Linear Equations in Two Variables

Practice set 5.1

Q. 1. By using variables x and y form any five linear equations in two variables.

Answer: a) x + y = 5

- **b)** x + 2y = 6
- **c)** 2x + y = 4
- **d)** 3x + 4y = 8
- **e)** 5x + 9y = 1

Q. 2. Write five solutions of the equation x + y = 7.

Answer: (a)

Let x = 1,

As, x + y = 7

 \Rightarrow 1 + y = 7

 \Rightarrow y = 6

Hence, solution is x = 1 and y = 6.

(b)

Let x = 2,

As, x + y = 7

 \Rightarrow 2 + y = 7

 \Rightarrow y = 5

Hence, solution is x = 2 and y = 5.

(c)

Let
$$x = 3$$
,

As,
$$x + y = 7$$

$$\Rightarrow$$
 3 + y = 7

$$\Rightarrow$$
 y = 4

Hence, solution is x = 3 and y = 4.

(d)

Let
$$x = 4$$
,

As,
$$x + y = 7$$

$$\Rightarrow$$
 4 + y = 7

$$\Rightarrow$$
 y = 3

Hence, solution is x = 4 and y = 3.

(e)

Let
$$x = 5$$
,

As,
$$x + y = 7$$

$$\Rightarrow$$
 5 + y = 7

$$\Rightarrow$$
 y = 2

Hence, solution is x = 5 and y = 2.

Q. 3. Solve the following sets of simultaneous equations.

i.
$$x + y = 4$$
; $2x - 5y = 1$

ii.
$$2x + y = 5$$
; $3x - y = 5$

iii.
$$3x - 5y = 16$$
; $x - 3y = 8$

iv.
$$2y - x = 0$$
; $10x + 15y = 105$

v.
$$2x + 3y + 4 = 0$$
; $x - 5y = 11$

vi. 2x - 7y = 7; 3x + y = 22

Answer : (i)

$$x + y = 4 eq.[1]$$

$$2x - 5y = 1 \text{ eq.}[2]$$

We can write eq.[1] as,

$$x = 4 - y eq.[3]$$

Substituting eq.[3] in eq.[2],

$$\Rightarrow 2(4 - y) - 5y = 1$$

$$\Rightarrow$$
 8 - 2y - 5y = 1

$$\Rightarrow$$
 -7y = -7

$$\Rightarrow$$
 y = 1

Substituting 'y' in eq.[3]

$$\Rightarrow$$
 x = 4 - 1

$$\Rightarrow$$
 x = 3

Hence, solution is x = 3 and y = 1.

(ii)

$$2x + y = 5 \text{ eq.}[1]$$

$$3x - y = 5 \text{ eq.}[2]$$

We can write eq.[1] as,

$$y = 5 - 2x eq.[3]$$

Substituting eq.[3] in eq.[2],

$$\Rightarrow 3x - (5 - 2x) = 5$$

$$\Rightarrow 3x - 5 + 2x = 5$$

$$\Rightarrow$$
 5x = 10

$$\Rightarrow$$
 x = 2

Substituting 'x' in eq.[3]

$$\Rightarrow$$
 y = 5 - 2(2)

$$\Rightarrow$$
 y = 1

Hence, solution is x = 2 and y = 1.

(iii)

$$3x - 5y = 16 \text{ eq.}[1]$$

$$x - 3y = 8 \text{ eq.}[2]$$

We can write eq.[2] as,

$$x = 8 + 3y eq.[3]$$

Substituting eq.[3] in eq.[1],

$$\Rightarrow 3(8 + 3y) - 5y = 16$$

$$\Rightarrow 24 + 9y - 5y = 16$$

$$\Rightarrow$$
 4y = -8

$$\Rightarrow$$
 y = -2

Substituting 'y' in eq.[3]

$$\Rightarrow x = 8 + 3(-2)$$

$$\Rightarrow$$
 x = 8 - 6 = 2

Hence, solution is x = 2 and y = -2

(iv)

$$2y - x = 0 \text{ eq.}[1]$$

$$10x + 15y = 105 \text{ eq.}[2]$$

We can write eq.[1] as,

$$x = 2y eq.[3]$$

Substituting eq.[3] in eq.[2],

$$\Rightarrow$$
 10(2y) + 15y = 105

$$\Rightarrow$$
 20y + 15y = 105

$$\Rightarrow$$
 35y = 105

$$\Rightarrow$$
 y = 3

Substituting 'y' in eq.[3]

$$\Rightarrow$$
 x = 2(3)

$$\Rightarrow$$
 x = 6

Hence, solution is x = 6 and y = 3.

