

# ELECTROMAGNETIC INDUCTION AND ALTERNATING CURRENT

PHYSICS - VOL 1

UNIT - 4



NAME :

STANDARD : 12 SECTION :

SCHOOL :

EXAM NO :

உவப்பத் தலைக்கூடி உள்ளப் பிரிதல்

அனைத்தே புலவர் தொழில்

மகிழும் படியாக கூடிப்பழகி இனி இவரை எப்போது காண்போம் என்று வருந்தி நினைக்கும்

படியாகப் பிரிதல் புலவரின் தொழிலாகும்

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**PART - II 2 MARK QUESTIONS & ANSWERS****1. Define magnetic flux.**

- ♣ The magnetic flux through an area 'A' in a magnetic field is defined as the number of magnetic field lines passing through that area normally.
- ♣ The S.I unit of magnetic flux is  $T\ m^2$  (or) **weber**

**2. Define electromagnetic induction.**

- ♣ Whenever the magnetic flux linked with a closed coil changes, an emf is induced and hence an electric current flows in the circuit.
- ♣ This emf is called induced emf and the current is called induced current. This phenomenon is called electromagnetic induction.

**3. What is the importance of electromagnetic induction?**

- ♣ There is an ever growing demand for electric power for the operation of almost all the devices used in present day life.
- ♣ All these are met with the help of electric generators and transformer which function on electromagnetic induction.

**4. State Faraday's laws of electromagnetic induction.**

- Whenever magnetic flux linked with a closed circuit changes, an emf is induced in the circuit.
- The magnitude of induced emf in a closed circuit is equal to the time rate of change of magnetic flux linked with the circuit.

**5. State Flemming's right hand rule.**

- ♣ The thumb, index finger and middle finger of right hand are stretched out in mutually perpendicular directions. If index finger points the direction of magnetic field and the thumb points the direction of motion of the conductor, then the middle finger will indicate the direction of the induced current.
- ♣ Flemming's right hand rule is also known as **generator rule**.

**6. What is called inductor?**

- ♣ Inductor is a device used to store energy in a magnetic field when an electric current flows through it.  
(e.g.) solenoids and toroids

**7. What is called self induction?**

- ♣ The phenomenon of inducing an emf in a coil, when the magnetic flux linked with the coil itself changes is called self induction.
- ♣ The emf induced is called self-induced emf.

**8. Define self inductance or coefficient of self induction.**

- ♣ Self inductance of a coil is defined as the flux linkage of the coil, when 1 A current flows through it.
- ♣ Its S.I unit is  $H$  (or)  $Wb\ A^{-1}$  (or)  $V\ s\ A^{-1}$  and its dimension is  $[M\ L^2\ T^{-2}\ A^{-2}]$

**9. Define the unit of self inductance (one henry)**

- ♣ The inductance of the coil is one henry, if a current changing at the rate of  $1\ A\ s^{-1}$  induces an opposing emf of 1 V in it.

**10. What is called mutual induction?**

- ♣ When an electric current passing through a coil changes with time, an emf is induced in the neighbouring coil. This phenomenon is known as mutual induction and the emf is called mutually induced emf.

**11. Define mutual inductance or coefficient of mutual induction.**

- ♣ Mutual inductance is also defined as the opposing emf induced in the one coil, when the rate of change of current through the other coil is  $1\ A\ s^{-1}$
- ♣ Its S.I unit is  $H$  (or)  $Wb\ A^{-1}$  (or)  $V\ s\ A^{-1}$  and its dimension is  $[M\ L^2\ T^{-2}\ A^{-2}]$

**12. What the methods of producing induced emf?**

- ♣ By changing the magnetic field 'B'
- ♣ By changing the area 'A' of the coil
- ♣ By changing the relative orientation 'θ' of the coil with magnetic field.

**13. How an emf is induced by changing the magnetic field?**

- ♣ Change in magnetic flux of the field is brought about by,
  - The relative motion between the circuit and the magnet
  - Variation in current flowing through the nearby coil

**14. What is called transformer?**

- ♣ It is a stationary device used to transform electrical power from one circuit to another without changing its frequency.

- ♣ The applied alternating voltage is either increased or decreased with corresponding decrease or increase in current in the circuit.

**15. Distinguish between step up and step down transformer.**

Step up transformer	Step down transformer
If the transformer converts an alternating current with low voltage in to an alternating current with high voltage is called step up transformer.	If the transformer converts an alternating current with high voltage in to an alternating current with low voltage is called step down transformer.

**16. State the principle of transformer.**

- ♣ The principle of transformer is the **mutual induction** between two coils. (i.e.) when an electric current passing through a coil changes with time, and emf is induced in the other coil.

**17. Define the efficiency of the transformer.**

- ♣ The efficiency ( $\eta$ ) of a transformer is defined as the ratio of the useful output power to the input power.  $\therefore \eta = \frac{\text{output power}}{\text{input power}} \times 100\%$

**18. Define Sinusoidal alternating voltage.**

- ♣ If the waveform of alternating voltage is a sine wave, then it is known as sinusoidal alternating voltage and it is given by,  $v = V_m \sin \omega t$

**19. Define mean value or average value of AC.**

- ♣ The mean or average value of alternating current is defined as the average of all values of current over a positive half cycle or negative half cycle.

$$I_{avg} = \frac{2I_m}{\pi} = 0.6371 I_m$$

**20. Define RMS value of AC.**

- ♣ The root mean square value of an alternating current is defined as the square root of the mean of the square of all currents over one cycle.

$$I_{RMS} = \frac{I_m}{\sqrt{2}} = 0.707 I_m$$

**21. Define effective value of alternating current.**

- ♣ RMS value of AC is also called effective value of AC
- ♣ The effective value of AC ( $I_{eff}$ ) is defined as the value of steady current which when flowing through a given circuit for a given time produces the same amount of heat as produced by the alternating current when flowing through the same circuit for the same time.

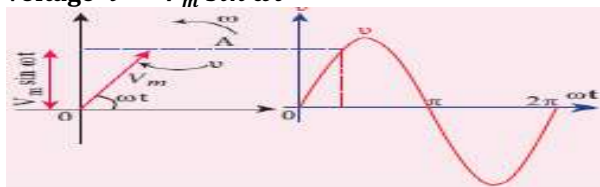
**22. The common house hold appliances, the voltage rating is specified as 230 V, 50 Hz. What is the meaning of it?**

- ♣ The voltage rating specified in the common house hold appliances indicates the RMS value or effective value of AC. (i.e.)  $V_{eff} = 230\text{ V}$
- ♣ Its peak value will be,  
 $V_m = V_{eff} \sqrt{2} = 230 \times 1.414 = 325\text{ V}$
- ♣ Also 50 Hz indicates, the frequency of domestic AC supply.

**23. Define phasor and phasor diagram.**

- ♣ A sinusoidal alternating voltage or current can be represented by a vector which rotates about the origin in anti-clockwise direction at a constant angular velocity ' $\omega$ '. Such a rotating vector is called a phasor.
- ♣ The diagram which shows various phasors and phase relations is called phasor diagram.

**24. Draw the phasor diagram for an alternating voltage  $v = V_m \sin \omega t$**



**25. Define inductive reactance.**

- ♣ The resistance offered by the inductor in an AC circuit is called inductive reactance and it is given by ;  $X_L = \omega L = 2\pi f L$
- ♣ Its unit is  $\text{ohm } (\Omega)$

**26. An inductor blocks AC but it allows DC. Why?**

- ♣ The DC current flows through an inductor produces uniform magnetic field and the magnetic flux linked remains constant. Hence there is no self induction and self induced emf (opposing emf). So DC flows through an inductor.
- ♣ But AC flows through an inductor produces time varying magnetic field which in turn induces self induced emf and this opposes any change in the current. Since AC varies both in magnitude and direction, its flow is opposed by the back emf induced in the inductor and hence inductor blocks AC

**27. Define capacitive reactance.**

- ♣ The resistance offered by the capacitor is an AC circuit is called capacitive reactance and it is given by ;  $X_C = \frac{1}{\omega C} = \frac{1}{2\pi f C}$
- ♣ Its unit is  $\text{ohm } (\Omega)$

**28. A capacitor blocks DC but it allows AC. Why?**

- ♣ When DC flows through capacitor, electrons flow from negative terminal and accumulated at one plate making it negative and hence another plate becomes positive. This process is known as charging and once capacitor is fully charged, the current will stop and we say capacitor blocks DC.
- ♣ But AC flows through capacitor, the electron flow in one direction while charging the capacitor and its direction is reversed while discharging. Though electrons flow in the circuit, no electron crosses the gap between the plates. In this way, AC flows through a capacitor.

