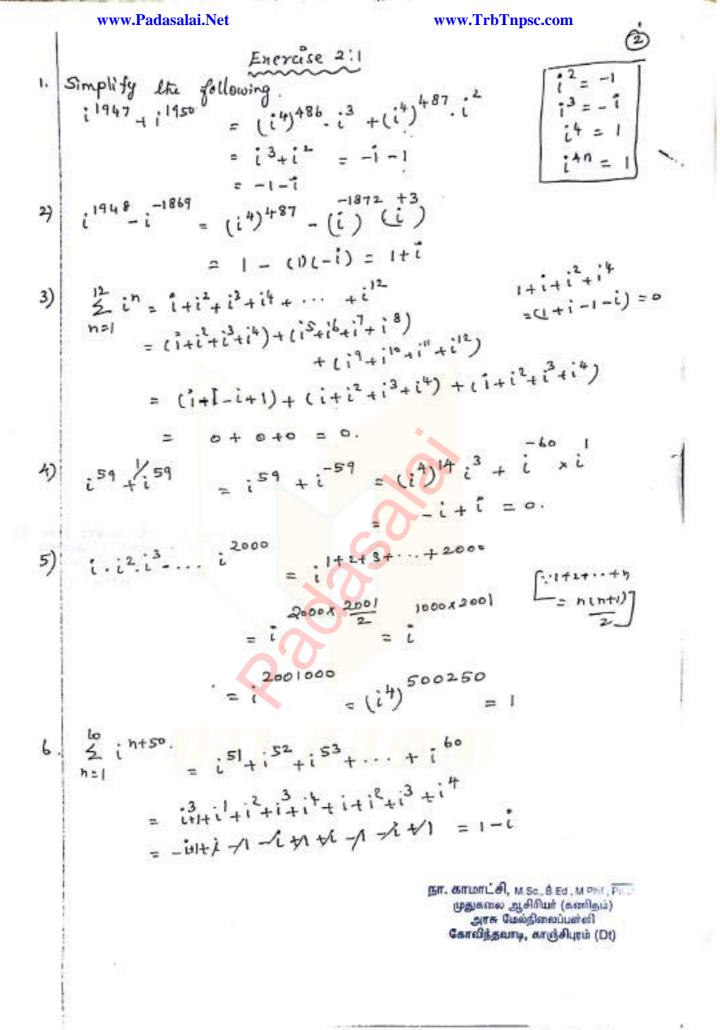
CHAPTER 2: Complex Number 1. $\sqrt{4} = +i$, $i^2 = -1$, $i^3 = -i$, $i^4 = 1$, $i^4 = 1$ YneN 2. 121+221 = 12/1+1221 (Triangle inequality 5) | 121-22/ 3/ 1211-122/ 4. $)\overline{z_{1}+z_{2}} = \overline{z_{1}}+\overline{z_{2}}$ 2) $\overline{z_{1}-z_{2}} = \overline{z_{1}}-\overline{z_{2}}$ 3) $\overline{z_{1}z_{2}} = \overline{z_{1}}$ 4) $\left(\frac{\overline{z_1}}{z_1}\right) = \frac{\overline{z_1}}{z_1}, z_2 \neq 0$ 5) $Pe(z) = \frac{2+\overline{z_2}}{z_1}$ () $Im(z) = \frac{2-\overline{z_2}}{z_1}$ 1) z" = (z) " yn EZ 8) Ziskud iff Z= Z 9) z is purely imaginary iff z= = = 10) == = 2. 2) 12,22 = 12,1 122 | 3) 5)) 121 = 121 5) Pe(z) ≤ 121 6) Im(z) ∈ 121. 4) 12" = 121" 61 2=n+iy . =) 121 = Valty2 7) Square Kest of atil vis Vatib = = 1 where Z= a+ib, and b Fo. 8) 196lax form Z = or coso + isince) BIT. BITLIFTLE A, M.Sc., B.Ed., M.Phil., Ph.D. முதுகலை ஆசிரியர் (கணிதம்) 2) z = + (coso - isine) அரசு மேல்நிலைப்பள்ளி 5) Z 1 Z 2 = ۲,72 [(ம். (மி. +ம்.) + i Sin (மி. + ம்.) கோவித்தவாடி, காஞ்சிபுரம் (Dt) 4) =1 = 11 [(() () + i sin | Q (- O)] 9) Demoivre's theorem (Coso +isino) = cosno + isinna. Ynez 10) nto roots of a complex number Z = losa +isine Z'/h = y'n [cos(0+2+1)+ isin (6+2+1)]. k =0,1,2..(n-1) ()) 1 = coso fisino, 3) i = cos m fisin m2, 3) -1 = cost fisin T. 12) Sinoti cosa = $cos(9_2-a) + i sin(9_2-a)$ 131 whe roof of unity 1) w3=1 2) 1+10+102 =0 3) $\omega = -1 + i\sqrt{3}$ +) $\omega^2 = -1 - i\sqrt{3}$ 14) nth door of unity 1+w+w+ ...+w1-1=0 151: Principle argument of a complex trumber &= 17-4



equal.

Energise 2.2 Evaluate the following if z=5- di and w= -1+3i (i) Z+w = 5-2i -1+3i = 4+i (1) z-iw = (5-2i) -i(-1+3i) = 5-2i+(-3i = 5-21+1+3 = 8-1 (11) 22+3w = 2(5-2i) +3(-1+3i) = 10-4i-3+9i = 7+51 (10) Zw = (5-2i) (-1+3i) = -5+15i+ ai -6i2 = -5+17i -6(-1) = -5+17i+6 = 1+17i (V) x2+22w+w2 = (5-2i)2+2(5-2i)(-1+3i)+(-1+3i)2 = 25+4i2-20i+2(-5+15i+2i-6i2)+1+3i2-6i = 25-4-201-10+301+41+12+1-3-61 15+81 2. Given the complex number Z = 27 31 represent diagram Complex numbers in Argand (U Z, iz and Zeiz. Z = 2+3i [z = i(2+3i) = 2i+3i2 7+12= (2+3i) -3+2i (ii) z, -iz, z-iz Z= 2+3i -(z = -1 (2+3i) = - 2i - 3i Z-iz = 2+3i +3+2i : -. = -1+51 3) Find the values of the real numbers andy if the Complex numbers. (3-1)2- (2-1)y+2i+5 and 2n+(-1+2i)y+3+2i are

> நா. காமாட்சி, M.Sc., B.Ed., M.Phil., Ph.D. முதுகளை ஆசிரியர் (கணிதம்) Acad Connellmax named Come yearny, anytheris (DI)