(v)

$$2x + 3y + 4 = 0$$
 eq.[1]

$$x - 5y = 11 \text{ eq.}[2]$$

We can write eq.[2] as,

$$x = 11 + 5y eq.[3]$$

Substituting eq.[3] in eq.[1],

$$\Rightarrow$$
 2(11 + 5y) + 3y + 4 = 0

$$\Rightarrow 22 + 10y + 3y + 4 = 0$$

$$\Rightarrow$$
 13y + 26 = 0

Substituting 'y' in eq.[3]

$$\Rightarrow x = 11 + 5(-2)$$

$$\Rightarrow$$
 x = 11 - 10 = 1

Hence, solution is x = 1 and y = -2.

(vi)

$$2x - 7y = 7 \text{ eq.}[1]$$

$$3x + y = 22 \text{ eq.}[2]$$

We can write eq.[2] as,

$$y = 22 - 3x eq.[3]$$

Substituting eq.[3] in eq.[1],

$$\Rightarrow$$
 2x - 7(22- 3x) = 7

$$\Rightarrow$$
 2x - 154 + 21x = 7

$$\Rightarrow$$
 23x = 161

$$\Rightarrow x = 7$$

Substituting 'x' in eq.[3]

$$\Rightarrow y = 22 - 3(7)$$

$$\Rightarrow$$
 y = 22 - 21 = 1

Hence, solution is x = 7 and y = 1.

Practice set 5.2

Q. 1. In an envelope there are some 5 rupee notes and some 10 rupee notes. Total amount of these notes together is 350 rupees. Number of 5 rupee notes are less by 10 than number of 10 rupee notes. Then find the number of 5 rupee and 10 rupee notes.

Answer : Let the number of 5 rupees notes = x

Let the number of 10 rupees notes = y

Given, Total amount is 350 Rupees

$$\Rightarrow$$
 5x + 10y = 350 eq.[1]

Also,

Number of 5 rupees notes are less by 10 than number of 10 rupees note,

$$y = x - 10$$

$$\Rightarrow$$
 x = y + 10 eq.[2]

Putting [2] in [1]

$$\Rightarrow$$
 5(y + 10) + 10y = 350

$$\Rightarrow$$
 5y + 50 + 10y = 350

$$\Rightarrow$$
 15y = 300

$$\Rightarrow$$
 y = 20

Then,
$$x = y + 10$$

$$\Rightarrow$$
 x = 20 + 10

$$\Rightarrow$$
 x = 30.

Answer: 30 notes of Rs 5 and 20 notes of Rs. 10.

- Q. 2. The denominator of a fraction is 1 more than twice its numerator. If 1 is added to numerator and denominator respectively, the ratio of numerator to denominator is
- 1: 2. Find the fraction.

Answer: Let the numerator be 'x' and denominator be 'y'

Given.

The denominator of a fraction is 1 more than twice its numerator

$$\Rightarrow$$
 y =2 x + 1

$$\Rightarrow$$
 y - 2 x = 1 (1)

If 1 is added to numerator and denomination, the ratio of the numerator to denominator becomes 1:2.

$$\Rightarrow \frac{x+1}{y+1} = \frac{1}{2}$$

$$\Rightarrow$$
 2(x + 1) = y + 1

$$\Rightarrow$$
 2x + 2 = y + 1

$$\Rightarrow$$
 y - 2x = 1 (2)

As (1) and (2) are the same, there can be infinitely many solutions for x and y. One such solution is: x = 4 and y = 9Now, y - 2 x = 9 - 2(4) = 9 - 8 = 1

Q. 3. The sum of ages of Priyanka and Deepika is 34 years. Priyanka is elder to Deepika by 6 years. Then find their today's ages.

Answer : Let the ages of Priyanka and Deepika be 'x' and 'y' respectively.

Given,

Sum of ages is 34

$$\Rightarrow$$
 x + y = 34

$$\Rightarrow$$
 y = 34 - x eq.[1]

Also, Priyanka is elder to Deepika by 6 years

$$\Rightarrow$$
 x = y + 6

Using eq.[1] we have

$$\Rightarrow$$
 x = 34 - x + 6

$$\Rightarrow$$
 2x = 40

$$\Rightarrow x = 20$$

Putting this value in eq.[1]

$$\Rightarrow$$
 y = 34 - 20 = 14 years.

Hence, Age of Priyanka = x = 20 Years

Age of Deepika = y = 14 years.

Q. 4. The total number of lions and peacocks in a certain zoo is 50. The total number of their legs is 140. Then find the number of lions and peacocks in the zoo.