**29. Define resonance.**

- ♣ When the frequency of the applied source is equal to the natural frequency of the RLC circuit, the current in the circuit reaches its maximum value. Then the circuit is said to be in electrical resonance.
- ♣ The frequency at which resonance takes place is called resonant frequency.
- ♣ Hence the condition for resonance is :  $X_L = X_C$

**30. What are the applications of series RLC resonant circuit?**

- ♣ RLC circuits have many applications like filter circuits, oscillators, voltage multipliers etc.,
- ♣ An important use of series RLC resonant circuits is in the tuning circuits of radio and TV systems. To receive the signal of a particular station among various broadcasting stations at different frequencies, tuning is done.

**31. Resonance will occur only in LC circuits. Why?**

- ♣ When the circuit contains both L and C, then voltage across L and C cancel one another when  $V_L$  and  $V_C$  are  $180^\circ$  out of phase and the circuit becomes purely resistive.
- ♣ This implies that resonance will not occur in a RL and RC circuits.

**32. Define power in an AC circuit.**

- ♣ Power of a circuit is defined as the rate of consumption of electric energy in that circuit.
- ♣ It is the product of the voltage and current.

**33. Define power factor.**

- ♣ Power factor ( $\cos \phi$ ) of a circuit is defined as the cosine of the angle of lead or lag
- ♣ Power factor is also defined as the ratio of true power to the apparent power.

**34. Define wattless current.**

- ♣ If the power consumed by an AC circuit is zero, then the current in that circuit is said to be wattless current.
- ♣ This wattless current happens in a purely inductive or capacitive circuit.

**35. What are called LC oscillations?**

- ♣ Whenever energy is given to a circuit containing a pure inductor of inductance L and a capacitor of capacitance C, the energy oscillates back and forth between the magnetic field of the inductor and the electric field of the capacitor.
- ♣ Thus the electrical oscillations of definite frequency are generated. These oscillations are called LC oscillations.

**36. Define Flux linkage.**

- ♣ The product of magnetic flux ( $\Phi_B$ ) linked with each turn of the coil and the total number of turns (N) in the coil is called flux linkage ( $N\Phi_B$ )

**37. Define impedance of RLC circuit.**

- ♣ The effective opposition by resistor, inductor and capacitor to the circuit current in the series RLC circuit is called impedance (Z)

$$Z = \sqrt{R^2 + (X_L - X_C)^2}$$

**PART - III 3 MARK QUESTIONS AND ANSWERS****1. State and explain Faraday's laws of electromagnetic induction.****Faraday's first law :**

- Whenever magnetic flux linked with a closed circuit changes, an emf is induced in the circuit.
- The induced emf lasts so long as the change in magnetic flux continues.

**Faraday's second law :**

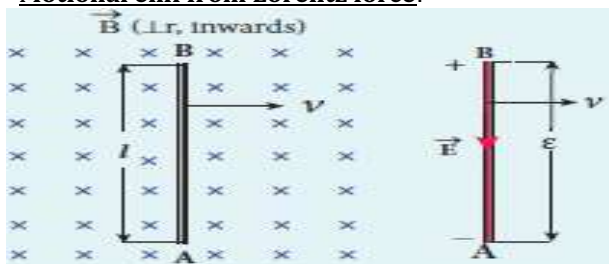
- The magnitude of induced emf in a closed circuit is equal to the time rate of change of magnetic flux linked with the circuit.
- If magnetic flux linked with the coil changes by  $d\Phi_B$  in time  $dt$ , then the induced emf is given by,

$$\epsilon = - \frac{d\Phi_B}{dt}$$

- The negative sign in the above equation gives the direction of the induced current
- If a coil consisting of 'N' turns, then

$$\epsilon = -N \frac{d\Phi_B}{dt} = - \frac{d(N\Phi_B)}{dt}$$

- Here  $N\Phi_B$  is called flux linkage.

**2. Obtain an expression for motional emf from Lorentz force.****Motional emf from Lorentz force:**

- Consider a straight conductor rod AB of length 'l' in a uniform magnetic field  $\vec{B}$  which is directed perpendicularly in to plane of the paper.
- Let the rod move with a constant velocity  $\vec{v}$  towards right side.
- When the rod moves, the free electrons present in it also move with same velocity  $\vec{v}$  in  $\vec{B}$
- As a result, the Lorentz force acts on free electron in the direction from B to A and it is given by,

$$\vec{F}_B = -e(\vec{v} \times \vec{B}) \quad \text{----- (1)}$$

- Due to this force, all the free electrons are accumulate at the end A which produces the potential difference across the rod which in turn establishes an electric field  $\vec{E}$  directed along BA
- Due to the electric field, the Coulomb force starts acting on the free electron along AB and it is given by,

$$\vec{F}_E = -e\vec{E} \quad \text{----- (2)}$$

- At equilibrium,  $|\vec{F}_B| = |\vec{F}_E|$   
 $|-e(\vec{v} \times \vec{B})| = |-e\vec{E}|$   
 $B e v \sin 90^\circ = e E$   
 $B v = E \quad \text{----- (3)}$

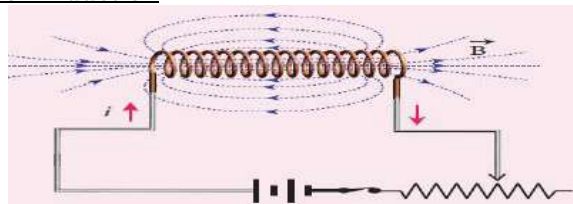
- The potential difference between two ends of the rod is ,

$$V = E l = B v l$$

- Thus the Lorentz force on the free electrons is responsible to maintain this potential difference and hence produces an emf

$$\epsilon = B l v \quad \text{----- (4)}$$

- Since this emf is produced due to the movement of the rod, it is often called as **motional emf**.

**3. Explain self induction and define coefficient of self induction on the basis of (1) magnetic flux and (2) induced emf****Self induction :**

- When an electric current flowing through a coil changes, an emf is induced in the same coil. This phenomenon is known as self induction. The emf induced is called self-induced emf.
- Let  $\Phi_B$  be the magnetic flux linked with each turn of the coil of turn 'N', then total flux linkage ( $N\Phi_B$ ) is directly proportional to the current 'i'

$$N\Phi_B \propto i \quad (\text{or}) \quad N\Phi_B = L i$$

$$\therefore L = \frac{N\Phi_B}{i}$$

- Where, L  $\rightarrow$  constant called coefficient of self induction (or) self inductance

- When the current (i) changes with time, an emf is induced in the coil and it is given by,

$$\epsilon = - \frac{d(N\Phi_B)}{dt} = - \frac{d(L i)}{dt} = -L \frac{di}{dt}$$

$$\therefore L = - \frac{\epsilon}{\left(\frac{di}{dt}\right)} \quad \text{----- (2)}$$

**Coefficient of self induction - Definition :**

- Self inductance of a coil is defined as the flux linkage of the coil, when 1 A current flows through it.
- Self inductance of a coil is also defined as the opposing emf induced in the coil, when the rate of change of current through the coil is  $1 \text{ A s}^{-1}$

**4. How will you define the unit of inductance?****Unit of inductance :**

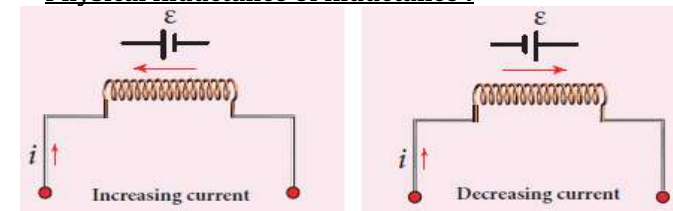
- Inductance is a scalar and its unit is  $\text{Wb A}^{-1}$  (or)  $\text{V s A}^{-1}$  (or) **henry (H)**
- Its dimension is  $[M L^2 T^{-2} A^{-2}]$

**Definition - 1 :**

- The self inductance is given by,  $L = \frac{N\Phi_B}{i}$
- The inductance of the coil is one henry if a current of 1 A produces unit flux linkage in the coil.