(1)
$$-3+y+2 = 2y+2$$

 $3-y-2+2y+2 = 0$
 $3+y=0$ -2

solve
$$0 + 8$$
 $x-y=-2$

$$3+y=0$$

$$2x=-2$$

$$3=-1$$
Put in 0 $x+y=0$

நா. காமாட்சி, M.Sc., B.Ed., M.Phil., Ph. U முதுக்கை ஆசிரியர் (கணிதம்) அரசு மேல்நிலைப்பள்ளி கோவிந்தவாடி, காஞ்சிபுரம் (Dt)

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              Exercise 2.3
1. If Z1 = 1-3i, Z2 = -4i and Z3 = 5 Show that
  () (Z1+Z2)+Z3 = Z1+ (Z2+Z3)
   LHS: (21+22)+23 = (1-3i-4i)+(5) =(1-7i)+5 =6-7'
        2,+(22+23) = (1-3i) + (-4i+5)= 6-7i
         .. LHS = RHS.
   (ii) (2,22) 23 = 2, (2, 23)
       Z122 = (1-3i)(-4i) = -4i+12i2 = -4i-12
   (Z122) Z3 = (-12-4i) 5 = -60-20i
        (22 23) = (-4i)(5) = -20i
     Z1(22Z3) = (1-3i)(-20i) = -20i+60i2
                = -20i-60 = -60 -20 i
          .. LHS = 2 H3.
  If z = 3 = = = - 7 i and z = 5 + 4 i show that
   (i) Z((22+23) = Z, Z2 + Z, Z3.
   LHS z, (z,+23) = 3(-7i+5+4i) = 3(5-3i)
        Z, Z2 = 3(-7i) = -21i
   RHS
        Z1 Z3 = 3 (5+4i) = 15+12i
  Z1 Z2 + Z1 Z3 = -21 i + 15 + 12 i = 15 - 9 i
                                    BIT, CATUMELER, M.Sc., B.Ed., M.Phil., Ph.D.
          LHS = RHP.
                                      முதுகலை ஆசிரியர் (கணிதம்)
                                        அரசு மேற்நிளவப்பள்ளி
  (il) (2,+22) 23 = 2, 23 + 22 23
                                      கோவித்தவாடி, காஞ்சியும் (Dt)
         (21+22) 23 = (3-7i)(5+4i)
                      = 15+121-351-2812
                      = 15 -231 +28 = 43-231
              3 (5+41) = 15+121
       ZZZZ = -7i (5+4i) = -35i - 28i2 = -35i+28
   2123+2223 = 15+121-351+28 = 43-231
              : LH3 = RHS.
```

3) If $Z_1 = 2+5i$, $Z_2 = -3-4i$ and $Z_3 = 1+i$ find the G additive and multiplicative inverse of $Z_1, Z_2 = Z_3$.

Solon $Z_1 = a+5i$ additive inverse $-Z_1 = -2-5i$ additive inverse $-Z_1 = -2-5i$ multiplicative inverse $\frac{1}{Z_1} = \frac{1}{2+5i} = \frac{2-5i}{(2-5i)} = \frac{2-5i}{2^2+5^2}$ $= \frac{2-5i}{29} = \frac{2}{29} - \frac{5i}{29} = \frac{(-2+5i)(9-ib)}{(2+5i)(9-ib)}$

(1) $Z_2 = -3-4i$ additive inverse $-Z_2 = 3+4i$ multiplicative inverse $\frac{1}{Z_2} = \frac{1}{(-3+4i)} (-3+4i)$ $= -\frac{3+4i}{(-3)^2+4^2} = \frac{-3+4i}{9+16} = \frac{-3}{25} + i \frac{4}{25}.$

(iii) $z_3 = 1 + i$ additive in verse $-z_3 = -1 - i$ bnultiplicative in verse $\frac{1}{z_3} = \frac{1}{1 + i} \frac{(1 - i)}{(1 - i)}$ $= \frac{1 - i}{12 + i^2} = \frac{1 - i}{2} = \frac{1}{2} - i \left(\frac{1}{2}\right)$

நா. காமாட்சி, M.Sc. B.Ed 14 இவி முதுக்கை ஆசிரிவர் (சு.மி.மி.) அரசு மேல்நிலைப்பர்வி கோவிந்தவாடி, காஞ்சிபுரம் (Dt)

Exercise 2.4

Write the following in the sectangular form.

(i)
$$(5+9i)+(2-4i) = 7+5i = 7-5i$$

(ii) $\frac{10-5i}{1+2i} = \frac{10-5i}{15+2i} \frac{(6-2i)}{(6-2i)} = \frac{60-20i-30i+10i^2}{12+2^2}$

$$= \frac{60-50i-10}{36+4} = \frac{+50-50i}{40} = \frac{50}{40} - \frac{50}{40}i$$

$$= \frac{5}{4} - \frac{5}{4}i$$

(iii) $3i+\frac{1}{2-i} = -3i+\frac{1}{4-i} (\frac{2+i}{2+i}) = -3i+\frac{2+i}{2^2+1^2}$

$$= -3i+\frac{2+i}{4-i} = -3i+\frac{2+i}{5}$$

$$= -3i+\frac{2+i}{5} = \frac{2-14i}{5} = \frac{2}{5} - \frac{14}{5}i$$

2) $2f = 2+iy$ find the following in rectangular form.

(i) $2f = 1+iy$ find the following in rectangular form.

(ii) $2f = 1+iy$ find the following in rectangular form.

(iii) $2f = 1+iy$ find the following in rectangular form.

(iii) $2f = 1+iy$ find the following in rectangular form.

(iii) $2f = 1+iy$ find the following in rectangular form.

(iii) $2f = 1+iy$ find the following in rectangular form.

(iii) $2f = 1+iy$ find the following in rectangular form.

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(iii) $2f = 1+iy$ find the following in rectangular form.

(iii) $2f = 1+iy$ find the following in rectangular form.

(iii) $2f = 1+iy$ find the following in rectangular form.

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(3)

3) If
$$z_1 = 2 - i$$
 & $z_2 = -4 + 3i$ find the inverse of $z_1 z_2 = \frac{2i}{z_2}$
Soln $z_1 z_2 = (2 - i)(-4 + 3i) = -8 + 6i + 4i - 3i^2$
 $= -8 + 10i + 3 = -5 + 10i$

$$\frac{1}{2_{1}z_{2}} = \frac{1}{-5+10i} = \frac{1}{-5+10i} = \frac{(-5-10i)}{(-5-10i)} = \frac{-5-(0i)}{(-5)^{2}+10^{2}}$$

$$= \frac{5-10i}{2-5+100} = \frac{-5-10i}{12.5} = \frac{-81}{12.5} - \frac{125}{12.5}$$

$$= \frac{1}{25} (1+2i)$$

$$\frac{z_2}{z_1} = \frac{-4+3i}{2-1} = \frac{(-4+3i)}{(2-i)} \sqrt{\frac{(2+i)}{(2+i)}}$$

$$= -8 - 4i + 6i + 3i^{2} - 8 + 2i - 3 = -11 + 2i$$

$$= -8 - 4i + 6i + 3i^{2} - 3 + 2i - 3 = -11 + 2i$$

