

Instructions: Solve all questions. Show your work where applicable.

**Question 1 (2 marks)**

Construct a DFA that accepts all strings from the language  $L = \{\text{strings of size not divisible by } 3\}$ . Draw the state diagram and provide the transition table.

**Question 2 (2 marks)**

Given the following DFA, determine whether the strings "1011" and "1010" are accepted or rejected. Show the path of computation for each string.

State diagram:

- States:  $\{q_0, q_1, q_2\}$       Initial state:  $q_0$       Final state:  $q_2$
- Transitions:
  - $\delta(q_0, 0) = q_0, \delta(q_0, 1) = q_1$
  - $\delta(q_1, 0) = q_2, \delta(q_1, 1) = q_0$
  - $\delta(q_2, 0) = q_2, \delta(q_2, 1) = q_2$

**Question 3 (1 mark)**

How many states can the equivalent DFA have in the worst case if the original NFA has  $N$  states?

**Question 5**

Find the minimum automata: (Use Table Filling / Equivalence method)

State / $\Sigma$	0	1
$\rightarrow q_0$	$q_1$	$q_2$
$q_1$	$q_3$	$q_4$
$q_2$	$q_5$	$q_6$
$q_3$	$q_3$	$q_4$
$q_4$	$q_5$	$q_6$
$*q_5$	$q_3$	$q_4$
$q_6$	$q_5$	$q_6$