

Real Numbers

Practice set 2.1

Q. 1. Classify the decimal form of the given rational numbers into terminating and non-terminating recurring type

i. $\frac{13}{5}$ ii. $\frac{2}{11}$

iii. $\frac{29}{16}$ iv. $\frac{17}{125}$

v. $\frac{11}{6}$

Answer : i.

$$\frac{13}{5} = 2.6$$

∴ The division is exact

∴ it is a terminating decimal.

ii.

$$\frac{2}{11} = 0.181818 \dots$$

∴ The division never ends and the digits '18' is repeated endlessly

∴ it is a non-terminating recurring type decimal.

iii.

$$\frac{29}{16} = 1.8125$$

∴ The division is exact

∴ it is a terminating decimal.

iv.

$$\frac{17}{125} = 0.136$$

∴ The division is exact

∴ it is a terminating decimal.

v.

$$\frac{11}{6} = 1.83333 \dots$$

∴ The division never ends and the digit '3' is repeated endlessly

∴ it is a non-terminating recurring type decimal.

Q. 2. Write the following rational numbers in decimal form.

i. $\frac{127}{200}$ ii. $\frac{25}{99}$

iii. $\frac{23}{7}$ iv. $\frac{4}{5}$

v. $\frac{17}{8}$

Answer :

i. $\frac{127}{200} = 0.635$

ii. $\frac{25}{99} = 0.252525 \dots$

iii. $\frac{23}{7} = 3.285714285714285714 \dots$

iv. $\frac{4}{5} = 0.8$

$$v. \frac{17}{8} = 2.125$$

Q. 3. Write the following rational numbers in form.

i. $0.\dot{6}$ ii. $0.\overline{37}$

iii. $3.\overline{17}$ iv. $15.\overline{89}$

v. $2.\overline{514}$

Answer :

i. $0.\dot{6}$

Let $x = 0.\dot{6} = 0.6666 \dots$

$$\Rightarrow 10x = 6.6666 \dots$$

Now,

$$10x - x = 6.66 - 0.6666$$

$$\Rightarrow 9x = 6$$

$$\Rightarrow x = \frac{6}{9}$$

$$\Rightarrow 0.\dot{6} = \frac{6}{9} = \frac{2}{3}$$

ii. $0.\overline{37}$

Let $x = 0.\overline{37} = 0.3737 \dots$

$$\Rightarrow 100x = 37.3737 \dots$$

Now,

$$100x - x = 37.3737 - 0.3737$$

$$\Rightarrow 99x = 37$$

$$\Rightarrow x = \frac{37}{99}$$

$$\Rightarrow 0.\overline{37} = \frac{37}{99}$$

iii. $3.\overline{17}$

$$\text{Let } x = 3.\overline{17} = 3.1717 \dots$$

$$\Rightarrow 100x = 317.1717 \dots$$

Now,

$$100x - x = 317.1717 - 3.1717$$

$$\Rightarrow 99x = 314$$

$$\Rightarrow x = \frac{314}{99}$$

$$\Rightarrow 3.\overline{17} = \frac{314}{99}$$

iv. $15.\overline{89}$

$$\text{Let } x = 15.\overline{89} = 15.8989 \dots$$

$$\Rightarrow 100x = 1589.8989 \dots$$

Now,

$$100x - x = 1589.8989 - 15.8989$$

$$\Rightarrow 99x = 1574$$

$$\Rightarrow x = \frac{1574}{99}$$

$$\Rightarrow 15.\overline{89} = \frac{1574}{99}$$

$$\text{v. } 2.\overline{514}$$

$$\text{Let } x = 2.\overline{514} = 2.514514 \dots$$

$$\Rightarrow 1000x = 2514.514514 \dots$$

Now,

$$1000x - x = 2514.514514 - 2.514514$$

$$\Rightarrow 999x = 2512$$

$$\Rightarrow x = \frac{2512}{999}$$

$$\Rightarrow 2.\overline{514} = \frac{2512}{999}$$

Practice set 2.1

Q. 1. Show that $4\sqrt{2}$ is an irrational number.

Answer : Let us assume that $4\sqrt{2}$ is a rational number

$$\therefore 4\sqrt{2} = \frac{a}{b}$$

where, $b \neq 0$ and a, b are integers

$$\Rightarrow \sqrt{2} = \frac{a}{4b}$$

$\therefore a, b$ are integers $\therefore 4b$ is also integer

$\Rightarrow \frac{a}{4b}$ is rational which cannot be possible

$\therefore \frac{a}{4b} = \sqrt{2}$ which is an irrational number

\therefore it is contradicting our assumption

\therefore the assumption was wrong

Hence, $4\sqrt{2}$ is an irrational number

Q. 2. Prove that $3 + \sqrt{5}$ is an irrational number.

Answer : Let us assume that $3 + \sqrt{5}$ is a rational number

$$\therefore 3 + \sqrt{5} = \frac{a}{b}$$

where, $b \neq 0$ and a, b are integers

$$\Rightarrow \sqrt{5} = \frac{a}{b} - 3$$

$$\Rightarrow \sqrt{5} = \frac{a - 3b}{b}$$

$\therefore a, b$ are integers $\therefore a - 3b$ is also integer

$\Rightarrow \frac{a-3b}{b}$ is rational which cannot be possible

$\therefore \frac{a-3b}{b} = \sqrt{5}$ which is an irrational number

\therefore it is contradicting our assumption \therefore the assumption was wrong

Hence, $3 + \sqrt{5}$ is an irrational number

Q. 3. Represent the numbers $\sqrt{5}$ and $\sqrt{10}$ on a number line.

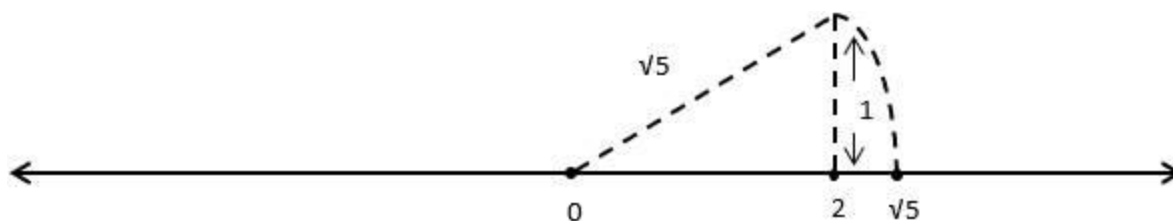
Answer : By Pythagoras theorem,

$$(\sqrt{5})^2 = 2^2 + 1^2$$

$$\Rightarrow (\sqrt{5})^2 = 4 + 1$$

$$\Rightarrow \sqrt{5} = \sqrt{4 + 1}$$

First mark 0 and 2 on the number line. Then, draw a perpendicular of 1 unit from 2. And Join the top of perpendicular and 0. This line would be equal to $\sqrt{5}$. Now measure the line with compass and mark an arc on the number line with the same measurement. This point is $\sqrt{5}$.



Also,

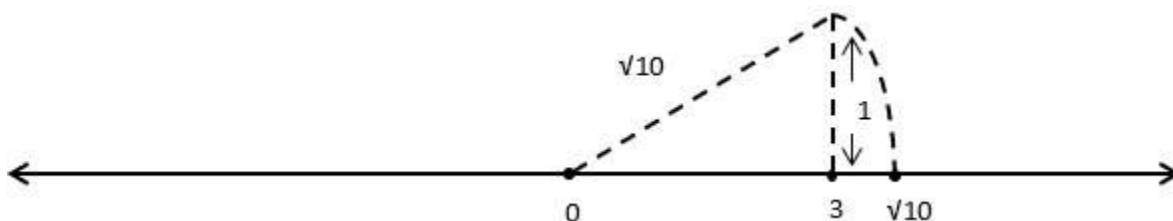
By Pythagoras theorem,

$$(\sqrt{10})^2 = 3^2 + 1^2$$

$$\Rightarrow (\sqrt{10})^2 = 9 + 1$$

$$\Rightarrow \sqrt{10} = \sqrt{9 + 1}$$

First mark 0 and 3 on the number line. Then, draw a perpendicular of 1 unit from 3. And Join the top of perpendicular and 0. This line would be equal to $\sqrt{10}$. Now measure the line with compass and mark an arc on the number line with the same measurement. This point is $\sqrt{10}$.



Q. 4 A. Write any three rational numbers between the two numbers given below.

0.3 and -0.5

Answer : 0.3 and -0.5

To find a rational number x between two rational numbers $\frac{a}{b}$ and $\frac{c}{d}$, we use

$$x = \frac{1}{2} \left(\frac{a}{b} + \frac{c}{d} \right)$$

Therefore, to find rational number x (let) between

$$0.3 = \frac{3}{10} \text{ and } -0.5 = \frac{-5}{10}$$

$$x = \frac{1}{2} \left(\frac{3}{10} + \frac{-5}{10} \right)$$

$$\Rightarrow x = \frac{1}{2} \times \left(\frac{3-5}{10} \right)$$

$$\Rightarrow x = \frac{1}{2} \times \frac{-2}{10}$$

$$\Rightarrow x = \frac{-1}{10} = -0.1$$

Now if we find a rational number between $\frac{3}{10}$ and $\frac{-1}{10}$ it will also be between 0.3 and -0.5 since $\frac{-1}{10}$ lies between 0.3 and -0.5.