**Definition - 2 :**

- The self inductance is given by,  $L = - \frac{\epsilon}{\left(\frac{di}{dt}\right)}$
- The inductance of the coil is one henry if a current changing at the rate of  $1 \text{ A s}^{-1}$  induces an opposing emf of 1 V in it.

**5. Discuss the physical significance of inductance.****Physical significance of inductance :**

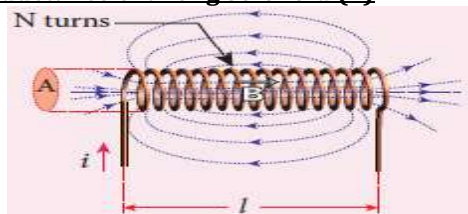
- Generally inertia means opposition to change the state of the body.
- In translational motion, mass is a measure of inertia, whereas in rotational motion, moment of inertia is a measure of rotational inertia.



- Similarly inductance plays the same role in a circuit as the mass and moment of inertia play in mechanical motion.
- When a circuit is switched on, the increasing current induces an emf which opposes the growth of current in a circuit.
- Similarly, when a circuit is broken, the decreasing current induces an emf in the reverse direction which opposed the decay of the current.
- Thus inductance on the coil opposes any change in current and tries to maintain the original state.

**6. Assuming that the length of the solenoid is large when compared to its diameter, find the equation for its inductance.**

**Self inductance of a long solenoid (L) :**



- Consider a long solenoid of length 'l', area of cross section 'A' having 'N' number of turns
- Let 'n' be number of turns per unit length (i.e.) turn density
- When an electric current 'i' is passed through the coil, a magnetic field at any point inside the solenoid is,

$$B = \mu_0 n i$$

- Due to this field, the magnetic flux linked with the solenoid is,

$$\Phi_B = \oint \vec{B} \cdot d\vec{A} = \oint B dA \cos 90^\circ = B A$$

$$\Phi_B = [\mu_0 n i] A$$

- Hence the total magnetic flux linked (i.e.) flux linkage

$$N \Phi_B = N \mu_0 n i A = (n l) \mu_0 n i A$$

$$N \Phi_B = \mu_0 n^2 i A l$$

- Let 'L' be the self inductance of the solenoid, then

$$L = \frac{N \Phi_B}{i} = \frac{\mu_0 n^2 i A l}{i}$$

$$L = \mu_0 n^2 A l$$

- If the solenoid is filled with a dielectric medium of relative permeability ' $\mu_r$ ', then

$$L = \mu_0 \mu_r n^2 A l = \mu n^2 A l$$

- Thus, the inductance depends on

(i) geometry of the solenoid

(ii) medium present inside the solenoid

**7. An inductor of inductance 'L' carries an electric current 'i'. How much energy is stored while establishing the current in it?**

**Energy stored in a solenoid :**

- Whenever a current is established in the circuit, the inductance opposes the growth of the current.
- To establish the current, work has to be done against this opposition. This work done is stored as magnetic potential energy.
- Consider an inductor of negligible resistance, the induced emf ' $\epsilon$ ' at any instant 't' is

$$\epsilon = -L \frac{di}{dt}$$

- Let 'dW' be the workdone in moving a charge 'dq' in a time 'dt' against the opposition, then

$$dW = -\epsilon dq = -\epsilon i dt$$

$$dW = -\left[-L \frac{di}{dt}\right] i dt = L i di$$

- Total work done in establishing the current 'i' is

$$W = \int dW = \int L i di = L \left[\frac{i^2}{2}\right]_0^i = \frac{1}{2} L i^2$$

- This work done is stored as magnetic potential energy. (i.e.)

$$U_B = \frac{1}{2} L i^2$$

- The energy stored per unit volume of the space is called **energy density** ( $u_B$ ) and it is given by,

$$u_B = \frac{\text{energy } (U_B)}{\text{volume } (A l)} = \frac{\frac{1}{2} L i^2}{A l} = \frac{1}{2} \frac{(\mu_0 n^2 A l) i^2}{A l}$$

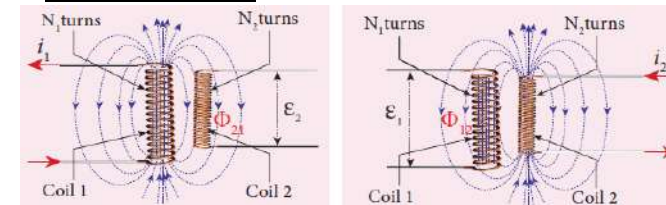
$$u_B = \frac{\mu_0 n^2 i^2}{2}$$

$$u_B = \frac{B^2}{2 \mu_0}$$

$$[\because B = \mu_0 n i]$$

**8. Explain mutual induction. Define coefficient of mutual induction on the basis of (1) magnetic flux and (2) induced emf**

**Mutual induction :**



- When an electric current passing through a coil changes with time, an emf is induced in the neighbouring coil. This phenomenon is known as mutual induction and the emf is called mutually induced emf.

- Consider two coils 1 and 2 which are placed close to each other. If an electric current ' $i_1$ ' is sent through coil -1, the magnetic field produced by it is also linked with the coil -2

- Let ' $\Phi_{21}$ ' be the magnetic flux linked with each turn of the coil-2 of  $N_2$  turns due to coil -1, then the total flux linked with coil -2 is proportional to the current ' $i_1$ ' in the coil -1 (i.e.)

$$N_2 \Phi_{21} \propto i_1 \quad (\text{or}) \quad N_2 \Phi_{21} = M_{21} i_1$$

$$\therefore M_{21} = \frac{N_2 \Phi_{21}}{i_1} \quad \text{--- (1)}$$

- Here  $M_{21} \rightarrow$  constant called coefficient of mutual induction or mutual inductance coil -2 with respect to coil -1

- When the current ' $i_1$ ' changes with time, an emf ' $\epsilon_2$ ' is induced in coil -2 and it is given by,

$$\epsilon_2 = -\frac{d(N_2 \Phi_{21})}{dt} = -\frac{d(M_{21} i_1)}{dt} = -M_{21} \frac{di_1}{dt}$$

$$\therefore M_{21} = -\frac{\epsilon_2}{\left(\frac{di_1}{dt}\right)} \quad \text{--- (2)}$$

- Similarly,

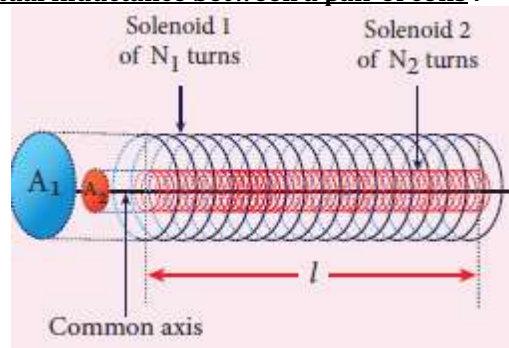
$$M_{12} = \frac{N_1 \Phi_{12}}{i_2} \quad \text{--- (3)}$$

$$\& M_{12} = -\frac{\epsilon_1}{\left(\frac{di_2}{dt}\right)} \quad \text{--- (4)}$$

- Here  $M_{21} \rightarrow$  constant called coefficient of mutual induction or mutual inductance coil -2 with respect to coil -1

**Coefficient of mutual induction - Definition :**

- ♣ The mutual inductance is defined as the flux linkage of the one coil, when 1 A current flow through other coil.
- ♣ Mutual inductance is also the opposing emf induced in one coil, when the rate of change of current through other coil is  $1 \text{ A s}^{-1}$

**9. Show that the mutual inductance between a pair of coils is same ( $M_{12} = M_{21}$ )****Mutual inductance between a pair of coils :**

