and
$$t=6$$
 seconds.
 $g(t)=2t^2+3t$
 $a=3$ $b=6$
 $g(3)=2(3)^2+3(3)$ $g(6)=2(6)^2+3(6)$
 $g(3)=27$ $g(6)=90$

(i) Find the instantaneous velocities at t=3

instantaneous vate of change at t=3 (Crelocity)

$$= 9^{1}(3)$$

= $4(3)+3 = 12+3$

=15 m/s instantaneous Gate of change) velocity at to

2) A camera is accidentally knocked off an =27 m/s Send Your Questions & Answer Keys to our email id - padasalai retegnail.com
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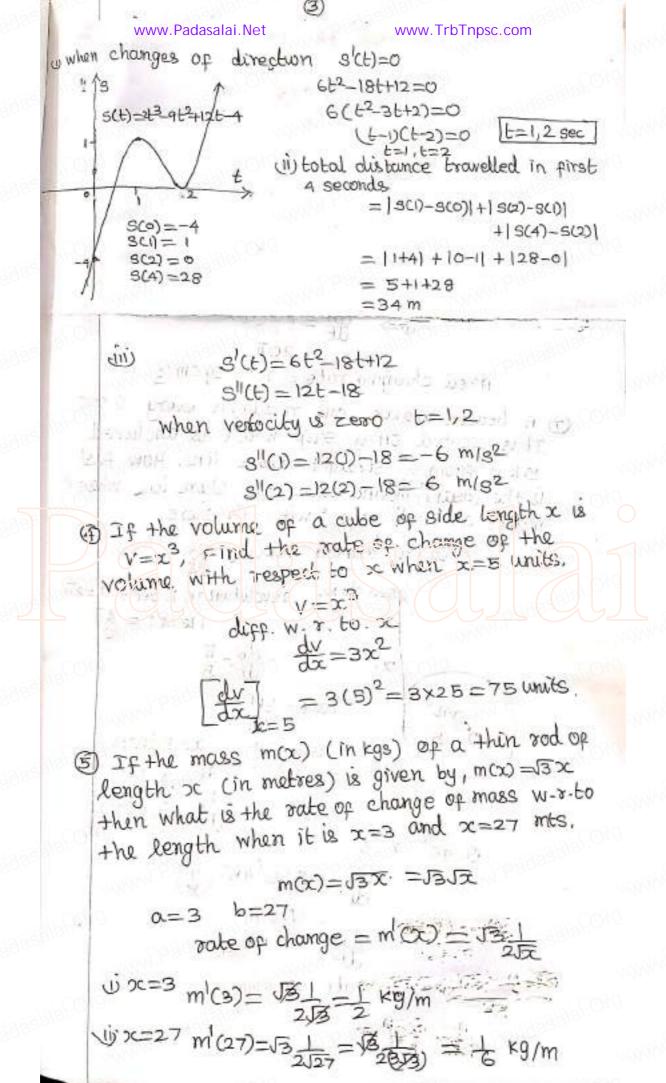
www.Padasalai.Net a distance of S=16t2 in www.etch.Thosc.com is now long does the camera fall before it hits the ground ii what is the average velocity with which the camera palls during the last 2 seconds? (iii) what is the instantaneous velocity of the camera when it hits the ground, S(t)=16t2 when hits the ground 3=400 1662=400 400 pt. $L^2 = 400 - 100 = 25$ Girowia t2=25 ヒニエラ t=5 sec. average velocity in last two seconds t=3 , t=5 average velocity = S(5)-S(3) $= \frac{16(5^2) - 16(3)^2}{2} + \frac{8}{6}(25-9)$ =8x16 =128 Pt/s Intantaneous velocity = S(t) = 16(2t)when it huls on the ground . t=5 s(5)=32(5)= 160 fts 3 A particle moves along a line according to the LOW 3(t) = 2+3-9+2+12+-4, where E>0 i) At what time the particle changes direction? (ii) Find the total distance travelled by the particle in the pirst. 4 seconds. (iii) Find the particles acceleration each time

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s/(t)=6t2-18t+12

S(t)= 2t3-9t2+12t-4

the velocity is zero.



www.Padasalaij.Net ped into owwpornatups.Comesing replaced into owwpornatups.Comesing replaced in the radius tof the inthe concentric circles. The radius tof the outer ripple is increasing at 2 cm/s. What outer ripple is increasing at 2 cm/s. What the radius is 5cm find the rate of changing of the total area of the disturbed water?

Let A be the area at time to

Area of the circle A = Tr2

diff w-r to t

diff = 1127 dir

when r=5 dir =2

Area changing rate = 2017 Sqcm/S

This located on a ship which is anchored skin from a straight share line. How fast is the beam moving along the share line when it makes an angle of 45° with the share.

Let the ungillar velocity de

Sea show. The volution in 10 sec = $1=2\pi$ 1 sec = $\frac{3}{10}$ 2 to $1=\frac{3}{10}$ 3 to $1=\frac{3}{10}$ 3 to $1=\frac{3}{10}$ 4 to $1=\frac{3}{10}$ 4 to $1=\frac{3}{10}$ 4 to $1=\frac{3}{10}$ 4 to $1=\frac{3}{10}$ 5 to $1=\frac{3}{10}$ 6 to $1=\frac{3}{10}$ 7 to $1=\frac{3}{10}$ 6 to $1=\frac{3}{10}$ 7 to $1=\frac{3}{10}$ 8 to $1=\frac{3}{10}$ 9 to $1=\frac{3}{10}$ 10 to $1=\frac{3}{10}$ 10 to $1=\frac{3}{10}$ 11 to $1=\frac{3}{10}$ 12 to $1=\frac{3}{10}$ 12 to $1=\frac{3}{10}$ 13 to $1=\frac{3}{10}$ 14 to $1=\frac{3}{10}$ 15 to $1=\frac{3}{10}$ 16 to $1=\frac{3}{10}$ 17 to $1=\frac{3}{10}$ 18 to $1=\frac{3}{10}$ 19 to $1=\frac{3}{10}$ 10 to $1=\frac{3}{10}$ 10 to $1=\frac{3}{10}$ 10 to $1=\frac{3}{10}$ 10 to $1=\frac{3}{10}$ 11 to $1=\frac{3}{10}$ 12 to $1=\frac{3}{10}$ 13 to $1=\frac{3}{10}$ 14 to $1=\frac{3}{10}$ 15 to $1=\frac{3}{10}$ 16 to $1=\frac{3}{10}$ 17 to $1=\frac{3}{10}$ 18 to $1=\frac{3}{10}$ 19 to $1=\frac{3}{10}$ 10 to $1=\frac{3}{10}$ 10

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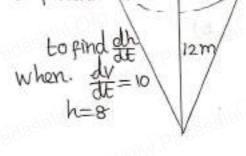
@ A conical water tank with vertex down of 12 metres height has a radius of 5 metres at the top. If water flows into the tank at a rate 10 - cubic m/min, how fast is the depth of the water increases when the water is 8 metres deep?

Let v be the volume of tank at any time t

8=5 h=12

 $\frac{r}{h} = \frac{5}{12}$

7=5h



volume of cone V=== 1782h

V==== 17 25h2h

 $V = \frac{2517}{3\times144} h^3$

diff. W- & to tat

clv = 2511 23/2 dh.

G. Kasthikeyari 10 = 2517 x8 x8 dh.

PG. T. GGHSS

Thirumak kottafox9 = dh.

Thiruwarur Di 2511 x4 dt.

11

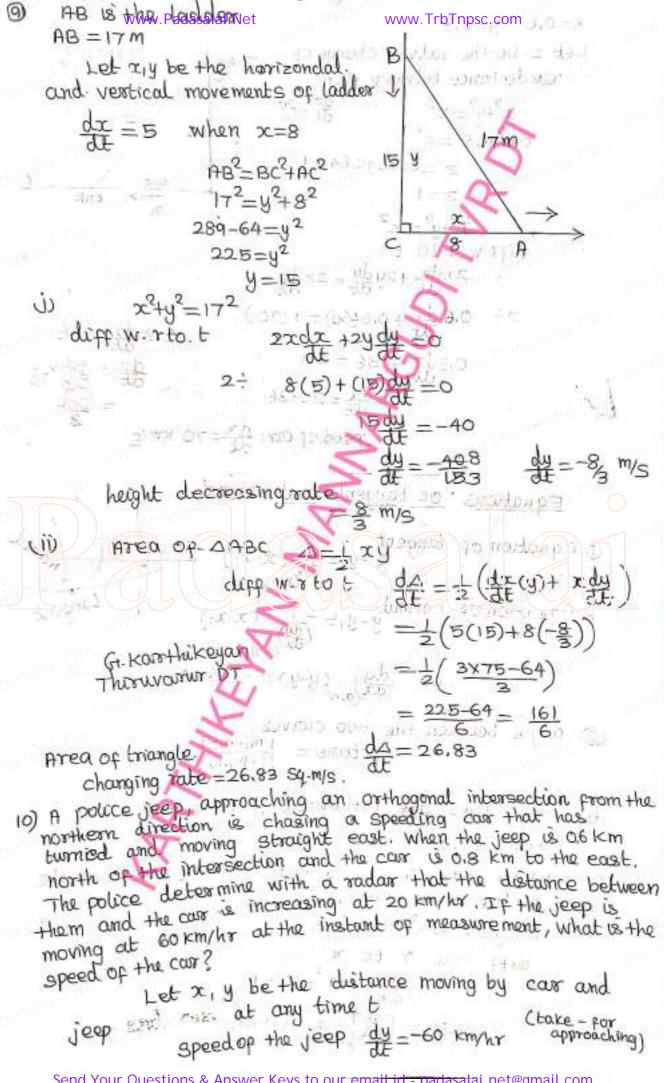
 $\frac{dh}{dt} = \frac{90}{10011} \qquad \frac{dh}{dt} = \frac{9}{1011} \text{ m/min}$

depth increase rate 10th m/min.

9) A ladder 17 metre long is leaning against thewall, The base of the ladder is pulled away from the wall at a rate of 5 m/s. When the base of the ladder is 8 m. from the wall,

W HOW fast is the top of the ladder moving down

(ii) At what rate, the area of the triangle formed by the Ladder, wall, and the floor, is changing?



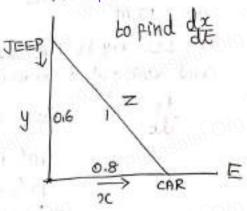
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2=0,6 4=0.8

Let z be the rate of change of distance between them.

$$x^2+y^2=z^2$$
 $dz=20$

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Equations of langent and Normal