Therefore, to find rational number y (let) between $\frac{3}{10}$ and $\frac{-1}{10}$

$$y = \frac{1}{2} \left(\frac{3}{10} + \frac{-1}{10} \right)$$

$$\Rightarrow y = \frac{1}{2} \left(\frac{3-1}{10} \right)$$

$$\Rightarrow y = \frac{1}{2} \times \frac{2}{10}$$

$$\Rightarrow y = \frac{1}{10} = 0.1$$

Now if we find a rational number between $\frac{-1}{10}$ and $\frac{1}{10}$ it will also be between 0.3 and -0.5 since $\frac{1}{10}$ lies between 0.3 and -0.5.

Therefore, to find rational number z (let) between $\frac{1}{10}$ and $\frac{-5}{10}$.

$$z = \frac{1}{2} \left(\frac{1}{10} + \frac{-5}{10} \right)$$

$$\Rightarrow z = \frac{1}{2} \left(\frac{1-5}{10} \right)$$

$$\Rightarrow z = \frac{1}{2} \times \frac{-4}{10}$$

$$\Rightarrow z = \frac{-2}{10} = -0.2$$

Hence the numbers are -0.2, -0.1 and 0.1

Q. 4 B. Write any three rational numbers between the two numbers given below.

-2.3 and -2.33

Answer : -2.3 and -2.33

To find a rational number x between two rational numbers $\frac{a}{b}$ and $\frac{c}{d}$, we use

$$x = \frac{1}{2} \left(\frac{a}{b} + \frac{c}{d} \right)$$

Therefore, to find rational number x (let) between $-2.3 = \frac{-23}{10}$ and $-2.33 = \frac{-233}{100}$

$$x = \frac{1}{2} \left(\frac{-23}{10} + \frac{-233}{100} \right)$$

$$\Rightarrow x = \frac{1}{2} \times \left(\frac{-230 - 233}{100} \right)$$

$$\Rightarrow x = \frac{1}{2} \times \frac{-463}{100}$$

$$\Rightarrow x = -2.315$$

Now if we find a rational number between $-2.315 = \frac{-2315}{1000}$ and $-2.3 = \frac{-23}{10}$ it will also be between -2.3 and -2.33 since -2.315 lies between -2.3 and -2.33

Therefore, to find rational number y (let) between $\frac{-2315}{1000}$ and $\frac{-23}{10}$

$$y = \frac{1}{2} \left(\frac{-2315}{1000} + \frac{-23}{10} \right)$$

$$\Rightarrow y = \frac{1}{2} \left(\frac{-2315 - 2300}{1000} \right)$$

$$\Rightarrow y = \frac{1}{2} \times \frac{-4615}{1000}$$

$$\Rightarrow y = -2.3075$$

Now if we find a rational number between $-2.315 = \frac{-2315}{1000}$ and $-2.33 = \frac{-233}{100}$ it will also be between -2.3 and -2.33 since -2.315 lies between -2.3 and -2.33

Therefore, to find rational number z (let) between $\frac{-2315}{1000}$ and $\frac{-233}{100}$

$$z = \frac{1}{2} \left(\frac{-2315}{1000} + \frac{-233}{100} \right)$$

$$\Rightarrow z = \frac{1}{2} \left(\frac{-2315 - 2330}{1000} \right)$$

$$\Rightarrow z = \frac{1}{2} \times \frac{-4645}{1000}$$

$$\Rightarrow z = -2.3225$$

Hence the numbers are -2.3225, -2.3075 and -2.315

Q. 4 C. Write any three rational numbers between the two numbers given below.

5.2 and 5.3

Answer : 5.2 and 5.3

To find a rational number x between two rational numbers $\frac{a}{b}$ and $\frac{c}{d}$, we use

$$x = \frac{1}{2} \left(\frac{a}{b} + \frac{c}{d} \right)$$

Therefore, to find rational number x (let) between $5.2 = \frac{52}{10}$ and $5.3 = \frac{53}{10}$

$$x = \frac{1}{2} \left(\frac{52}{10} + \frac{53}{10} \right)$$

$$\Rightarrow x = \frac{1}{2} \times \left(\frac{52 + 53}{10} \right)$$

$$\Rightarrow x = \frac{1}{2} \times \frac{105}{10}$$

$$\Rightarrow x = 5.25$$

Now if we find a rational number between $5.25 = \frac{525}{100}$ and $5.2 = \frac{52}{10}$ it will also be between 5.2 and 5.3 since 5.25 lies between 5.2 and 5.3

Therefore, to find rational number y (let) between $5.25 = \frac{525}{100}$ and $5.2 = \frac{52}{10}$

$$y = \frac{1}{2} \left(\frac{525}{100} + \frac{52}{10} \right)$$

$$\Rightarrow y = \frac{1}{2} \left(\frac{525 + 520}{100} \right)$$

$$\Rightarrow y = \frac{1}{2} \times \frac{1045}{100}$$

$$\Rightarrow y = 5.225$$

Now if we find a rational number between $5.25 = \frac{525}{100}$ and $5.3 = \frac{53}{10}$ it will also be between 5.2 and 5.3 since 5.25 lies between 5.2 and 5.3

Therefore, to find rational number z (let) between $5.25 = \frac{525}{100}$ and $5.3 = \frac{53}{10}$

$$z = \frac{1}{2} \left(\frac{525}{100} + \frac{53}{10} \right)$$

$$\Rightarrow z = \frac{1}{2} \left(\frac{525 + 530}{100} \right)$$

$$\Rightarrow z = \frac{1}{2} \times \frac{1055}{100}$$

$$\Rightarrow z = 5.275$$

Hence the numbers are 5.225, 5.25 and 5.275

Q. 4 D. Write any three rational numbers between the two numbers given below.

-4.5 and 4.6

Answer : -4.5 and 4.6

To find a rational number x between two rational numbers $\frac{a}{b}$ and $\frac{c}{d}$, we use

$$x = \frac{1}{2} \left(\frac{a}{b} + \frac{c}{d} \right)$$

Therefore, to find rational number x (let) between $-4.5 = \frac{-45}{10}$ and $4.6 = \frac{46}{10}$

$$x = \frac{1}{2} \left(\frac{-45}{10} + \frac{46}{10} \right)$$

$$\Rightarrow x = \frac{1}{2} \times \left(\frac{-45 + 46}{10} \right)$$

$$\Rightarrow x = \frac{1}{2} \times \frac{1}{10}$$

$$\Rightarrow x = 0.05$$

Now if we find a rational number between $-4.5 = \frac{-45}{10}$ and $0.05 = \frac{5}{100}$ it will also be between -4.5 and 4.6 since 0.05 lies between -4.5 and 4.6

Therefore, to find rational number y (let) between $-4.5 = \frac{-45}{10}$ and $0.05 = \frac{5}{100}$

$$y = \frac{1}{2} \left(\frac{-45}{10} + \frac{5}{100} \right)$$

$$\Rightarrow y = \frac{1}{2} \left(\frac{-450 + 5}{100} \right)$$

$$\Rightarrow y = \frac{1}{2} \times \frac{-445}{100}$$

$$\Rightarrow y = -2.225$$

Now if we find a rational number between $4.6 = \frac{46}{10}$ and $0.05 = \frac{5}{100}$ it will also be between -4.5 and 4.6 since 0.05 lies between -4.5 and 4.6

Therefore, to find rational number z (let) between $4.6 = \frac{46}{10}$ and $0.05 = \frac{5}{100}$

$$z = \frac{1}{2} \left(\frac{46}{10} + \frac{5}{100} \right)$$

$$\Rightarrow z = \frac{1}{2} \left(\frac{460 + 5}{100} \right)$$

$$\Rightarrow z = \frac{1}{2} \times \frac{465}{100}$$

$$\Rightarrow z = 2.325$$

Hence the numbers are -2.225, 0.05 and 2.325

Practice set 2.3

Q. 1. State the order of the surds given below.

i. $\sqrt[3]{7}$ ii. $5\sqrt{12}$

iii. $\sqrt[4]{10}$ iv. $\sqrt{39}$

v. $\sqrt[3]{18}$

Answer : In $\sqrt[n]{a}$, n is called the order of the surd.

Therefore,

i. $\sqrt[3]{7}$

In this, the order of surd is 3.

ii. $\sqrt[5]{12}$

In this, the order of surd is 5.

iii. $\sqrt[4]{10}$

In this, the order of surd is 4.

iv. $\sqrt{39}$

In this, the order of surd is 2.

v. $\sqrt[3]{18}$

In this, the order of surd is 3

Q. 2. State which of the following are surds. Justify.

i. $\sqrt[3]{51}$ ii. $\sqrt[4]{51}$

iii. $\sqrt[5]{81}$ iv. $\sqrt{256}$

v. $\sqrt[3]{64}$ vi. $\sqrt{\frac{22}{7}}$

Answer : Surds are numbers left in root form ($\sqrt{}$) to express its exact value. It has an infinite number of non-recurring decimals. Therefore, surds are irrational numbers.