Answer: Let the number of lions be 'x' and peacocks be 'y'

Given, Total no of lions and peacocks is 50

$$\Rightarrow$$
 x + y = 50

$$\Rightarrow$$
 x = 50 - y eq.[1]

Also, Total no of their legs is 140, as lion has four legs and peacocks has 2 legs

$$\Rightarrow$$
 4x + 2y = 140

$$\Rightarrow$$
 4(50 - y) + 2y = 140

$$\Rightarrow$$
 200 - 4y + 2y = 140

$$\Rightarrow$$
 2y = 60

$$\Rightarrow$$
 y = 30

Using this in eq.[1]

$$\Rightarrow$$
 x = 50 - 30 = 20

Therefore,

No of lions, x = 20

No of peacocks, y = 30

Q. 5. Sanjay gets fixed monthly income. Every year there is a certain increment in his salary. After 4 years, his monthly salary was Rs. 4500 and after 10 years his monthly salary became 5400 rupees, then find his original salary and yearly increment.

Answer: Let the original salary be 'x' and yearly increment be 'y'

After 4 years, his salary was Rs. 4500

$$\Rightarrow x + 4y = 4500$$

$$\Rightarrow$$
 x = 4500 - 4y eq.[1]

After 10 years, his salary becomes 5400

$$\Rightarrow$$
 x + 10y = 5400

$$\Rightarrow$$
 4500 - 4y + 10y = 5400

$$\Rightarrow$$
 6y = 900

$$\Rightarrow$$
 y = 150

Putting this in eq.[1],

$$\Rightarrow$$
 x = 4500 - 4(150)

$$\Rightarrow$$
 x = 4500 - 600 = 3900

Hence, his original salary was Rs. 3900 and increment per year was 150 Rs.

Q. 6. The price of 3 chairs and 2 tables is 4500 rupees and price of 5 chairs and 3 tables is 7000 rupees, then find the price of 2 chairs and 2 tables.

Answer: Let the price of one chair be 'x' and one table be 'y'.

Given,

Price of 3 chairs and 2 tables = 4500 Rs

$$\Rightarrow 3x + 2y = 4500$$

Multiplying by 3 both side,

$$\Rightarrow$$
 9x + 6y = 13500

$$\Rightarrow$$
 6y = 13500 - 9x eq.[1]

Price of 5 chairs and 3 tables = 7000 Rs

$$\Rightarrow 5x + 3y = 7000$$

Multiplying by eq.[2] both side,

$$\Rightarrow$$
 10x + 6y = 14000

$$\Rightarrow$$
 10x + 13500 - 9x = 14000 eq.[From 1]

$$\Rightarrow$$
 x = 500

Putting this in eq.[1]

$$\Rightarrow$$
 6y = 13500 - 9(500)

$$\Rightarrow$$
 6y = 13500- 4500

$$\Rightarrow$$
 6y = 9000

Also, Price of 2 chairs and 2 tables = 2x + 2y

$$= 2(500) + 2(1500)$$

$$= 1000 + 3000 = 4000 Rs.$$

Q. 7. The sum of the digits in a two-digits number is 9. The number obtained by interchanging the digits exceeds the original number by 27. Find the two-digit number.

Answer: Let the unit digit be 'x'

Let the digit at ten's place be 'y'

The original number will be 10y + x

Given,

Sum of digits = 9

$$\Rightarrow x + y = 9$$

$$\Rightarrow$$
 x = 9 - y eq.[1]

Also,

If the digits are interchanged,

Reversed number will be = 10x + y

As, reversed number exceeds the original number by 27,

$$\Rightarrow$$
 (10x + y) - (10y + x) = 27

$$\Rightarrow$$
 10x + y - 10y - x = 27

$$\Rightarrow$$
 9x - 9y = 27

$$\Rightarrow$$
 x - y = 3

$$\Rightarrow$$
 9 - y - y = 3 eq.[using 1]

$$\Rightarrow$$
 -2y = -6

$$\Rightarrow$$
 y = 3

Using this in eq.[1]

$$\Rightarrow$$
 x = 9 - 3 = 6

Hence the original number is 10y + x = 10(3) + 6 = 30 + 6 = 36.

Q. 8. In $\triangle ABC$, the measure of angle A is equal to the sum of the measures of $\angle B$ and $\angle C$. Also the ratio of measures of $\angle B$ and $\angle C$ is 4 : 5. Then find the measures of angles of the triangle.