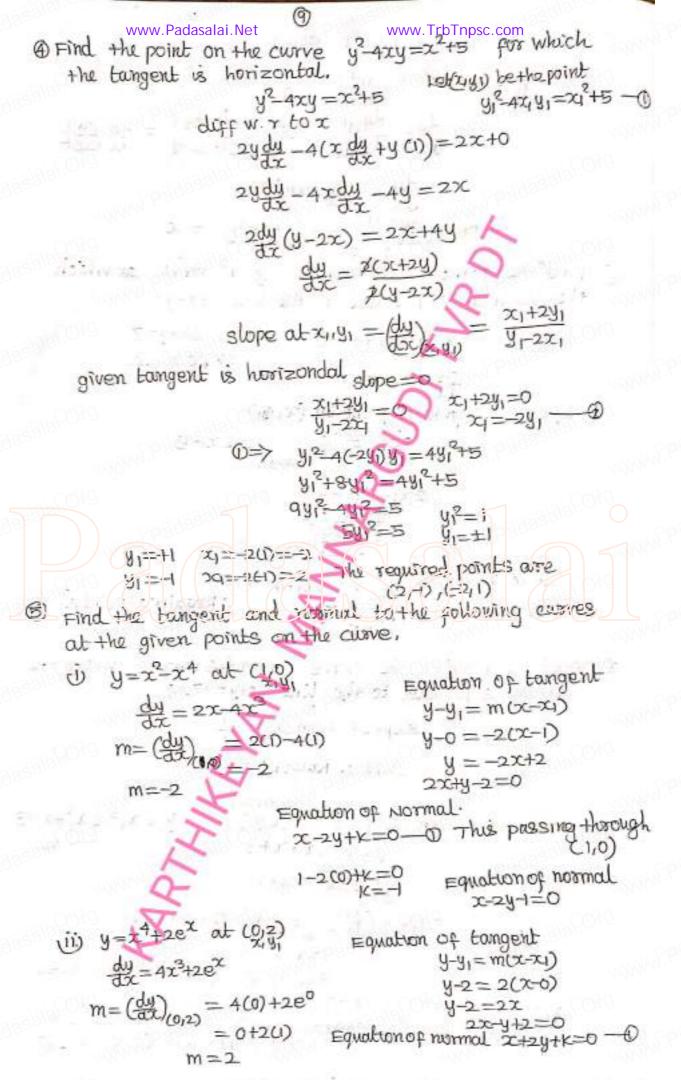
(i) Equation of languent
$$y - y_1 = (y_1)(x-x_1)$$

angle between the two curves

$$tano = \left| \frac{m_1 - m_2}{1 + m_1 m_2} \right|$$

- 1 two curves are orthogonal if mixm2= Exercise 7,2
- 1 Find the slope of the tangent to the curves at the respective given points,

$$y = x^4 + 2x^2 - x$$
 at $x = 1$
 $\frac{dy}{dx} = 4x^3 + 4x - 1$



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                              0+2(2)+K=0
                     D ⇒ Equation of normal x+2y-4=0
(ii) y=xsinx at(15,13)
                                           Equation of tangent
          \frac{dy}{dx} = x \cos x + \sin x(\theta)
                                                y-y1 = m (x-x1)
      m=(dy) = Ts costs +sints
= Ts (0)+1
                                         y-1/2=1 (x-1/2)
                                                 y-1/2=x-1/2
                                      Equation of normal
                 m=1
                         This normal passing through (15.1%)
                           O=> x+y-1=0
(iv) x=cost, y=2sin2t at t=173
                                                   G. Kartlukayan
         de=-sint du= 22sint cost
                                                   Thiruvarus DT
               \frac{dy}{dx} = \frac{4 \sin t \cos t}{-3 i \pi t} = -4 \cos t
         slope m = \left(\frac{dy}{dx}\right) = -4\cos i\hat{y} = -4(\hat{y}) = -2
    (文y) =(cos 1/3,2sin 1/3)=(为,2(達)))=(2,2(達))
 Equation of tangent y-y1=m(x-x1)
                                           Equation of normal is
                                                  2x-4y=K -0
               y-3 = -2(x-12)
                                           Thus-passing through(知多)
                                              2(美)-4(美)=K
                24-3--2x+3
               2y-3 = -4x+2
                                         O ⇒ 2x-4y=-5
              4x+2y=5
6 Find the equations of the tangents to the curve y=1+x^3 for which the tangent is orthogonal with the line x+rzy=12
              y=1+23
                                               x+12y=12
     Let the tangential point be (2,141)
                     y1=1+213 -0
                                                slope = -t
              없=0+3x²
                                            m_1 \times m_2 = -1
  tangent slope at(x,y)=32,2
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$$x_1=+2$$
 $0\Rightarrow y_1=1+2^3=H8$ $y_1=-2$ $0\Rightarrow y_1=1-8=-7$ $y_1=9$ $y_1=1-8=-7$ point $(x_1,y_1)=(x_1,y_$

$$y = \frac{2\pi}{2\pi}$$
 $y = \frac{2\pi}{2\pi}$
 $y = \frac{2\pi}{2\pi}$

$$(x_1-1)=4$$

$$x_1-1=\pm 2$$

$$x_1=3,-1$$

$$x_1 = 3$$
 $0 \Rightarrow y_1 = \frac{3+1}{3-1} = \frac{4}{2} = 2$ (3,2)

$$\infty_1 = -1$$
 $0 \Rightarrow y_1 = \frac{-1+1}{-1-1} = 0$ $(-1,0)$

Equation of tangents x+2y=K-0at (3,2) 0=3 $3+2(2)=K_1$ x+2y=7 $K_1=7$

$$at(-1,0) \oplus > 1+0=k_0$$
 $x+2y=-1$

(3) Find the equation of tangent and normal to the curve given by x=7 cost and y=2 sint, ter out any point on the curve.

= 75int # = 2 cost

12 www.Padasalai.Net www.TrbTnpsc.com -78int Equation of tangent y-y1= of (x-x1) $y-2sint = \frac{2\cos t}{-7\cos t}$ (x-7cost) -749int +145inft = 2xcoust -14cost 149in ++14008t = 2xcost+745int 2xcost+7ysint=14(1) 2000st+7ysint=14 Equation of normal 75int x-zycost = K - 0 passing through (700st,2 sint) ter 7sint 7cost -2cost 2sint = K 4991ntcost-45intcost=k k=459mtcost 0=> 78intx -24cost -455intcost 1 Find the angle between the rectangular hyperbola xy=2 and the parabola x2+4y=0 xy=2-0 202-44-0 $2^2 = -i\binom{2}{2}$. G. Korthikuyan Thi. Tuvanur DT $2^3 = -2$ $0 \Rightarrow z(y) = z1$ point of intersection is (-2,-1) $4\frac{dy}{dx} = -2x$ $m_2 = \left[\frac{dy}{dy}\right] = \frac{+2}{2} = 1$ angle between the curves tamo = $\frac{m_1 - m_2}{1 + m_1 m_2}$ $=\left(\frac{-15-1}{1+(-15)(1)}\right)$ $tano = \left| \frac{-3\pi}{k_2} \right|$ tano=3 0=tan(3)/

www.Padasalai.Net 22-y=2 and 2y=c2 whose c, r are constants, cut orthogonally, $x^2-y^2=r^2$ $xy=c^2$ Let the point of intersection be (x1141) $x_1^2 y_1^2 = r^2 = 0$ $x_1 y_1 = c^2 = 0$ $\frac{x^2y^2=r^2}{\text{diff w. r. to x}}$ 2x-2ygy=0 diff w. 7 to x 1/3/14 = 1/2x $\frac{dy}{dx} = \frac{2}{y}$ $m_2 = \left(\frac{dy}{dx}\right)_{0 \le 1 \le 1} = -\frac{c^2}{2}$ m1=(84)=31 $m_1 m_2 = \frac{x_1}{y_1} \times \left(\frac{-c^2}{x_1}\right)$ signed sequel substitutions of = -c2 = -c2 min and but the m1m2 =-1 ... The curves care cut orthogonally. Mean value theorem G. Kousthakehore 1 Rolle's Theorem Thirtuvarius D7 Let foo be a function U foois continuous on [a16] -(ii) foots differentiable on (a,b) air fra=fcb), then there exist atleast one point cecarb) s.t flcc)=0. Slagrange's mean value Theorem Let poor be a punction i) for is continuous in [a, b] di) from is differentiable in carb) there exist atleast one point ce carb) s.t $f(c) = \frac{f(b) - f(a)}{b-a}$ 3 If footis continuous in [a16] and differentiable in carb) and if \$10070 \times \alpha (a,b) then for x1,x2 & (a16) s.t. x1<x2 we have fox1) < f(x2) Exercise 7.3

1) Explain why Rollés theorem is not applicable to the following function in the respective intervals.

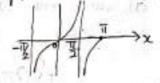
· fcx)=一, xe[小]

foo) is not continuous on [-1,1], (foo) is discontinuous at x=0)

-. Rolle's Theorem cannot be applicable,

(i) fox) = tanx, x ∈ [0,1]

fox) is not continuous on [0,17]



fix is discontinuous at x=1/2

Rollés Theorem cannot be applicable.

(ii) fix=x-2 logx, x ∈ [2/7]

i) fox) is continuous on [2,7]

(i) fox) is differentiable on (2,7)

$$f(a) = f(2) = 2 - 2\log 2$$

2-2 log2 = 7-7 log 7 - (1)

foo) does not satisfy the 3 conditions

: Rolle's theorem cannot be applicable,

2) Using the Rolle's theorem, determine the value of or at which the tangent is parallel to the z axis for the following functions.

(i) f(x)=x-x, x = [0,1]

in fix) is continuous on [0,1]

(ii) fox) is differentiable on (0,1)

(iv f(a)=f(o)=0-0=0

$$t(p) = t(1) = 1 - 1 = 0$$
 $t(a) = t(p)$

-: By Rolle's theorem Theore exist ce (O11) such that at which

the tangent is parallel to the x axis

$$f(x)=x_{\delta}-x$$

x=1/2 the tangent is parallel to x axis.

(ii)
$$f(x) = \frac{x^2 - 2x}{x + 2}, x \in [-1, 6]$$

poor is continuous on [-1,6] and differentiable on (-1,6)

$$f(\alpha) = f(-1) = \frac{1+2}{-1+2} = 3$$

$$f(6) = f(6) = \frac{36-12}{6+2} = \frac{24}{8} = 3$$

- By Rolle's Theorem, J CE(1,6) such that f'(c)=0 at which the tangent is parallel to a axis

$$f(x) = \frac{x^2 - 2x}{x + 2}$$

 $\rho(x) = \frac{(x+2)(2x-2) - (x^2 - 2x)(1)}{(x+2)^2} = \frac{2x^2 - 2x + 4x - 4 - x^2 + 2x}{(x+2)^2}$

$$f(x) = \frac{x^2 + 4x - 4}{(x+2)^2}$$

$$\rho(c)=0 \Rightarrow c^{2}+4c^{-4}=0$$

$$c^{2}+4c^{-4}=+8$$

at $x=-2+2\sqrt{2}$ the tangent's parallel to x axis,

ののなった。それのの

flows is continuous on to, or , and oligiperentiable on (0,9)

at which the tangent is parallel to racis

Thirmorner DI

Gr. karr+lukeyan

$$P(cc)=0$$
 $\frac{1}{2\sqrt{c}}=\frac{1}{3}=0$

Thirmwarur DT

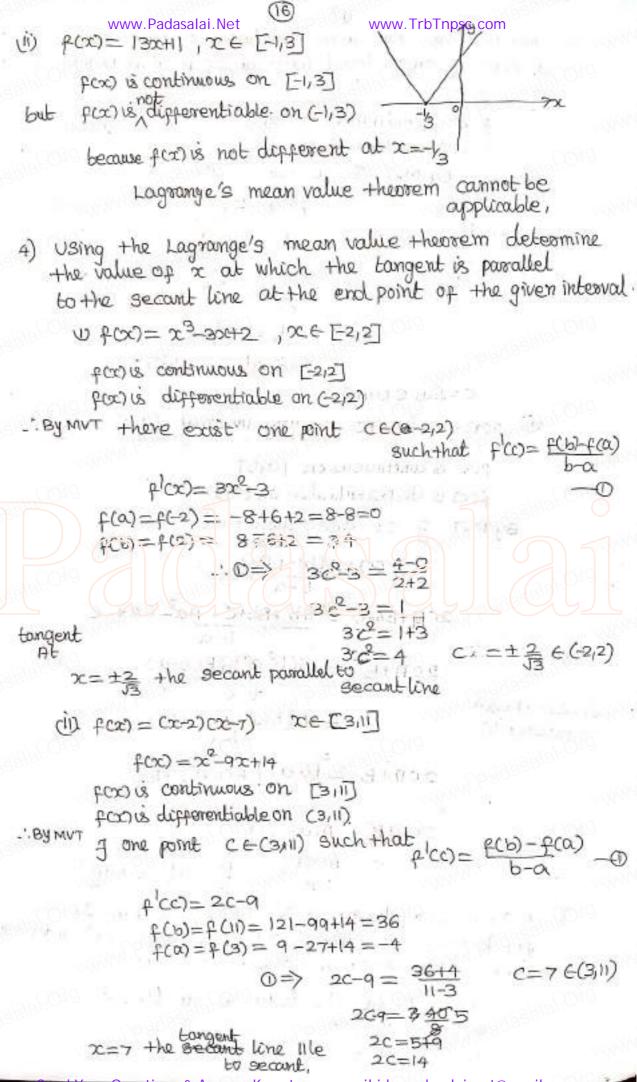
 $\frac{1}{2\sqrt{c}}=\frac{1}{3}$
 $\frac{2\sqrt{c}=3}{2\sqrt{c}=3}$

C=9 E(0,9) x=9 the tangent purallel to x axis.