Therefore,

i. $\sqrt[3]{51}$

It is a surd \because it cannot be expressed as a rational number.

ii. $\sqrt[4]{51}$

It is a surd \because it cannot be expressed as a rational number.

iii. $\sqrt[5]{81} = \sqrt[5]{3^4}$

It is a surd \because it cannot be expressed as a rational number.

iv. $\sqrt{256} = \sqrt{16^2} = 16$

It is not a surd \because it is a rational number.

v. $\sqrt[3]{64} = \sqrt[3]{4^3} = 4$

It is not a surd \because it is a rational number.

vi. $\sqrt{\frac{22}{7}}$

It is a surd \because it cannot be expressed as a rational number.

Q. 3. Classify the given pair of surds into like surds and unlike surds.

i. $\sqrt{52}, 5\sqrt{13}$

ii. $\sqrt{68}, 5\sqrt{3}$

iii. $4\sqrt{18}, 7\sqrt{2}$

iv. $19\sqrt{12}, 6\sqrt{3}$

v. $5\sqrt{22}, 7\sqrt{33}$

vi. $5\sqrt{5}, \sqrt{75}$

Answer : Two or more surds are said to be similar or like surds if they have the same surd-factor.

And,

Two or more surds are said to be dissimilar or unlike when they are not similar.

Therefore,

i. $\sqrt{52}, 5\sqrt{13}$

$$\sqrt{52} = \sqrt{(2 \times 2 \times 13)} = 2\sqrt{13}$$

$$5\sqrt{13}$$

\because both surds have same surd-factor i.e., $\sqrt{13}$.

\therefore they are like surds.

ii. $\sqrt{68}, 5\sqrt{3}$

$$\sqrt{68} = \sqrt{(2 \times 2 \times 17)} = 2\sqrt{17}$$

$$5\sqrt{3}$$

\because both surds have different surd-factors $\sqrt{17}$ and $\sqrt{3}$.

\therefore they are unlike surds.

iii. $4\sqrt{18}, 7\sqrt{2}$

$$4\sqrt{18} = 4\sqrt{(2 \times 3 \times 3)} = 4 \times 3\sqrt{2} = 12\sqrt{2}$$

$$7\sqrt{2}$$

\because both surds have same surd-factor i.e., $\sqrt{2}$.

∴ they are like surds.

iv. $19\sqrt{12}$, $6\sqrt{3}$

$$19\sqrt{12} = 19\sqrt{(2 \times 2 \times 3)} = 19 \times 2\sqrt{3} = 38\sqrt{3}$$

$$6\sqrt{3}$$

∴ both surds have same surd-factor i.e., $\sqrt{3}$.

∴ they are like surds.

v. $5\sqrt{22}$, $7\sqrt{33}$

∴ both surds have different surd-factors $\sqrt{22}$ and $\sqrt{33}$.

∴ they are unlike surds.

vi. $5\sqrt{5}$, $\sqrt{75}$

$$5\sqrt{5}$$

$$\sqrt{75} = \sqrt{(5 \times 5 \times 3)} = 5\sqrt{3}$$

∴ both surds have different surd-factors $\sqrt{5}$ and $\sqrt{3}$.

∴ they are unlike surds.

Q. 4. Simplify the following surds.

i. $\sqrt{27}$

ii. $\sqrt{50}$

iii. $\sqrt{250}$

iv. $\sqrt{112}$

v. $\sqrt{168}$

Answer : i. $\sqrt{27} = \sqrt{3 \times 3 \times 3}$

$$\Rightarrow \sqrt{27} = \sqrt{3 \times (3)^2}$$

$$\Rightarrow \sqrt{27} = 3\sqrt{3}$$

ii. $\sqrt{50} = \sqrt{2 \times 5 \times 5}$

$$\Rightarrow \sqrt{50} = \sqrt{2 \times (5)^2}$$

$$\Rightarrow \sqrt{50} = 5\sqrt{2}$$

iii. $\sqrt{250} = \sqrt{2 \times 5 \times 5 \times 5}$

$$\Rightarrow \sqrt{250} = \sqrt{10 \times (5)^2}$$

$$\Rightarrow \sqrt{250} = 5\sqrt{10}$$

$$\text{iv. } \sqrt{112} = \sqrt{2 \times 2 \times 2 \times 2 \times 7}$$

$$\Rightarrow \sqrt{112} = \sqrt{(2)^2 \times (2)^2 \times 7}$$

$$\Rightarrow \sqrt{112} = 2 \times 2 \times \sqrt{7}$$

$$\Rightarrow \sqrt{112} = 4\sqrt{7}$$

$$\text{v. } \sqrt{168} = \sqrt{2 \times 2 \times 2 \times 3 \times 7}$$

$$\Rightarrow \sqrt{168} = \sqrt{(2)^2 \times 2 \times 3 \times 7}$$

$$\Rightarrow \sqrt{168} = 2 \times \sqrt{42}$$

$$\Rightarrow \sqrt{168} = 2\sqrt{42}$$

Q. 5. Compare the following pair of surds.

i. $7\sqrt{2}$, $5\sqrt{3}$

ii. $\sqrt{247}$, $\sqrt{274}$

iii. $2\sqrt{7}$, $\sqrt{28}$

iv. $5\sqrt{5}$, $7\sqrt{2}$

v. $4\sqrt{42}$, $9\sqrt{2}$

vi. $5\sqrt{3}$, 9

vii. 7, $2\sqrt{5}$

Answer : i. $7\sqrt{2}$, $5\sqrt{3}$

$$(7\sqrt{2})^2 = 7 \times 7 \times \sqrt{2} \times \sqrt{2}$$

$$\Rightarrow (7\sqrt{2})^2 = 49 \times 2$$

$$\Rightarrow (7\sqrt{2})^2 = 98$$

And

$$(5\sqrt{3})^2 = 5 \times 5 \times \sqrt{3} \times \sqrt{3}$$

$$\Rightarrow (5\sqrt{3})^2 = 25 \times 3$$

$$\Rightarrow (5\sqrt{3})^2 = 75$$

Clearly,

$$98 > 75$$

$$\therefore 7\sqrt{2} > 5\sqrt{3}$$

ii. $\sqrt{247}$, $\sqrt{274}$

$$(\sqrt{247})^2 = 247$$

And

$$(\sqrt{274})^2 = 274$$

Clearly,

$$247 < 274$$

$$\therefore \sqrt{247} < \sqrt{274}$$

iii. $2\sqrt{7}$, $\sqrt{28}$

$$(2\sqrt{7})^2 = 2 \times 2 \times \sqrt{7} \times \sqrt{7}$$

$$\Rightarrow (2\sqrt{7})^2 = 4 \times 7$$

$$\Rightarrow (2\sqrt{7})^2 = 28$$

And

$$(\sqrt{28})^2 = 28$$

Clearly,

$$28 = 28$$

$$\therefore 2\sqrt{7} = \sqrt{28}$$

iv. $5\sqrt{5}$, $7\sqrt{2}$

$$(5\sqrt{5})^2 = 5 \times 5 \times \sqrt{5} \times \sqrt{5}$$

$$\Rightarrow (5\sqrt{5})^2 = 25 \times 5$$

$$\Rightarrow (5\sqrt{5})^2 = 125$$

And

$$(7\sqrt{2})^2 = 7 \times 7 \times \sqrt{2} \times \sqrt{2}$$

$$\Rightarrow (7\sqrt{2})^2 = 49 \times 2$$

$$\Rightarrow (7\sqrt{2})^2 = 98$$

Clearly,

$$125 > 98$$

$$\therefore 5\sqrt{5} > 7\sqrt{2}$$

v. $4\sqrt{42}$, $9\sqrt{2}$

$$(4\sqrt{42})^2 = 4 \times 4 \times \sqrt{42} \times \sqrt{42}$$

$$\Rightarrow (4\sqrt{42})^2 = 16 \times 42$$

$$\Rightarrow (4\sqrt{42})^2 = 672$$

And

$$(9\sqrt{2})^2 = 9 \times 9 \times \sqrt{2} \times \sqrt{2}$$

$$\Rightarrow (9\sqrt{2})^2 = 81 \times 2$$

$$\Rightarrow (9\sqrt{2})^2 = 162$$

Clearly,

$$672 > 162$$

$$\therefore 4\sqrt{42} > 9\sqrt{2}$$

vi. $5\sqrt{3}$, 9

$$(5\sqrt{3})^2 = 5 \times 5 \times \sqrt{3} \times \sqrt{3}$$

$$\Rightarrow (5\sqrt{3})^2 = 25 \times 3$$

$$\Rightarrow (5\sqrt{3})^2 = 75$$

And

$$(9)^2 = 9 \times 9$$

$$\Rightarrow (9)^2 = 81$$

Clearly,

$$75 < 81$$

$$\therefore 5\sqrt{3} < 9$$

vii. $7, 2\sqrt{5}$

$$(2\sqrt{5})^2 = 2 \times 2 \times \sqrt{5} \times \sqrt{5}$$

$$\Rightarrow (2\sqrt{5})^2 = 4 \times 5$$

$$\Rightarrow (2\sqrt{5})^2 = 20$$

And

$$(7)^2 = 7 \times 7$$

$$\Rightarrow (7)^2 = 49$$

Clearly,

$$49 > 20$$

$$\therefore 7 > 2\sqrt{5}$$

Q. 6. Simplify.

i. $5\sqrt{3} + 8\sqrt{3}$

ii. $9\sqrt{5} - 4\sqrt{5} + \sqrt{125}$

iii. $7\sqrt{48} - \sqrt{27} - \sqrt{3}$

iv.

