

BIRLA INSTITUTE OF TECHNOLOGY, MESRA, RANCHI
(MID SEMESTER EXAMINATION MO/2024)

CLASS: B.TECH.
BRANCH: CSE/AI/ML

SEMESTER : III/ADD
SESSION : MO/2024

TIME: 02 Hours

SUBJECT: MA205 DISCRETE MATHEMATICS

FULL MARKS: 25

INSTRUCTIONS:

1. The question paper contains 5 questions each of 5 marks and total 25 marks.
2. Attempt all questions.
3. The missing data, if any, may be assumed suitably.
4. Tables/Data handbook/Graph paper etc., if applicable, will be supplied to the candidates

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|--|-----|----|----|
| Q.1(a) Construct a truth table for the compound proposition $(p \vee q) \rightarrow (p \wedge q)$. | [2] | 1 | 3 |
| Q.1(b) Check whether $[(p \rightarrow q) \wedge (q \rightarrow r)] \rightarrow (p \rightarrow r) \equiv T$ or not. | [3] | 1 | 4 |
| Q.2(a) If $p \rightarrow q$ is true, determine the truth value of $\neg p \wedge (p \rightarrow q)$. | [2] | 1 | 3 |
| Q.2(b) Show that the premises $p \rightarrow q, q \rightarrow r, \neg r$ lead to the conclusion $\neg p$. | [3] | 1 | 4 |
| Q.3 Solve the recurrence relation $a_{n+2} - 6a_{n+1} + 9a_n = 3(2^n) + 7(3^n), n \geq 0$ given that $a_0 = 1$ and $a_1 = 4$. | [5] | 2 | 4 |
| Q.4 Use generating function to solve the recurrence relation $a_r = 8a_{r-1} + 10^{r-1}, r \geq 1$ with $a_0 = 1$. | [5] | 2 | 4 |
| Q.5 Use Warshall's algorithm to find transitive closure of the relation $R = \{(a, b), (b, a), (b, c), (c, d), (d, a)\}$ defined on the set $A = \{a, b, c, d\}$. | [5] | 3 | 4 |