- ♣ Consider two long co-axial solenoids of same length ' $l$ '
- ♣ Let  $A_1$  and  $A_2$  be the area of cross section of the solenoids. Here  $A_1 > A_2$
- ♣ Let the turn density of these solenoids are  $n_1$  and  $n_2$  respectively.
- ♣ Let ' $i_1$ ' be the current flowing through solenoid -1, then the magnetic field produced inside it is,

$$B_1 = \mu_0 n_1 i_1$$

- ♣ Hence the magnetic flux linked with each turn of solenoid -2 due to solenoid -1 is

$$\Phi_{21} = \oint \vec{B}_1 \cdot d\vec{A}_2 = \oint B_1 dA_2 \cos 0^\circ = B_1 A_2$$

$$\Phi_{21} = (\mu_0 n_1 i_1) A_2$$

- ♣ Then total flux linkage of solenoid -2 of  $N_2$  turns is
- ♣ So the mutual inductance of solenoid -2 with respect to solenoid -1 is given by,

$$M_{21} = \frac{N_2 \Phi_{21}}{i_1} = \frac{\mu_0 n_1 n_2 A_2 l i_1}{i_1}$$

$$M_{21} = \mu_0 n_1 n_2 A_2 l \quad \text{--- (2)}$$

- ♣ Similarly, Let ' $i_2$ ' be the current flowing through solenoid -2, then the magnetic field produced inside it is,

$$B_2 = \mu_0 n_2 i_2$$

- ♣ Hence the magnetic flux linked with each turn of solenoid -1 due to solenoid -2 is

$$\Phi_{12} = \oint \vec{B}_2 \cdot d\vec{A}_1 = \oint B_2 dA_1 \cos 0^\circ = B_2 A_1$$

$$\Phi_{12} = (\mu_0 n_2 i_2) A_1$$

- ♣ Then total flux linkage of solenoid -1 of  $N_1$  turns is
- ♣ So the mutual inductance of solenoid -1 with respect to solenoid -2 is given by,

$$M_{12} = \frac{N_1 \Phi_{12}}{i_2} = \frac{\mu_0 n_1 n_2 A_2 l i_2}{i_2}$$

$$M_{12} = \mu_0 n_1 n_2 A_2 l \quad \text{--- (4)}$$

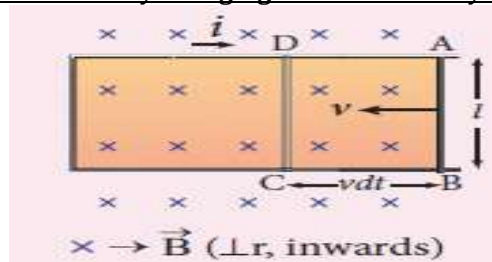
- ♣ From equation (2) and (4),  $M_{12} = M_{21}$
- ♣ In general, the mutual inductance between two long co-axial solenoids is given by

$$M = \mu_0 n_1 n_2 A_2 l$$

- ♣ If the solenoid is filled with a dielectric medium of relative permeability ' $\mu_r$ ', then

$$M = \mu_0 \mu_r n_1 n_2 A_2 l = \mu n_1 n_2 A_2 l$$

- ♣ Thus, the inductance depends on
  - geometry of the solenoids
  - medium present inside the solenoids
  - proximity of the two solenoids

**10. How will you induce an emf by changing the area enclosed by the coil.****EMF induced by changing area enclosed by the coil**

- ♣ Consider a conducting rod of length ' $l$ ' moving with a velocity ' $v$ ' towards left on a rectangular metallic frame work.
- ♣ The whole arrangement is placed in a uniform magnetic field ' $\vec{B}$ ' acting perpendicular to the plane of the coil inwards.

- ♣ As the rod moves from AB to DC in a time ' $dt$ ', the area enclosed by the loop and hence the magnetic flux through the loop decreases.

- ♣ The change in magnetic flux in time ' $dt$ ' is

$$d\Phi_B = B dA = B (l \times v dt)$$

$$\frac{d\Phi_B}{dt} = B l v$$

- ♣ This change in magnetic flux results and induced emf and it is given by,

$$\epsilon = \frac{d\Phi_B}{dt}$$

$$\epsilon = B l v$$

- ♣ This emf is called motional emf. The direction of induced current is found to be clockwise from Fleming's right hand rule.

**11. Explain various energy losses in a transformer.****Energy losses in a transformer :****(i) Core loss or Iron loss :**

- ♣ Hysteresis loss and eddy current loss are known as core loss or Iron loss.
- ♣ When transformer core is magnetized or demagnetized repeatedly by the alternating voltage applied across primary coil, hysteresis takes place and some energy is lost in the form of heat. It is minimized by using **silicone steel** in making transformer core.
- ♣ Alternating magnetic flux in the core induces eddy currents in it. Therefore there is energy loss due to the flow of eddy current called eddy current loss. It is minimized by using **very thin laminations** of transformer core.

**(ii) Copper loss :**

- ♣ The primary and secondary coils in transformer have electrical resistance.
- ♣ When an electric current flows through them, some amount of energy is dissipated due to Joule's heating and it is known as copper loss. It is minimized by using **wires of larger diameter (thick wire)**

**(iii) Flux leakage :**

- ♣ The magnetic flux linked with primary coil is not completely linked with secondary. Energy loss due to this flux leakage is minimized by **winding coils one over the other**.

## 12. Discuss the advantages of AC in long distance power transmission.

### Long distance power transmission :

- ♣ The electric power is generated in power stations using AC generators are transmitted over long distances through transmission lines to reach towns or cities. This process is called **power transmission**.
- ♣ But during power transmission, due to Joules's heating ( $I^2 R$ ) in the transmission lines, sizable fraction of electric power is lost.
- ♣ This power loss can be reduced either by reducing current ( $I$ ) or by reducing resistance ( $R$ )
- ♣ Here the resistance 'R' can be reduced with thick wires of copper or aluminium. But this increases the cost of production of transmission lines and hence this method is not economically viable.
- ♣ Thus by using transformer, the current is reduced by stepped up the alternating voltage and thereby reducing power losses to a greater extent.

### Illustration :

- ♣ Let an electric power of 2 MW is transmitted through the transmission lines of resistance  $40 \Omega$  at 10 kV and 100 kV

(i)  $P = 2 \text{ MW}$ ,  $R = 40 \Omega$ ,  $V = 10 \text{ kV}$ , then

$$I = \frac{P}{V} = \frac{2 \times 10^6}{10 \times 10^3} = 200 \text{ A}$$

$$\text{Power loss} = I^2 R = (200)^2 \times 40 = 1.6 \times 10^6 \text{ W}$$

$$\% \text{ of Power loss} = \frac{1.6 \times 10^6}{2 \times 10^6} = 0.8 = \mathbf{80 \%}$$

(ii)  $P = 2 \text{ MW}$ ,  $R = 40 \Omega$ ,  $V = 100 \text{ kV}$ , then

$$I = \frac{P}{V} = \frac{2 \times 10^6}{100 \times 10^3} = 20 \text{ A}$$

$$\text{Power loss} = I^2 R = (20)^2 \times 40 = 0.016 \times 10^6 \text{ W}$$

$$\% \text{ of power loss} = \frac{0.016 \times 10^6}{2 \times 10^6} = 0.008 = \mathbf{0.8 \%}$$

- ♣ Thus it is clear that, when an electric power is transmitted at high voltage, the power loss is reduced to a large extent.
- ♣ So at transmitting point the voltage is increased and the corresponding current is decreased by using step-up transformer. At receiving point, the

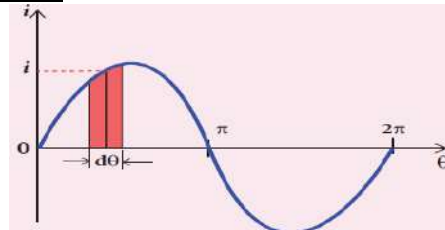
voltage is decreased and the current is increased by using step-down transformer

## 13. Obtain the expression for average value of alternating current.

### Average or Mean value of AC :

- ♣ The average value of AC is defined as the average of all values of current over a positive half-cycle or negative half-cycle.

### Expression :



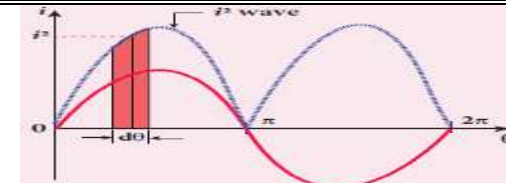
- ♣ The average or mean value of AC over one complete cycle is zero. Thus the average or mean value is measured over one half of a cycle.
- ♣ The alternating current at any instant is  $i = I_m \sin \omega t = I_m \sin \theta$
- ♣ The sum of all currents over a half-cycle is given by area of positive half-cycle (or) negative half-cycle.
- ♣ Consider an elementary strip of thickness 'dθ' in positive half-cycle,  
Area of the elementary strip =  $i d\theta$
- ♣ Then area of positive half-cycle,  
$$= \int_0^\pi i d\theta = \int_0^\pi I_m \sin \theta d\theta = I_m [-\cos \theta]_0^\pi$$
$$= -I_m [\cos \pi - \cos 0] = -I_m [-1 - 1] = 2 I_m$$
- ♣ Then Average value of AC,  
$$I_{av} = \frac{\text{area of positive or negative half - cycle}}{\text{base length of half - cycle}}$$
$$I_{avg} = \frac{2 I_m}{\pi} = \mathbf{0.637 I_m}$$
- ♣ For negative half-cycle ;  $I_{avg} = -0.637 I_m$

## 14. Obtain an expression for RMS value of alternating current.

### RMS value of AC ( $I_{RMS}$ ) :

- ♣ The root mean square value of an alternating current is defined as the square root of the mean of the squares of all currents over one cycle.