$$\sqrt{7} - \frac{3}{5}\sqrt{7} + 2\sqrt{7}$$

Answer : i. $5\sqrt{3} + 8\sqrt{3}$

$$5\sqrt{3} + 8\sqrt{3} = (5 + 8)\sqrt{3}$$

$$\Rightarrow 5\sqrt{3} + 8\sqrt{3} = 13\sqrt{3}$$

ii. $9\sqrt{5} - 4\sqrt{5} + \sqrt{125}$

$$9\sqrt{5} - 4\sqrt{5} + \sqrt{125} = 9\sqrt{5} - 4\sqrt{5} + \sqrt{(5 \times 5 \times 5)}$$

$$\Rightarrow 9\sqrt{5} - 4\sqrt{5} + \sqrt{125} = 9\sqrt{5} - 4\sqrt{5} + \sqrt{(5 \times 5 \times 5)}$$

$$\Rightarrow 9\sqrt{5} - 4\sqrt{5} + \sqrt{125} = 9\sqrt{5} - 4\sqrt{5} + 5\sqrt{5}$$

$$\Rightarrow 9\sqrt{5} - 4\sqrt{5} + \sqrt{125} = (9 - 4 + 5)\sqrt{5}$$

$$\Rightarrow 9\sqrt{5} - 4\sqrt{5} + \sqrt{125} = 10\sqrt{5}$$

iii. $7\sqrt{48} - \sqrt{27} - \sqrt{3}$

$$7\sqrt{48} - \sqrt{27} - \sqrt{3} = 7\sqrt{(2 \times 2 \times 2 \times 2 \times 3)} - \sqrt{(3 \times 3 \times 3)} - \sqrt{3}$$

$$\Rightarrow 7\sqrt{48} - \sqrt{27} - \sqrt{3} = 7 \times 4\sqrt{3} - 3\sqrt{3} - \sqrt{3}$$

$$\Rightarrow 7\sqrt{48} - \sqrt{27} - \sqrt{3} = 28\sqrt{3} - 3\sqrt{3} - \sqrt{3}$$

$$\Rightarrow 7\sqrt{48} - \sqrt{27} - \sqrt{3} = (28 - 3 - 1)\sqrt{3}$$

$$\Rightarrow 7\sqrt{48} - \sqrt{27} - \sqrt{3} = 24\sqrt{3}$$

iv. $\sqrt{7} - \frac{3}{5}\sqrt{7} + 2\sqrt{7}$

$$\sqrt{7} - \frac{3}{5}\sqrt{7} + 2\sqrt{7} = \left(1 - \frac{3}{5} + 2\right)\sqrt{7}$$

$$\Rightarrow \sqrt{7} - \frac{3}{5}\sqrt{7} + 2\sqrt{7} = \left(\frac{5 - 3 + 10}{5}\right)\sqrt{7}$$

$$\Rightarrow \sqrt{7} - \frac{3}{5}\sqrt{7} + 2\sqrt{7} = \frac{12}{5}\sqrt{7}$$

Q. 7. Multiply and write the answer in the simplest form.

i. $3\sqrt{12} \times \sqrt{18}$

ii. $3\sqrt{12} \times 7\sqrt{15}$

iii. $3\sqrt{8} \times \sqrt{5}$

iv. $5\sqrt{8} \times 2\sqrt{8}$

Answer : i. $3\sqrt{12} \times \sqrt{18}$

$$3\sqrt{12} \times \sqrt{18} = 3\sqrt{(2 \times 2 \times 3)} \times \sqrt{(2 \times 3 \times 3)}$$

$$\Rightarrow 3\sqrt{12} \times \sqrt{18} = 3 \times 2\sqrt{3} \times 3\sqrt{2}$$

$$\Rightarrow 3\sqrt{12} \times \sqrt{18} = 6\sqrt{3} \times 3\sqrt{2}$$

$$\Rightarrow 3\sqrt{12} \times \sqrt{18} = 18\sqrt{6}$$

ii. $3\sqrt{12} \times 7\sqrt{15}$

$$3\sqrt{12} \times 7\sqrt{15} = 3\sqrt{(2 \times 2 \times 3)} \times 7\sqrt{(3 \times 5)}$$

$$\Rightarrow 3\sqrt{12} \times 7\sqrt{15} = 3 \times 2\sqrt{3} \times 7\sqrt{(3 \times 5)}$$

$$\Rightarrow 3\sqrt{12} \times 7\sqrt{15} = 3 \times 2 \times 7 \times \sqrt{(3 \times 3 \times 5)}$$

$$\Rightarrow 3\sqrt{12} \times 7\sqrt{15} = 3 \times 2 \times 7 \times 3\sqrt{5}$$

$$\Rightarrow 3\sqrt{12} \times 7\sqrt{15} = 126\sqrt{5}$$

iii. $3\sqrt{8} \times \sqrt{5}$

$$3\sqrt{8} \times \sqrt{5} = 3\sqrt{(2 \times 2 \times 2)} \times \sqrt{5}$$

$$\Rightarrow 3\sqrt{8} \times \sqrt{5} = 3 \times 2\sqrt{2} \times \sqrt{5}$$

$$\Rightarrow 3\sqrt{8} \times \sqrt{5} = 3 \times 2 \times \sqrt{(2 \times 5)}$$

$$\Rightarrow 3\sqrt{8} \times \sqrt{5} = 6\sqrt{10}$$

iv. $5\sqrt{8} \times 2\sqrt{8}$

$$5\sqrt{8} \times 2\sqrt{8} = 5\sqrt{(2 \times 2 \times 2)} \times 2\sqrt{(2 \times 2 \times 2)}$$

$$\Rightarrow 5\sqrt{8} \times 2\sqrt{8} = 5 \times 2\sqrt{2} \times 2 \times 2\sqrt{2}$$

$$\Rightarrow 5\sqrt{8} \times 2\sqrt{8} = 5 \times 2 \times 2 \times 2 \times \sqrt{(2 \times 2)}$$

$$\Rightarrow 5\sqrt{8} \times 2\sqrt{8} = 5 \times 2 \times 2 \times 2 \times 2$$

$$\Rightarrow 5\sqrt{8} \times 2\sqrt{8} = 80$$

Q. 8. Divide, and write the answer in simplest form.

i. $\sqrt{98} \div \sqrt{2}$

ii. $\sqrt{125} \div \sqrt{50}$

iii. $\sqrt{54} \div \sqrt{27}$

iv. $\sqrt{310} \div \sqrt{5}$

Answer :

i. $\sqrt{98} \div \sqrt{2}$

$$\sqrt{98} \div \sqrt{2} = \sqrt{\frac{98}{2}}$$

$$\Rightarrow \sqrt{98} \div \sqrt{2} = \sqrt{49}$$

$$\Rightarrow \sqrt{98} \div \sqrt{2} = 7$$

ii. $\sqrt{125} \div \sqrt{50}$

$$\sqrt{125} \div \sqrt{50} = \sqrt{\frac{125}{50}}$$

$$\Rightarrow \sqrt{125} \div \sqrt{50} = \sqrt{\frac{5 \times 5 \times 5}{5 \times 2 \times 5}}$$

$$\Rightarrow \sqrt{125} \div \sqrt{50} = \sqrt{\frac{5}{2}}$$

iii. $\sqrt{54} \div \sqrt{27}$

$$\sqrt{54} \div \sqrt{27} = \sqrt{\frac{54}{27}}$$

$$\Rightarrow \sqrt{54} \div \sqrt{27} = \sqrt{2}$$

iv. $\sqrt{310} \div \sqrt{5}$

$$\sqrt{310} \div \sqrt{5} = \sqrt{\frac{310}{5}}$$

$$\Rightarrow \sqrt{310} \div \sqrt{5} = \sqrt{\frac{2 \times 5 \times 31}{5}}$$

$$\Rightarrow \sqrt{310} \div \sqrt{5} = \sqrt{62}$$

Q. 9. Rationalize the denominator.

i. $\frac{3}{\sqrt{5}}$ ii. $\frac{1}{\sqrt{14}}$

iii. $\frac{5}{\sqrt{7}}$ iv. $\frac{6}{9\sqrt{3}}$

v. $\frac{11}{\sqrt{3}}$

Answer : i. We know that $\sqrt{5} \times \sqrt{5} = 5$, \therefore to rationalize the denominator of $\frac{3}{\sqrt{5}}$ multiply both numerator and denominator by $\sqrt{5}$.