3 explain why Lagrange's mean value theorem is not applicable.

poor is not continuous in [-1,27 when x=0 fcx)=00 not defined

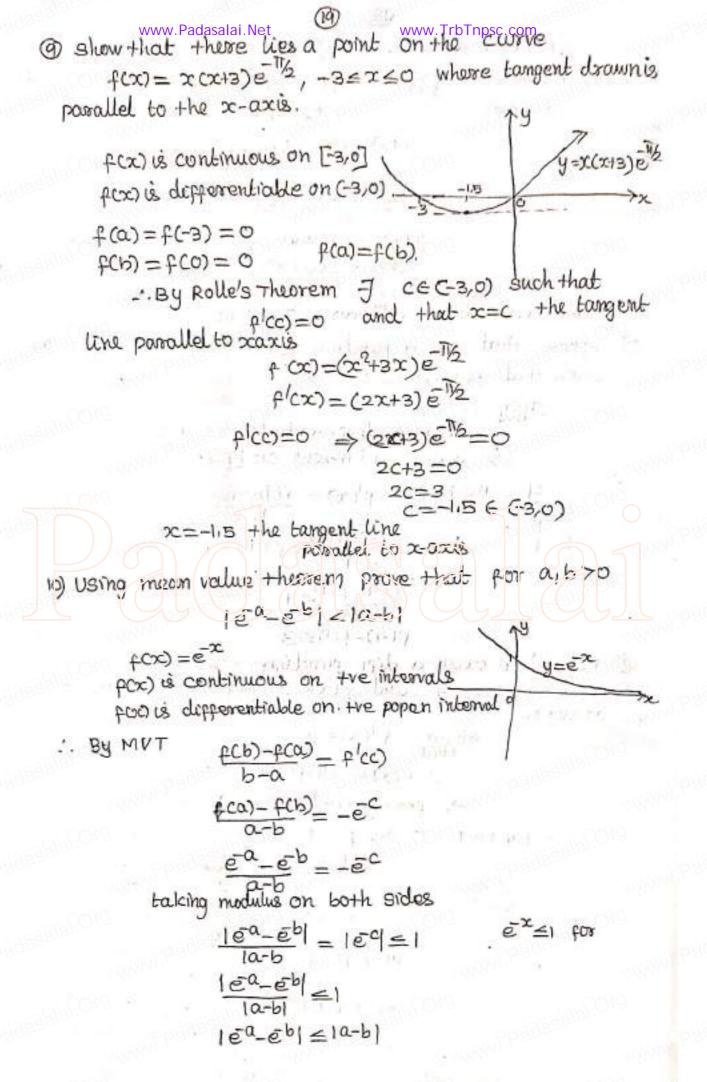
-: .: Lagrange's mean value Theorem connot



5) Show that the value in the conclusion of MVT for is fox)= = on a closed interval of positive number [a,b] 13 Valo fox) is confirmous on [a,b] (arb) are positive fexis continuous on (a16) ... By MVT J cecaib) such that t,(cc) = t(p)-t(a) -== 35 x-(0+0) 1 = 1 ab c2=ab c=vato C=Vab @(a1b) @ fcx= Ax2+Bx+c on any interval [a,b] is atb fix) is continuous on [a, b] fox is differentiable on (a,b)= By MVT I CE COUD Such that $\frac{b-a}{b-a}$ 20: +B. +O = Ab2+Bb+C-Aa2-Ba -C $2CA+B = A(b^2-a^2)+B(b-a)$ b-a G. Karthi Keyan $=\frac{A(b+a)(b-a)+B(b-a)}{b-a}$ Thiruvariur DT 2 CA+B = (b-0) [A(a+b)+B] 2CA+18 = A(Q+6)+18 C= Aca+b) (C= a+b & Ca,b) 6 A race car driver is racing at 20th km If his speed never exceeds 150 km/hr what is the maximum distance he can cover in the next two hours, Let S(t) be the distance at time t S(t)=20 $S(t_2)=?$ Send Your Questions & Answer Keys to our email id - padasalai net@gmail.com Scanned by CamScanner

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S(t) & Continuous [0,2] and Continuous on (0,2)
        ... BY MYT
                        S'(t) = S(t_2) - S(t_1) S'(t) = specials
         J te (0,2).
                           \frac{3(t_2)-20}{2-9}=9'(t)\leq 150
                          · . S(62)-20 ≤ 150
                         S(t2)-20 < 300
                           s(t2) ≤ 300+20
                           S(b) = 320 min
maximum distance cover = 320 km.
@ suppose that for a function fcx), fcx>≤1 for all 1≤x≤4
     show that f(4)-fcn=3
           given flox=1
                  - fcx) is differentiable on (14)
                => fcx) is continuous on [1,4]
            : By MVT plan = 1(b)-p(a)
                            f(a)-f(x)=f(x)≤1
        b=4
                           fcaj-fco 1 and many page 1
                            f(4)-f(1)≤3
(8) Does there exist a deep function for such that
   fco) = -1 .fcz)=4 and fcxo=2 for all x Justify your
   answer.
                   given 1 (x) =2
                        Pox is differentiable on (0,2)
                     fex) is continuous on [0,2]
            By MT J one point x ∈ (0,2) such that
                                 f(x)= f(b)-f(a)
                                f(x) = \frac{f(x) - f(x)}{2 - 0}
                            \frac{f(2)-f(0)}{2} = f(x) \le 2
\frac{f(x) = \frac{4+1}{2-0}}{f(x) = \frac{5}{2}} \le 2
\frac{f(x)-f(0)}{2} \le 2
f(x) = \frac{5}{2} \le 2
f(x) = \frac{5}{2} \le 2
    f(x) \stackrel{f(x)}{4+} = 2 \stackrel{f(x)}{\log_2 not} \stackrel{2.5}{\log_2 not} Contractive twon. 2.5 \stackrel{2}{=} 2 have given Send Your Questions & Answer Keys to our email id - padasalai net@gmail.com Scanned by CamScanner
                                                      ficx) cannot be
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(18)



Senies www.Padasalai.Net

(a) Taylor's series

fcx) is inpinitely differentiable at $x=\alpha$ $f(x) = f(\alpha) + \frac{f'(\alpha)}{11}(x-\alpha) + \cdots + \frac{f''(\alpha)}{n!}(x-\alpha)^n + \cdots$

b) Maclaurin's series

If a=0, the expansion takes the form.

$$p(x) = f(0)$$
, $\frac{p(0)}{1!}x + \cdots + \frac{p^{n}(0)}{n!}x^{n+1} \cdots$

Exercise 7.4

1) write the Maclaurin's series expansion

(1) ez	Function'	exand derivatives	value at x=0
18381811	fox)=ex	ex	e°=1
	61CX)	ex	e0=1
	plicx)	ex	e0=1
140	ปอบ ขางโอ ออกเอล) = f(0)+F(0)	c+f=10;x2+
0019			21

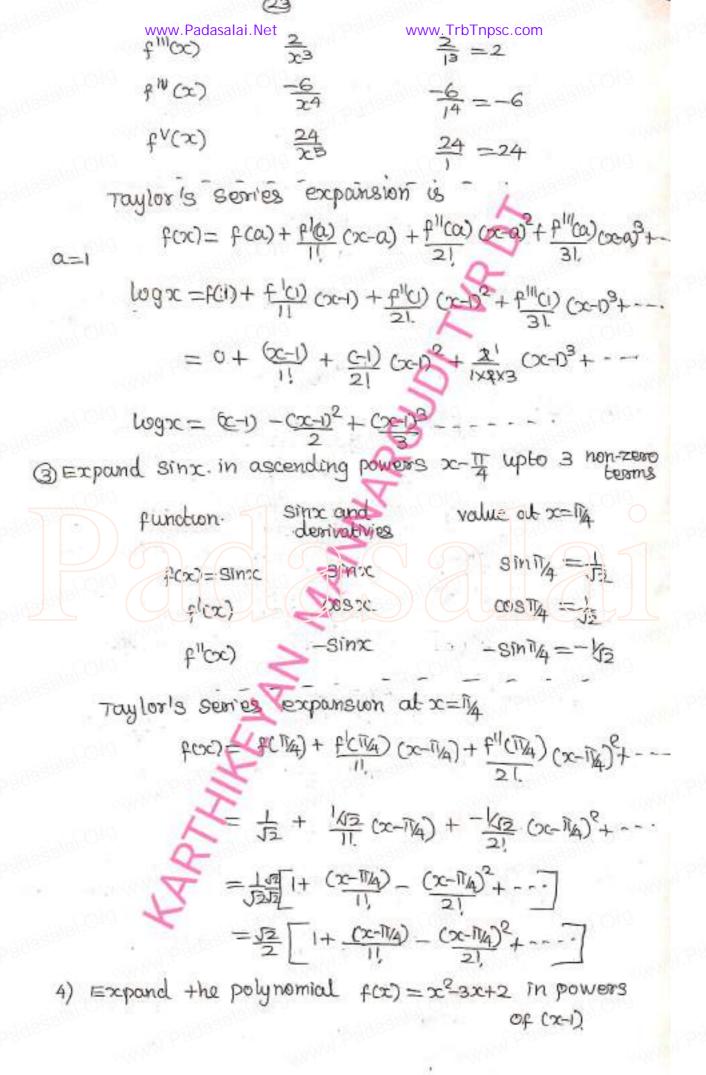
value at x=0 sino=0 fcx)=sinx Sinx Flox) coso = 1 0032 -Sinc filox) -SINO = O -cwsx PIII(X) $- \cos 0 = -1$ +9inx (C) (C) Smo =0 COSX to(x) C030 = 1

Maclaurin's series expansion $f(x) = f(0) + \frac{f(0)}{2}x^2 + \frac{f''(0)}{2}x^3 + \frac{f''$

Sinx= 0+ 1 x+ = x2+ = 1x3+ = x4+ = 1x4...

	Padasalai.Net 21	www.Ti	rbTnpsc.com
(iii) cosa	function	cosoc and derivatives	value at x=0
	fcx)=cussc	cusx	coso = 1
	floo)	-sinx	$-\sin \alpha = 0$
1000 AM	£1100	-cosx	-0080=-1
	Encoc)	Sinoc	Sino=0
TITE OF	En Coc)	ധാമാ	0030 = 1
	t _A CxC)	-simc	_sino=0
2.10 = 44.63	to(co)	-wsx	-0030=-1
evac langin	r's somes exq	F-9100-1500-5	
Moctatall	(0)4 = (x0)	+ f (0) x+ f (0) x	2+ f"(0)+3+~~~~·
A STATE OF THE STA	- 6 /////E		1///////// Market - 1///////////////////////////////////
Cos	$3x = 1 + \frac{0}{1!}x$	-#x2+3 x3+	1 x4+0 x5 -1 x6+
co	$80c = 1 - \frac{x^2}{2!} + \frac{x}{4}$	$\frac{4}{1} - \frac{\times 6}{61} + \cdots$	paids
زن لموداء			
	fundation	log(1-x) and derivatives	value at x=0
	foot=logu-		log1=0
	plcx')	1-x	- <u>i</u> -bi
G. Karthikeyan Thinwarm DT	blicx)	-L-2)2	- <u>i</u> 1
onchi e	fill(cx)	2 CI-203	(1-0)3 = 12
\$12000 pt 22	f ^{IV} (xx)	CI-x)*	$\frac{-6}{(1-0)}4 = -6$
Y.	into anima on	roaveion	
Macrana	p(x) = f	$(0) + \frac{p(0)}{11} x + \frac{p(0)}{2}$	CO) x2+ f1/0) x3+ - · · ·
lo	19(1-20) = 0 =	-1 x -1 x2-	<u>k</u> x ³ _ <u>6</u> x ⁴
		2-3-24-	
salah Olip W	=-(x	+쏠+쏠+쭈+…	
(v) tanicx)	-1ex=1		Man. " " " " " " " " " " " " " " " " " " "
(y) current	function		
	fcx=tan	h tarilz	
	flox)	1+22	$\frac{1}{1+0} = 1$
6/690	ARCH 200		

$$f(x) = \frac{1}{1+x^2} = \frac{1}{1+$$



fundww.Padasalai.Net-3x+2 and www.TrbTnpsc.com value at x=1 desivatives $f(x) = x^2 = 3x + 2$ x2-3x+2 1-3+2 =0 ticx) 2-3 =-1 2x - 3flicx) $t_{111}(x)$ 0 Toylor's series expansion i at x=1 is too= to) + + (1) (00-1) + + (01) (00-02+ $x_6 - 3x + 5 = 0 + (-1)(x - 1) + \frac{3}{5}(x - 0)^5 + 0$

$$x_{5-3x+5} = 0 + (-1)(x-1) + \frac{3}{5}(x-1)_{5} + 0$$

$$x_{5-3x+5} = 0 + (-1)(x-1) + \frac{3}{5}(x-1)_{5} + 0$$

Indeterminate forms

8,0x0,0x0,10,00,00

The L'Hopital's Rule

ecoc) which give are duff, and g'(x) \$0 $\lim_{x\to a} f(x) = 0 = \lim_{x\to a} g(x) + \text{hen } \lim_{x\to a} \frac{f(x)}{g(x)} = \lim_{x\to a} \frac{f(x)}{g(x)}$

 $\lim_{x \to a} f(x) = \pm \infty = \lim_{x \to a} g(x)$ then $\lim_{x \to a} \frac{f(x)}{g(x)} = \lim_{x \to a} \frac{f(x)}{g(x)}$

Exercise 7,5

Evaluate the following limits, if necessary use l'Hopital's Rule.

