## 2020 MATHEMATICS

Total marks : 80	Time: 3 hours
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## **General Instructions:**

1.

- *i)* Approximately 15 minutes is allotted to read the question paper and revise the answers.
- *ii)* The question paper consists of 22 questions.
- iii) All questions are compulsory.

(i) *xy* 

- iv) Internal choice has been provided in some questions.
- v) Marks allocated to every question are indicated against it.

N.B: Check that all pages of the question paper is complete as indicated on the top left side.

## Section-A

Cho	ose the correct answe	er from the give	n alternatives.		
(a)	If the sum of squares is $\frac{-2}{3}$ , then the value	_	uadratic polynon	$nial 3x^2 + 5x + k$	1
(b)	(i) $\frac{31}{6}$ The pair of equations which are	(ii) $\frac{25}{7}$	graphically repre	,	1
	<ul><li>(i) parallel</li><li>(iii) intersecting at (3,</li></ul>	4)	<ul><li>(ii) coincident</li><li>(iv) intersecting</li></ul>	g at (4, 3)	
(c)	If one root of the quantities other, then $b^2$ : $ac$ is 6 (i) 16:3	equal to	$ax^2 + bx + c = 0$ is (iii) 16:9		1
(d)	If the sum of $n$ terms (i) $4n-3$		$^{2} + 5n$ , then its $n^{t}$ (iii) $4n + 3$		1
(e)	If the distance between the negative value of (i) -2	a is	2, –3) and B (2, <i>a</i> (iii) –4		1
(f)	If $\sin \theta = x$ and $\sec \theta$	. ,	, ,	· /	1

(iii)  $\frac{1}{xy}$ 

(iv) x-y

(ii) x+y

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	(g)	•	at a point P of a circ t a point Q such that		_	1
		(i) 8.5 cm	(ii) $\sqrt{119}$ cm	(iii) 12 cm	(iv) 13 cm	
	(h)	If the perimete (i) 21 cm	r of a semicircle is 3 (ii) 14 cm	36 cm, then its radi (iii) 7 cm	us is (iv) 3.5 cm	1
	(i)	The number of side 6 cm is	cubes of side 2 cm	which can be cut	from a cube of	1
		(i) 56	(ii) 54	(iii) 28	(iv) 27	
	(j)	A die is thrown	n once. The probabil		nber less than 3 is	1
		(i) $\frac{1}{3}$	(ii) $\frac{2}{3}$	(iii) $\frac{1}{6}$	(iv) 1	
			Sec	tion – B		
2.	Prov	we that $6 + \sqrt{2}$ is	irrational.			2
3.	Find	the quadratic ed	quation whose one r	oot is $1+\sqrt{2}$ and t	he sum of its roots is 2.	2
4.			in in which AB $\parallel$ DC at O. If $ar(\Delta AOB) =$			2
5.	Find	I the point on the	x-axis which is equ	aidistant from (2, –	5) and (-2, 9).	2
6.	Find	I the area of a qu	adrant of a circle w	hose circumferenc	e is 22 cm.	2
			Sect	tion – C		
7.			ros of the quadratic		` '	
	that	one zero is $\frac{11}{6}$ r	more than the other,	find the value of $k$		3
8.	a.		wing pair of linear ea and $9x = 2y + 7$ .	quations by elimina	ation method:	
			Or			3
	<b>b.</b>	Find the roots of the quadratic for	of the quadratic equatormula.	ation $x - \frac{1}{x} = 3$ , $(x \neq x)$	± 0) by applying	
9.	a.	Find the 31 <sup>st</sup> te	rm of an A.P. whos	e 11 <sup>th</sup> term is 38 a	nd the 16 <sup>th</sup> term is 73.	
			Or			3

-3- *NB-T/M/1* 

**b.** If the sum of the first 7 terms of an A.P. is 49 and that of 17 terms is 289, find the sum of the first *n* terms.

10. **a.** Find the coordinates of a point A, where AB is the diameter of a circle whose centre is (2, -3) and B is (1, 4).