$$= -8 - 4i + 6i + 3i^{2} - 3 + 2i - 3 = -11 + 2i$$

4) The Complen numbers u, v and w are related by
$$\frac{1}{4} = \frac{1}{4} + \frac{1}{4}$$
. If $v = 3 - 4i$, and $w = 4 + 3i$ find u in sectiongulae yerm.

$$\frac{90 \text{ in}}{V} = \frac{1}{3-4 i} \frac{(3+4 i)}{3+4 i} = \frac{3+4 i}{3^2+4^2} = \frac{3+4 i}{5+1 4} = \frac{3+4 i}{25}$$

$$\frac{1}{W} = \frac{1}{4+3 i} \frac{(4-3 i)}{(4-3 i)} = \frac{4-3 i}{4^2+3^2} = \frac{4-3 i}{16+9} = \frac{4-3 i}{25}$$

0

(ii) $\frac{(9+i)\sqrt{3}}{(9+i)}^{12} + \frac{(20-5i)}{(7-6i)}^{12} = 171 - \frac{(9+i)}{(7-6i)}^{12} = 171 - \frac{(9+i)}{(7-6i)}^{12} = 170 + \frac{85i}{(7-6i)}^{12} = 2 - i$ $\frac{(20-5i)}{(7+6i)} = \frac{(7+6i)}{(7+6i)} = \frac{(20-5i)}{(7-6i)}^{12} = 2 + i$ $\frac{(20-5i)}{(7+6i)} = \frac{(7+6i)}{(7+6i)}^{12} = \frac{(20-5i)}{(7-6i)}^{12} = 2 + i$ $Z = \frac{(19-7i)}{(9+i)}^{12} + \frac{(20-5i)}{(7-6i)}^{12} = (2-i)^{12} + (2+i)^{12} = (2-i)^{12} + (2+i)^{12}$ $= (2-i)^{12} + (2+i)^{12} = \frac{(2-i)^{12}}{(2-5i)^{12}} + (2-i)^{12}$ $= (2+i)^{12} + (2-i)^{12}$ $= (2+i)^{12} + (2-i)^{12}$

: 2 is real. : \(\frac{19-7i}{3+i}\)^2 + \(\frac{20-5i}{7-ki}\)^{12} is real.

= Z

Find the modulus of the following complex number. Solni 21 3+41 $\frac{\partial i}{\partial t + i} \frac{(3-4i)}{(3-4i)} = \frac{6i-8i^2}{3^2+4^2} = \frac{6i+8}{16+9} = \frac{8+6i}{25}$ $\left|\frac{2i}{3+4i}\right| = \left|\frac{8+6i}{25}\right| = \frac{1}{25}\sqrt{8^2+6^2} = \frac{1}{25}\sqrt{64+34} = \frac{1}{25}\sqrt{100}$ = 1 (10) = 2 (1) $\frac{2-i}{1+i} + \frac{(-2i)}{1-i} = (2-i) \frac{(1-i)}{(1+i)} \frac{(1-2i) \frac{(1+i)}{(1-i)}}{(1+i)}$ $= 2 - 2i - (1 + i^{2} + 1 + (i - 2i - 2i^{2} = 3 - 4i - 1 + 2)$ $= 2 - 2i - (1 + i^{2} + 1 + (i - 2i - 2i^{2} = 3 - 4i - 1 + 2)$ நா. காமாட்சி, M.Sc., B.Ed., M.Phil., Ph.D. = 4-4i = விட்ட-2i) = 2 -2i முறுக்கை ஆசிரியர் (கணிதம்) அரசு மேல்நிலைப்பள்ளி கோவிந்தவரை, காஞ்சிபரம் (Dt) 12-2i1= V22+22 = V4+4 = V8 = 2 V2. 2i(3-4i)(4-3i) = 2i(1/2-9i-16i-1/2) (11) = 2i(-25i) = -50i2 = 50 1501 = 50. 1) For any two complex numbers Z1 & Z2 such that 1211 = 1221=1 and 2,22 f-1 then show that is a real number. 121 = 1221 = 1 $\left|\frac{2_1+2_2}{1+2_12_2}\right| = \frac{|2_1+2_1|}{|+|2_1|2_1} \leq \frac{|2_1|+|2_2|}{|+|2_1||2_2|}$ ≤ 1+1 ≤1 121+2L 51 lies between [0,1]

172122 6 9 real humber.

$$(2) \stackrel{\text{Www.Padasalai.Net}}{\text{Aliter}} = 1 = 1 = 12.1^{2} = 1 \stackrel{\text{www.TrhTnpsc/com}}{\text{2}}$$

$$\frac{z_{1}}{z_{2}} = \frac{1}{z_{1}} \qquad (2.1z_{2} + 1)$$

$$= \frac{21+2z}{1+z_{1}z_{2}} = \frac{1}{z_{1}} + \frac{1}{z_{2}} = \frac{21+2z}{1+z_{1}z_{2}}$$

$$= \frac{21+2z}{1+z_{1}z_{2}} = \frac{1}{z_{1}} + \frac{1}{z_{2}} = \frac{21+2z}{1+z_{1}z_{2}}$$

$$= \frac{1+2z_{2}}{1+z_{1}z_{2}} = \frac{1}{z_{1}} + \frac{1}{z_{2}} = \frac{1+2z_{2}}{1+z_{1}z_{2}}$$

$$= \frac{1+2z_{2}}{1+z_{1}z_{2}} = \frac{1+2z_{2}}{1+z_{1}z_{2}} = \frac{1+2z_{2}}{1+z_{1}z_{2}}$$

$$= \frac{1+2z_{2}}{1+z_{1}z_{2}} = \frac{1+2z_{2}}{1+z_{1}z_{2}} = \frac{1+2z_{2}}{1+z_{1}z_{2}} = \frac{1+2z_{2}}{1+z_{1}z_{2}} = \frac{1+2z_{2}}{1+z_{1}z_{2}}$$

$$= \frac{1+2z_{1}}{1+z_{1}z_{2}} = \frac{1+2z_{2}}{1+z_{1}z_{2}} = \frac{1+2z_{2}}{1+z_{2}} =$$

3) which one of the points 10-8i, 11thi is closesto Iti

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4) if
$$121=3$$
 8how that $7 \le |2+6-8i| \le 13$

Solin $|2+6-8i| \le |2|+|6-8i|$ $|2+2| \le |2|+|2|$
 $\le 3 + \sqrt{6^2+8^2}$
 $\le 3 + \sqrt{36+64} = 3 + \sqrt{100} = 3 + 10 = 13$
 $\le 13 - 0$.

 $|2+6-8i| > |12| - |6-8i|$
 $> 7 - 0$

BT. EMOTE A, M.Sc. B.Ed. M.Phi., Ph.D. முகுகலை ஆசிரியர் (கணிதம்)

அரசு மேற்நிலைப்பள்ளி கோவிந்தவாடி, காஞ்சியும் (Dt)

by
$$0 1 \otimes 7 \leq |2+6-8i| \leq |3|$$
.

5) If $|2|=|3how+ka_1| \leq |2^2-3| \leq 4$

solh $|2^2-3| \geq ||2|^2-3| = ||2^2-3| \leq ||2^2|+|-3|$

$$\geq ||-3| = ||2^2-3| \leq 4 - 0$$
by $0 \leq 0 \leq 2 \leq ||2^2-3| \leq 4$.

2) If
$$|z-\frac{2}{2}|=2$$
 show that the greatest and least value of $|z|$ are $\sqrt{3}+1$ * $\sqrt{3}-1$ respectively.

$$|2|^2 - 2|2| + 2 \le 0$$

$$|2|^{2} - 2|2| - 2 \le 0$$

$$|2| = +2 \pm \sqrt{4 - 4 \cdot 1 \cdot (-2)} = 2 \pm \sqrt{4 + 8} = 2 \pm \sqrt{12}$$

$$|2| = +2 \pm \sqrt{4 - 4 \cdot 1 \cdot (-2)} = 2 \pm \sqrt{4 + 8} = 2 \pm \sqrt{12}$$

Soly
$$|Z_{1}| = | |Z_{2}| = 2 | |Z_{3}| = 3, |Z_{3}|^{2} = 9$$

$$|Z_{1}|^{2} = | |Z_{2}|^{2} = 1 | |Z_{3}|^{2} = 1 | |Z_{$$

8) If the area of the margle formed by the vertex z, iz, and z+iz is square unib. find the value g |z|value g |z|solh but A, B, C be z', iz, z+iz.