Answer: Given that, In ΔABC

$$\angle A = \angle B + \angle C \text{ eq.}[1]$$

Let
$$\angle B = x$$
 and $\angle C = y$

Then,

$$\angle A = x + y$$

In ΔABC, By angle sum property of triangle

$$\angle A + \angle B + \angle C = 180^{\circ}$$

$$\Rightarrow$$
 x + y + x + y = 180

$$\Rightarrow$$
 2x + 2y = 180

$$\Rightarrow$$
 x + y = 90

$$\Rightarrow$$
 x = 90 - y eq.[2]

Also, Given that

$$\frac{\angle B}{\angle C} = \frac{4}{5}$$

$$\Rightarrow \frac{x}{y} = \frac{4}{5}$$

$$\Rightarrow$$
 5x = 4y

From eq.[2]

$$\Rightarrow$$
 5(90 - y) = 4y

$$\Rightarrow$$
 450 - 5y = 4y

$$\Rightarrow$$
 9y = 450

$$\Rightarrow$$
 v = 50°

Putting this in eq.[2]

$$\Rightarrow$$
 x = 90 - 50 = 40°

Therefore, we have

$$\angle A = x + y = 40^{\circ} + 50^{\circ} = 90^{\circ}$$

$$\angle B = x = 40^{\circ}$$

$$\angle C = y = 50^{\circ}$$

Q. 9. Divide a rope of length 560 cm into 2 parts such that twice the length of the smaller part is equal to 1/3 of the larger part. Then find the length of the larger part.

Answer: Let the length of smaller part be 'x' cm and larger part be 'y' cm.

Length of rope = 560 cm

$$\Rightarrow$$
 x + y = 560

$$\Rightarrow$$
 y = 560 - x eq.[1]

Also,

Twice the length of smaller part is equal to $\frac{1}{3}$ of the larger part

$$\Rightarrow 2x = \frac{1}{3}y$$

$$\Rightarrow$$
 6x = y

$$\Rightarrow$$
 6x = 560 - x

$$\Rightarrow$$
 7x = 560

$$\Rightarrow$$
 x = 80

Using this in eq.[1]

$$\Rightarrow$$
 y = 560 - 80 = 480

Therefore,

Length of smaller part = 'x' cm = 80 cm

Length of larger part = 'y' cm = 480 cm

Q. 10. In a competitive examination, there were 60 questions. The correct answer would carry 2 marks, and for incorrect answer 1 mark would be subtracted. Yashwant had attempted all the questions and he got total 90 marks. Then how many questions he got wrong?

Answer: Let the no of questions he got wrong be 'x'

And the no of questions he got right be 'y'

As, he attempted all the questions,

$$\Rightarrow$$
 x + y = 60

$$\Rightarrow$$
 y = 60 - x eq.[1]

Also, he carries 2 for each corrects question and (-1) for each wrong question, also he got 90 marks

$$\Rightarrow y(2) + x(-1) = 90$$

$$\Rightarrow$$
 2y - x = 90

$$\Rightarrow$$
 2(60 - x) - x = 90 eq.[Using 1]

$$\Rightarrow$$
 120 - 2x - x = 90

$$\Rightarrow$$
 -3x = -30

$$\Rightarrow$$
 x = 10

⇒ he got 10 wrong questions.

Problem set 5

Q. 1 A. Choose the correct alternative answers for the following questions.

If 3x + 5y = 9 and 5x + 3y = 7 then What is the value of x + y?

- A. 2
- B. 16
- C. 9
- D. 7

Answer: 3x + 5y = 9 eq.[1]

$$5x + 3y = 7 \text{ eq.}[2]$$

Adding eq.[1] and eq.[2] we get

$$3x + 5y + 5x + 3y = 9 + 7$$

$$\Rightarrow$$
 8x + 8y = 16

Dividing both side by 8, we get

$$\Rightarrow x + y = 2$$

Q. 1 B. 'When 5 is subtracted from length and breadth of the rectangle, the perimeter becomes 26.' What is the mathematical form of the statement?

A.
$$x - y = 8$$

B.
$$x + y = 8$$

C.
$$x + y = 23$$

D.
$$2x + y = 21$$

Answer : Let the length be 'x' and breadth be 'y' units.

Perimeter of triangle = 2(x + y) units

If 5 is subtracted from length and breadth

Perimeter = 26 units eq.[Given]

$$\Rightarrow$$
 2(x - 5 + y - 5) = 26

$$\Rightarrow$$
 2(x + y - 10) = 26

$$\Rightarrow$$
 x + y - 10 = 13

$$\Rightarrow$$
 x + y = 23

Q. 1 C. Ajay is younger than Vijay by 5 years. Sum of their ages is 25 years. What is Ajay's age?

- A. 20
- B. 15
- C. 10
- D. 5

Answer: Let Ajay's age be 'x' years and Vijay's age be 'y' years.