### Expression :



- ♣ The alternating current at any instant is  $i = I_m \sin \omega t = I_m \sin \theta$
- ♣ The sum of the squares of all currents over one cycle is given by the area of one cycle of squared wave.
- ♣ Consider an elementary area of thickness 'dθ' in the first half-cycle of the squared current wave.  
Area of the element =  $i^2 d\theta$
- ♣ Area of one cycle of squared wave,

$$= \int_0^{2\pi} i^2 d\theta = \int_0^{2\pi} I_m^2 \sin^2 \theta d\theta$$

$$= I_m^2 \int_0^{2\pi} \left[ \frac{1 - \cos 2\theta}{2} \right] d\theta$$

$$[\because \cos 2\theta = 1 - 2 \sin^2 \theta]$$

$$= \frac{I_m^2}{2} \left[ \int_0^{2\pi} d\theta - \int_0^{2\pi} \cos 2\theta d\theta \right]$$

$$= \frac{I_m^2}{2} \left[ \theta - \frac{\sin 2\theta}{2} \right]_0^{2\pi}$$

$$= \frac{I_m^2}{2} \left[ 2\pi - \frac{\sin 4\pi}{2} - 0 + \frac{\sin 0}{2} \right]$$

$$[\because \sin 0 = \sin 4\pi = 0]$$

$$= \frac{I_m^2}{2} [2\pi] = I_m^2 \pi$$

- ♣ Hence,

$$I_{RMS} = \sqrt{\frac{\text{area of one cycle of squared wave}}{\text{base length of one cycle}}}$$

$$I_{RMS} = \sqrt{\frac{I_m^2 \pi}{2\pi}} = \sqrt{\frac{I_m^2}{2}}$$

$$I_{RMS} = \frac{I_m}{\sqrt{2}} = \mathbf{0.707 I_m}$$

- ♣ Similarly for alternating voltage, it can be shown that,

$$V_{RMS} = \frac{V_m}{\sqrt{2}} = \mathbf{0.707 V_m}$$

- ♣ RMS value of AC is also called effective value ( $I_{eff}$ )



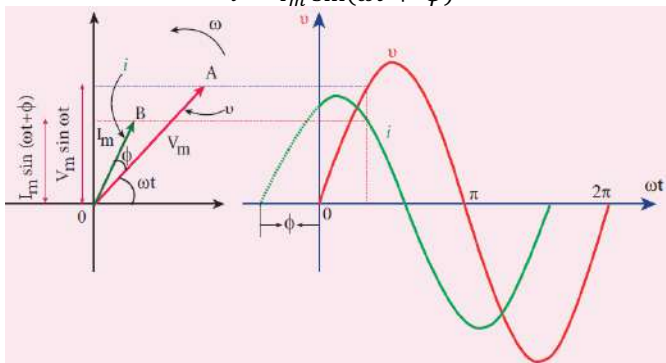
15. Draw the phasor diagram and wave diagram for that current ' $i$ ' leads the voltage ' $V$ ' by phase angle of ' $\phi$ '

Phasor and wave diagram of ' $i$ ' leads ' $V$ ' by ' $\phi$ '

- Let the alternating current and voltage at any instant is,

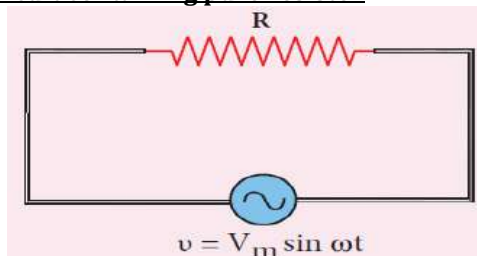
$$v = V_m \sin \omega t$$

$$i = I_m \sin(\omega t + \phi)$$



16. Find out the phase relation ship between voltage and current in a pure resistive circuit.

AC circuit containing pure resistor :



- Let a pure resistor of resistance ' $R$ ' connected across an alternating voltage source ' $v$ '
- The instantaneous value of the alternating voltage is given by,

$$v = V_m \sin \omega t \quad \text{----- (1)}$$

- Let ' $i$ ' be the alternating current flowing in the circuit due to this voltage, then the potential drop across ' $R$ ' is

$$V_R = i R \quad \text{----- (2)}$$

- From Kirchoff's loop rule,  $v - V_R = 0$

$$(or) \quad v = V_R$$

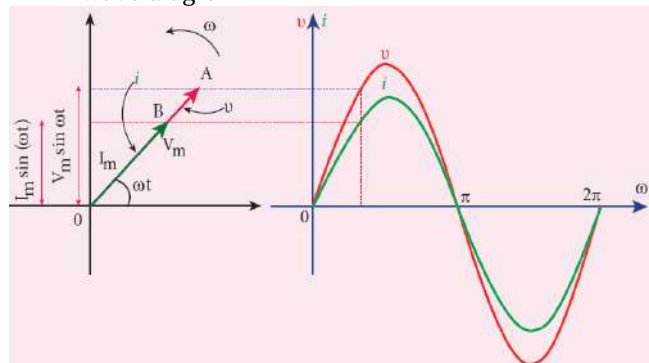
$$V_m \sin \omega t = i R$$

$$i = \frac{V_m}{R} \sin \omega t$$

$$i = I_m \sin \omega t \quad \text{----- (3)}$$

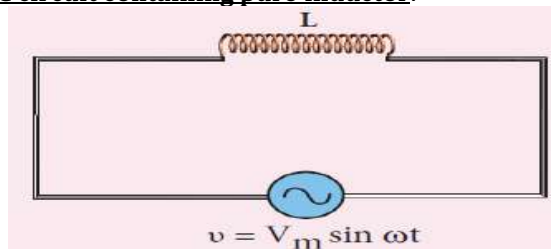
Here,  $\frac{V_m}{R} = I_m \rightarrow$  Peak value of AC

- From equation (1) and (3), it is clear that, the applied voltage and the current are in phase with each other. This is indicated in the phasor and wave diagram.



17. Find out the phase relation ship between voltage and current in a pure inductive circuit.

AC circuit containing pure inductor:



- Let a pure inductor of inductance ' $L$ ' connected across an alternating voltage source ' $v$ '
- The instantaneous value of the alternating voltage is given by,

$$v = V_m \sin \omega t \quad \text{----- (1)}$$

- Let ' $i$ ' be the alternating current flowing in the circuit due to this voltage, which induces a self induced emf (back emf) across ' $L$ ' and it is given by

$$\epsilon = -L \frac{di}{dt} \quad \text{----- (2)}$$

- From Kirchoff's loop rule,  $v - (-\epsilon) = 0$   
(or)  $v = -\epsilon$

$$V_m \sin \omega t = - \left( -L \frac{di}{dt} \right)$$

$$V_m \sin \omega t = L \frac{di}{dt}$$

$$\therefore \quad di = \frac{V_m}{L} \sin \omega t \, dt$$

- Integrate on both sides,

$$i = \frac{V_m}{L} \int \sin \omega t \, dt$$

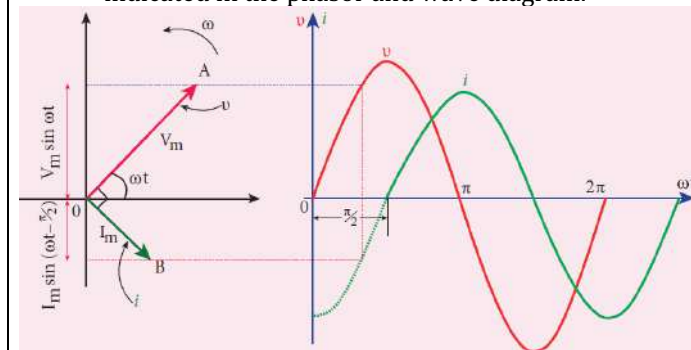
$$i = \frac{V_m}{L} \left( \frac{-\cos \omega t}{\omega} \right) = \frac{V_m}{\omega L} \left[ -\sin \left( \frac{\pi}{2} - \omega t \right) \right]$$

$$i = \frac{V_m}{\omega L} \sin \left( \omega t - \frac{\pi}{2} \right)$$

$$i = I_m \sin \left( \omega t - \frac{\pi}{2} \right) \quad \text{----- (3)}$$

Where,  $\frac{V_m}{\omega L} = I_m \rightarrow$  peak value of AC

- From equation (1) and (3), it is clear that current lags behind the applied voltage by  $\frac{\pi}{2}$ . This is indicated in the phasor and wave diagram.