1) $\lim_{x\to\infty} \frac{1-\cos x}{x^2}$

 $\frac{1}{2} = \frac{1-\cos x}{x^2} = \frac{1-\cos x}{x} = \frac{$

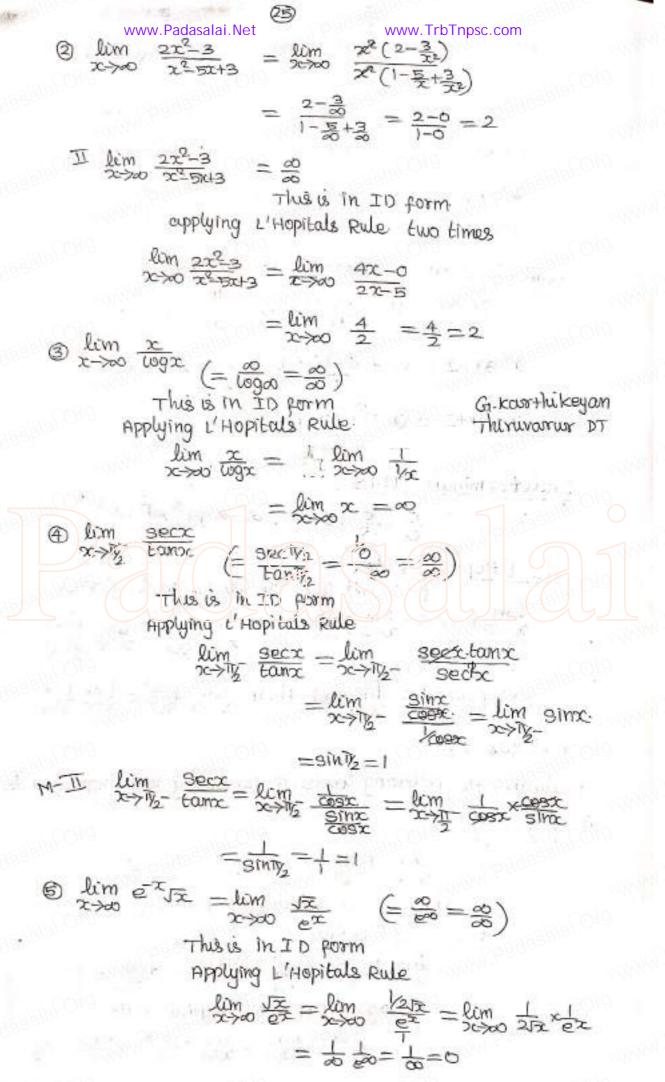
This is in indeterminate form. (0)

Use L'Hopitals Rule

 $\lim_{x\to 0} \frac{1-\cos x}{x^2} = \lim_{x\to 0} \frac{0+\sin x}{2x} = \frac{+\sin 0}{2(0)} = 0$

again applying l'Hopital's Rule.

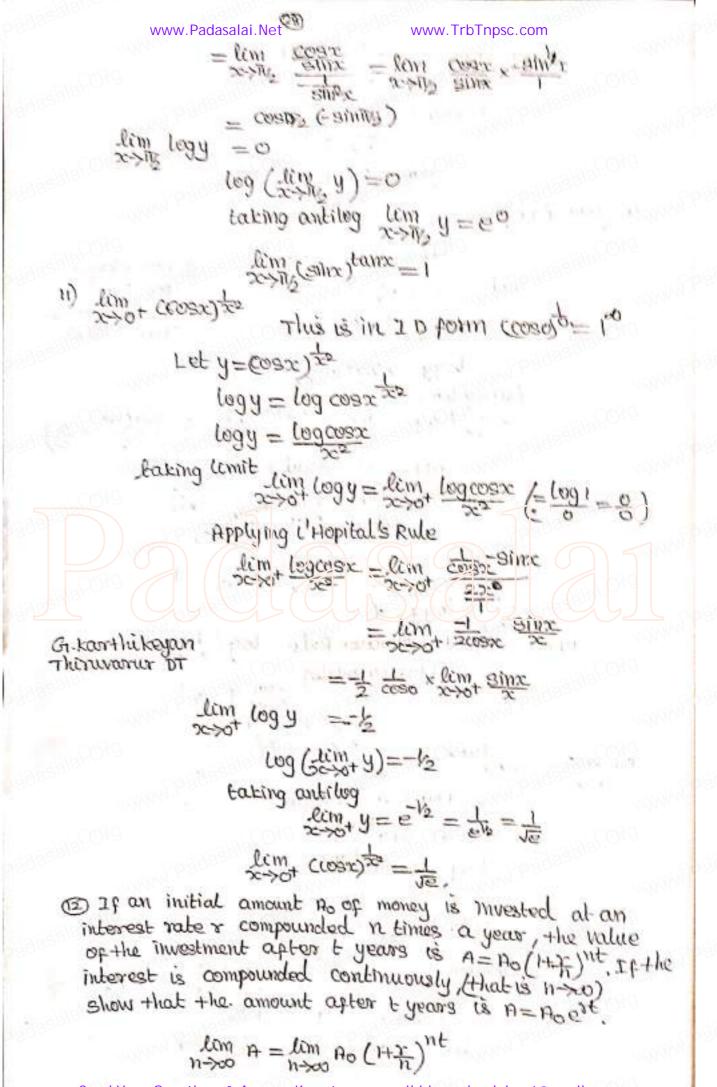
lim +sinx = lim + cosx = +coso = +1/2



```
www.Padasalai.Net = sime www.TrbTnpsc.com = sime = 
                                                         This is in ID form
                                                                             cupply L'Hopital Rule
                                                \lim_{x\to\infty} \frac{x-\sin x}{x\cos x+\sin x} = \lim_{x\to\infty} \frac{1-\cos x}{x\cos x+\sin x}
                                                      again Apply l'Hopital's Rule.
                                      \lim_{x\to\infty} \frac{1-\cos x}{\cos x+\sin x} = \lim_{x\to\infty} \frac{\cos x+\sin x}{\cos x+\cos x}
                                                                                                          = Sino
0+000+0000
         いか (差一点)
                                                                              = Lim (2
20+12004) - 20-1
                                                                               =\lim_{|x|\to 1^+} \left(\frac{2-x(x+1)}{x+1}\right) = \lim_{|x|\to 1^+} \left(\frac{2-x^2-x}{x^2-1}\right)
                                                                                                                                                                                      (= 2++ = 0)
                                               This is in I.D. form
                                        applying l'Hopital's Rule
                                                                            \lim_{x \to 1^+} \left( \frac{2-x-x^2}{x^2} \right) = \lim_{x \to 1^+} \frac{(5-1-2x)}{25c}
                                                                                                                                       8) lim x 2
                                                                                             composite function. Theorem
                (=0°)
                                                                                                 \lim_{n\to\infty} \log f(n) = \log (\lim_{n\to\infty} f(n))
   This is In ID form
                                                  Let y=xx
                                                                   \log y = \log x^{x}
                                                                logy = xlogx
                                        tascing lamit
                                                               Slim logy = lim logx (= logo = -0)
                                                                                   This is INID form
                                                                         applying L'Hopital Rule
                                                      = lim + logsc = lim + = lim + x - x2
                                                                                                              = lim -x =0
```

(26)

```
UNIVARIANTAINE PUNCTUN RILLIONW.TrbTnpsc.com
                       \log(\lim_{\infty} y) = 0
                  taking antilog
                             ( Lim y) = e0
                       20m xx=1
(1+1) ) (= (1+1) ) (= (1+1) (0) = 10)
                    Thus is in ID form
                                                     G Karthikeyan.
              rot 2=(1+7)x
                                                        PGT GGHSS
                    logy = log(1+4)x
                                                        Thirumakkettai
                                                       Thermounter DT
                     logy=xlog(1+1/2)
              taking wmit
               \lim_{x\to\infty}\log y=\lim_{x\to\infty}\frac{\log(1+kx)}{kx}\in\frac{\log(1+0)}{k0}=\frac{0}{0}
                      Applying L'Hopital Rule
               lim (log(1+/2) = lim (1+/2 (1/2))
                                 =\frac{1}{1+20}\cdot =\frac{1}{1+20}=1
              lim Logy == 1
       Apply composite function Rule log ( sim y)=1
                         taking antilog lim y = e1
                                 500 (1+7)x= 6
10) lim (sinx)tanx
                     This is in ID from 000
               Let y= sinxtanc
                  logy = log sinxtanx
                  logy = tanz logsinz
                  legy = legainx cotx
          taking limit \lim_{x \to 1/2} \log y = \lim_{x \to 1/2} \frac{\log \sin x}{\cot x} = \left(\frac{\log x}{\cot x} = 0\right)
                       applying L'Hopital's Rule
                    lim Logsinx = lim sinx cosx -cosecox
```



W. K.T
$$\lim_{n\to\infty} (H + \frac{n}{n})^n = e^k$$
 $\lim_{n\to\infty} (H + \frac{n}{n})^n$ $\lim_{$



Mono tonicity of functions.

Increasing function

A function fcx) is increasing function. In an interval I if a < b => f(a) ≤ f(b) ∀a,b∈I

pecreasing function

foot is decreasing function in I if a < b => f(a) > f(b). VaibeI

* pcx) is differentiable in an open interval carb)

If is placed then from is increasing in carb)

in fax >0 then fax is strictly increasing in carb?

in floos≤0 then food is decreasing in (a16)

UV) flow =0 then fox is strictly decreasing in (a16)

Vxea,b)

Statumory point.

A stationary point (xo, fixo)) of a diff. punction

ex) is whose place)=0

critical number and critical point

where ploxo)=0 or does not exist ... (that no is called critical number)

Absolute maximum & minimum

f(xo) is called absolute max of f(xx) f(xxo) ≥ f(xx) > f(xxo) > f

Aprocedure for finding the absolute extrema

1) find critical number of fix)

2) Evaluate value of fcx) at that critical no.
and also find fco, f(b)

3) largest value in steps 2 is absolute max, smallest value in steps is absolute min.

Fermat Theorem

If c is a critical number fox has relative extremum at x=c. Invariably there will be critical numbers of fox) obtained by flow=0 or flow does not exist values, First Derivative test.

OIF flow changes its sign the to the then fow has local max @ If flox) changes frome -ve to the then fox) has local min

@ flox) is the on both sides of c or -ve on both sides of c then fco is neither local max nor min.

EXERCISE 7.6.

1) Find the absolute extrema.