$$\frac{3}{\sqrt{5}} = \frac{3}{\sqrt{5}} \times \frac{\sqrt{5}}{\sqrt{5}} = \frac{3\sqrt{5}}{5}$$

$$\Rightarrow \frac{3}{\sqrt{5}} = \frac{3}{5} \sqrt{5}$$

ii. We know that $\sqrt{14} \times \sqrt{14} = 14$, \therefore to rationalize the denominator of $\frac{1}{\sqrt{14}}$ multiply both numerator and denominator by $\sqrt{14}$.

$$\frac{1}{\sqrt{14}} = \frac{1}{\sqrt{14}} \times \frac{\sqrt{14}}{\sqrt{14}} = \frac{\sqrt{14}}{14}$$

$$\Rightarrow \frac{1}{\sqrt{14}} = \frac{1}{14} \sqrt{14}$$

iii. We know that $\sqrt{7} \times \sqrt{7} = 7$, \therefore to rationalize the denominator of $\frac{5}{\sqrt{7}}$ multiply both numerator and denominator by $\sqrt{7}$.

$$\frac{5}{\sqrt{7}} = \frac{5}{\sqrt{7}} \times \frac{\sqrt{7}}{\sqrt{7}} = \frac{5\sqrt{7}}{7}$$

$$\Rightarrow \frac{5}{\sqrt{7}} = \frac{5}{7}\sqrt{7}$$

iv. We know that $\sqrt{3} \times \sqrt{3} = 3$, \therefore to rationalize the denominator of $\frac{6}{9\sqrt{3}}$ multiply both numerator and denominator by $\sqrt{3}$.

$$\frac{6}{9\sqrt{3}} = \frac{6}{9\sqrt{3}} \times \frac{\sqrt{3}}{\sqrt{3}} = \frac{6\sqrt{3}}{9 \times 3} = \frac{2\sqrt{3}}{9}$$

$$\Rightarrow \frac{6}{9\sqrt{3}} = \frac{2}{9}\sqrt{3}$$

v. We know that $\sqrt{3} \times \sqrt{3} = 3$, \therefore to rationalize the denominator of $\frac{11}{\sqrt{3}}$ multiply both numerator and denominator by $\sqrt{3}$.

$$\frac{11}{\sqrt{3}} = \frac{11}{\sqrt{3}} \times \frac{\sqrt{3}}{\sqrt{3}} = \frac{11\sqrt{3}}{3}$$

$$\Rightarrow \frac{11}{\sqrt{3}} = \frac{11}{3}\sqrt{3}$$

Practice set 2.4

Q. 1. Multiply

i. $\sqrt{3}(\sqrt{7} - \sqrt{3})$

ii. $(\sqrt{5} - \sqrt{7})\sqrt{2}$

iii. $(3\sqrt{2} - \sqrt{3})(4\sqrt{3} - \sqrt{2})$

Answer :

i. $\sqrt{3}(\sqrt{7} - \sqrt{3})$

$$= \sqrt{3} \times \sqrt{7} - \sqrt{3} \times \sqrt{3}$$

$$[\because \sqrt{a}(\sqrt{b} - \sqrt{c}) = \sqrt{a} \times \sqrt{b} - \sqrt{a} \times \sqrt{c}]$$

$$= \sqrt{21} - 3$$

$$\text{ii. } (\sqrt{5} - \sqrt{7})\sqrt{2}$$

$$= \sqrt{5} \times \sqrt{2} - \sqrt{7} \times \sqrt{2}$$

$$[\because \sqrt{a}(\sqrt{b} - \sqrt{c}) = \sqrt{a} \times \sqrt{b} - \sqrt{a} \times \sqrt{c}]$$

$$= \sqrt{10} - \sqrt{14}$$

$$\text{iii. } (3\sqrt{2} - \sqrt{3})(4\sqrt{3} - \sqrt{2})$$

$$= 3\sqrt{2}(4\sqrt{3} - \sqrt{2}) - \sqrt{3}(4\sqrt{3} - \sqrt{2})$$

$$= 3\sqrt{2} \times 4\sqrt{3} - 3\sqrt{2} \times \sqrt{2} - \sqrt{3} \times 4\sqrt{3} + \sqrt{3} \times \sqrt{2}$$

$$[\because \sqrt{a}(\sqrt{b} - \sqrt{c}) = \sqrt{a} \times \sqrt{b} - \sqrt{a} \times \sqrt{c}]$$

$$= 12\sqrt{6} - 3 \times 2 - 4 \times 3 + \sqrt{6}$$

$$= 12\sqrt{6} - 6 - 12 + \sqrt{6}$$

$$= 13\sqrt{6} - 18$$

Q. 2. Rationalize the denominator.

$$\text{i. } \frac{1}{\sqrt{7} + \sqrt{2}} \quad \text{ii. } \frac{3}{2\sqrt{5} - 3\sqrt{2}}$$

$$\text{iii. } \frac{4}{7 + 4\sqrt{3}} \quad \text{iv. } \frac{\sqrt{5} - \sqrt{3}}{\sqrt{5} + \sqrt{3}}$$

Answer : i. The rationalizing factor of $\sqrt{7} + \sqrt{2}$ is $\sqrt{7} - \sqrt{2}$. Therefore, multiply both numerator and denominator by $\sqrt{7} - \sqrt{2}$.

$$\frac{1}{\sqrt{7} + \sqrt{2}} = \frac{1}{\sqrt{7} + \sqrt{2}} \times \frac{\sqrt{7} - \sqrt{2}}{\sqrt{7} - \sqrt{2}}$$

$$\Rightarrow \frac{1}{\sqrt{7} + \sqrt{2}} = \frac{\sqrt{7} - \sqrt{2}}{(\sqrt{7} + \sqrt{2})(\sqrt{7} - \sqrt{2})}$$

$$\Rightarrow \frac{1}{\sqrt{7} + \sqrt{2}} = \frac{\sqrt{7} - \sqrt{2}}{(\sqrt{7})^2 - (\sqrt{2})^2}$$

$$[\because (a-b)(a+b) = a^2 - b^2]$$

$$\Rightarrow \frac{1}{\sqrt{7} + \sqrt{2}} = \frac{\sqrt{7} - \sqrt{2}}{7 - 2}$$

$$\Rightarrow \frac{1}{\sqrt{7} + \sqrt{2}} = \frac{\sqrt{7} - \sqrt{2}}{5}$$

ii. The rationalizing factor of $2\sqrt{5} - 3\sqrt{2}$ is $2\sqrt{5} + 3\sqrt{2}$. Therefore, multiply both numerator and denominator by $2\sqrt{5} + 3\sqrt{2}$.

$$\frac{3}{2\sqrt{5} - 3\sqrt{2}} = \frac{3}{2\sqrt{5} - 3\sqrt{2}} \times \frac{2\sqrt{5} + 3\sqrt{2}}{2\sqrt{5} + 3\sqrt{2}}$$

$$\Rightarrow \frac{3}{2\sqrt{5} - 3\sqrt{2}} = \frac{3(2\sqrt{5} + 3\sqrt{2})}{(2\sqrt{5} - 3\sqrt{2})(2\sqrt{5} + 3\sqrt{2})}$$

$$\Rightarrow \frac{3}{2\sqrt{5} - 3\sqrt{2}} = \frac{6\sqrt{5} + 9\sqrt{2}}{(2\sqrt{5})^2 - (3\sqrt{2})^2}$$

$$[\because (a-b)(a+b) = a^2 - b^2]$$

$$\Rightarrow \frac{3}{2\sqrt{5} - 3\sqrt{2}} = \frac{6\sqrt{5} + 9\sqrt{2}}{20 - 18}$$

$$\Rightarrow \frac{3}{2\sqrt{5} - 3\sqrt{2}} = \frac{6\sqrt{5} + 9\sqrt{2}}{2}$$

iii. The rationalizing factor of $7 + 4\sqrt{3}$ is $7 - 4\sqrt{3}$. Therefore, multiply both numerator and denominator by $7 - 4\sqrt{3}$.

$$\frac{4}{7 + 4\sqrt{3}} = \frac{4}{7 + 4\sqrt{3}} \times \frac{7 - 4\sqrt{3}}{7 - 4\sqrt{3}}$$

$$\Rightarrow \frac{4}{7 + 4\sqrt{3}} = \frac{4(7 - 4\sqrt{3})}{(7 + 4\sqrt{3})(7 - 4\sqrt{3})}$$

$$\Rightarrow \frac{4}{7 + 4\sqrt{3}} = \frac{28 - 16\sqrt{3}}{(7)^2 - (4\sqrt{3})^2}$$

$$[\because (a-b)(a+b) = a^2 - b^2]$$

$$\Rightarrow \frac{4}{7 + 4\sqrt{3}} = \frac{28 - 16\sqrt{3}}{49 - 48}$$

$$\Rightarrow \frac{4}{7 + 4\sqrt{3}} = 28 - 16\sqrt{3}$$

iv. The rationalizing factor of $\sqrt{5} + \sqrt{3}$ is $\sqrt{5} - \sqrt{3}$. Therefore, multiply both numerator and denominator by $\sqrt{5} - \sqrt{3}$.