Given, Ajay is younger than Vijay by 5 years

$$\Rightarrow$$
 x = y - 5 eq.[1]

Also, Sum of their ages is 25 years,

$$\Rightarrow$$
 x + y = 25

From eq.[1]

$$\Rightarrow$$
 y - 5 + y = 25

$$\Rightarrow$$
 2y = 30

Putting this in eq.[1]

$$\Rightarrow$$
 x = 15 - 5 = 10

Age of Ajay =
$$x = 10$$
 Years

Age of Vijay =
$$y = 15$$
 Years

Q. 2. Solve the following simultaneous equations.

i.
$$2x + y = 5$$
; $3x - y = 5$

ii.
$$x - 2y = -1$$
; $2x - y = 7$

Answer: (i)

$$2x + y = 5$$

$$\Rightarrow$$
 y = 5 - 2x eq.[1]

$$3x - y = 5$$

Using eq.[1] we have

$$\Rightarrow$$
 3x - (5 - 2x) = 5

$$\Rightarrow 3x - 5 + 2x = 5$$

$$\Rightarrow$$
 5x = 10

$$\Rightarrow$$
 x = 2

Using 'x' in eq.[1]

$$\Rightarrow$$
 y = 5 - 2(2)

$$\Rightarrow$$
 y = 5 - 4 = 1 cm

(ii)

$$x - 2y = -1$$

$$\Rightarrow$$
 x = 2y - 1 eq.[1]

$$2x - y = 7$$

Using eq.[1], we have

$$\Rightarrow 2(2y - 1) - y = 7$$

$$\Rightarrow$$
 4y - 2 - y = 7

$$\Rightarrow$$
 3y = 9

$$\Rightarrow$$
 y = 3

Using this value in eq.[1]

$$\Rightarrow x = 2(3) - 1$$

$$\Rightarrow$$
 x = 5

(iii)

$$x + y = 11$$

$$\Rightarrow$$
 y = 11 - x eq.[1]

$$2x - 3y = 7$$

Using eq.[1], we have

$$\Rightarrow$$
 2x - 3(11 - x) = 7

$$\Rightarrow 2x - 33 + 3x = 7$$

$$\Rightarrow$$
 5x = 40

$$\Rightarrow$$
 x = 8

Using this in eq.[1]

$$\Rightarrow$$
 y = 11 - 8

$$\Rightarrow$$
 y = 3

(iv)

$$2x + y = -2$$

$$\Rightarrow$$
 y = -2x - 2 eq.[1]

$$3x - y = 7$$

Using eq.[1]

$$3x - (-2x - 2) = 7$$

$$\Rightarrow$$
 3x + 2x + 2 = 7

$$\Rightarrow$$
 5x = 5

$$\Rightarrow$$
 x = 1

Using this in eq.[1]

$$\Rightarrow$$
 y = -2(1) - 2

$$\Rightarrow$$
 y = -2 - 2 = -4

(v)

$$2x - y = 5$$

$$\Rightarrow$$
 y = 2x - 5 eq.[1]

$$3x + 2y = 11$$

Using eq.[1]

$$\Rightarrow$$
 3x + 2(2x - 5) = 11

$$\Rightarrow 3x + 4x - 10 = 11$$

$$\Rightarrow$$
 7x = 21

$$\Rightarrow$$
 x = 3

Using this in eq.[1]

$$\Rightarrow$$
 y = 2(3) - 5

$$\Rightarrow$$
 y = 1

(vi)

$$x - 2y = -2$$

$$x = 2y - 2 eq.[1]$$

$$x + 2y = 10$$

using eq.[1], we have

$$\Rightarrow 2y - 2 + 2y = 10$$

$$\Rightarrow$$
 4y = 12

$$\Rightarrow$$
 y = 3

Using this in eq.[1]

$$\Rightarrow$$
 x = 2(3) - 2

$$\Rightarrow$$
 x = 4

Q. 3. By equating coefficients of variables, solve the following equations.

i.
$$3x - 4y = 7$$
; $5x + 2y = 3$

ii.
$$5x + 7y = 17$$
; $3x - 2y = 4$

iii.
$$x - 2y = -10$$
; $3x - 5y = -12$

iv.
$$4x + y = 34$$
; $x + 4y = 16$

Answer: (i)

$$3x - 4y = 7 \text{ eq.}[1]$$

$$5x + 2y = 3 \text{ eq.}[2]$$

Multiplying eq.[2] by 2 both side, we get

$$10x + 4y = 6 \text{ eq.}[3]$$

Adding eq.[1] and eq.[3], we get

$$3x - 4y + 10x + 4y = 7 + 6$$

$$\Rightarrow$$
 13x = 13

$$\Rightarrow$$
 x = 1

Putting this in eq.[1], we get

$$3(1) - 4y = 7$$

$$\Rightarrow$$
 -4y = 7 - 3

$$\Rightarrow$$
 -4y = 4

$$\Rightarrow$$
 y = -1

(ii)