Area of a margle $= \frac{1}{2} \times \frac{AB}{AB} \times PC$.

A P B AB = |z-iz|P is midpoint of $AB = A+B = \frac{1}{2} = \frac{1}$

Œ

$$\frac{7}{4} \left| \frac{2^{2}+2^{2}}{2^{12}} \right| = 50$$

$$\frac{121^{2}}{4} = 50$$

$$\frac{121^{2}}{2} = 50$$

$$\frac{121^{2}}{121} = 100$$

1 Show that The equation Z 3+ 2 = 0 Las the where

$$z^{3} = -2^{\frac{1}{2}}$$

$$z^{2}(z^{2}) = -2^{\frac{1}{2}}$$

$$z^{4} = -2^{\frac{1}{2}}$$

$$|z|^{4} + 2^{\frac{1}{2}}|^{2} = 0$$

$$|z|^{2} (|z|^{2} + 2)^{\frac{1}{2}}$$

$$|z|^{2} = 0$$

$$|z|^{2} = 0$$

121 = 0

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$$z^3 = -2\overline{z} = z^3 = -2\frac{1}{z}$$

it has four solution wicheding 200

23+2== It has five solution.

10) find the square roots of
$$0 + 3i$$

Solh

 $\sqrt{a+ib} = \pm \left[\sqrt{\frac{121+9}{2}} + i \frac{b}{161} \sqrt{\frac{121-9}{2}} \right]$
 $121 = 14+3i = \sqrt{4^2+3^2} = \sqrt{16+9} = \sqrt{25} = 5$
 $4 = 4$
 $4 = 3$
 $\sqrt{4+3}i = \pm \left(\sqrt{\frac{5+4}{2}} + i \frac{3}{131} \sqrt{\frac{5-4}{2}} \right)$

$$= \pm \left(\sqrt{\frac{1}{2}} + i\sqrt{\frac{1}{2}}\right) = \pm \left(\frac{3}{\sqrt{2}} + i\frac{1}{\sqrt{2}}\right)$$

$$= \pm \left(\frac{3+i}{\sqrt{2}}\right)$$
(ii) $-6+8i$

$$\sqrt{-6+87} = \pm \left(\sqrt{\frac{10-6}{2}+i\frac{8}{8}}\sqrt{\frac{10+6}{2}}\right) = \pm \left(\sqrt{2}+i\sqrt{8}\right)$$

$$= \pm \left(\sqrt{2}+i2\sqrt{2}\right)$$

(ili)
$$-5-12i$$

 $121=\sqrt{-5^2+(42)}=\sqrt{25+144}=\sqrt{169}=13$

$$\sqrt{-5-12i} = \pm \left(\sqrt{\frac{13-5}{2}} + i \frac{12}{12} \sqrt{\frac{13+5}{2}}\right)$$

$$= \pm \left(\sqrt{4} + i \sqrt{9}\right) = \pm \left(2 - i 3\right).$$

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1117114116000

Exercise 26

To Z= mily is a complex humber such that
$$\left|\frac{z-qi}{z+qi}\right|=1$$

Show that the locus of z is head ance $\left|\frac{z-qi}{z+ai}\right|=1$
 $z=n+iy$
 $\left|\frac{z-4i}{z+4i}\right|=1$
 $z=n+iy$
 $\left|\frac{z+iy-4i}{z+iy+hi}\right|=1$
 $\left|\frac{z+iy-4i}{z+iy+hi}\right|=1$
 $\left|\frac{z+i(y-4)}{z+i(y+4)}\right|=1$
 $\left|\frac{z+i(y-4)}{z+i(y+4)}\right|=1$
 $\left|\frac{z+i(y-4)}{z+i(y+4)}\right|=1$
 $\left|\frac{z+i(y-4)}{z+i(y+4)}\right|=1$
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 $\left|\frac{z+i(y-4)}{z+i(y+4)}\right|=1$
 $\left|\frac{z+i(y+4)}{z+i(y+4)}\right|=1$
 $\left|\frac{z+i$

$$|z-4|^2 - |z-1|^2 = 16$$

$$|z-4|^2 - |z-1|^2 = 16$$

$$|z-4|(z-4) - (z-1)(z-1) = 16$$

$$|z-4|^2 - |z-1|^2 = 2z$$

$$|z-4|^2 - |z-1|^2 = 16$$

$$|z-4|^2 - |z-1|^2 = 16$$

$$|z-4|^2 - |z-1| = 16$$

$$|z-4|^2 - |z-1| = 16$$

$$|z-4|^2 - |z-4| = 16$$

$$|z$$

நா. காமாட்சி, M.Sc., B Ed., M Phr., Phr., முதுகலை ஆசிரியர் (கணிதம்) அரசு மேல்நிலைப்பள்ளி கோவிந்தவாடி, காஞ்சிபுரம் (DI)

(i) write in polar form of the following Complex numbers

(i) did
$$3\sqrt{3}$$
. = $7(\omega \sin + i \sin n)$

$$Y = \sqrt{2^{2}+(2\sqrt{3})^{2}} = \sqrt{4+(4\times 3)} = \sqrt{4+12} = \sqrt{16} = 4$$

$$Y(\cos a) = 2 \qquad Y(\sin a) = 2\sqrt{3}$$

$$\cos a = \frac{2}{4} = \frac{1}{2}. \qquad Sin a = 2\sqrt{3}$$

$$\cos a = \frac{2}{4} = \frac{1}{2}. \qquad Sin a = 4\sqrt{2}$$

$$0 = d = 93. \qquad \left[\begin{array}{c} Sin a = +\sqrt{2} \\ Cosa = +\sqrt{2} \end{array}\right]$$

$$2 + i 2\sqrt{3} = 4 \quad \left(\begin{array}{c} \cos 0 \\ 2 + i \sin n \end{array}\right) + i \sin n \quad \left(2 \times 11 + 92\right) \quad V \times G = 2$$

(ii) $3 - i \sqrt{3} = 2 \quad \left(\cos 0 + i \sin n \right)$

$$Y = \sqrt{3^{2}+(-\sqrt{3})^{2}} = \sqrt{1+3} = \sqrt{12} = 2\sqrt{3}. \qquad \left(\begin{array}{c} sin a = -\sqrt{3} \\ 2\sqrt{3} \end{array}\right) = \frac{1}{2} \left(\begin{array}{c} sin a = -\sqrt{3} \\ 2\sqrt{3} \end{array}\right) = \frac{1}{2} \left(\begin{array}{c} sin a = -\sqrt{3} \\ 2\sqrt{3} \end{array}\right) = \frac{1}{2} \left(\begin{array}{c} sin a = -\sqrt{3} \\ 2\sqrt{3} \end{array}\right) = \frac{1}{2} \left(\begin{array}{c} sin a = -\sqrt{2} \\ 3 - i \sqrt{3} \end{array}\right) = \frac{2}{2} \left(\begin{array}{c} sin a = -\sqrt{2} \\ 2\sqrt{3} \end{array}\right) = \frac{1}{2} \left(\begin{array}{c} sin a = -\sqrt{2} \\ 3 - i \sqrt{3} \end{array}\right) = \frac{2}{2} \left(\begin{array}{c} sin a = -\sqrt{2} \\ 3 - i \sqrt{3} \end{array}\right) = \frac{2}{2} \left(\begin{array}{c} sin a = -\sqrt{2} \\ 3 - i \sqrt{3} \end{array}\right) = \frac{2}{2} \left(\begin{array}{c} sin a = -\sqrt{2} \\ 3 - i \sqrt{3} \end{array}\right) = \frac{2}{2} \left(\begin{array}{c} sin a = -\sqrt{2} \\ 3 - i \sqrt{3} \end{array}\right) = \frac{2}{2} \left(\begin{array}{c} sin a = -\sqrt{2} \\ 3 - i \sqrt{3} \end{array}\right) = \frac{2}{2} \left(\begin{array}{c} sin a = -\sqrt{2} \\ 3 - i \sqrt{3} \end{array}\right) = \frac{2}{2} \left(\begin{array}{c} sin a = -\sqrt{2} \\ 3 - i \sqrt{3} \end{array}\right) = \frac{2}{2} \left(\begin{array}{c} sin a = -\sqrt{2} \\ 3 - i \sqrt{3} \end{array}\right) = \frac{2}{2} \left(\begin{array}{c} sin a = -\sqrt{2} \\ 3 - i \sqrt{3} \end{array}\right) = \frac{2}{2} \left(\begin{array}{c} sin a = -\sqrt{2} \\ 3 - i \sqrt{3} \end{array}\right) = \frac{2}{2} \left(\begin{array}{c} sin a = -\sqrt{2} \\ 3 - i \sqrt{3} \end{array}\right) = \frac{2}{2} \left(\begin{array}{c} sin a = -\sqrt{2} \\ 3 - i \sqrt{3} \end{array}\right) = \frac{2}{2} \left(\begin{array}{c} sin a = -\sqrt{2} \\ 3 - i \sqrt{3} \end{array}\right) = \frac{2}{2} \left(\begin{array}{c} sin a = -\sqrt{2} \\ 3 - i \sqrt{3} \end{array}\right) = \frac{2}{2} \left(\begin{array}{c} sin a = -\sqrt{2} \\ 3 - i \sqrt{3} \end{array}\right) = \frac{2}{2} \left(\begin{array}{c} sin a = -\sqrt{2} \\ 3 - i \sqrt{3} \end{array}\right) = \frac{2}{2} \left(\begin{array}{c} sin a = -\sqrt{2} \\ 3 - i \sqrt{3} \end{array}\right) = \frac{2}{2} \left(\begin{array}{c} sin a = -\sqrt{2} \\ 3 - i \sqrt{3} \end{array}\right) = \frac{2}{2} \left(\begin{array}{c} sin a = -\sqrt{2} \\ 3 - i \sqrt{3} \end{array}\right) = \frac{2}{2} \left(\begin{array}{c} sin a = -\sqrt{2} \\ 3 - i \sqrt{3} \end{array}\right) = \frac{2}{2} \left(\begin{array}{c} sin a = -\sqrt{2} \\ 3 - i \sqrt{3} \end{array}\right) = \frac{2}{2} \left(\begin{array}{c} sin a = -\sqrt{2} \\ 3 - i \sqrt{3} \end{array}\right) = \frac{2}{2} \left(\begin{array}{c} sin a = -\sqrt{2} \\ 3 - i \sqrt{3} \end{array}\right) = \frac{2}{2} \left(\begin{array}{c} sin a = -\sqrt{2} \\ 3 - i \sqrt{3} \end{array}\right) = \frac{2}{2} \left(\begin{array}{c} sin a = -\sqrt{2} \\ 3 - i \sqrt{3} \end{array}\right) = \frac{2}{2} \left(\begin{array}{c} sin a = -\sqrt{2} \\$$

Find the rectangular form of the complex number (1) ($\cos \mathcal{D}_{6}$ + $i\sin \mathcal{D}_{12}$) ($\cos \mathcal{D}_{12}$ + $i\sin \mathcal{D}_{12}$) $= \cos \left(\mathcal{D}_{6} + \mathcal{D}_{12}\right) + i\sin \left(\mathcal{D}_{6} + \mathcal{D}_{12}\right)$ $= \cos \left(\frac{3\pi}{12}\right) + i\sin \left(\frac{3\pi}{12}\right) = \cos \mathcal{D}_{4} + i\sin \mathcal{D}_{4}$

 $=\frac{1}{\sqrt{2}}+i\frac{1}{\sqrt{2}}=\frac{1}{\sqrt{2}}$ (1+i)

www.Padasalai.Net www.TrbTnpsc.com 2(11) cos The -isin The $= \frac{1}{a} \frac{e^{-i\eta_{k}}}{e^{i\eta_{3}}} = \frac{1}{a} e^{-i\eta_{k} - i\eta_{3}} \stackrel{\text{(2)}}{=}$ Q (cos)3 +isin)3) $=\frac{1}{2}e^{-i(\eta_6+\eta_3)}=\frac{1}{2}e^{-i\eta_2}$ BIT. CONTINUED, M.Sc., B.Ed., M.Phil. Ph.D. $= 1 \left(\cos \theta_2 - i \sin \theta_2 \right) \begin{array}{l} \text{p.m. estumi. el., M. Sc., B. Ed., M. Phil., F. } \\ \text{cycloresis of Gurich Constitution} \end{array}$ அரசு போற்றிசைகள்ளி சொலித்துவரை, காத்சியும் (Dt) $=\frac{1}{2}(0-i)=-i/2.$ 3) If (x1+141) {x2+142) (x3+143) + · · · + (xn+14n) = a+16 show that (i) (x12+412) (x2+422) + · · + (xn2+422) = a2462 (i) 2 tant (3/2) = tant (3/4) +2 K71 YEEZ. Soln (2, +iy) (72+iy2) (72+iy3)+ . + (2n+iyn) = a+ib Take modulus on both stdis (nitial) (nitial) (xitial) - (xutial) = 14+ip) [x1+iy1) | n2+i42 | 1x3+i43] ... | xx+iyn) = 1 ++ib) $\sqrt{{{{{\gamma _1}^2} + {{y_1}^2}}}} \cdot \sqrt{{{{{\gamma _1}^2} + {{y_2}}}} \cdot \sqrt{{{{\gamma _1}^2} + {{y_3}^2}}} \cdot \dots } \sqrt{{{{\gamma _1}^2} + {{y_n}^2}}} = \sqrt{{{a^2} + {b^2}}}$ Take square on both sides. (m12+412) (m2+42) (m3+432) ... (m+42) = (a2+62) In (1) Take argument on both sides. ang[(x1+iy1) (x2+iy2) + ... (xn+iyn)] = asegi(++ib) =) arg (x1+141) + arg (x2+142) +... + aug (nn+iyn) = aug (9+16) (: ang (x+i'y) tranty + tanty 12 + . - + tanty n = tant 2

transmed 2 tanty = 2KT+tant (4) V KEZ Hence proved.

www.Padasalai.Net If 1+z = cos 20 +isinza show that z = itano. 1+2 = (coso +isina) (1+2)(1+2) = (coso+isine)2 (1+2) = (coso + isine) 1+2 = cosa + i'sina 1+2 = cosa + isina

1+2 = 1+ i fana

: z = i Lang

நா. காமாட்சி, M.Sc., B.Ed., M.Phil., Ph.D. முறுகலை ஆசிரியர் (கணிதம்) Here proved. அரசு மேல்நிலைப்பள்ளி கோவிந்தவாடி, காஞ்சிபுரம் (Dt)

