

Instructions:

- There are 4 questions, each 8 marks, for a total of 32 marks. Total time available 30 minutes.
- Provide answers in the space provided only. You may do your rough work on a separate blank sheet.
- You may use a calculator, but nothing else. **Pl. keep your phones/laptops, books etc. away from you.**
- Do not use unfair means, else action will be taken. Do not use material such as books, notes, etc. or a computer, smart phone, etc. And do not share information with other students.

1. Alice & Bob plan to use ElGamal Cryptosystem to exchange messages confidentially. Bob sends to Alice a message, M_1 , that is encrypted using ElGamal Cryptosystem that itself uses Diffie-Hellman generated shared key, K . The underlying Diffie-Hellman parameters are: prime $q = 19$, and its primitive root $a = 10$. While Alice and Bob select private keys, X_A & X_B , unknown to an intruder, the public keys shared by Alice & Bob are $Y_A = 3$ and $Y_B = 11$. What is message, M_1 , given that the intruder has access to the computed cipher, $C_1 = 9$? That is, what is M_1 , given: $\langle q=19, \text{root } a=10, \text{public keys } Y_A=3, Y_B=11, \text{cipher } C_1=9 \rangle$. **Show all details.**

ALL
CALC
ARE
MOD 19
→

Given $q=19, a=10, Y_A=3, Y_B=11, C_1=9$

What is X_A , given $Y_A=3=10^{X_A} \Rightarrow X_A=5$

OR What is X_B , given $Y_B=11=10^{X_B} \Rightarrow X_B=6$

What is shared Diffie-Hellman key, $K = Y_B^{X_A} = 11^5 \pmod{19} = 7$

OR $K = Y_A^{X_B} = 3^6 \pmod{19} = 7$

Given cipher $C_1=9 = K * M_1 = 7 * M_1$, compute K^{-1} .

$K * K^{-1} = 1 \Rightarrow 7 * K^{-1} = 1 \Rightarrow K^{-1} = 11$

Given cipher $C_1=9, K^{-1}=11, M_1 = K^{-1} * C_1 = 11 * 9 = 4$

OR directly given cipher $C_1=9 = K * M = 7 * M \Rightarrow M_1=4$

2. Device A wishes to send to device B a text, T_1 , and expects device B to reply with an acknowledgement, A_1 . Device B will accept text, T_1 , from A and then reply to it with an acknowledgement, A_1 , only if it is able to verify the origin & integrity of text sent by device A. Similarly, device A will accept the acknowledgement from device B only if it is able to (i) verify the origin and integrity of the reply, and (ii) the acknowledgement makes a reference to the earlier text, T_1 .

We assume devices A and B use an RSA-based public-key cryptosystem. They both have access to an RSA Certification Authority, CA, whose public key is known to both devices, A and B.

Write below:

- a. What specific information should device A seek from Certification Authority, CA? And for what purpose?

A seeks from CA the public-key certificate of B, so as to obtain public-key of B, viz K_{PU-B}

- b. What specific information should device B seek from Certification Authority, CA? And for what purpose?

B seeks from CA the public key certificate of A, so as to obtain the public-key of A, viz K_{PU-A}

Also write below:

- c. what is the structure & content of the overall message that A sends to B, together with text T_1 , hash value, if any, encryption, if any, Nonce, if any.

$A \rightarrow B: E(K_{PR-A}, [T_1, \text{Nonce}_1])$

- d. what is the structure & content of the overall message that B sends to A, together with ack, A_1 , hash value, if any, encryption, if any, Nonce, if any.

$B \rightarrow A: E(K_{PR-B}, [A_1, f(\text{Nonce}_1)])$

(For an example from Kerberos, the structure & content of a communication from device AS to device C is specified as:

$AS \rightarrow C: E(K_C, [K_B || ID_{TGS}]) || Ticket_{TGS}$

3. Take a look at table below that describes a message together with the hash function/value. Here characters x_0, x_1, \dots, x_6 are message characters. The 8-bits of any character x_j are shown as: $x_{j7}, x_{j6}, \dots, x_{j0}$, where x_{j7} is the (EVEN) parity bit. That is $x_{07} + x_{06} + \dots + x_{00} = 0$; $x_{17} + x_{16} + \dots + x_{10} = 0$; ..., $x_{67} + x_{66} + \dots + x_{60} = 0$

A last character x_7 is added and forms part of the hash value. It is obtained by computing:
 $x_{70} + x_{60} + \dots + x_{00} = 0$; $x_{71} + x_{61} + \dots + x_{01} = 0$; ..., $x_{77} + x_{67} + \dots + x_{07} = 0$