$$5x + 7y = 17 \text{ eq.}[1]$$

$$3x - 2y = 4 \text{ eq.}[2]$$

Multiplying eq.[1] by 3 both side and Multiplying eq.[2] by 5 both side we get,

$$15x + 21y = 51 \text{ eq.}[3]$$

$$15x - 10y = 20 eq.[4]$$

Subtracting eq.[4] from eq.[3], we get

$$15x + 21y - 15x + 10y = 51 - 20$$

$$\Rightarrow$$
 31y = 31

$$\Rightarrow$$
 y = 1

Putting this in eq.[1], we get

$$5x + 7(1) = 17$$

$$\Rightarrow$$
 5x = 10

$$\Rightarrow$$
 x = 2

(iii)

$$x - 2y = -10 \text{ eq.}[1]$$

$$3x - 5y = -12 \text{ eq.}[2]$$

Multiplying eq.[1] by 3

$$3x - 6y = -30 \text{ eq.}[3]$$

Subtracting eq.[2] from eq.[3], we get

$$3x - 6y - 3x + 5y = -30 + 12$$

$$\Rightarrow$$
 -y = -18

$$\Rightarrow$$
 y = 18

Putting this in eq.[1], we get

$$x - 2(18) = -10$$

$$\Rightarrow$$
 x - 36 = -10

$$\Rightarrow$$
 x = 26

(iv)

$$4x + y = 34 \text{ eq.}[1]$$

$$x + 4y = 16 \text{ eq.}[2]$$

Multiplying eq.[2] by 4 both side, we get

$$4x + 16y = 64 \text{ eq.}[3]$$

Subtracting eq.[3] from eq.[1], we get

$$4x + 16y - 4x - y = 64 - 34$$

$$\Rightarrow$$
 15y = 30

$$\Rightarrow$$
 y = 2

Putting this in eq.[2], we get

$$x + 4(2) = 16$$

$$\Rightarrow$$
 x + 8 = 16

$$\Rightarrow x = 8$$

Q. 4. Solve the following simultaneous equations.

$$\mathbf{i} \cdot \frac{\mathbf{x}}{3} + \frac{\mathbf{y}}{4} = 4 \; ; \; \frac{\mathbf{x}}{2} - \frac{\mathbf{y}}{2} - \frac{\mathbf{y}}{4} = 1$$

ii.
$$\frac{x}{3} + 5y = 13$$
; $2x + \frac{y}{2} = 19$

iii.
$$\frac{2}{x} + \frac{3}{y} = 13$$
; $\frac{5}{x} - \frac{4}{y} = -2$

Answer : (i)

$$\frac{x}{3} + \frac{y}{4} = 4$$

$$\Rightarrow \frac{4x + 3y}{12} = 4$$

$$\Rightarrow$$
 4x + 3y = 48 eq.[1]

$$\frac{x}{2} - \frac{y}{2} - \frac{y}{4} = 1$$

$$\frac{2x-2y-y}{4}=1$$

$$\Rightarrow$$
 2x - 3y = 4 eq.[2]

Adding eq.[1] and eq.[2], we get

$$\Rightarrow$$
 4x + 3y + 2x - 3y = 48 + 4

$$\Rightarrow$$
 6x = 52

$$\Rightarrow x = \frac{52}{6} = \frac{26}{3}$$

Using this in eq.[1], we have

$$4\left(\frac{26}{3}\right) + 3y = 48$$

$$\Rightarrow \frac{104 + 9y}{3} = 48$$

$$\Rightarrow 104 + 9y = 144$$

$$\Rightarrow y = \frac{40}{9}$$

$$\frac{x}{3} + 5y = 13$$

$$\Rightarrow \frac{x + 15y}{3} = 13$$

$$\Rightarrow$$
 x + 15y = 39

$$\Rightarrow$$
 x = 39 - 15y eq.[1]

$$2x + \frac{y}{2} = 19$$

$$\Rightarrow \frac{4x + y}{2} = 19$$

$$\Rightarrow$$
 4x + y = 38

Using eq.[1], we have

$$\Rightarrow$$
 4(39 - 15y) + y = 38

$$\Rightarrow$$
 156 - 60y + y = 38

$$\Rightarrow$$
 y = 2

Putting this value in eq.[2]

$$\Rightarrow$$
 x = 39 - 15(2)

$$\Rightarrow x = 39 - 30$$

$$\Rightarrow x = 9$$

(iii)

$$\frac{2}{x} + \frac{3}{y} = 13$$

$$\Rightarrow \frac{(2y+3x)}{xy} = 13$$

$$\Rightarrow$$
 2y + 3x = 13xy eq.[1]

$$\frac{5}{x} - \frac{4}{y} = -2$$

$$\Rightarrow \frac{5y - 4x}{xy} = -2$$

$$\Rightarrow$$
 5y - 4x = -2xy eq.[2]