$$\frac{\sqrt{5} - \sqrt{3}}{\sqrt{5} + \sqrt{3}} = \frac{\sqrt{5} - \sqrt{3}}{\sqrt{5} + \sqrt{3}} \times \frac{\sqrt{5} - \sqrt{3}}{\sqrt{5} - \sqrt{3}}$$

$$\Rightarrow \frac{\sqrt{5} - \sqrt{3}}{\sqrt{5} + \sqrt{3}} = \frac{(\sqrt{5} - \sqrt{3})(\sqrt{5} - \sqrt{3})}{(\sqrt{5} + \sqrt{3})(\sqrt{5} - \sqrt{3})}$$

$$\Rightarrow \frac{\sqrt{5} - \sqrt{3}}{\sqrt{5} + \sqrt{3}} = \frac{(\sqrt{5} - \sqrt{3})^2}{(\sqrt{5})^2 - (\sqrt{3})^2}$$

$$[\because (a-b)(a+b) = a^2 - b^2]$$

$$\Rightarrow \frac{\sqrt{5} - \sqrt{3}}{\sqrt{5} + \sqrt{3}} = \frac{(\sqrt{5})^2 + (\sqrt{3})^2 - 2(\sqrt{5})(\sqrt{3})}{(\sqrt{5})^2 - (\sqrt{3})^2}$$

$$[\because (a-b)^2 = a^2 + b^2 - 2ab]$$

$$\Rightarrow \frac{\sqrt{5} - \sqrt{3}}{\sqrt{5} + \sqrt{3}} = \frac{5 + 3 - 2\sqrt{15}}{5 - 3}$$

$$\Rightarrow \frac{\sqrt{5} - \sqrt{3}}{\sqrt{5} + \sqrt{3}} = \frac{8 - 2\sqrt{15}}{2}$$

$$\Rightarrow \frac{\sqrt{5} - \sqrt{3}}{\sqrt{5} + \sqrt{3}} = \frac{2[4 - \sqrt{15}]}{2}$$

$$\Rightarrow \frac{\sqrt{5} - \sqrt{3}}{\sqrt{5} + \sqrt{3}} = 4 - \sqrt{15}$$

Practice set 2.5

Q. 1. Find the value.

(i) $|15 - 2|$

(ii) $|4 - 9|$

(iii) $|7| \times |-4|$

Answer : Absolute value describes the distance of a number on the number line from 0 without considering which direction from zero the number lies. The absolute value of a number is never negative.

Therefore,

i. $|15 - 2| = |13| = 13$

ii. $|4 - 9| = |-5| = 5$

iii. $|7| \times |-4| = 7 \times 4 = 28$

Q. 2. Solve.

i. $|3x - 5| = 1$

ii. $|7 - 2x| = 5$

iii. $\left| \frac{8 - x}{2} \right| = 5$

iv. $\left| 5 + \frac{x}{4} \right| = 5$

Answer : i. $|3x - 5| = 1$

$$\Rightarrow 3x - 5 = 1 \text{ or } 3x - 5 = -1$$

$$\Rightarrow 3x = 1 + 5 \text{ or } 3x = -1 + 5$$

$$\Rightarrow 3x = 6 \text{ or } 3x = 4$$

$$\Rightarrow x = \frac{6}{3} \text{ or } x = \frac{4}{3}$$

$$\Rightarrow x = 2 \text{ or } x = \frac{4}{3}$$

$$\text{ii. } |7 - 2x| = 5$$

$$\Rightarrow 7 - 2x = 5 \text{ or } 7 - 2x = -5$$

$$\Rightarrow 2x = 7 - 5 \text{ or } 2x = 7 + 5$$

$$\Rightarrow 2x = 2 \text{ or } 2x = 12$$

$$\Rightarrow x = 1 \text{ or } x = \frac{12}{2}$$

$$\Rightarrow x = 1 \text{ or } x = 6$$

$$\text{iii. } \left| \frac{8-x}{2} \right| = 5$$

$$\Rightarrow \frac{8-x}{2} = 5 \text{ or } \frac{8-x}{2} = -5$$

$$\Rightarrow 8 - x = 2 \times 5 \text{ or } 8 - x = 2 \times -5$$

$$\Rightarrow 8 - x = 10 \text{ or } 8 - x = -10$$

$$\Rightarrow x = 8 - 10 \text{ or } x = 8 + 10$$

$$\Rightarrow x = -2 \text{ or } x = 18$$

$$\text{iv. } \left| 5 + \frac{x}{4} \right| = 5$$

$$\Rightarrow 5 + \frac{x}{4} = 5 \text{ or } 5 + \frac{x}{4} = -5$$

$$\Rightarrow \frac{20+x}{4} = 5 \text{ or } \frac{20+x}{4} = -5$$

$$\Rightarrow 20 + x = 4 \times 5 \text{ or } 20 + x = 4 \times -5$$

$$\Rightarrow 20 + x = 20 \text{ or } 20 + x = -20$$

$$\Rightarrow x = 20 - 20 \text{ or } x = -20 - 20$$

$$\Rightarrow x = 0 \text{ or } x = -40$$

Problem set 2

Q. 1 A. Choose the correct alternative answer for the questions given below.

i. Which one of the following is an irrational number?

A. $\sqrt{16/25}$

B. $\sqrt{5}$

C. $3/9$

D. $\sqrt{196}$

Answer : An irrational number is a number that cannot be expressed as a fraction $\frac{p}{q}$ for any integers p and q and $q \neq 0$.

$\sqrt{\frac{16}{25}} = \frac{4}{5}$ since it can be written as $\frac{p}{q}$, it is a rational number.

$\frac{3}{9} = \frac{1}{3}$ since it can be written as $\frac{p}{q}$, it is a rational number.

$\sqrt{196} = 14 = \frac{14}{1}$ since it can be written as $\frac{p}{q}$, it is a rational number.

Since $\sqrt{5}$ cannot be written as $\frac{p}{q}$ it is an irrational number

Therefore $\sqrt{5}$ is an irrational number.

Q. 1 B. Which of the following is an irrational number?

A. 0.17

B. $1.\overline{513}$

C. $0.27\overline{46}$

D. 0.101001000....

Answer : An irrational number is a number that cannot be expressed as a fraction $\frac{p}{q}$ for any integers p and q and $q \neq 0$.

$$0.17 = \frac{17}{100}.$$

Since it can be written as $\frac{p}{q}$,

it is a rational number.

$1.\overline{513}$ is a rational number because it is a non-terminating but repeating decimal.

$0.27\overline{46}$ is a rational number because it is a non-terminating but repeating decimal.

0.101001000.... is an irrational number because it is a non-terminating and non-repeating decimal.

Therefore, 0.101001000.... is an irrational number.

Q. 1 C. Decimal expansion of which of the following is non-terminating recurring?

- A. $\frac{2}{5}$
- B. $\frac{3}{16}$
- C. $\frac{3}{11}$
- D. $\frac{137}{25}$

Answer : A non-terminating recurring decimal representation means that the number will have an infinite number of digits to the right of the decimal point and those digits will repeat themselves.

$$\frac{2}{5} = 0.4$$

∴ it does not have an infinite number of digits to the right of the decimal point ∴ it is not a non-terminating recurring decimal.

$$\frac{3}{16} = 0.1875$$

∴ it does not have an infinite number of digits to the right of the decimal point ∴ it is not a non-terminating recurring decimal.

$$\frac{3}{11} = 0.2727 \dots = 0.\overline{27}$$

∴ it has an infinite number of digits to the right of the decimal point which are repeating themselves ∴ it is a non-terminating recurring decimal.

$$\frac{137}{25} = 5.48$$

∴ it does not have an infinite number of digits to the right of the decimal point ∴ it is not a non-terminating recurring decimal.

Therefore, $\frac{3}{11}$ is a non-terminating recurring decimal.

Q. 1 D. Every point on the number line represent, which of the following numbers?

- A. Natural numbers**
- B. Irrational numbers**
- C. Rational numbers**
- D. Real numbers.**

Answer : Every point of a number line is assumed to correspond to a real number, and every real number to a point. Therefore, Every point on the number line represent a real number.

Q. 1 E. The number 0.4 in p/q form is

- A. 4/9**
- B. 40/9**
- C. 3.6/9**
- D. 36/9**

Answer :

$$0.4 = \frac{4}{10}$$

∴ the denominator of all the above options is 9 ∴ we multiply both numerator and denominator by 0.9 as $10 \times 0.9 = 9$

$$\Rightarrow 0.4 = \frac{4 \times 0.9}{10 \times 0.9}$$

$$\Rightarrow 0.4 = \frac{3.6}{9}$$

Q. 1 F. What is \sqrt{n} , if n is not a perfect square number?

- A. Natural number
- B. Rational number
- C. Irrational number
- D. Options A, B, C all are correct.

