## Tutorial -

- Q.1 Find the volume of the region bounded above by the surface  $Z = 2 Sin \times Cosy$  and below by the rectangle  $R! O S \times SIZ$ ,  $O S \times SIZ$ ,
- Double integrate  $f(s,t) = e^{s} \ln t$  over the region in the 1st quadrant of the st-plane that lies above the curve  $s = \ln t$  from t = 1 to t = 2.
- Q.3 Sketch—the region of integration and write an equivalent double ntegral with the order of integration reversed.
  - (1) Si se dydx
- (1) 52 54-x2 6xdydx
  - (11) je slonx ny dy dn
    - (IV) J'3 Janly (xy da dy

Sketch the regen. of interating to valuate the Integral. Then change the order of integration and evaluate tree interval.  $\int_{0}^{3} \int_{\sqrt{3}}^{4} e^{y^{3}} dy dx$ Observe that et you directly example the Integral wetnaut changing the order of integration tues it is very difficult to evaluate. So sometimes changing the order of integration makes out task much easier. Find the volume of the solid in the first octant bounded by the coordinate planes, the cylinder relyingly, and the plane 244=3. Find the average value of flyg) = x Cosxy
over the rectargle R: 0 = x = 1, 0 = y = 1. (Hinty: Average value of fore R = Tread R [f (my) of A) Q.7 Find two volume (Using tople internal)

true cylinder 7: y2 and true xx-plane trust y

bounded by true planes x=0, x=1, y=1, y=1

Tutoral (D

V= Sf-fenis)dA

= \$ 1 mg 2 Sinx Gory dy dx

= J1/2 [asinx siny] of dx

= 5 (25inx x tz) dr

= V2 (- Cosx) 12 = 150 (12)

= 12[-0+1]= 12

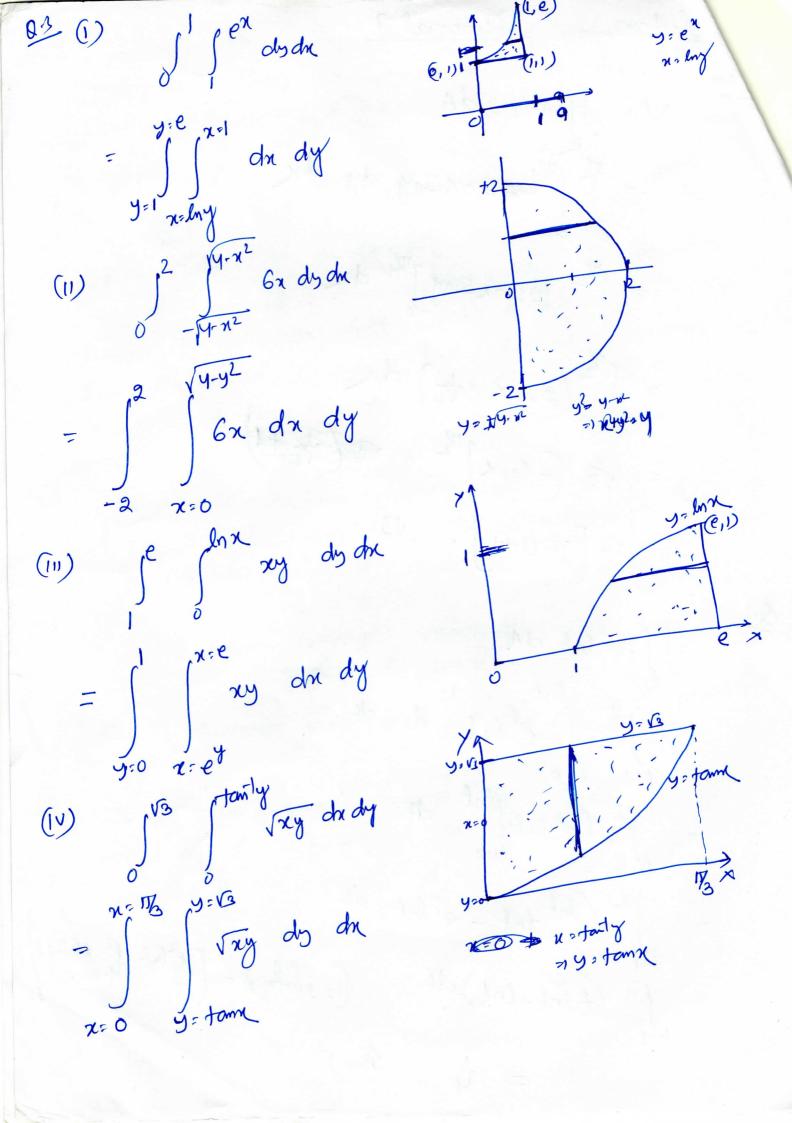
IS eshit da

= 12 Short de at

=  $\int_{0.0}^{2} \left[e^{g} \ln t\right]_{10}^{10} dt$ 

=  $\int^2 (e^{lnt} lnt - e^{0} lnt) dt$ 

= 12 (t lnt-lnt) dt (3, parts) = [ 2 lnt- 4 - thit +t]



Q.6 Sol The value of the internal of f over Ry = IT [XSINXY] du = IT SINX du TIN = [-Cosx] = 1+1=2 The area of R = IT So average value of over R = 2 TT between 7: y2

1 xy-plane (7:0)  $V = \int \int_{0}^{1} \int_{0}^{y^{2}} dt dy dx$ So 7-limit y /8-=  $\int_{x=0}^{1} \int_{y=1}^{1} (z)^{y^2} dy dx = \int_{x=0}^{1} \int_{y=1}^{1} y^2 dy dx$  $= \int_{X = 0}^{1} \left[ \frac{y^3}{3} \right]^{1} dx = \int_{1}^{1} \left( \frac{1}{3} - \frac{(-1)}{3} \right) dx$  $= \int_{3}^{2} \frac{2}{3} dx \cdot \frac{2}{3} (x)^{3} \cdot \frac{2}{3} (A)$