5) If cost + cosp + cosp = sing + sing + sing = 0 Show that (i) cos 3d+cos3B+cos38=3 cos(d+B+7) and (i) Sin 3d + Sin 373 + Sin 34 = 3 sin (x+ 13+7) solh but us baice A = cosa + i GiAN b= cosprising C= cosprising. a+b+c = (cosd+cosp+cosv) +i (sinx+sinx) 2 0 + 1 p 9+6+6. =0 if atbec =0 We know that 93+63+c3 = 3966 (cosatisina) + (cosptising) + (cosptising) = 3 [(cosd+isind) ded (losp+ising) (cos Vtisiny)]

Exercise 2.8 1. If wat I is a cube root of unity, then show that $\frac{a+b\omega+c\omega^2}{b+c\omega+a\omega^2}+\frac{a+b\omega+c\omega^2}{c+a\omega+b\omega^2}=-1.$ = a+ bw+/cw2 = co $\frac{a + b\omega + (\omega^{2})}{c + a\omega + b\omega^{2}} = \frac{1}{\omega} \frac{(a\omega + b\omega^{2} + c)}{(c + a\omega + b\omega^{2})} = \frac{1}{\omega} \times \frac{\omega^{2}}{\omega^{2}} = \frac{\omega^{2}}{\omega^{3}} = \omega^{2}$ LHS = W+W2 2. Show that ($\frac{\sqrt{3}}{2} + \frac{1}{2}$) $\frac{5}{1} + (\frac{\sqrt{3}}{2} + \frac{1}{2})^{\frac{5}{2}} = -\frac{\sqrt{3}}{2}$ Bit. Bit. Bit. M. Sc., B. Ed., M. Phil. Ph. D. (UBJISBON) SUBHILLIAN (BOXINGUE) Soln V2 + = Y (wie + istno) அரசு மேல்நிலைப்பள்ளி கோவிந்தவாடி, காஞ்சிபுரம் (Dt) Y= V(2) R+ (1) 2 = V 4 = V1 = 1 Ywsa = 1/2 Ysina = 1/2 Cosa = V3/2 d2 D6 [which is I quadwant.
gino = tve, wso = tve) 0= d= 91. 12+1= 1 (ws0)6+1sin 196) (\frac{\sqrt{3}}{2} + \frac{1}{2} \sqrt{5} = \cos 5 \gamma f i sin 5 \gamma \gamma) similarly (13-16) = cus 5-96- 1sin 5-96. (3+12)5+(12-1/2)5= 2003 5M6 = 2003 (TT-M6) = -2 cos ng = -2 (=) = - V3 / Proved. Scanned by CamScanner

Find the value of
$$\left(\frac{1+\sin\frac{\pi}{10}+i\cos\frac{\pi}{10}}{1+\sin\frac{\pi}{10}-i\cos\frac{\pi}{10}}\right)^{10}$$

Soln

$$Z = \cos \frac{\pi}{10} + i\sin \frac{\pi}{10} = i(\sin\frac{\pi}{10}-i\cos\frac{\pi}{10})$$

$$\frac{1}{2} = \cos\frac{\pi}{10} - i\sin\frac{\pi}{10} = \left(\frac{1+i(\cos\frac{\pi}{10}-i\sin\frac{\pi}{10})}{1-i(\cos\frac{\pi}{10}-i\sin\frac{\pi}{10})}\right)^{10}$$

$$= \left(\frac{1+\sin\frac{\pi}{10}-i\cos\frac{\pi}{10}}{1-iz}\right)^{10} = \left(\frac{1+i(\cos\frac{\pi}{10}-i\sin\frac{\pi}{10})}{1-i(\cos\frac{\pi}{10}-i\sin\frac{\pi}{10})}\right)^{10}$$

$$= \left(\frac{1+i\frac{1}{2}}{1-iz}\right)^{10} = \left(\frac{2i-1}{1-iz}\right)^{10} = \left(\frac{2i-1}{1-iz}\right)^{10} = \left(\frac{1}{1-iz}\right)^{10} = \left(\frac{1}{1-iz}\right)^{10}$$

a = cosatisina.

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Similhardy

$$y = los \beta + i sin \beta$$
 $n : cos d + i sin d$
 $y = cos \beta + i sin \beta$
 $n : cos d + i sin d$
 $n : cos d +$

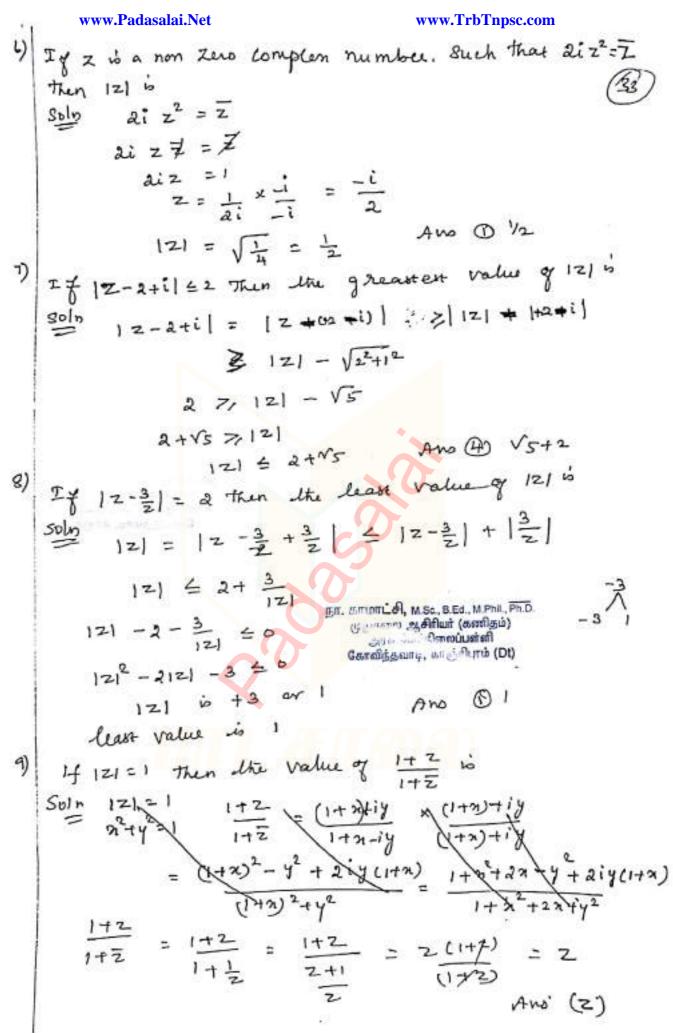
5) Solve the equation z3+27=0 F: -1 = cos D+isIn F) $Z = (27)^{1/3} (-1)^{1/3} = (3^3)^{1/3} [\cos \pi + i \sin \pi]^{1/3}$ = 3 [cos (2KT+T) +isin (2KT+T)] 1/3 = 3 [cos (2k+1) + isin (2k+1)] K=0,1,2 k =0, Z = 3(cos)3+isin)3) = 3 cis)3 k=1, z =3(cos 30/3 +isin 20/3) = 3(-1+i10) = -3 k=2, z= 3 (cos 593+ isin 593) = 3 cis593. b) If w = 1 is a cube root of unity, Show that the roots of the equation (2-13+8=0 are -1, 1-200, 1-2002. Soln (2-1)3+8=0 $(Z-1)^3 = -8 = 8(-1)$ $Z-1 = 8^{1/3} (-1)^{1/3}$ நா. காமாட்சி, M.Sc., B.Ed., M.Phil., Ph.D. முதுகளை ஆசிரியர் (கணிதம்) அரசு மேற்நிலைப்பள்ளி கோவித்தவாடி, காஞ்சிபாம் (Dt) 2-1 = (23) 1/3 (ws7 +isin)] = 2 [cos (2KT +T) + isin (2KT +T)] 13 = 2 [ws (2k+1) 1 + isin (2k+1) 17] R=0.1/2. $z_{-1} = a cis \eta_3 = a \left[\frac{1}{2} + \frac{iv_3}{2} \right] = -2 \left(\frac{1}{2} - \frac{iv_3}{2} \right)$ k=1, Z-1 = 2 cis } = 2 [-1+0] = -2 K=2 Z-1 = 2 cis5 3 = 2 (Cos (17-3)+isin(7-3)) = 2 [-cos n3 +isin n3] = 2 [-1+1 13] $2 = 1 - 2\omega^2$ = -2 + 1 = -1 $= -2\omega$ = -1Aws: 2 = -1, 1-2w. 1-2w2.

Find the value of
$$\frac{3}{2}$$
 cos $\left(\frac{2k\pi}{q}\right)$ + is in $\left(\frac{2k\pi}{q}\right)$ (3)

Solu

Expression $\frac{2k\pi}{q}$ + is in $\left(\frac{2k\pi}{q}\right)$ + is in $\left(\frac{2k\pi}{q$

· Soot are ± /2" ± i to = ± /1/2 (1±1) / Ans.





The solution of the equation
$$|z| - 2 = 1 + 2i$$
 is $\frac{|z|}{|z|^2} = z = (|z| - 1 - 2i)(1 - 2i)(1 - 1 + 2i)$
 $|z|^2 = z = (|z| - 1 - 2i)(1 - 1 + 2i)$
 $|z|^2 = |z|^2 + |z|(-1 + 2i - 1 - 2i) + (-1 - 2i)(-1 + 2i)$
 $|z|^2 = |z|^2 - 2|z| + 5 \Rightarrow 2|z| = 5$
 $|z| = 5/2$

Put in (1)

 $|z| = 5/2$

Put in (2)

 $|z| = 5/2$

Put in (3)

 $|z| = 5/2$

Put in (4)

 $|z| = 5/2$

Put in (5)

 $|z| = 5/2$

Put in (6)

 $|z| = 5/2$

Put in (7)

 $|z| = 5/2$

Put in (8)

 $|z| = 5/2$

Put in (9)

 $|z| = 5/2$

Put in (10)

 $|z| = 5$

In Fy z is a Complex number such that zecle and z+1/2 GR then 121 is

|21+22+23| = | 92,22+42,23+2223 = 1-2.8=1

Ans. 1

72 = 1-11

121+22+23 =1

고+는 =