(i) f(x) = x2-12x+10 (i) [1/2] = 10/2 = 10/2 p(00) = 200-12

floor=0 => 122-12=0) = or make a pulse to

27 = 12 20 - 12 6 TEMP - 1 - 15

critical number is x=6 \$ [D12] we connect f(8)=16/12(9)+10=36-72+10=-26 toke x=6

f(D = 1 - 12 + 10 = -1)

 $f(2)=2^{2}-12(2)+10=4-24+10=-10$

absolute maximum =-1, absolute minimum =-2610

(1) fcx?=3x4-4x3; [-1,2] [Change the interval

f(x)=12x3-12x2 as [1, 7] we get book answer]

plan=0 => 12x2(x-1)=0

22=0 x-1=0 x=0 x=1

critical numbers x=0,11

f(0) = 3(0) - 4(0) = 0

f(1) = 3(1) - 4(1) = 3 - 4 = -1

f(-1) = 3(-1)4-4(-1)3 = 3+4=7

 $f(2) = 3(2)^4 - 4(2)^3 = 48 - 32 = 16$

absolute maximum = 16 absolute minimum = -1

```
www.Padasalai.Net f(x) = 6x^3 - 3x^3
                                           www.TrbTnpsc.com
            tox = g(3) x 12-1-3Tx 12-1
                  =8x13-x113x-1
                  = x^{\frac{1}{3}}(8 - \frac{1}{4}) = x^{\frac{1}{3}}(8x - 1) = \frac{8x - 1}{2}
               \rho(x)=0 \Rightarrow 9x+=0
                                  8x=1
                                             critical numbers
   at x=0 f'ex) does not exist
                                                        x=0, b_0
     t(0) = 0
        f(8)=6 (8) 1/3-3(8)3
               =6(\frac{1}{2})^4 - 3(\frac{1}{2}) = \frac{3}{8} - \frac{3}{2} = \frac{3-12}{8} = -\frac{9}{8}
         f(-1) = 6(-1)9-3(-1)13 = 6+3=9
        f(n) = 6-3=3
    absolute maximum == q absolute minimum = -2
( ) f(x) = 2005x +511200 ; [0,174]
            P(cx) = 2(-sinx)+2(08:2)c
           flow = 2 (-strict + cosex)
           t)(x)=0 =>
                     -sinx+1-2sin2x=0
                  23in8x+3inx-1=0
                      @inx+2) (sinz-1)=0
                     sincatl=0 sinc=13
                          I-=xriie
                          Sinx = sin-ig Sinx = sin ig
                         x = n\pi + c_0 \frac{2}{(c_0)^2} x = n\pi + c_0 \frac{2}{(c_0)^2}
              take one value
             Critical number 2 = 31/3 ,
       f(3) = 2\cos 3 + \sin 3 
       f(1/6) = 20031/6+811/2/1/63 = 2/3 + 1/3 = 3/3
       f(0) = 2\cos(0) + \sin 0 = 3\cos = 3
       fcTg) = 2 cosTg + sinaTg = 0+0 = 0
          absolute maximum = 356
```

@ Find the interval of monotonicities and hence find the local extremum.

(i)
$$f(x) = 2x^3 + 3x^2 - 12x$$

 $f(x) = 36x^2 + 6x - 12$
 $f(x) = 0 \Rightarrow 6x^2 + 6x - 12 = 0$
 $6(x^2 + x - 2) = 0$
 $(x+2)(x-1) = 0$
 $x+2 = 0 \quad x-1 = 0$
 $x = -2$, $x = 1$

critical numbers are -2,1

- ob -2 | 100

intervals are (-00,-2), (-2,1), (1,00).

Interval value $f(\infty)=$ sign of (∞) monotonitity $(-\infty)-2$ 3 $(-\infty)-3$ $(-\infty)-2$ 3 $(-\infty)-3$ $(-\infty)-2$ 3 $(-\infty)-3$ 3 $(-\infty)-3$

(-2,1) 0 6(0+2)(0-1) _ strictly decreasing =-12 (1,00) 2 6(-4) (1)=-24 + strictly increasing

is flow changes from the to -ve through =-2

fcx) has local max at x=-2

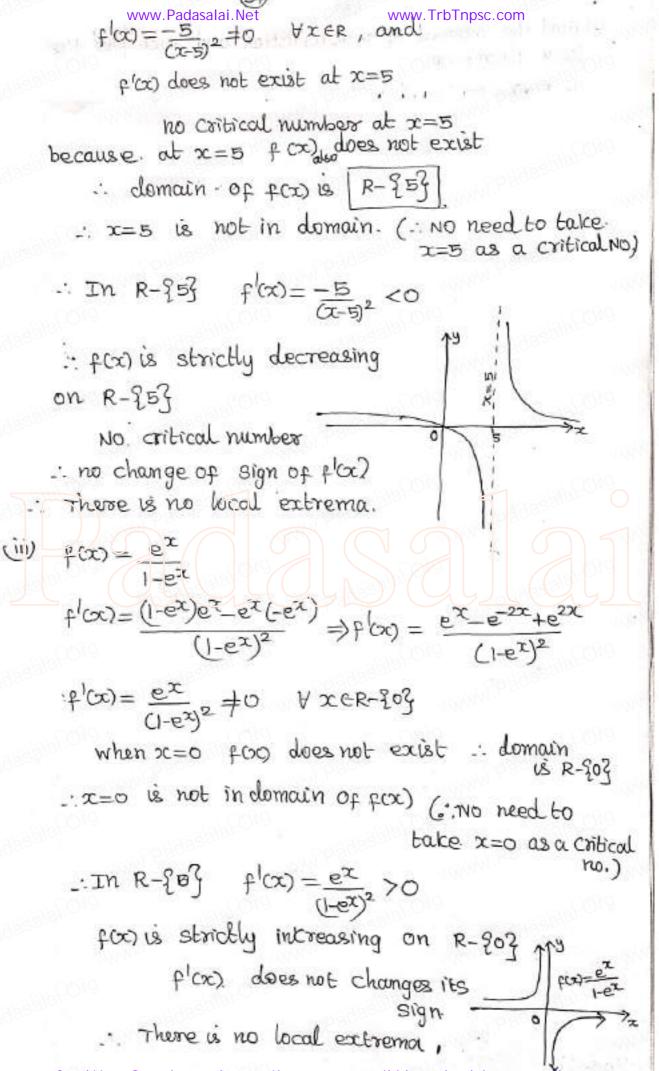
max value is $f(-2) = 2(-8) + 3(-2)^2 - 12(-2)$ = -16+12+24 = 20

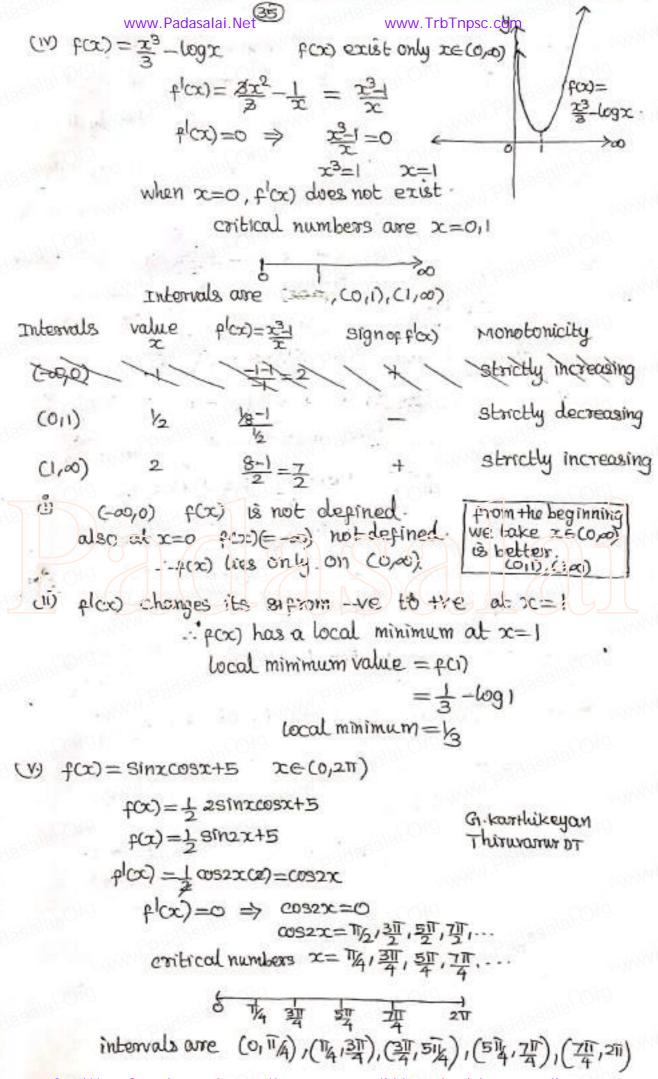
(ii) f(x) changes from -ve to +ve +hrough x=1 f(x) has local in minimum at x=1

minimum value = f(1)= 2+3-12= -7

Local maximum = 20, Local minimum = -7

(ii) $f(x) = \frac{x}{x-5}$ $f(x) = \frac{(x-5)(1)-x(1)}{(x-5)^2} = \frac{x-5x}{(x-5)^2} = \frac{-5}{(x-5)^2}$





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Intervals	value	p(x)=0032x	signof f(x)	mohotoniaty	
(0,14)	TT/6	cosTy3=1	+	strictly increasing	
(平,平)	11/2	Cos 11 = −1	- 1000	strictly decreasing	
(3필,필)	T T	COS211=1	+	Strictly Increasing	
(텔,패)	311	C05317=-1	1 1 2 NOV	strictly decreasing	
(711 /211)	111	05 11/3 05 660=05-60=1	+	strictly Increasing	

fcx) is increasing on (小似), (翠), (翠), (翠,如) and strictly decreasing on (瓜), (翠),

i) $f(\infty)$ changes is from +ve to -ve at $x=\frac{17}{4},\frac{517}{4}$ f(x) has local maximum at $x=\frac{17}{4},x=\frac{517}{4}$

$$f(\bar{x}) = \frac{1}{2}\sin x\bar{x} + 5 = \frac{1}{2} + 5 = \frac{1}{2}$$

$$f(\bar{x}) = \frac{1}{2}\sin x(\bar{x}) + 5$$

$$= \frac{1}{2}\sin x + 5 = \frac{1}{2} + 5 = \frac{1}{2}$$

Localmax = 1/2

(i) flox) changes from -= 1-ve to tre through $x = \frac{3\pi}{4}, \frac{7\pi}{4}$

 $f(\infty)$ has local minimum at x = 31,71

Local minimum values are

$$f(\frac{34}{4}) = \frac{1}{2} \sin^2(\frac{34}{4}) + 5 = \frac{1}{2} (-1) + 5 = \frac{1}{2}$$

 $f(\frac{34}{4}) = \frac{1}{2} \sin^2(\frac{34}{4}) + 5 = \frac{1}{2} \sin^2(\frac{1}{2}) + \frac{1}{2} \sin^2(\frac{1}{2}$

Local maximum = 1/2 10cal minimum = 9/2

www.Padasalai.Net www.TrbTnpsc.com Applications of second derivatives

Test of concavity

(1) If floor >0 on an open interval. I, then fox is concave up on I

If $f^{(1)}(\infty) < 0$ on I, then $f(\infty)$ is concave down on I point of Inflection

i) If flice) exists and flice) changes sign or -veto+ve through x=c then (c, fcc)) is called point of inflection

(i) If files) exists at point of inflection, then files=0.