	(parity) bit_7	bit_6	bit_5	bit_4	bit_3	bit_2	Bit_1	bit_0
x_0 I	x_{07}	x_{06}	x_{05}	x_{04}	x_{03}	x_{02}	x_{01}	x_{00}
x_1 0	x_{17}	x_{16}	x_{15}	x_{14}	x_{13}	x_{12}	x_{11}	x_{10}
x_2 u	x_{27}	x_{26}	x_{25}	x_{24}	x_{23}	x_{22}	x_{21}	x_{20}
x_3 1	x_{37}	x_{36}	x_{35}	x_{34}	x_{33}	x_{32}	x_{31}	x_{30}
x_4 2	x_{47}	x_{46}	x_{45}	x_{44}	x_{43}	x_{42}	x_{41}	x_{40}
x_5 0	x_{57}	x_{56}	x_{55}	x_{54}	x_{53}	x_{52}	x_{51}	x_{50}
x_6 0	x_{67}	x_{66}	x_{65}	x_{64}	x_{63}	x_{62}	x_{61}	x_{60}
(parity) x_7	x_{77}	x_{76}	x_{75}	x_{74}	x_{73}	x_{72}	x_{71}	x_{70}

To summarize, the sum of all bits in a given row is 0. And the sum of all bits in a given column is 0. The hash function consists of all the shaded bits from the table, viz. the bit_7 in each character, and the 8 bits in char_7. The rest is the original text.

I prepare a message consisting of 7 characters, "I O U 1 2 0 0", where the characters in the message are encoded as 8-bits including the parity bit. An 8th character is added to complete the hash function/value. I now create a digital signature using the above hashing function, $H(x)$, and RSA with my private key PR-BNJ.

- ② a. Is it possible to replace the message to something else without this change being detected at the receiver's end? Yes
 And why do you think so? At the very least, the numbers/letters can be permuted, while the parity bits remain the same, e.g. 1200 → 2100.
- ② b. Give one more example where it is possible to replace "IOU1200" without this change being detected at the receiver's end? IOU 2100 as also IOU 1233
- ① c. Give one example where a change will in fact be detected at the receiver's end? IOU 1201
- ③ d. What change in the IOU note can be made by an intruder that will result in the largest value being owed by me, the sender? IOU 9974. If a student has written IOU 99xx give full marks.

4. A portion of the Kerberos v4 protocol is given below.

- (1) $C \rightarrow AS \ ID_C \| ID_{TGS} \| TS_1$
 (2) $AS \rightarrow C \ E(K_{C,AS}, [K_{C,TGS} \| ID_{TGS} \| TS_2 \| Lifetime_2 \| Ticket_{TGS}])$
 $Ticket_{TGS} = E(K_{TGS}, [K_{C,TGS} \| ID_C \| AD_C \| ID_{TGS} \| TS_2 \| Lifetime_2])$

(a) Authentication Service Exchange to obtain ticket-granting ticket

- (3) $C \rightarrow TGS \ ID_V \| Ticket_{TGS} \| Authenticator_C$
 (4) $TGS \rightarrow C \ E(K_{C,TGS}, [K_{C,V} \| ID_V \| TS_4 \| Ticket_V])$
 $Ticket_V = E(K_{TGS}, [K_{C,TGS} \| ID_C \| AD_C \| ID_V \| TS_4 \| Lifetime_4])$
 $Authenticator_C = E(K_{C,TGS}, [ID_C \| AD_C \| TS_3])$

(b) Ticket-Granting Service Exchange to obtain service-granting ticket

- (5) $C \rightarrow V \ Ticket_V \| Authenticator_C$
 (6) $V \rightarrow C \ E(K_{C,V}, [TS_5 + 1])$ (for mutual authentication)
 $Ticket_V = E(K_{V,TGS}, [K_{C,V} \| ID_C \| AD_C \| ID_V \| TS_4 \| Lifetime_4])$
 $Authenticator_C = E(K_{C,V}, [ID_C \| AD_C \| TS_3])$

② Pinpoint exactly which message, and specifically what content in the message, that allows:

A. The Authentication server (AS) to authenticate the client, C?
Message (2) $AS \rightarrow C$ the contents are encrypted using shared key $K_{C,AS}$, without which client is unable to extract $Ticket_{TGS}$

B. Client, C, to authenticate itself to the Ticket-granting server, TGS?
Message (3) $C \rightarrow TGS$. Specifically "Authenticator_C" is encrypted by C using shared $K_{C,TGS}$ created / sent by AS.

C. Client, C, to authenticate the Ticket-granting server, TGS?
From (3) $Ticket_{TGS}$, the TGS can obtain key $K_{C,TGS}$ that TGS uses to send message (4).

D. Client, C, to authenticate the sever, V?
As in C. above the server V obtains the key $K_{C,V}$ from $Ticket_V$ and uses that to reply message (6)