```
13) Z1, Z2 and Z3 are complex numbers such that
     ZI+72+73=0 and 1211=1221=1231=1 九m Z12+ Z2+ T32 is
           Soln 1지=! 12시키 : 1231=1
             (21+2月+23)= = = 1 1 生 + 生 三 三 三 1 21 22 23)
                                               0 = 12,2,+2,2,+2,2,) => 12,2,+2,2,+2,2,1)=6
                 ·(21+22+23)2= 212+222+232+2322+2321)
14) If \frac{z-1}{z+1} is purely imaginary then 121 is
                    \frac{2-1}{2+1} = \frac{3+iy-1}{3+iy+1} = \frac{(3-i)+iy}{(3+i)+iy} = \frac{(3+i)-iy}{(3+i)-iy} = \frac{(3+i)+iy}{(3+i)-iy}
\frac{2-1}{3+iy+1} = \frac{3+iy+1}{(3+i)+iy} = \frac{(3+i)-iy}{(3+i)-iy} = \frac{(3+i)+iy}{(3+i)-iy} = \frac{(
                                     = (x2-1) - i y(x-1)+iy(x+1) + 42
                                                                                                                                                                         கோவிந்தவாடி, காஞ்சிபுரம் (Dt)
                                                                      (h+1)2+42.
                                 it is purely imaginare Re (2-1) =0
15) if z = n+iy is a complex number such that 12+21=12-21
           Then the locus of x is
                                             |Z+2| = |Z-2|
                                          1n+iy+21 = 1n+iy-2/
                                           V (2+2)2+y1 = V (2-2)2+y2
                                            12+4n+4 = x -4n+4
                                                                                  n co which is rein agi hay anis
                                                                                                                                                              Ans (2)
```

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                                           www.TrbTnpsc.com
   The principal argument of 3 is
   \frac{36}{2} \frac{3}{1+i} \frac{(-1-i)}{(-1-i)} = \frac{3(-1-i)}{-1^2+1^2} = \frac{3}{2} (-1-i)
    -1-i = r (\cos \theta + i \sin \theta)

r = \sqrt{2} \cos \theta = \sqrt{2} \sin \theta = \sqrt{2}
                          x = D4 which is I quadrant
            0= 10X-11 = 94-11 = -3194.
   -1-i = V2 [ cos (-30)4) + isin (-30)4).
        = 3 v2 (cos (-30/4) + isin (-30/4))
                 argument is -394
  The principal argument of (sin46 +1 cos 40) 6
      regarder la grand Erran Alle de de de la company
    (Sin40'+180846)5 = . ( cos56 + isin 56)5
                         = (cas 250'+ isin 250)
                          = cos (360-110) + isin (360-110)
                                          நா. காமாட்சி, M.Sc., B.Ed., M.Phil., Ph.D.
   Principal argument is (-110°)
                                             முதுகலை ஆசிரியர் (கணிகம்)
                                               அரசு மேல்நிலைப்பள்ளி
                                             கோவிந்தவாடி, காஞ்சிபுரம் (Dt)
18) If (Hi)[Hai)(1+3i)-... (Hni) = n+iy then
     2.5.10 · ·· (1+n2) 5
       V12+12 V1+23 +V1+9 ... V1+n2 = V20+42
          (2) (5) (10) ... (14n2) = xr4x2.
                  Ans 3 72+42.
   If with is a cube lost of unity and (1+w)=A+BW
     Then I Ag B) equals.
```

