dataset	Execution Time of Sorting Algorithms (in nanoseconds)							
	Insertion			Merge		Quick		Heap
	Normal	Comparable	Binary	TD	BU	Normal/ Basic	Median Three Partition	Normal
$2^{14}$	1571460600	493304300	1650140300	301912900	328316800	10274400	8302300	8969500
$2^{16}$	28396546700	16684189900	31359960900	28897596300	12315396700	21291600	86323800	31695300