Multiplying eq.[1] by 4 both side, and Multiplying eq.[2] by 3 both side, we get

$$8y + 12x = 52xy eq.[3]$$

$$15y - 12x = -6xy eq.[4]$$

Adding eq.[3] and eq.[4]

$$\Rightarrow$$
 8y + 12x + 15y - 12x = 52xy - 6xy

$$\Rightarrow$$
 1 = 2x

$$\Rightarrow x = \frac{1}{2}$$

Putting this in eq.[1]

$$\Rightarrow 2y + 3\left(\frac{1}{2}\right) = 13\left(\frac{1}{2}\right)y$$

$$\Rightarrow 2y + \frac{3}{2} = \frac{13}{2}y$$

$$\Rightarrow \frac{13}{2}y - 2y = \frac{3}{2}$$

$$\Rightarrow \frac{9y}{2} = \frac{3}{2}$$

$$\Rightarrow y = \frac{3}{9} = \frac{1}{3}$$

Q. 5. A two-digit number is 3 more than 4 times the sum of its digits. If 18 is added to this number, the sum is equal to the number obtained by interchanging the digits. Find the number.

Answer: Let the unit digit be 'x'

Let the digit at ten's place be 'y'

The original number will be 10y + x

Given, number is 3 more than 4 times the sum of its digits

$$\Rightarrow$$
 10y + x = 4(x + y) + 3

$$\Rightarrow$$
 10y + x = 4x + 4y + 3

$$\Rightarrow$$
 6y - 3x = 3

$$\Rightarrow$$
 2y - x = 1

$$\Rightarrow$$
 x = 2y - 1 eq.[1]

Also,

If the digits are interchanged,

Reversed number will be = 10x + y

As, reversed number exceeds the original number by 18,

$$\Rightarrow$$
 (10x + y) - (10y + x) = 18

$$\Rightarrow$$
 10x + y - 10y - x = 18

$$\Rightarrow$$
 9x - 9y = 18

$$\Rightarrow$$
 x - y = 2

$$\Rightarrow$$
 2y - 1 - y = 2 eq.[using 1]

$$\Rightarrow$$
 y = 3

Using this in eq.[1]

$$\Rightarrow$$
 x = 2(3) - 1 = 5

Hence the original number is 10y + x = 10(3) + 5 = 30 + 5 = 35.

Q. 6. The total cost of 6 books and 7 pens is 79 rupees and the total cost of 7 books and 5 pens is 77 ruppees. Find the cost of 1 book and 2 pens.

Answer : Let the cost of one book be 'x' rupees and cost of one pen be 'y' rupees.

Cost of 6 books and 7 pens = 79 Rs

$$\Rightarrow$$
 6x + 7y = 79 eq.[1]

Cost of 7 books and 5 pens = 77 Rs

$$\Rightarrow$$
 7x + 5y = 77 eq.[2]

Multiplying eq.[1] by 5 both side, and Multiplying eq.[2] by 7 both side, we get

$$\Rightarrow$$
 30x + 35y = 395 eq.[3]

$$\Rightarrow$$
 49x + 35y = 539 eq.[4]

Subtracting eq.[3] from eq.[4], we get

$$\Rightarrow$$
 49x + 35y - 30x - 35y = 539 - 395

$$\Rightarrow$$
 19x = 144

$$\Rightarrow x = \frac{144}{19}$$

Using this in eq.[1]

$$\Rightarrow 6\left(\frac{144}{19}\right) + 7y = 79$$

$$\Rightarrow \frac{864}{19} + 7y = 79$$

$$\Rightarrow$$
 864 + 19×7y = 79×19

$$\Rightarrow 19x7y = 79x19 - 864$$

$$\Rightarrow y = \frac{1501 - 864}{19 \times 7}$$

$$\Rightarrow$$
 y = 5

$$\& 6x + 7y = 79$$

$$\Rightarrow 6x + 35 = 79$$

$$\Rightarrow$$
 6x = 44

$$\Rightarrow$$
 x = 7

Hence, the cost of 1 pen & 2 books = Rs 1(y) + 2x

$$= 5 + 14 = Rs 19.$$

Q. 7. The ratio of incomes of two persons is 9 : 7. The ratio of their expenses is 4 : 3. Every person saves rupees 200, find the income of each.

