8.6-6.5-1.1

EE24BTECH11063 - Y. Harsha Vardhan Reddy

Question:

Find the minimum value of the function

$$f(x) = (2x - 1)^2 + 3$$

Solution:

Theoritical solution:

Given.

$$\frac{dy}{dx} = 4(2x - 1) = 0 ag{0.1}$$

$$\implies x = \frac{1}{2} \tag{0.2}$$

$$\frac{d^2y}{dx^2} = 8\tag{0.3}$$

(0.4)

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Since, $\frac{d^2y}{dx^2} > 0$, at $x = \frac{1}{2}$ there exists minimum

Therefore, $f\left(\frac{1}{2}\right) = 3$ is the minimum value of the function

Computational Solution Using Gradient Descent

To verify the analytical results, we use gradient descent to find the local minimum Gradient Descent for local minimum :

- Start with $x_0 = 4$
- Update x iteratively using

$$x_{n+1} = x_n - \eta \cdot f'(x_n) \tag{0.5}$$

where:

$$\eta = 0.1 \tag{0.6}$$

$$f'(x) = 4(2x - 1) \tag{0.7}$$

$$x_{n+1} = x_n - \eta \cdot (4(2x_n - 1)) \tag{0.8}$$

Computational Results

- Local minimum

$$x \approx 0.5, \ g(x) \approx 3.000$$
 (0.9)