www.Padasalai.Net www.TrbTnpsc.com (37) [(1+w)2]3 = (1+w)6 = w6 = 1 (AIB) = (VII) 20) The principal argument of the complex rumber arg ((1+iv3) 2 = arg (1+iv3) 2 - arg 4i - arg (1-iv3) = 2 aug (1+iv3) - aug (0+4i) - aug (1-iv3) = 2 tant V3 - bant (4) - tant (- 1) = 2 9/3 - 9/2 + 9/3 = 17 - 19/2 BIT. BITUTE A, M.Sc., B.Ed., M.Phil., Ph.D. முதுகலை ஆசிரியர் (கணிதம்) அரசு பேல்நிலைப்பள்ளி கோவிந்தவாடி, காஞ்சிபுரம் (Dt) a) If d & B are the 100to of 2 + 2+1=0 Then d + B is X= -1+143 , B= -1-143 = w/+2 = ev+w2 Am ((+)

1+ V31 = 12 e 183 = e 12 93

(1+43i) 10 = (e 1293) 10

(39)

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25) If w = cis 20, then the number of diotines doors by $\begin{vmatrix} 2+1 & w & w^2 \\ w & z+w^2 & 1 \\ w^2 & 1 & z+w \end{vmatrix} = 0$.

Sold $\begin{vmatrix} z+1 & w & w^2 \\ w & z+w^2 & 1 \end{vmatrix} = 0$. $\begin{vmatrix} z+1 & w & w^2 \\ w & z+w^2 & 1 \end{vmatrix} = 0$ $\begin{vmatrix} z+1 & w & w^2 \\ w & z+w^2 & 1 \end{vmatrix} = 0$ $\begin{vmatrix} z+1 & w & w^2 \\ (z+2w) & 1 \end{vmatrix} = 0$ $\begin{vmatrix} z+1 & w & w^2 \\ (z+2w) & 1 \end{vmatrix} = 0$ $\begin{vmatrix} z+1 & w & w^2 \\ (z+2w) & 1 \end{vmatrix} = 0$ $\begin{vmatrix} z+1 & w & w^2 \\ (z+2w) & 2 \end{vmatrix} = 0$ $\begin{vmatrix} z+1 & w & w^2 \\ (z+2w) & 2 \end{vmatrix} = 0$ $\begin{vmatrix} z+1 & w & w^2 \\ (z+2w) & 2 \end{vmatrix} = 0$ $\begin{vmatrix} z+1 & w & w^2 \\ (z+2w) & 2 \end{vmatrix} = 0$ $\begin{vmatrix} z+1 & w & w^2 \\ (z+2w) & 2 \end{vmatrix} = 0$ $\begin{vmatrix} z+1 & w & w^2 \\ (z+2w) & 2 \end{vmatrix} = 0$ $\begin{vmatrix} z+1 & w & w^2 \\ (z+2w) & 2 \end{vmatrix} = 0$ $\begin{vmatrix} z+1 & w & w^2 \\ (z+2w) & 2 \end{vmatrix} = 0$ $\begin{vmatrix} z+1 & w & w^2 \\ (z+2w) & 2 \end{vmatrix} = 0$ $\begin{vmatrix} z+1 & w & w^2 \\ (z+2w) & 2 \end{vmatrix} = 0$ $\begin{vmatrix} z+1 & w & w^2 \\ (z+2w) & 2 \end{vmatrix} = 0$ $\begin{vmatrix} z+1 & w & w^2 \\ (z+2w) & 2 \end{vmatrix} = 0$ $\begin{vmatrix} z+1 & w & w^2 \\ (z+2w) & 2 \end{vmatrix} = 0$

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