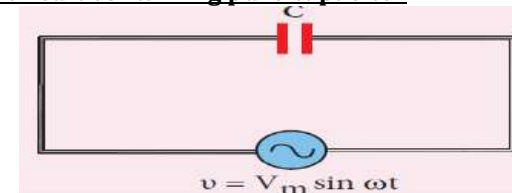
Inductive reactance ( $X_L$ ) :

- In pure inductive circuit, ' $\omega L$ ' is the resistance offered by the inductor and it is called inductive reactance ( $X_L$ ). Its unit is **ohm ( $\Omega$ )**

$$X_L = \omega L = 2 \pi f L$$

18. Find out the phase relation ship between voltage and current in a pure capacitive circuit.

AC circuit containing pure capacitor :



- Let a pure capacitor of capacitance ' $C$ ' connected across an alternating voltage source ' $v$ '
- The instantaneous value of the alternating voltage is given by,

$$v = V_m \sin \omega t \quad \text{----- (1)}$$



- Let 'q' be the instantaneous charge on the capacitor. The emf across the capacitor at that instant is,

$$\epsilon = \frac{q}{C} \quad \text{----- (2)}$$

- From Kirchoff's loop rule,  $v - \epsilon = 0$   
(or)  $v = \epsilon$

$$V_m \sin \omega t = \frac{q}{C}$$

$$\therefore q = C V_m \sin \omega t$$

- By the definition of current,

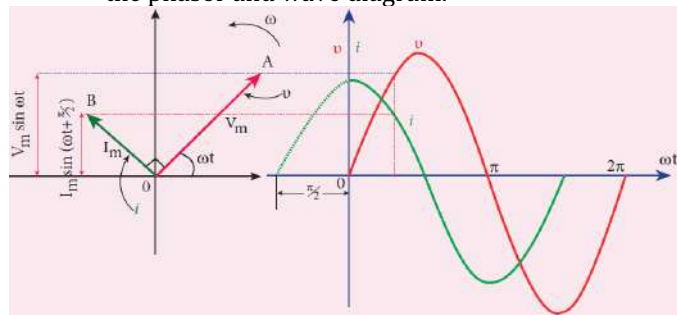
$$i = \frac{dq}{dt} = C V_m \frac{d(\sin \omega t)}{dt} = C V_m (\cos \omega t) \omega$$

$$i = \omega C V_m \sin\left(\frac{\pi}{2} + \omega t\right) = \frac{V_m}{(1/\omega C)} \sin\left(\frac{\pi}{2} + \omega t\right)$$

$$i = I_m \sin\left(\omega t + \frac{\pi}{2}\right) \quad \text{----- (3)}$$

where,  $\frac{V_m}{(1/\omega C)} = I_m \rightarrow$  Peak value of AC

- From equation (1) and (3), it is clear that current leads the applied voltage by  $\frac{\pi}{2}$ . This is indicated in the phasor and wave diagram.



#### Capacitive reactance ( $X_C$ ):

- In pure capacitive circuit, ' $1/\omega C$ ' is the resistance offered by the capacitor and it is called capacitive reactance ( $X_C$ ). Its unit is **ohm ( $\Omega$ )**

$$X_C = \frac{1}{\omega C} = \frac{1}{2\pi f C}$$

#### 19. Explain resonance in series RLC circuit.

##### Resonance on series in RLC circuit:

- When the frequency of applied alternating source is increases, the inductive reactance ( $X_L$ ) increases, where as capacitive reactance ( $X_C$ ) decreases.
- At particular frequency ( $\omega_R$ ),  $X_L = X_C$

- At this stage, the frequency of applied source ( $\omega_R$ ) is equal to the natural frequency of the RLC circuit, the current in the circuit reaches its maximum value.

- Then the circuit is said to be in **electrical resonance**. The frequency at which resonance takes place is called **resonant frequency**.

- Thus at resonance,

$$X_L = X_C$$

$$\omega_R L = \frac{1}{\omega_R C}$$

$$\omega_R^2 = \frac{1}{L C}$$

- Hence the resonant angular frequency,

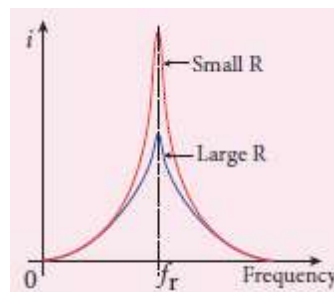
$$\omega_R = \frac{1}{\sqrt{L C}}$$

- And resonant frequency,

$$f_R = \frac{1}{2\pi \sqrt{L C}}$$

##### Effects of series resonance:

- When series resonance occurs, the **impedance of the circuit is minimum** and is equal to the resistance of the circuit. So the current in the circuit becomes maximum.
- (i.e.) At resonance,  $Z = R$  &  $I_m = \frac{V_m}{R}$
- The maximum current at resonance depends on the value of resistance (R)
- For smaller resistance, larger the current with sharper curve is obtained. But for larger resistance, smaller the current with flat curve is obtained.



#### 20. Obtain an expression for average power of AC over a cycle. Discuss its special cases.

##### Average power of AC:

- Power of a circuit is defined as the rate of consumption. It is given by the product of the voltage and current.
- The alternating voltage and alternating current in the series RLC circuit at an instance are given by,

$$v = V_m \sin \omega t$$

$$i = I_m \sin(\omega t + \phi)$$

- Then the instantaneous power is given by,

$$P = v i = V_m \sin \omega t I_m \sin(\omega t + \phi)$$

$$P = V_m I_m \sin \omega t (\sin \omega t \cos \phi - \cos \omega t \sin \phi)$$

$$P = V_m I_m (\sin^2 \omega t \cos \phi - \sin \omega t \cos \omega t \sin \phi)$$

- Here the average of  $\sin^2 \omega t$  over a cycle is  $\frac{1}{2}$  and that of  $\sin \omega t \cos \omega t$  is zero.

- Thus average power over a cycle is,

$$P_{avg} = V_m I_m \left(\frac{1}{2} \cos \phi\right) = \frac{V_m}{\sqrt{2}} \frac{I_m}{\sqrt{2}} \cos \phi$$

$$P_{avg} = V_{RMS} I_{RMS} \cos \phi$$

Where,  $V_{RMS} I_{RMS} \rightarrow$  apparent power  
 $\cos \phi \rightarrow$  power factor

##### Special cases:

- (i) For purely resistive circuit,  $\phi = 0$  and  $\cos \phi = 1$

$$\therefore P_{avg} = V_{RMS} I_{RMS}$$

- (ii) For purely inductive or capacitive circuit,

$$\phi = \pm \frac{\pi}{2} \text{ and } \cos \phi = 0. \quad \therefore P_{avg} = 0$$

- (iii) For series RLC circuit,  $\phi = \tan^{-1} \left[ \frac{X_L - X_C}{R} \right]$

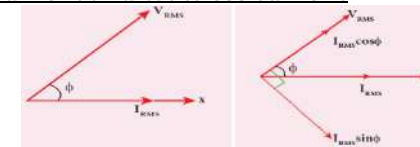
$$\therefore P_{avg} = V_{RMS} I_{RMS} \cos \phi$$

- (iv) For series RLC circuit at resonance,  $\phi = 0$  and  $\cos \phi = 1$ .

$$\therefore P_{avg} = V_{RMS} I_{RMS}$$

#### 21. Write a note on wattful current and wattless current.

##### Wattful current and Wattless current:



- Consider an AC circuit in which the voltage ( $V_{RMS}$ ) leads the current ( $I_{RMS}$ ) by phase angle ' $\phi$ '
- Resolve the current in to two perpendicular components,
  - (i)  $I_{RMS} \cos \phi$  - Component along  $V_{RMS}$
  - (ii)  $I_{RMS} \sin \phi$  - Component perpendicular to  $V_{RMS}$

- ♣ Here the component of current ( $I_{RMS} \cos \phi$ ) which is **inphase** with the voltage is called active component. The power consumed by this component =  $V_{RMS} I_{RMS} \cos \phi$ . It is known as wattfull current
- ♣ The other component of current which has a phase angle of with the voltage is called reactive component. The power consumed by this current is zero. It is known as wattles current.