Answer: As the ratio of incomes is 9:7,

Let income of first person = 9x

Income of second person = 7x

Also, ratio of incomes is 4:3,

Let expenses of first person = 4y

Expenses of second person = 3y

Each person saves 200 Rs,

$$\Rightarrow$$
 9x - 4y = 200 eq.[1]

$$\Rightarrow$$
 7x - 3y = 200 eq.[2]

Multiplying eq.[1] by 3 both side and Multiplying eq.[2] by 4 both side, we get

$$\Rightarrow$$
 27x - 12y = 600 eq.[3]

$$\Rightarrow$$
 28x - 12y = 800 eq.[4]

Subtracting eq.[3] from eq.[4], we get

$$\Rightarrow$$
 28x - 12y - (27x - 12y) = 800 - 600

$$\Rightarrow$$
 28x - 12y - 27x + 12y = 200

$$\Rightarrow$$
 x = 200

Income of first person = 9x = 9(200) = 1800 Rs

Income of second person = 7x = 7(200) = 1400 Rs

Q. 8. If the length of a rectangle is reduced by 5 units and its breadth is increased by 3 units, then the area of the rectangle is reduced by 8 square units. If length is reduced by 3 units and breadth is increased by 2 units, then the area of rectangle will increase by 67 square units. Then find the length and breadth of the rectangle.

Answer : Let the length be 'x' and breadth be 'y'

Area of rectangle = length x breadth

Area of rectangle = xy

First case:

Length =
$$x - 5$$

Breadth =
$$y + 3$$

As, area is reduced by 8 sq. units

$$\Rightarrow$$
 xy - (x - 5)(y + 3) = 8

$$\Rightarrow$$
 xy - (xy + 3x - 5y - 15) = 8

$$\Rightarrow$$
 xy - xy - 3x + 5y + 15 = 8

$$\Rightarrow$$
 3x - 5y = 7 eq.[1]

Second case:

Length =
$$x - 3$$

Breadth =
$$y + 2$$

As, the area is increased by 67 units

$$\Rightarrow (x - 3)(y + 2) - xy = 67$$

$$\Rightarrow xy + 2x - 3y - 6 - xy = 67$$

$$\Rightarrow 2x - 3y = 73 \text{ eq.}[2]$$

Multiplying eq.[1] by 2 both side, and Multiplying eq.[2] by 3 both side, we get

$$\Rightarrow$$
 6x - 10y = 14 eq.[3]

$$\Rightarrow$$
 6x - 9y = 219 eq.[4]

Subtracting eq.[3] from eq.[4]

$$\Rightarrow$$
 6x - 9y - 6x + 10y = 219 - 14

$$\Rightarrow$$
 y = 205

Using this in eq.[1]

$$\Rightarrow 3x - 5(205) = 7$$

$$\Rightarrow$$
 3x - 1025 = 7

$$\Rightarrow$$
 3x = 1032

$$\Rightarrow$$
 x = 344

Hence, length = x = 344 units

Breadth = y = 219 units.

Q. 9. The distance between two places A and B on road is 70 kilometers. A car starts from A and the other from B. If they travel in the same direction, they will meet after 7 hours. If they travel towards each other they will meet after 1 hour, then find their speeds.

Answer: Let the speed of car at place A is x km/h and that of car at place B is y km/h

If they travel in same direction, they will meet after 7 hours, i.e. the difference of distance covered by them in 7 hours will be equal to distance b/w A and B.

As, distance = speed x time, and distance from A to B is 70 km

$$\Rightarrow 7x - 7y = 70$$

$$\Rightarrow$$
 x - y = 10

$$\Rightarrow$$
 x = y + 10 eq.[1]

If they, travel in opposite direction, they will meet after 1 hour i.e. sum of distance travelled by both cars will be equal to the distance b/w A and B.

$$\Rightarrow$$
 x + y = 70

Using eq.[1], we have

$$\Rightarrow$$
 y + 10 + y = 70

$$\Rightarrow$$
 2y = 60

$$\Rightarrow$$
 y = 30

Using this in eq.[1], we have

$$x = 30 + 10 = 40$$

Hence,

Speed of car at A = x = 40 km/h

Speed of car at B = y = 30 km/h

Q. 10. The sum of a two-digit number and the number obtained by interchanging its digits is 99. Find the number.

Answer : Let the unit digit be 'x' and digit at ten's place be 'y'

Original Number = 10y + x

Number obtained by interchanging digits = 10x + y

Given,

$$10y + x + 10x + y = 99$$

$$\Rightarrow 11x + 11y = 99$$

$$\Rightarrow$$
 x + y = 9

If x = 1, y = 8 and number is 18

If x = 2, y = 7 and number is 27

If x = 3, y = 6 and number is 36

If x = 4, y = 5 and number is 45

If x = 5, y = 4 and number is 54

If x = 6, y = 3 and number is 63

If x = 7, y = 2 and number is 72

If x = 8, y = 1 and number is 81