The second Derivative Test

flow) exists gand give the critical point

find f"(x). then.

floc) <0 at x=c. then fox) has relative plication at x==c then fact has relative floged that x=c The test is not informative,

Exercise 7.7

i) Find the intervals of concavity and points of inflection,

(i)
$$f(x) = x(x-4)^3$$

$$f^{1}(x) = xx(x-4)^2 + (x-4)^3(y)$$

$$= (x-4)^2(3x+x-4)$$

$$= (x-4)^2(4x-4)$$

$$= 4(x-4)^2(x-1)$$

$$f^{1}(x) = 4(x-4)^2(y) + 4(x-1) + 2(x-4)$$

$$= 4(x-4)[x-4+2(x-1)]$$

$$= 4(x-4)[x-4+2(x-1)]$$

$$= 4(x-4)[x-4+2(x-2)]$$

$$f^{1}(x) = 12(x-4)(x-2)$$

$$f^{1}(x) = 0 \implies 12(x-4)(x-2) = 0$$

$$x = 2/4$$

intervals are (-00,2),(2,4), (4,00) Send Your Questions & Answer Keys to our email id - padasalai net@gmail.com Scanned by CamScanner

www.Padasalai.Net $p^{\parallel}(x) = \frac{1}{2}(x^2 + \frac{1}{2}(x^2 - 4)(x - 2)$ Sign of $p^{\parallel}(x)$ www.TrbTnpsc.com Interval concavity (-00,2) 12(-4)(-2)=96 concove up (2,4) 12(-1)(1) =-12 concave down (4,00) 12(1)(3)=36 + / concowe up The curve is concave up on (-00,2), (4,00). concave downward on (24), +11cx) changes its sign. through == 2 and x=4 $f(2)=2(-2)^3=-16$ point of inflection f(4) = 4(0) = 0(C3,-16) (4,0). (i) for = sinx+cosx, oxxx2TT flox) = cosx-sinx $f^{II}(x) = -\sin x - \cos x$ £11(0x0)=(0 => -Sinx-cosx=0SI'MX =- COS'X tanx=-1 = tan-4.50 100 X= itilited x=nti-tily nez intervals oure (0) 翠)(翠) (翠) (翠) E(01211) value flow) =- (sinctusx) flow sign concavity Y-Binitz+cosite) concowe down =-(1+0)=-TI -(0+G))=1concave up 111/6=330° - (-9in30°+00330°) concave down -(-15+程)=下湿 fco is concave upward on $(\frac{317}{4}, \frac{717}{4})$ concave downward on (0, 21), (71) 211) fac changes its sign through x=34,74

www.Padasalai.Net www.TrbTnpsc.com f(311)= sin 135°+cos 135°= sin(180-45)+cos(180-45) = 9in45 - 80945一五一五一0 t(計)=0 f(元)= sin 3150+cos 3150=-sin45+cos450=-12+2=0 point of inflection (314,10), (717,0) (iii) f(x)=== (ex-ex) t/cx)=1 (ex+ex) f"(x)=1 (ex-ex) f"(α)=0 ⇒ ex-ex=0 ex=ex Intervals (-0,0), (0,00) DC=01 Interval value $f(\infty) = e^{x} = e^{x}$ sign of $f(\infty)$ concavity concave down ward e-e1; (-00,0) 121-0 (10/00) concave upward.

for is concave upward on (000)

place) changes its sign through x=0 $p(0) = \frac{e^{0}-e^{0}}{2} = \frac{11}{2} = 0 \quad \text{Insterior} = (0,0)$

2) Find the local extrema for the following functions using second derivative test..

i) $f(x) = -3x^5 + 5x^3$ $f(x) = -15x^4 + 15x^2$ $= 15x^2(x^2 - 1)$ $f(x) = 0 \Rightarrow 15x^2(x + 1)(x - 1) = 0 \Rightarrow x = 0, 1, -1$ $f(x) = 0 \Rightarrow 15x^2(x + 1)(x - 1) = 0 \Rightarrow x = 0, 1, -1$ The critical numbers are x = 0, 1, -1

f ((α) = -60x3+30x (i) x=-1 ⇒ f ((-1) = +60-30 = 30>0

f(x) has local minimum at x=1Send Your Questions & Answer Keys to but email to - padasalar net@gmail.com Scanned by CamScanner

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(i)
$$x=1$$
 $f^{(1)}(1)=-60+30=-30<0$
 $f(x)$ has weal maximum at $x=1$
 $f(x)$ has weal maximum value = $f(1)$
 $f(1)=-60+30=-30<0$

(iii) x=1 $f^{(1)}(0)=0$ second derivative test is not informative of Local extremum of f(x).

Local min=-2 Local max=2.

$$f^{(\infty)} = x(\frac{1}{2}) + \log x \qquad p^{(\infty)} = 1 + \log x$$

$$f^{(\infty)} = 0 \Rightarrow 1 + \log x = 0$$

$$\log x = -1$$

$$x = e^{-1} \Rightarrow x = \frac{1}{2}$$

critical number is x=1/2

when x=/e fl(ke)=//e== >0

fix) has local numinium out x=1/e.

local minimum value = f(/e)

$$\hat{z}(\hat{n})$$
 $f(x) = x^2 e^{-2x^2}$

$$f(x) = e^{2x}(2x) + x^{2}e^{2x}(2x)$$

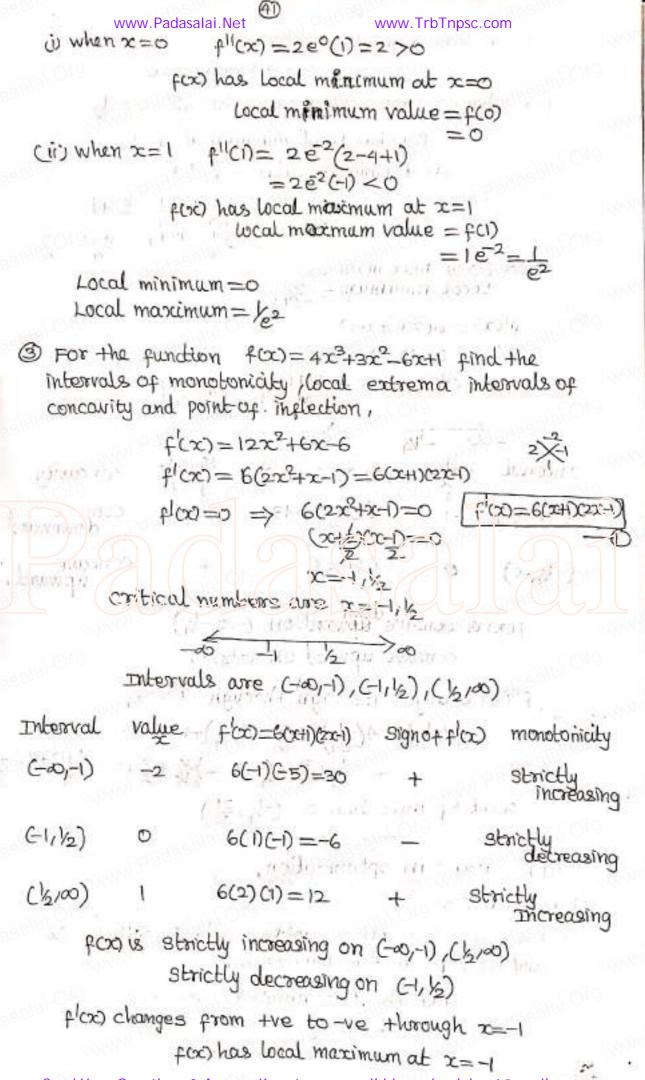
$$f(x)=0 \Rightarrow 2e^{-2x}(x-x^2)=0$$

critical numbers are x=0 x=1

$$= 3e_{5x}(1-5x + (x-x_6)(-5))$$

$$= 3e_{5x}(1-5x + (x-x_6)(-5))$$

 $=2e^{2x}(1-2x-2x+2x^{e})$



Locol maxi mum value = f(-1)www.TrbTnpsc.com =-4+3+6+1=6f(x) changes from -ve to +ve through >c= 1/2 foo has bocal minimumat x=15 Local minimum value = f(b) = 41+31-6+1 $\frac{2+3-12+4}{4} = \frac{9-12}{4} = \frac{-3}{4}$ teo Local maximum = 6 Local minimum = -34. (11) $b_1(x) = 9(5x_5 + x - 1)$ f'(x) = 6(4x+1)1 1 11 11 1 flica)=0 => 4xH=0 4x=-1 -50 -VA Interval value place =6(4x+1) and of concavity Ph(ax) (-a),-1/4) -1 6(-4+1)=-18 Concave deiwnward 6C)==6 (-1400) 0 concave upward. for is concave upward on (-00,-14) concave upward on (-14,00)

 $f^{(1)}(x)$ changes its sign +horough $x=-\frac{1}{4}$ $f(-\frac{1}{4})=4\left(-\frac{1}{64}\right)+3\frac{1}{16}-6\left(-\frac{1}{4}\right)+1$ $=-\frac{1}{16}+\frac{3}{16}+\frac{6}{4}+1=\frac{1}{8}+\frac{3}{2}+1=\frac{1+12+8-21}{8}$ point of inflection is $\left(-\frac{1}{4},\frac{3}{4}\right)$

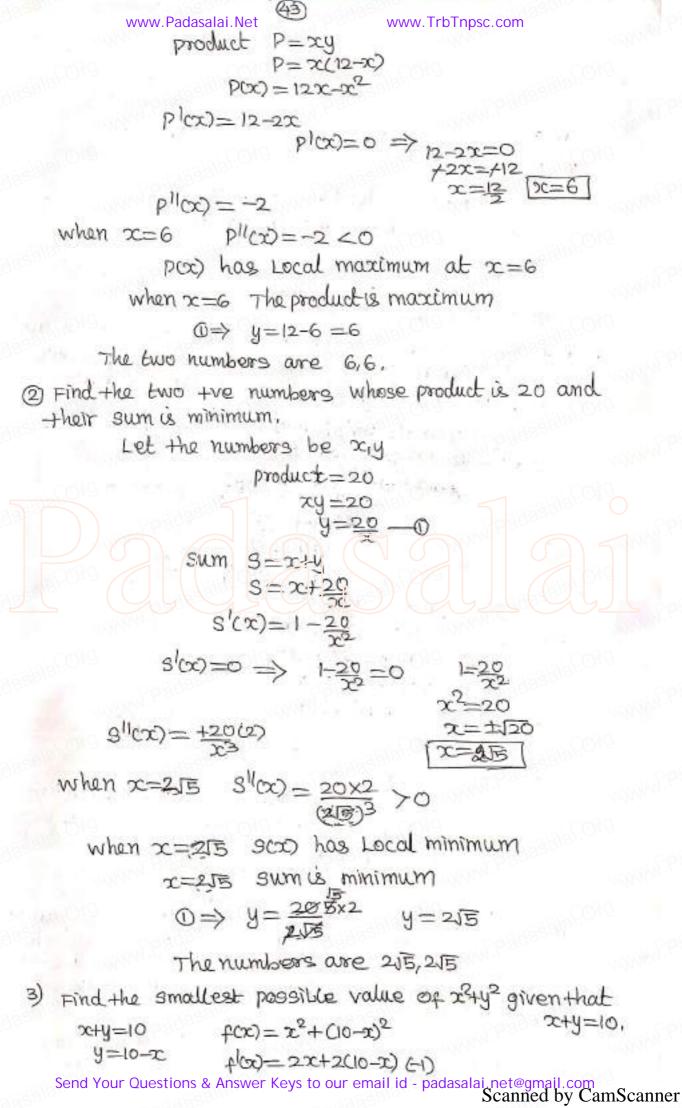
Applications in optimization,

Exercise 7.8

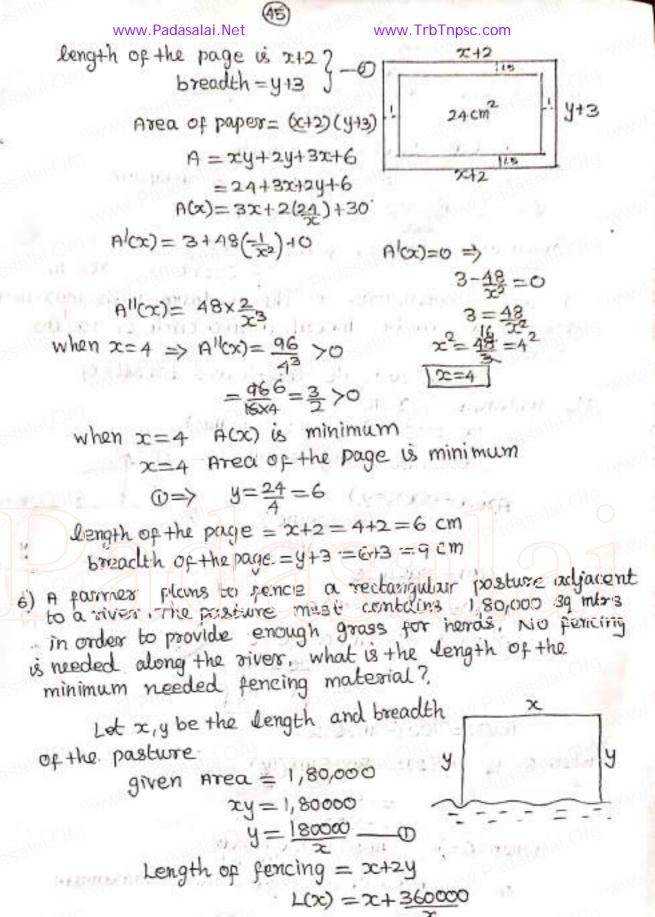
12 and their product is maximum.