## 22. Define power factor in various ways. Give some examples for power factor.

### Power factor - Definitions :

- The cosine of the angle lead or lag is called power factor (power factor =  $\cos \phi$ )
- Power factor =  $\frac{R}{Z} = \frac{\text{Resistance}}{\text{Impedance}}$
- Power factor =  $\frac{V I \cos \phi}{V I} = \frac{\text{True power}}{\text{Apparent power}}$

### Examples :

- ♣ For purely resistive circuit,  $\phi = 0$  and  $\cos \phi = 1$
- ♣ For purely inductive or capacitive circuit,  $\phi = \pm \frac{\pi}{2}$  and  $\cos \phi = 0$
- ♣ For RLC circuit, power factor lies between 0 and 1

## 23. What are the advantages and disadvantages of AC over DC?

### Advantages of AC over DC :

- ♣ The generation of AC is cheaper than that of DC
- ♣ When AC is supplied at higher voltages, the transmission losses are small compared to DC transmission.
- ♣ AC can easily be converted into DC with the help of rectifier.

### Disadvantages of AC over DC :

- ♣ Alternating voltages cannot be used for certain application. (e.g) charging of batteries, electroplating, electric traction etc.,
- ♣ At high voltages, it is more dangerous to work with AC than DC.

## 24. Show that the total energy is conserved during LC oscillations.

### Conservation of energy LC oscillations :

- ♣ During LC oscillations, the energy of the system oscillates between the electric field of the capacitor and the magnetic field of the inductor.

- ♣ Although these two energies vary with time, the total energy remains constant. (i.e)

$$U = U_E + U_B = \frac{q^2}{2C} + \frac{1}{2} L i^2 = \text{constant}$$

### Case (i) :

- ♣ When the charge of in the capacitor ;  $q = Q_m$  and the current through the inductor ;  $i = 0$

$$U = \frac{Q_m^2}{2C} + 0 = \frac{Q_m^2}{2C} \quad \text{--- (1)}$$

- ♣ The total energy is wholly electrical.

### Case (ii) :

- ♣ When charge  $q = 0$  ; Current  $i = I_m$ , the total energy,

$$U = 0 + \frac{1}{2} L I_m^2 = \frac{1}{2} L I_m^2$$

$$[\because i = -\frac{dq}{dt} = -\frac{d}{dt} (Q_m \cos \omega t) = Q_m \omega \sin \omega t = I_m \sin \omega t]$$

- ♣ Hence,  $I_m = Q_m \omega = \frac{Q_m}{\sqrt{LC}}$

$$\therefore U = \frac{1}{2} L \left[ \frac{Q_m^2}{LC} \right] = \frac{Q_m^2}{2C} \quad \text{--- (2)}$$

- ♣ Here the total energy is wholly magnetic

### Case (iii) :

- ♣ When charge =  $q$  , Current =  $i$ , then the total energy,

$$U = \frac{q^2}{2C} + \frac{1}{2} L i^2$$

- ♣ Here,  $q = Q_m \cos \omega t$  &  $i = Q_m \omega \sin \omega t$ . So

$$U = \frac{Q_m^2 \cos^2 \omega t}{2C} + \frac{1}{2} L Q_m^2 \omega^2 \sin^2 \omega t$$

- ♣ Since,  $\omega^2 = \frac{1}{LC}$

$$U = \frac{Q_m^2 \cos^2 \omega t}{2C} + \frac{L Q_m^2 \sin^2 \omega t}{2LC}$$

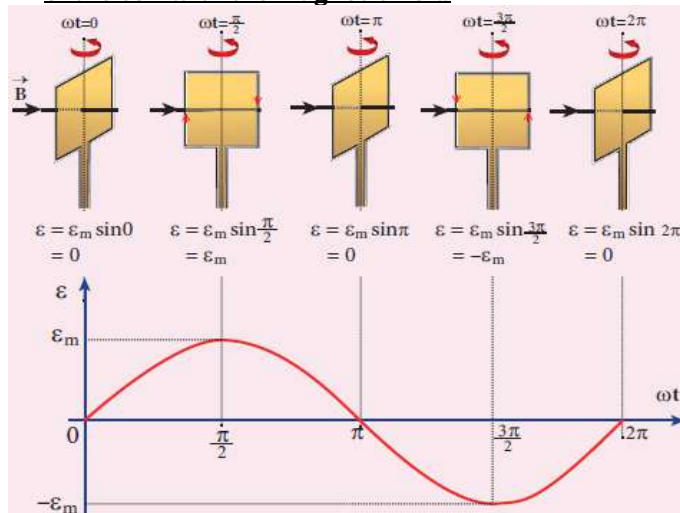
$$U = \frac{Q_m^2}{2C} (\cos^2 \omega t + \sin^2 \omega t) = \frac{Q_m^2}{2C} \quad \text{--- (3)}$$

- ♣ From equation (1), (2) and (3) it is clear that the total energy of the system remains constant

**PART - IV 5 MARK QUESTIONS AND ANSWERS**

1. Show mathematically that the rotation of a coil in a magnetic field over one rotation induces an alternating emf of one cycle.

Induction of emf by changing relative orientation of the coil with the magnetic field :



- Consider a rectangular coil of 'N' turns kept in a uniform magnetic field 'B'
- The coil rotates in anti-clockwise direction with an angular velocity ' $\omega$ ' about an axis.
- Initially let the plane of the coil be perpendicular to the field ( $\theta = 0$ ) and the flux linked with the coil has its maximum value. (i.e.)  $\Phi_m = BA$
- In time 't', let the coil be rotated through an angle  $\theta (= \omega t)$ , then the total flux linked is
- According to Faraday's law, the emf induced at that instant is,

$$\begin{aligned} \epsilon &= - \frac{d}{dt} (N\Phi_B) = - \frac{d}{dt} (N\Phi_m \cos \omega t) \\ &= -N\Phi_m (-\sin \omega t) \omega \\ \epsilon &= N\Phi_m \omega \sin \omega t \end{aligned} \quad \text{----- (1)}$$

- When  $\theta = 90^\circ$ , then the induced emf becomes maximum and it is given by,

$$\epsilon_m = N\Phi_m \omega = NBA\omega \quad \text{----- (2)}$$

- Therefore the value of induced emf at that instant is then given by,

$$\epsilon = \epsilon_m \sin \omega t \quad \text{----- (3)}$$

- Thus the induced emf varies as sine function of the time angle and this is called **sinusoidal emf** or **alternating emf**.

- If this alternating voltage is given to a closed circuit, a sinusoidally varying current flows in it. This current is called **alternating current** and is given by,

$$i = I_m \sin \omega t \quad \text{----- (4)}$$

- where,  $I_m \rightarrow$  peak value of induced current

2. Explain the principle, construction and working of transformer.

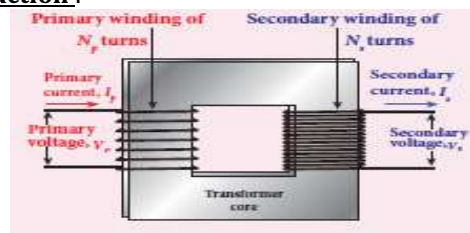
Transformer :

- It is a stationary device used to transform electrical power from one circuit to another without changing its frequency.
- It is done with either increasing or decreasing the applied alternating voltage with corresponding decrease or increase of current in the circuit.
- If the transformer converts an alternating current with low voltage in to an alternating current with high voltage, it is called **step-up transformer**.
- If the transformer converts an alternating current with high voltage in to an alternating current with low voltage, it is called **step-down transformer**.

Principle :

- Mutual induction between two coils.

Construction :



- It consists of two coils of high mutual inductance wound over the same transformer core made up of silicone steel.
- To avoid eddy current loss, the core is generally laminated
- The alternating voltage is applied across primary coil (P), and the output is taken across secondary coil (S)
- The assembled core and coils are kept in a container which is filled with suitable medium for better insulation and cooling purpose.

