

MCA-304: Automata Theory
Master of Computer Applications
Semester Third, Nov/Dec-2017

Time: Three Hours

Max. Marks: 70

Q1 ✓ a) What is ambiguity of CFG? Show that the given grammar ^{below} is ambiguous (7 marks)

$S \rightarrow SbS$

$S \rightarrow a$

b) Consider the given grammar

$E \rightarrow E * T \mid T$

$T \rightarrow E - T \mid F$

$F \rightarrow (E) \mid 0 \mid 1$

Write the leftmost and rightmost derivation and draw the parse tree.

$1 * (0 * 1) - 1 - 0$

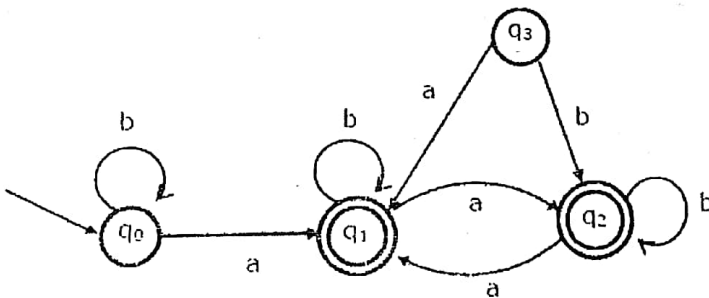
Q2 ✓ Define PDA formally. Design a PDA for language L and write the grammar corresponding to it, where $L = \{a^i b^j c^k : i=j \text{ or } j=k\}$ (7 marks)

Q3 ✓ Design a Turing machine to accept language L over $\Sigma = (a, b)$, where $L = \{w \mid w \text{ contains equal number of a's and b's}\}$. (7 marks)

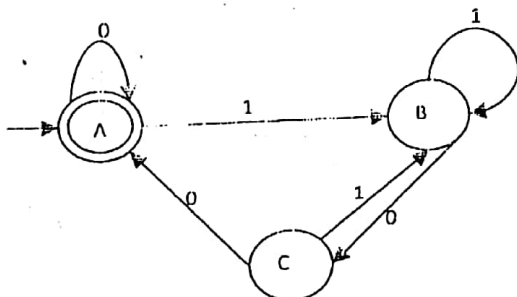
Q4 ✓ Define symbol and alphabet in automata theory. What is a regular expression? Write the regular expression for the language accepted by the given Finite State Automaton (7 marks)

in a) and b) below :

a)



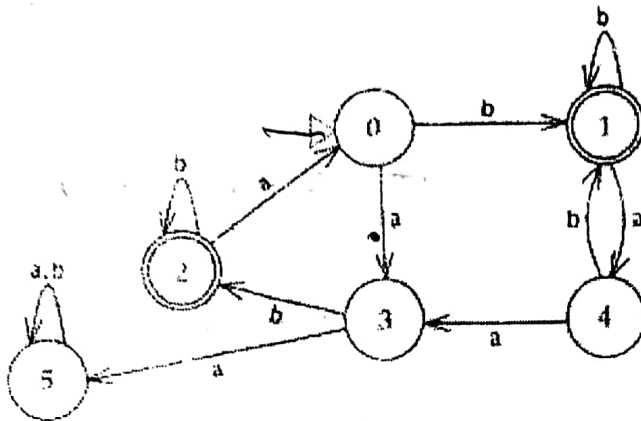
b)



Q. 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37, 38, 39, 40, 41, 42, 43, 44, 45, 46, 47, 48, 49, 50, 51, 52, 53, 54, 55, 56, 57, 58, 59, 60, 61, 62, 63, 64, 65, 66, 67, 68, 69, 70, 71, 72, 73, 74, 75, 76, 77, 78, 79, 80, 81, 82, 83, 84, 85, 86, 87, 88, 89, 90, 91, 92, 93, 94, 95, 96, 97, 98, 99, 100

given below

Q5 ✓ What is a dead state? Determine the dead state in the given DFA. Minimize the given DFA (7 marks)



Q6 Differentiate between Mealy and Moore machine. Design a Mealy machine for a full binary adder. (5 marks)

Q7 ✓ What is halting problem. Prove that halting problem is undecidable. (5 marks)

Q8 ✓ Determine the type of language L, where $L = \{wxw^R \mid x, w \in \{a, b\}^+\}$. Design the corresponding automaton which accepts L. (5 marks)

Q9 Design CFG for the given languages (5 marks)

- $L = \{w \mid w \text{ contains equal number of } a\text{'s and } b\text{'s}\}$
- $L = \{a^n w w^R b^n \mid w \in \{0, 1\}^* \text{ and } n > 1, |w| \geq 1\}$

Q10 ✓ What is CNF? Convert the given grammar *below* into CNF. (5 marks)

$S \rightarrow AB \mid AC$
 $A \rightarrow aA \mid bAa \mid a$
 $B \rightarrow bbA \mid aB \mid AB$
 $C \rightarrow aCa \mid aD$
 $D \rightarrow aD \mid bC$

Q11 ✓ Differentiate between multitape and multitrack turing machine. Simulate multitape turing machine on single tape. (5 marks)

Q12 ✓ Draw the finite state automata for the given regular expressions (5 marks)

- $(00+11)^*00(0+1)^*$
- $01(01+10)^*11$

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