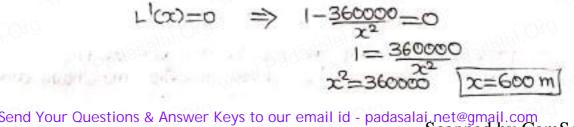
Let the two numbers be x,y

x+y=12 y=12-x ----



```
www.Padasalai.Net 2 (x+x-10) www.TrbTnpsc.com
                      =2(22-10)
                  f(x) = 4(x-5)
                            f(x)=0=>
                                        4(5(-5)=0
                                          7=5
             \rho^{\parallel}(\infty) = 4
   when 2=5 floo=4>0
             f(x) has local minimum at x=5
    at x=5 fox) has minimum value
                  f(B)= 52+ (10-5)2
     smallest value
1 A garden is to be laid out in a rectangular area and
 protected by whire fence, what is the largest possible
 arrea of the fenced garden with motives of wire,
       Let x, y be the longth and breadth
       of the Rectangular garden
given total encing = 40
                                            y
                                                   x
                       2x+2y=40
                          x+y=20
                            y=20-7 -
                 ATECC= TCY
                   ACX) = x(20-x)
                   A(x)=20x-x2
                 A(x) = 20-2x
                                      20-2X=0
                       A(x)=0 =>
                                         -2x = -20
           A^{\dagger}(\alpha) = -2
  when x=10, A^{11}(x)=-2<0
                 when x=10 A(x) is Local maximum
                                           x=10 \Rightarrow y=20-10
             oc=10 Area is maximum
               Largest possible arrea
                                 = xy = 10x10
                                 =100 m2
3 A rectangular page is contain 24cm2 of print. The margins
  at the top and bottom of the page ever 1.5cm and the margins at other sides of the page is 1cm. what should
  be the dimensions of the page so that the acrea of
  the paper is minimum.
           Let x, y be the length and breadth of the
                         Area=24
                                          y=겆 ------
    printed area.
                             xy =24
```





L'(x) = 1 - 360000

```
www.Padasalai.Net
                                www.TrbTnpsc.com
       L"(X) = 720000
 when x=600 L1 cx = 720000 >0
       ==600 LCX) (3 minimum
       x=600 g length of fencing is minimum
    0 \Rightarrow y = \frac{180000}{6000} \qquad y = 3000 \text{ m}
   minimum Length of Pencing = 2+24
                                =600+600 =1200 m
 Find the dimensions of the rectange with maximum
 area that can be inscribed in a circle of radius
  10 CM
        Let 2x, 2y be the length and breadth of
the rectangle.
                2=10
          2x = 2(00090) 2y = 2(109110)
          2x=200000,2y=205in0
        Area=(2x)(2y)
                                                     PCXIY)
             -(20030)(20sine)
             == 200 x 2.009031ns
         FH(19) == 2003 in 25
        丹((0) = 26% (2892年) 之
        A(co)=0 => 400 cos20=0
                          20= V2
                           0=1/4
       A (0) = 400 (-sin20)2
when 0=11/4 A"(0)=-800 sine(11/4)
                   =-800(I)
                   =-800<0
     when 0=1/4 A(0) is maximum
       0=114, Area of rectangle attains maximum.
     0=> 2x=20cosin 12g=20sinin/4
           2x = 20 = 1012 2y=1012
           dimension is 1052, 1052
  prove that among all the rectangles of the
     given perimeter, the square has the maximum area,
```

www.Padasalai.Net www.TrbTnpsc.com Let x, y be the length and breadth of the rectangle. Let L be the given perimeter 2x+2y=L

rectangle. Area = xy $f(x) = x\left(\frac{1}{2} - x\right)$ $A(x) = \frac{1}{2} - x^2$

A(x) = \frac{1}{2} -2x A(x)=0

A100=-2 40

when $x = \frac{1}{4}$ A(x) is maximum (local) $\left[\frac{x - \frac{1}{4}}{4}\right]$ when x=1/4 Area of rectangle is maximum

:c=y=== IEvs a square.

square has, maximum treat.

9) Find the dimensions of the largest rectangle that can be inscribed in a semicircle of rodius rem,

Let 2x, y be the length and breadth of the rectangle.

2x=2xcoso /y=rsino

Area = 2x (y) 2 rcoso rsino

A(0) = 228in20 A(0)= 2200320(2)

A(0)=0 => 2120520=0 000000

Al(0)=422sin20

20=1% 0=11/4

when 0=114, A1(0)=-422sine A1(0) =-482(1) <0

when 0=11/4 ACO) is (Local) maximum

0=11/4 Area of rectangle is maximum.

0今 2x=2xcos74=13反712=128

y=rsining=r=

length=Jzr breadth= x

10) A manufacturer wants to design cun open box having a square base and a surface arrea of 108 sq.cm. Determine the dimensions of the box for the maximum volume,

Let x, x, y be the dimensions of the box.

l=x, b=x, h=y

base area $=x^2$

sides area = 4xy

sarface Area = 108

 $x^{2} + 4xy = 108$

 $4xy = 108 - x^2$

(cuboid) $y = 108 - x^2 - 0$ volume of box = lbh

 $V = x^2y$

(31.07.19) G. Kartlikeyan. THIRUVARUE DT $V(\infty) = 28 \frac{(108 - x^2)}{4x}$

 $V\infty = \frac{1}{4}(108x - x^3)$

13x2=1908

when x=6 v1(0x)==3(6)=-9<0

when x=6 v(xx) is maximum (local)

when x=6 volume of box is maximum

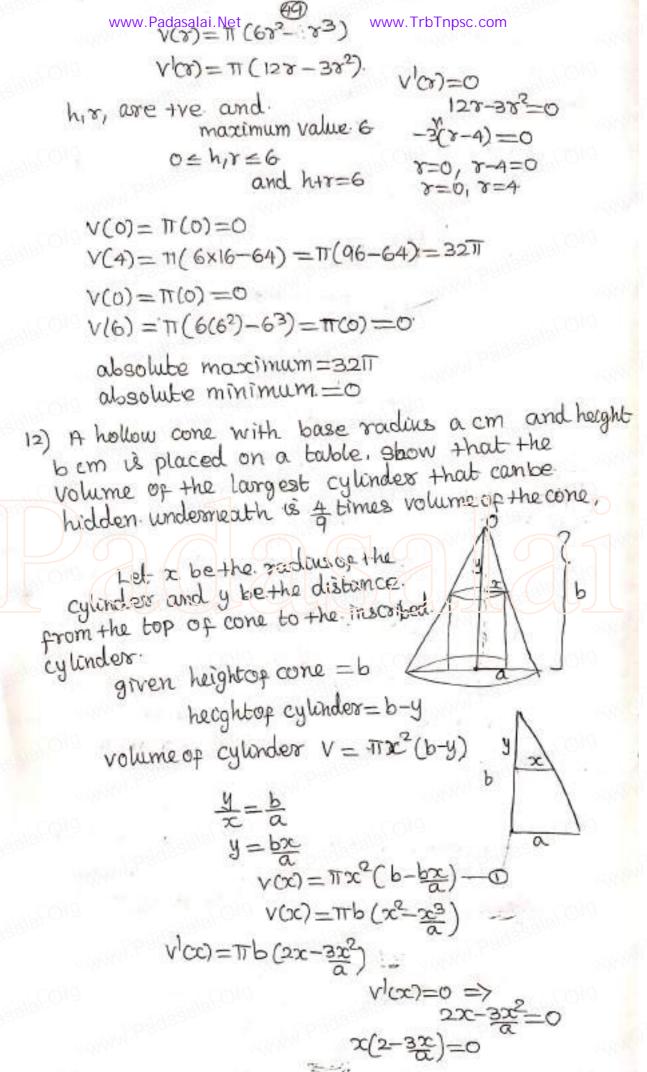
$$0 \Rightarrow y = \frac{108 - 6^2}{4(6)} = \frac{108 - 36}{24} = \frac{72}{24} = 3$$

dimension of box x, x, y = 6cm, 6cm, 3cm

11) The volume of a cylinder is given by the formula V=1172h, Find the greatest and least values of Vif oth=6

volume V=Tr2h

V(7) = TT (272) (6-8)



www.Padasalai.Net Net www.TrbTnpsc.com x=0 or 2− = =0 $V|(x) = \Pi b(2 - \frac{6x}{\alpha})$ when $x = \frac{2a}{3} \Rightarrow v'(x) = \pi b \left(2 - \frac{2}{2} \left(\frac{2a}{3}\right)\right) = \pi b \left(2-4\right)$ =-2116<0 when x==== , v1100<0 . >c==== vcx) is maximum oc=20 volume of cylinder is maximum. (b-bξ) volumeof cyclinder v(x)=πz²(b-bξ) 二丁(等) (1-是等) = T 40 (b(1-3)) $=410^{2}b(\frac{1}{3})$ = \$ (\frac{1}{2} Traceb) max volume of cylinder. = 4 volume of cone. Symmetry allxhas 1) symmetric wir to yaxis (fox) have x terms f(-x,y)=f(x,y) 2) symmetric w-r to x axis f(x,-y)=f(x,y) (all y has yetornes) 3) Bymmetric w-rto origin. if も(-スノータ)=キ(スノタ) (all 2,4 has 22,42 terms) Asymptote:

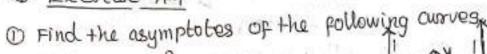
1 Horizontal asymptote lim fcx)=L

(11) vertical asymptote: lim foot= ±00 Send Your Questions & Answer Keys to our email id - padasalai net@gmail.com Scanned by CamScanner

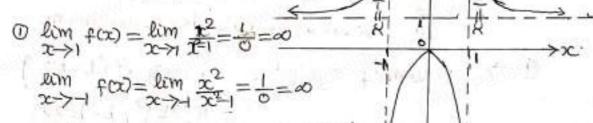
3 slant asymptote:

numerator degree > denominator degree divide the numerator by the denominator we get the slant asymptote:

Exercise 7,9



 $\omega f(x) = \frac{x^2}{x^2+1}$

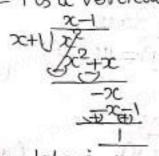


: x=1, x=-1 are vertical asymptotes

 $\frac{1}{2}(x) = \frac{1}{2} = \frac{1}{1+0} = \frac{1}{$ y=1 is a horizondal asymptoixes.