Answer : If n is not a perfect square number, then \sqrt{n} cannot be expressed as ratio of a and b where a and b are integers and $b \neq 0$

Therefore, \sqrt{n} is an Irrational number

Q. 1 G. Which of the following is not a surd?

- A. $\sqrt{7}$
- B. $\sqrt[3]{17}$
- C. $\sqrt[3]{64}$
- D. $\sqrt{193}$

Answer :

$$\sqrt[3]{64} = \sqrt[3]{4 \times 4 \times 4}$$

$$\Rightarrow \sqrt[3]{64} = \sqrt[3]{4^3}$$

$$\Rightarrow \sqrt[3]{64} = 4$$

Which is a rational number

Therefore, $\sqrt[3]{64}$ is not a surd.

Q. 1 H. What is the order of the surd $\sqrt[3]{\sqrt{5}}$?

- A. 3
- B. 2
- C. 6
- D. 5

Answer :

$$\sqrt[3]{\sqrt{5}} = \sqrt[3]{(5)^{\frac{1}{2}}}$$

$$\Rightarrow \sqrt[3]{\sqrt{5}} = \sqrt[3 \times 2]{5}$$

$$\Rightarrow \sqrt[3]{\sqrt{5}} = \sqrt[6]{5}$$

Therefore, the order of the surd $\sqrt[3]{\sqrt{5}}$ is 6.

Q. 1 I. Which one is the conjugate pair of $2\sqrt{5} + \sqrt{3}$?

- A. $-2\sqrt{5} + \sqrt{3}$**
- B. $-2\sqrt{5} - \sqrt{3}$**
- C. $2\sqrt{3} + \sqrt{5}$**
- D. $\sqrt{3} + 2\sqrt{5}$**

Answer : A math conjugate is formed by changing the sign between two terms in a binomial. For instance, the conjugate of $x + y$ is $x - y$.

Now,

$$2\sqrt{5} + \sqrt{3} = \sqrt{3} + 2\sqrt{5}$$

$$\text{Its conjugate pair} = \sqrt{3} - 2\sqrt{5} = -2\sqrt{5} + \sqrt{3}$$

$$\therefore \text{The conjugate pair of } 2\sqrt{5} + \sqrt{3} = -2\sqrt{5} + \sqrt{3}$$

Q. 1 J. The value of $|12 - (13 + 7) \times 4|$ is

- A. -68**
- B. 68**
- C. -32**
- D. 32**

Answer : $|12 - (13 + 7) \times 4| = |12 - 20 \times 4|$ (Solving it according to BODMAS)

$$\Rightarrow |12 - (13 + 7) \times 4| = |12 - 80|$$

$$\Rightarrow |12 - (13 + 7) \times 4| = |-68|$$

$$\Rightarrow |12 - (13 + 7) \times 4| = 68$$

Q. 2. Write the following numbers in p/q form.

i. 0.555 ii. $29.\overline{568}$

iii. $9.\overline{315}$ 315 ... iv. $357.\overline{417417}$...

v. $30.\overline{219}$

Answer : i.

$$0.555 = \frac{555}{1000}$$

$$\Rightarrow 0.555 = \frac{111}{200}$$

ii. Let

$$x = 29.\overline{568} = 29.568568 \dots$$

$$\Rightarrow 1000x = 29568.568568 \dots$$

Now,

$$1000x - x = 29568.568568 - 29.568568$$

$$\Rightarrow 999x = 29539.0$$

$$\Rightarrow x = \frac{29539}{999}$$

$$\Rightarrow 29.\overline{568} = \frac{29539}{999}$$

iii. Let $x = 9.315315 \dots$

$$\Rightarrow 1000x = 9315.315315 \dots$$

Now,

$$1000x - x = 9315.315315 - 9.315315$$

$$\Rightarrow 999x = 9306.0$$

$$\Rightarrow x = \frac{9306}{999}$$

$$\Rightarrow 9.315315 = \frac{29539}{999}$$

iv. Let $x = 357.417417\ldots$

$$\Rightarrow 1000x = 357417.417417\ldots$$

Now,

$$1000x - x = 357417.417417 - 357.417417$$

$$\Rightarrow 999x = 357060.0$$

$$\Rightarrow x = \frac{357060}{999}$$

$$\Rightarrow 357.417417\ldots = \frac{357060}{999}$$

v. Let $x = 30.\overline{219} = 30.219219 \ldots \ldots$

$$\Rightarrow 1000x = 30219.219219\ldots$$

Now,

$$1000x - x = 30219.219219 - 30.219219$$

$$\Rightarrow 999x = 30189.0$$

$$\Rightarrow x = \frac{30189}{999}$$

$$\Rightarrow 30.\overline{219} = \frac{30189}{999}$$

Q. 3. Write the following numbers in its decimal form.

i. $-\frac{5}{7}$

ii. $\frac{9}{11}$

iii. $\sqrt{5}$

iv. $\frac{121}{13}$

v. $\frac{29}{8}$

Answer : i.

$$\frac{-5}{7} = -0.714287142871428 \dots \dots$$

$$\Rightarrow \frac{-5}{7} = -0.\overline{71428}$$

ii.

$$\frac{9}{11} = 0.818181 \dots \dots$$

$$\Rightarrow \frac{9}{11} = 0.\overline{81}$$

iii. $\sqrt{5} = 2.236067977 \dots \dots$

iv.

$$\frac{121}{13} = 9.307692307692307692 \dots \dots$$

$$\Rightarrow \frac{121}{13} = 9.\overline{307692}$$

v.

$$\frac{29}{8} = 3.625$$

Q. 4. Show that $5 + \sqrt{7}$ is an irrational number.

Answer : Let us assume that $5 + \sqrt{7}$ is a rational number

$$\therefore 5 + \sqrt{7} = \frac{a}{b}$$

where, $b \neq 0$ and a, b are integers

$$\Rightarrow \sqrt{7} = \frac{a}{b} - 5$$

$$\Rightarrow \sqrt{7} = \frac{a - 5b}{b}$$

$\therefore a, b$ are integers $\therefore a - 5b$ and b are also integers

$$\Rightarrow \frac{a-5b}{b} \text{ is rational which cannot be possible } \therefore \frac{a-5b}{b} = \sqrt{7} \text{ which is an irrational number}$$

\therefore it is contradicting our assumption \therefore the assumption was wrong

Hence, $5 + \sqrt{7}$ is an irrational number

Q. 5. Write the following surds in simplest form.

i. $\frac{3}{4}\sqrt{8}$ ii. $-\frac{5}{9}\sqrt{45}$

Answer : i.

$$\frac{3}{4}\sqrt{8} = \frac{3}{4}\sqrt{2 \times 2 \times 2}$$

$$\Rightarrow \frac{3}{4}\sqrt{8} = \frac{3}{4} \times 2\sqrt{2}$$

$$\Rightarrow \frac{3}{4}\sqrt{8} = \frac{3}{2}\sqrt{2}$$

ii.

$$-\frac{5}{9}\sqrt{45} = -\frac{5}{9}\sqrt{3 \times 3 \times 5}$$

$$\Rightarrow -\frac{5}{9}\sqrt{45} = -\frac{5}{9} \times 3\sqrt{5}$$

$$\Rightarrow -\frac{5}{9}\sqrt{45} = -\frac{5}{3}\sqrt{5}$$

Q. 6. Write the simplest form of rationalizing factor for the given surds.

i. $\sqrt{32}$ ii. $\sqrt{50}$

iii. $\sqrt{27}$ iv. $\frac{3}{5}\sqrt{10}$

v. $3\sqrt{72}$ vi. $4\sqrt{11}$

Answer : i. $\sqrt{32}$

$$\sqrt{32} = \sqrt{2 \times 2 \times 2 \times 2 \times 2}$$

$$\Rightarrow \sqrt{32} = 2 \times 2 \times \sqrt{2}$$

$$\Rightarrow \sqrt{32} = 4\sqrt{2}$$

\therefore Its rationalizing factor = $\sqrt{2}$

ii. $\sqrt{50}$

$$\sqrt{50} = \sqrt{2 \times 5 \times 5}$$

$$\Rightarrow \sqrt{50} = 5\sqrt{2}$$

\therefore Its rationalizing factor = $\sqrt{2}$

iii. $\sqrt{27}$

$$\sqrt{27} = \sqrt{3 \times 3 \times 3}$$

$$\Rightarrow \sqrt{27} = 3\sqrt{3}$$

\therefore Its rationalizing factor = $\sqrt{3}$

iv. $\frac{3}{5}\sqrt{10}$

$\therefore \sqrt{10}$ cannot be further simplified

\therefore Its rationalizing factor = $\sqrt{10}$

v. $3\sqrt{72}$

$$3\sqrt{72} = \sqrt{2 \times 2 \times 2 \times 3 \times 3}$$

$$\Rightarrow 3\sqrt{72} = 2 \times 3 \times \sqrt{2}$$

$$\Rightarrow 3\sqrt{72} = 6\sqrt{2}$$

\therefore Its rationalizing factor = $\sqrt{2}$

vi. $4\sqrt{11}$

$\therefore \sqrt{11}$ cannot be further simplified

\therefore Its rationalizing factor = $\sqrt{11}$

Q. 7. Simplify.

i. $\frac{4}{7}\sqrt{147} + \frac{3}{8}\sqrt{192} - \frac{1}{5}\sqrt{75}$

ii. $5\sqrt{3} + 2\sqrt{27} + \frac{1}{\sqrt{3}}$

iii. $\sqrt{216} - 5\sqrt{6} + \sqrt{294} - \frac{3}{\sqrt{6}}$

iv. $4\sqrt{12} - \sqrt{75} - 7\sqrt{48}$

v. $2\sqrt{48} - \sqrt{75} - \frac{1}{\sqrt{3}}$

Answer : i.