Working :

- The alternating voltage given to the primary coil, set up an alternating magnetic flux in the laminated core.
- As the result of flux change, emf is induced in both primary and secondary coils.
- The emf induced in the primary coil ' $\epsilon_p$ ' is almost equal and opposite to the applied voltage ' $V_p$ ' and is given by,

$$V_p = \epsilon_p = -N_p \frac{d\Phi_B}{dt} \quad \text{----- (1)}$$

- The frequency of alternating magnetic flux is same as the frequency of applied voltage. Therefore induced in secondary will also have same frequency as that of applied voltage,
- The emf induced in the secondary coil ' $\epsilon_s$ ' is,

$$V_s = \epsilon_s = -N_s \frac{d\Phi_B}{dt} \quad \text{----- (2)}$$

- Dividing equation (1) by (2),

$$\frac{V_s}{V_p} = \frac{N_s}{N_p} \quad \text{----- (3)}$$

Where,  $K \rightarrow$  transformation ratio

- For an ideal transformer,

input power = output power

$$\begin{aligned} V_p i_p &= V_s i_s \\ \frac{V_s}{V_p} &= \frac{i_p}{i_s} \end{aligned} \quad \text{----- (4)}$$

- From equation (3) and (4), we have

$$\frac{V_s}{V_p} = \frac{N_s}{N_p} = \frac{i_p}{i_s} = K \quad \text{----- (5)}$$

- If  $K > 1$  (or)  $N_s > N_p$ , then  $V_s > V_p$  and  $i_s < i_p$ . This is step up transformer in which voltage increased and the corresponding current is decreased.
- If  $K < 1$  (or)  $N_s < N_p$ , then  $V_s < V_p$  and  $i_s > i_p$ . This is step down transformer in which voltage decreased and the corresponding current is increased.

Efficiency of a transformer :

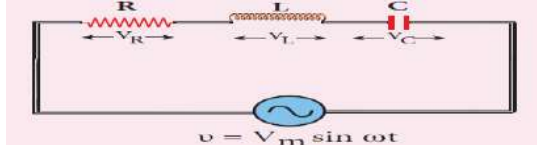
- The efficiency ( $\eta$ ) of a transformer is defined as the ratio of the useful output power to the input power.

$$\eta = \frac{\text{output power}}{\text{input power}} \times 100 \%$$

### 3. Derive an expression for phase angle between the applied voltage and current in a series RLC circuit.

#### Series RLC circuit :

- Consider a circuit containing a resistor of resistance 'R', an inductor of inductance 'L' and a capacitor of capacitance 'C' connected across an alternating voltage source.



- The applied alternating voltage is given by,  
 $v = V_m \sin \omega t$  ----- (1)

- Let 'i' be the current in the circuit at that instant.

- Hence the voltage developed across R, L and C

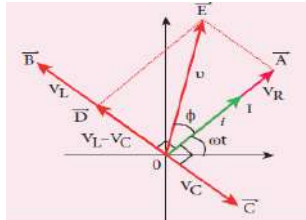
$$V_R = iR \quad (V_R \text{ is in phase with } i)$$

$$V_L = iX_L \quad (V_L \text{ leads } i \text{ by } \frac{\pi}{2})$$

$$V_C = iX_C \quad (V_C \text{ lags } i \text{ by } \frac{\pi}{2})$$

- The phasor diagram is drawn by representing current along  $\vec{OI}$ ,  $V_R$  along  $\vec{OA}$ ,  $V_L$  along  $\vec{OB}$  and  $V_C$  along  $\vec{OC}$

- If  $V_L > V_C$ , then the net voltage drop across LC combination is  $(V_L - V_C)$  which is represented by  $\vec{AD}$ .  
By parallelogram law, the diagonal  $\vec{OE}$  gives the resultant voltage 'v'



$$v = \sqrt{V_R^2 + (V_L - V_C)^2} = \sqrt{i^2 R^2 + (iX_L - iX_C)^2}$$

$$v = i\sqrt{R^2 + (X_L - X_C)^2}$$

$$(or) \quad i = \frac{v}{\sqrt{R^2 + (X_L - X_C)^2}} = \frac{v}{Z}$$

- Where,  $Z = \sqrt{R^2 + (X_L - X_C)^2}$  is called impedance of the circuit, which refers to the effective opposition to the circuit current by the series RLC circuit.

- From the phasor diagram, the phase angle between 'v' and 'i' is found out by

$$\tan \phi = \frac{V_L - V_C}{V_R} = \frac{X_L - X_C}{R} \quad \text{--- (6)}$$

#### Special cases :

- (i) When  $X_L > X_C$ , the phase angle  $\phi$  is **positive**. It means that  $v$  leads  $i$  by  $\phi$ .

$$(i.e.) \quad v = V_m \sin \omega t \quad \& \quad i = I_m \sin(\omega t - \phi)$$

This circuit is inductive.

- (ii) When  $X_L < X_C$ , the phase angle  $\phi$  is **negative**. It means that  $v$  lags behind  $i$  by  $\phi$ .

$$(i.e.) \quad v = V_m \sin \omega t \quad \& \quad i = I_m \sin(\omega t + \phi)$$

This circuit is capacitive

- (iii) When  $X_L = X_C$ , the phase angle  $\phi$  is **zero**. It means that  $v$  inphase with  $i$

$$(i.e.) \quad v = V_m \sin \omega t \quad \& \quad i = I_m \sin \omega t$$

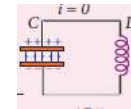
This circuit is resistive

### 4. What are called LC oscillations? Explain the generation of LC oscillations.

#### LC oscillations :

- Whenever energy is given to a circuit containing a pure inductor of inductance L and a capacitor of capacitance C, the energy oscillates back and forth between the magnetic field of the inductor and the electric field of the capacitor.

- Thus the electrical oscillations of definite frequency are generated. These oscillations are called LC oscillations.



#### Generation of LC oscillations :

- Whenever energy is given to a circuit containing a pure inductor of inductance L and a capacitor of capacitance C, the energy oscillates back and forth between the magnetic field of the inductor and the electric field of the capacitor.

- Thus the electrical oscillations of definite frequency are generated. These oscillations are called LC oscillations.

#### Stage -1 :

- Consider the capacitor is fully charged with maximum charge  $Q_m$ . So that the energy stored in the capacitor is maximum (i.e.)  $U_E = \frac{Q_m^2}{2C}$

- As there is no current in the inductor,  $U_B = 0$

- Therefore the total energy is wholly electrical.

#### Stage - 2 :

- The capacitor now begins to discharge through the inductor that establishes current 'i' clockwise direction.

- This current produces a magnetic field around the inductor and energy stored in the inductor which is given by  $U_B = \frac{Li^2}{2}$ . As the charge in the capacitor decreases, the energy stored in it also decreases and is given by  $U_E = \frac{q^2}{2C}$

- Thus the total energy is the sum of electrical and magnetic energies.

#### Stage - 3 :

- When the charge in the capacitor becomes zero, its energy becomes zero (i.e.)  $U_E = 0$ . In this stage maximum current ( $I_m$ ) flows through inductor and its energy becomes maximum. (i.e.)  $U_B = \frac{LI_m^2}{2}$ .

- Thus the total energy is wholly magnetic.

#### Stage - 4 :

- Eventhough the charge in the capacitor is zero, the current will continue to flow in the same direction.
- Since the current flow is in decreasing magnitude, the capacitor begins to charge in the opposite direction.
- Thus a part of the energy is transferred from the inductor back to the capacitor. The total energy is the sum of the electrical and magnetic energies.

#### Stage - 5 :

- When the current in the circuit reduces to zero, the capacitor becomes fully charged in the opposite direction.
- Thus the energy stored in the capacitor becomes maximum and the energy stored in the inductor is zero. So the total energy is wholly electrical.

#### Stage - 6 :

- This state of the circuit is similar to the initial state but the difference is that the capacitor is charged in opposite direction. So it will start discharge through inductor in anti-clockwise direction.
- The total energy is the sum of the electrical and magnetic energies.

#### Stage - 7 :

- The processes are repeated in opposite direction and finally the circuit returns to the initial state.
- Thus when the circuit goes through these stages, an alternating current flows in the circuit. As this process is repeated again and again, the electrical oscillations of definite frequency are generated.