Or 3

- **b.** If P(x, y) is any point on the line joining the points A (a, 0) and B (0, b), then show that  $\frac{x}{a} + \frac{y}{b} = 1$ .
- 11. If  $\cot \theta = \frac{7}{8}$ , evaluate  $\frac{(1+\sin \theta)(1-\sin \theta)}{(1+\cos \theta)(1-\cos \theta)}$  with the help of a right triangle.
- 12. **a.** Evaluate:  $\frac{5\cos^2 60^\circ + 4\sec^2 30^\circ \tan^2 45^\circ}{\sin^2 30^\circ + \cos^2 30^\circ}$

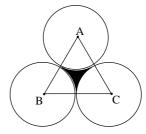
Or 3

**b.** Prove that 
$$\sqrt{\frac{1+\sin A}{1-\sin A}} = \sec A + \tan A$$

- 13. Draw a triangle ABC with side BC = 6 cm, AB = 5 cm and  $\angle$ ABC = 60°. Then construct a triangle whose sides are  $\frac{3}{4}$  of the corresponding sides of the triangle ABC.
- 14. **a.** The wheels of a car are of diameter 80 cm each. How many complete revolutions does each wheel make in 10 minutes when the car is travelling at a speed of 66 km per hour?

Or 3

**b.** In the adjoining figure, the area of an equilateral  $\triangle$ ABC is 17320.5 cm<sup>2</sup>. With each vertex of the triangle as centre, a circle is drawn with radius equal to half the length of the side of the triangle. Find the area of the shaded region. [Use  $\pi = 3.14$  and  $\sqrt{3} = 1.73205$ ]



3

15. The table below shows the daily expenditure on food of 25 households in a locality.

Daily expenditure (in `)	100-150	150-200	200-250	250-300	300-350
Number of households	4	5	12	2	2

Find the mean daily expenditure on food by the Assumed Mean Method. [Take assumed mean, a = 225]

3

- 16. A die is thrown once. Find the probability of getting:
  - (i) a prime number
- (ii) a number lying between 2 and 6
- (iii) an odd number

3

## Section - D

17. **a.** Mary travels 300 km to her home partly by train and partly by bus. She takes 4 hours if she travels 60 km by train and the remaining by bus. If she travels 100 km by train and the remaining by bus, she takes 10 minutes longer. Find the speed of the train and the bus separately.

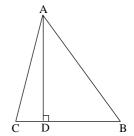
Or 5

- **b.** Two water taps together can fill a tank in  $9\frac{3}{8}$  hours. The tap of larger diameter takes 10 hours less than the smaller one to fill the tank separately. Find the time in which each tap can separately fill the tank. [Use quadratic equation]
- 18. **a.** Prove that the ratio of the areas of two similar triangles is equal to the square of the ratio of their corresponding sides.

Or

5

**b.** In the adjoining figure, the perpendicular from A on side BC of a  $\triangle$ ABC intersects BC at D such that DB = 3CD. Prove that  $2AB^2 = 2AC^2 + BC^2$ 



19. **a.** From the top of a 7 m high building, the angle of depression of the foot of a cable tower  $(7\sqrt{3} + 7)$  m high is 45°. Find the angle of elevation of the cable tower from the top of the building.

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Or 5

- **b.** From a point on the ground, the angles of elevation of the top and the bottom of a flagstaff fixed at the top of a 20 m high pillar are 60° and  $\theta$  respectively. If the height of the flagstaff is  $(\sqrt{3}-1)$  times the height of the pillar, find the value of  $\theta$ .
- 20. **a.** Prove that the parallelogram circumscribing a circle is a rhombus.

Or 5

- **b.** Prove that opposite sides of a quadrilateral circumscribing a circle subtend supplementary angles at the centre of the circle.
- 21. **a.** A tent is in the shape of a cylinder surmounted by a conical top. If the height and diameter of the cylindrical part are 2.1 m and 4 m respectively and the slant height of top is 2.8 m, find the area of the canvas used for making the tent. Also, find the cost of the canvas of the tent at the rate of `500 per m<sup>2</sup>.

Or 5

- **b.** A well of diameter 3 m is dug 14 m deep. The earth taken out of it has been spread evenly all around it in the shape of a circular ring of width 4 m to form an embankment. Find the height of the embankment.
- 22. **a.** If the median of the given data is 28.5, find the values of x and y.

Class interval	0-10	10-20	20-30	30-40	40-50	50-60	Total
Frequency	5	Х	20	15	у	5	60

Or 5

**b.** The following distribution gives the daily income of 50 workers of a factory.

Daily income (in `)	100-120	120-140	140-160	160-180	180-200
Number of workers	12	14	8	6	10

Convert the distribution above to a less than type cumulative frequency distribution and draw its ogive.

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