$$\frac{4}{7}\sqrt{147} + \frac{3}{8}\sqrt{192} - \frac{1}{5}\sqrt{75}$$

$$= \frac{4}{7}\sqrt{3 \times 7 \times 7} + \frac{3}{8}\sqrt{2 \times 2 \times 2 \times 2 \times 2 \times 3} - \frac{1}{5}\sqrt{3 \times 5 \times 5}$$

$$= \frac{4}{7} \times 7\sqrt{3} + \frac{3}{8} \times 2 \times 2 \times 2 \times \sqrt{3} - \frac{1}{5} \times 5\sqrt{3}$$

$$= \frac{4}{7} \times 7\sqrt{3} + \frac{3}{8} \times 8\sqrt{3} - \frac{1}{5} \times 5\sqrt{3}$$

$$= 4\sqrt{3} + 3\sqrt{3} - \sqrt{3}$$

$$= 7\sqrt{3} - \sqrt{3}$$

$$= 6\sqrt{3}$$

ii.

$$5\sqrt{3} + 2\sqrt{27} + \frac{1}{\sqrt{3}}$$

$$= 5\sqrt{3} + 2\sqrt{3 \times 3 \times 3} - \frac{1}{\sqrt{3}} \times \frac{\sqrt{3}}{\sqrt{3}}$$

$$= 5\sqrt{3} + 2 \times 3\sqrt{3} - \frac{\sqrt{3}}{3}$$

$$= \left(5 + 6 - \frac{1}{3}\right)\sqrt{3}$$

$$= \left(\frac{15 + 18 - 1}{3}\right)\sqrt{3}$$

$$= \frac{32}{3}\sqrt{3}$$

iii.

$$\sqrt{216} - 5\sqrt{6} + 2\sqrt{294} - \frac{3}{\sqrt{6}}$$

$$= \sqrt{6 \times 6 \times 6} - 5\sqrt{6} + 2\sqrt{2 \times 3 \times 7 \times 7} - \frac{3}{\sqrt{6}} \times \frac{\sqrt{6}}{\sqrt{6}}$$

$$= 6\sqrt{6} - 5\sqrt{6} + 2 \times 7\sqrt{6} - \frac{3\sqrt{6}}{6}$$

$$= 6\sqrt{6} - 5\sqrt{6} + 14\sqrt{6} - \frac{\sqrt{6}}{2}$$

$$= \left(6 - 5 + 14 - \frac{1}{2}\right)\sqrt{6}$$

$$= \left(\frac{12 - 10 + 28 - 1}{2}\right)\sqrt{6}$$

$$= \frac{29}{2}\sqrt{6}$$

iv.

$$4\sqrt{12} - \sqrt{75} - 7\sqrt{48}$$

$$= 4\sqrt{2 \times 2 \times 3} - \sqrt{3 \times 5 \times 5} - 7\sqrt{2 \times 2 \times 2 \times 2 \times 3}$$

$$= 4 \times 2\sqrt{3} - 5\sqrt{3} - 7 \times 4\sqrt{3}$$

$$= 8\sqrt{3} - 5\sqrt{3} - 28\sqrt{3}$$

$$= (8 - 5 - 28)\sqrt{3}$$

$$= (8 - 5 - 28)\sqrt{3}$$

$$= -25\sqrt{3}$$

v.

$$2\sqrt{48} - \sqrt{75} - \frac{1}{\sqrt{3}}$$

$$= 2\sqrt{2 \times 2 \times 2 \times 2 \times 3} - \sqrt{3 \times 5 \times 5} - \frac{1}{\sqrt{3}} \times \frac{\sqrt{3}}{\sqrt{3}}$$

$$= 2 \times 4\sqrt{3} - 5\sqrt{3} - \frac{\sqrt{3}}{3}$$

$$= 8\sqrt{3} - 5\sqrt{3} - \frac{\sqrt{3}}{3}$$

$$= (8 - 5 - \frac{1}{3})\sqrt{3}$$

$$= \left(\frac{24 - 15 - 1}{3}\right)\sqrt{3}$$

$$= \frac{8}{3}\sqrt{3}$$

Q. 8. Rationalize the denominator.

$$\text{i. } \frac{1}{\sqrt{5}} \quad \text{ii. } \frac{2}{3\sqrt{7}}$$

$$\text{iii. } \frac{1}{\sqrt{3}-\sqrt{2}} \quad \text{iv. } \frac{1}{3\sqrt{5}+2\sqrt{2}}$$

$$\text{v. } \frac{12}{4\sqrt{3}-\sqrt{2}}$$

Answer : i.

$$\frac{1}{\sqrt{5}} = \frac{1}{\sqrt{5}} \times \frac{\sqrt{5}}{\sqrt{5}}$$

$$\Rightarrow \frac{1}{\sqrt{5}} = \frac{\sqrt{5}}{5}$$

$$\Rightarrow \frac{1}{\sqrt{5}} = \frac{1}{5} \sqrt{5}$$

ii.

$$\frac{2}{3\sqrt{7}} = \frac{2}{3\sqrt{7}} \times \frac{3\sqrt{7}}{3\sqrt{7}}$$

$$\Rightarrow \frac{2}{3\sqrt{7}} = \frac{6\sqrt{7}}{(3\sqrt{7})^2}$$

$$\Rightarrow \frac{2}{3\sqrt{7}} = \frac{6\sqrt{7}}{63}$$

$$\Rightarrow \frac{2}{3\sqrt{7}} = \frac{6}{63} \sqrt{7}$$

$$\Rightarrow \frac{2}{3\sqrt{7}} = \frac{2}{21} \sqrt{7}$$

iii.

$$\frac{1}{\sqrt{3}-\sqrt{2}} = \frac{1}{\sqrt{3}-\sqrt{2}} \times \frac{\sqrt{3}+\sqrt{2}}{\sqrt{3}+\sqrt{2}}$$

$$\Rightarrow \frac{1}{\sqrt{3}-\sqrt{2}} = \frac{\sqrt{3}+\sqrt{2}}{(\sqrt{3}-\sqrt{2})(\sqrt{3}+\sqrt{2})}$$

$$\Rightarrow \frac{1}{\sqrt{3}-\sqrt{2}} = \frac{\sqrt{3}+\sqrt{2}}{(\sqrt{3})^2 - (\sqrt{2})^2}$$

$$\Rightarrow \frac{1}{\sqrt{3}-\sqrt{2}} = \sqrt{3} + \sqrt{2}$$

iv.

$$\frac{1}{3\sqrt{5}+2\sqrt{2}} = \frac{1}{3\sqrt{5}+2\sqrt{2}} \times \frac{3\sqrt{5}-2\sqrt{2}}{3\sqrt{5}-2\sqrt{2}}$$

$$\Rightarrow \frac{1}{3\sqrt{5}+2\sqrt{2}} = \frac{3\sqrt{5}-2\sqrt{2}}{(3\sqrt{5})^2 - (2\sqrt{2})^2}$$

$$\Rightarrow \frac{1}{3\sqrt{5}+2\sqrt{2}} = \frac{3\sqrt{5}-2\sqrt{2}}{45-8}$$

$$\Rightarrow \frac{1}{3\sqrt{5}+2\sqrt{2}} = \frac{3\sqrt{5}-2\sqrt{2}}{37}$$

v.

$$\begin{aligned}
& \frac{12}{4\sqrt{3}-\sqrt{2}} \\
& \frac{12}{4\sqrt{3}-\sqrt{2}} \times \frac{4\sqrt{3}+\sqrt{2}}{4\sqrt{3}+\sqrt{2}} \\
& = \frac{12(4\sqrt{3}+\sqrt{2})}{(4\sqrt{3})^2-(\sqrt{2})^2} \\
& = \frac{12(4\sqrt{3}+\sqrt{2})}{48-2} \\
& = \frac{12(4\sqrt{3}+\sqrt{2})}{46}
\end{aligned}$$