 $\lim_{x \to 1} f(x) = \lim_{x \to 1} \frac{x^2}{x+1} = \frac{1}{0} = \infty$

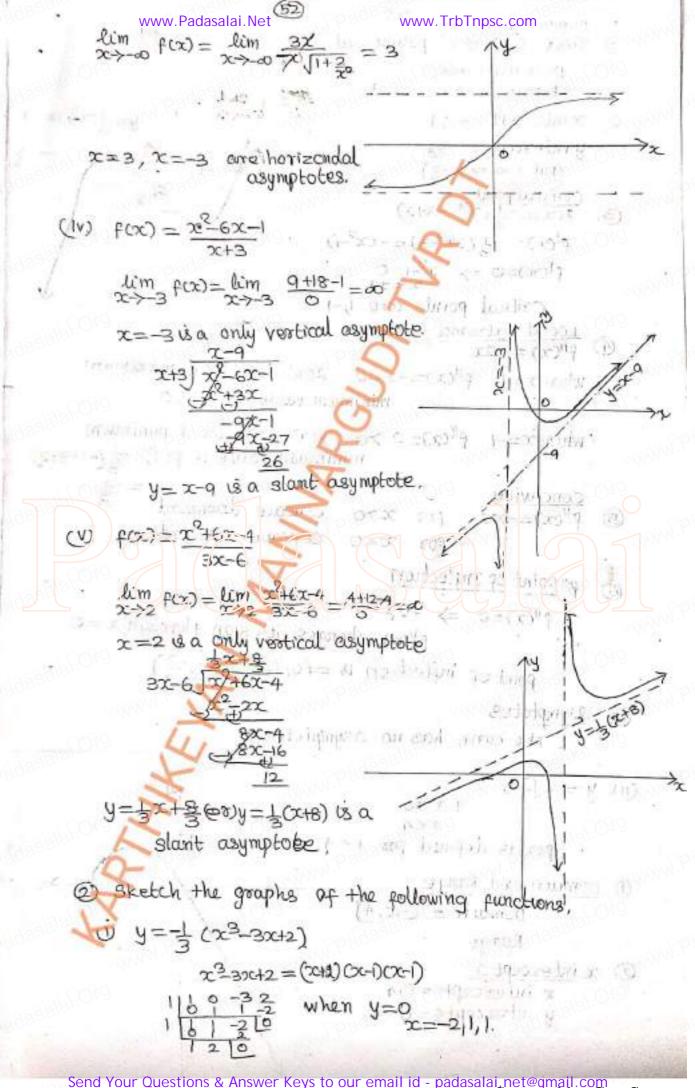
x=-1 is a vertical asymptote

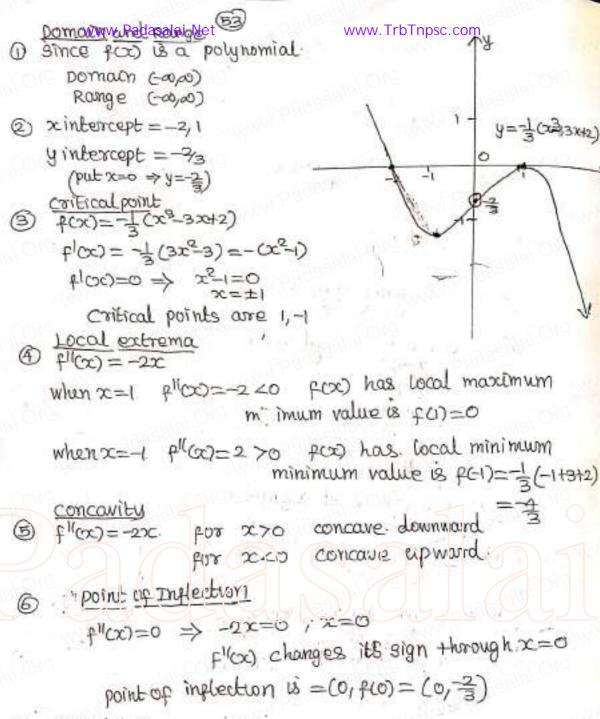


Slant asymptote is y=x-1

x2+2 to .. no vertical asymptotes

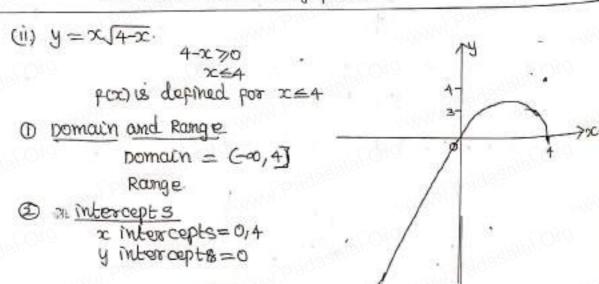
 $\lim_{x\to\infty} f(x) = \lim_{x\to\infty} \frac{3x}{x^2 + 2} = \frac{3}{1+6} = 3$ $\lim_{x\to\infty} f(x) = \lim_{x\to\infty} \frac{3x}{x^2 + 2} = 3$ Send Your Questions & Answer Keys to our email id - padasalai net@gmail.com Scanned by CamScanner





Flow changes its sign through x=0 point of inflection is = (0, f(0) = (0, =3)

@ asymptobes The curve has no asymptotes



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y==== (x==3x42)

$$f(x) = x (4-x)^{\frac{1}{2}}$$

$$f(x) = x \frac{1}{2} (4-x)^{\frac{1}{2}-1} (-1) + (4-x)^{\frac{1}{2}} (1)$$

$$= (4-x)^{\frac{1}{2}} \left[-\frac{x}{2} + (4-x) \right]$$

$$= (4-x)^{\frac{1}{2}} \left[-\frac{x+8-2x}{2} \right]$$

$$f(x) = \frac{8-3x}{2(4-x)^{\frac{1}{2}}}$$

$$f(x) = 0 \Rightarrow 8-3x = 0$$

when x=4, p(x), does not exist

critical numbers = 8/914

4) Local Extrema

$$f^{\parallel}(x) = \frac{8-3x}{2(4-x)^{\frac{1}{2}}}$$

$$f^{\parallel}(x) = \frac{1}{2} \frac{(4-x)^{\frac{1}{2}}(-3) - (8-3x)\frac{1}{2}(4-x)^{\frac{1}{2}}(-1)}{(4-x)}$$

$$= \underbrace{(4-x)^{1/2}}_{2(4-x)} \left[\underbrace{(4-x)(-3) + \frac{1}{2}}_{(8-3x)} (8-3x) \right]$$

$$= \underbrace{\frac{1}{2(4-x)^3/2}}_{2(4-x)^3/2} \left[-G(4-x) + \frac{1}{3} - 3x^2 \right]$$

 $= \frac{1}{2(4-x)^{3/2}} \left[-24+6x+8-3x \right] = \frac{1}{4(4-x)^{3/2}} \left(\frac{3x-16}{2} \right)$ i) when x=8/3 $f'(0x) = \frac{1}{4(4-8/3)^3} (8\frac{8}{8}-16) = \frac{-8}{4(4/3)^3} < 0$

when x=8/3 floor co fox has Local maximum max value = f(8) = \$ [4-8] = \$ [3-]

= 8/3 = 16

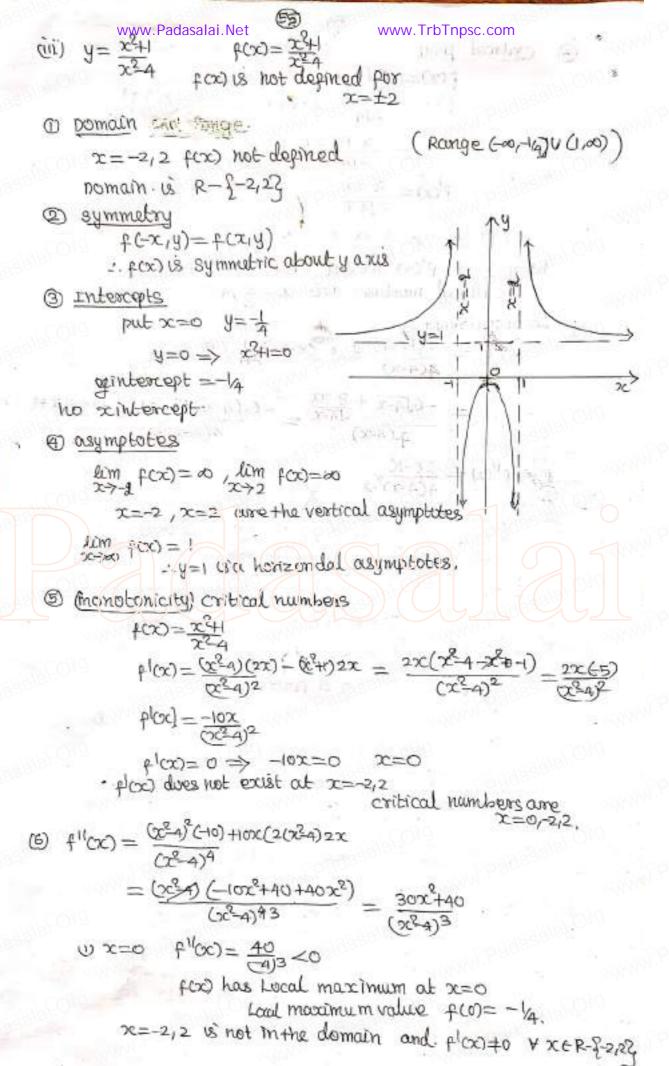
(b) concavity $f^{(1)}(x) = 0 \Rightarrow \frac{3x-16}{4(4-x)^{3}2} = 0$ 3x-16=0 x=16 But

domain of f(x) is (x=4) (-0,4] we test only on the domain.

bonnes its sign of relationary, In (-00,4] peop is does not changes the sign-cut x=163

No point of inflection. (No curve exast at 6,2)

6) asymptotes No asymptotes,



· @ concounity

does not exist at x = -2/2

Interval value
$$f'(x) = \frac{30x^2+40}{Cx^2+9^3}$$

pcx) is concave upward on (-00,-2), (2,00) downwardon (2,2)

(No point of Inflection,

- (1) Domain (-00,00)
 - Range (o(1)
- 2 Intercept no oxintencept (Put y == 0)
 - y intercept = 1
- asymptotes

a critical numbers.

$$e(cx) = \frac{1}{(1+e^{-x})^2} \frac{(-e^{-x})}{(1+e^{-x})^2} > 0$$
 no critical number

- The critical numbers in no sign changes of flow no Local extremun
- @ concavity

vity
$$f''(x) = \frac{(1+e^{-x})^2(e^{-x})}{(1+e^{-x})^4} - e^{x}(2(1+e^{-x})(-e^{-x})$$

$$= \frac{(\text{He}^{x})(-e^{-x}e^{2x}+2e^{2})}{(\text{He}^{x})^{43}} = \frac{e^{x}(e^{x}-1)}{(\text{He}^{x})^{3}}$$

$$e^{1/(x)}=0 \Rightarrow e^{-2x} - e^{x}=0$$

$$e^{-x}(e^{-x}-1)=0$$

$$e^{-x}=1$$

$$-x=\log 1 \quad |x=0|$$

Intervals (-00,0), (0,00)

when Go, o) flow to concave upward when xeGo,0), floor o concave downward.

1 Point of Inglection

fice changes its sign through x=0 point of inflection at x=0i.e. $(0,f(0)=(0,\frac{1}{14})=(0,\frac{1}{2})$

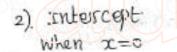
point of inflection. is (01/2)

(v)
$$y = \frac{2^3}{24} - \log x$$

orhis sum deleted in ramit medium book)

fix) exists only for 2>0

w domain (0,0).



when x=0 wgx. >- = no y intercept.

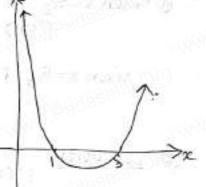
$$y=0 \Rightarrow \frac{x^3}{24} = \log x$$

x=3

3) asymptotes.

 $\lim_{\infty \to 0} f(x) = \infty$

x=0 is a vertical asymptotes



4) evitical numbers

$$p(x) = \frac{3x^{2}}{24} - \frac{1}{x} = \frac{x^{2} - 8}{8x}$$

$$p(x) = 0 \Rightarrow \frac{x^{2} - 8}{8x} = 0$$

$$x^{2} - 8 = 0 \quad x = \pm 0$$

 $x^2-8=0$ $x=\pm 2\sqrt{2}$ x>0 $(x=2\sqrt{2})$ when x=0, flow does no exist (also fox) not exist) x=0 is not a critical number

x=215 is only critical number.

$$f'(x) = \frac{x^2 - 8^{-}}{8x}.$$

$$f''(x) = \frac{8x(2x) - (x^2 - 8)(8)}{(8x)^2}$$

$$= \frac{16x^2 - 8x^2 + 64}{64x^2} = \frac{8x^2 + 8x8}{64x^2}$$

$$f''(x) = \frac{8(x^2 + 8)}{864x^2} = \frac{x^2 + 8}{8x^2} > 0$$

when

$$x=2\sqrt{3}$$
 $e^{1/3}(5c) = \frac{8+8}{8(8)} = \frac{16^{1}}{644} > 0$

fix) has a local minimum at x=252

minimum value=f(252)

$$= \frac{(2/2)^3 - (\log 2\sqrt{2})}{24}$$

$$= \frac{2/6\sqrt{2} - (\log 2\sqrt{2})}{324}$$

$$= \frac{2\sqrt{2} - (\log 2\sqrt{2})}{324}$$

6) floor or - for is always concave upward on CO/CO)

7) no change of sign of flow).

No point of inflection.

G. Karthikeyan 9715634957 Need suggestions (whatsapponly)