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Assignment-2

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CHAPTER 15 MATRICES AND DETERMINANTS

SINGLE CORRECT TYPE

- 1) Let k be an integer such that triangle with vertices (k, -3k), (5, k) and (-k, 2) has area 28sq.units. Then the orthocentre of the triangle is at the point: [JEE M 2017]
 - a) $(2, \frac{1}{2})$
- b) $(2, -\frac{1}{2})$
- c) $(1, \frac{3}{4})$
- d) $(1, -\frac{3}{4})$
- 2) Let ω be a complex number such that $2\omega + 1 = z$ where $z = \sqrt{-3}$. If

$$\begin{vmatrix} 1 & 1 & 1 \\ 1 & -\omega^2 - 1 & \omega^2 \\ 1 & \omega^2 & \omega^7 \end{vmatrix} = 3k \tag{1}$$

, then k is equal to:

[JEE M 2017]

a) 1

b) -z

c) z

- d) -1
- 3) If $A = \begin{pmatrix} 2 & -3 \\ -4 & 1 \end{pmatrix}$, then $adj(3A^2 + 12A)$ is equal [JEE M 2017]
 - a) $\begin{pmatrix} 72 & -63 \\ -84 & 51 \end{pmatrix}$ b) $\begin{pmatrix} 72 & -84 \\ -63 & 51 \end{pmatrix}$
 - c) $\begin{pmatrix} 51 & 63 \\ 84 & 72 \end{pmatrix}$ d) $\begin{pmatrix} 51 & 84 \\ 63 & 72 \end{pmatrix}$

4) If

$$\begin{vmatrix} x - 4 & 2x & 2x \\ 2x & x - 4 & 2x \\ 2x & 2x & x - 4 \end{vmatrix} = (A + Bx)(x - A)^{2} (2)$$

, then the ordered pair (A, B) is equal to: [JEE M 2018]

- a) (-4,3) b) (-4,5) c) (4,5)d) (-4, -5)
- 5) If the system of linear equations

$$x + ky + 3z = 0 \tag{3}$$

$$3x + ky - 2z = 0 \tag{4}$$

$$2x + 4y - 3z = 0 (5)$$

has a non-zero solution (x, y, z), then $\frac{xz}{v^2}$ is equal [JEE M 2018]

- a) 10
- b) -30
- c) 30
- d) -10
- 6) The system of linear equations

$$x + y + z = 2 \tag{6}$$

$$2x + 3y + 2z = 5 \tag{7}$$

$$2x + 3y + (a^2 - 1)z = a + 1$$
 (8)

[JEE M2019-9 Jan(M)]

- a) is consistent when a = 4
- b) has a unique solution for $|a| = \sqrt{3}$
- c) has infinitely many solutions for a = 4
- d) is consistent when $|a| = \sqrt{3}$
- 7) If $A = \begin{pmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{pmatrix}$, then the matrix A^{-50} when $\theta = \frac{\pi}{12}$, is equal to: [JEE M 2019-9] Jan(M)1

a)
$$\begin{pmatrix} \frac{1}{2} & -\frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$$
 b) $\begin{pmatrix} \frac{\sqrt{3}}{2} & -\frac{1}{2} \\ \frac{1}{2} & \frac{\sqrt{3}}{2} \end{pmatrix}$

b)
$$\begin{pmatrix} \frac{\sqrt{3}}{2} & -\frac{1}{2} \\ \frac{1}{2} & \frac{\sqrt{3}}{2} \end{pmatrix}$$

c)
$$\begin{pmatrix} \frac{\sqrt{3}}{2} & \frac{1}{2} \\ -\frac{1}{2} & \frac{\sqrt{3}}{2} \end{pmatrix}$$

c)
$$\begin{pmatrix} \frac{\sqrt{3}}{2} & \frac{1}{2} \\ -\frac{1}{2} & \frac{\sqrt{3}}{2} \end{pmatrix}$$
 d) $\begin{pmatrix} \frac{1}{2} & \frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$

8) If
$$\begin{pmatrix} 1 & 1 \\ 0 & 1 \end{pmatrix} \cdot \begin{pmatrix} 1 & 2 \\ 0 & 1 \end{pmatrix} \cdot \begin{pmatrix} 1 & 3 \\ 0 & 1 \end{pmatrix} \cdot \dots \begin{pmatrix} 1 & n-1 \\ 0 & 1 \end{pmatrix} = \begin{pmatrix} 1 & 78 \\ 0 & 1 \end{pmatrix}.$$

then the inverse of $\begin{pmatrix} 1 & n \\ 0 & 1 \end{pmatrix}$ is [JEE M2019-9] April(M)]

a)
$$\begin{pmatrix} 1 & 0 \\ 12 & 1 \end{pmatrix}$$

a)
$$\begin{pmatrix} 1 & 0 \\ 12 & 1 \end{pmatrix}$$
 b) $\begin{pmatrix} 1 & -13 \\ 0 & 1 \end{pmatrix}$

c)
$$\begin{pmatrix} 1 & -12 \\ 0 & 1 \end{pmatrix}$$

d)
$$\begin{pmatrix} 1 & 0 \\ 13 & 1 \end{pmatrix}$$

9) Let α and β be the roots of the equation

$$x^2 + x + 1 = 0$$

. Then for $y \neq 0$ in R,

$$\begin{vmatrix} y+1 & \alpha & \beta \\ \alpha & y+\beta & 1 \\ \beta & 1 & y+\alpha \end{vmatrix}$$
 (10)

[JEE M 2019-9 April(M)] is equal to:

a)
$$y(y^2 - 1)$$
 b) $y(y^2 - 3)$

b)
$$v(v^2 - 3)$$

c)
$$y^3$$

d)
$$y^3 - 1$$

Chapter 12 DIFFERENTIATION

E: SUBJECTIVE PROBLEMS

1) Let f be a twice differentiable function such that f''(x) = -f(x), and

$$f'(x) = g(x), h(x) = [f(x)]^2 + [g(x)]^2$$
 (11)

. Find h(10) if h(5) = 11 . (1982 - 3Marks)

2) If α be a repeated root of a quadratic equation f(x) = 0 and A(x), B(x) and C(x) be polynomials of degree 3,4 and 5 respectively, then show that

$$\begin{vmatrix} A(x) & B(x) & C(x) \\ A(\alpha) & B(\alpha) & C(\alpha) \\ A'(\alpha) & B'(\alpha) & C'(\alpha) \end{vmatrix}$$
(12)

is divisible by f(x), where prime denotes the (1984 - 4Marks)derivatives.

3) If $x = \sec \theta - \cos \theta$ and $y = \sec^n \theta - \cos^n \theta$, then show that

$$(x^2 + 4)\left(\frac{dy}{dx}\right)^2 = n^2(y^2 + 4)$$
 (13)

4) Find $\frac{dy}{dx}$ at x = -1, when

$$(\sin y)^{\sin(\frac{\pi}{2}x)} + \frac{\sqrt{3}}{2}\sec^{-1}(2x) + 2^x \tan(\ln(x+2)) = 0$$
(14)

(1991 - 4Marks)

5) If

$$y = \frac{ax^2}{(x-a)(x-b)(x-c)} + \frac{bx}{(x-b)(x-c)} + 1$$
(15)

, prove that

$$\frac{y'}{y} = \frac{1}{x} \left(\frac{a}{a-x} + \frac{b}{b-x} + \frac{c}{c-x} \right)$$
 (16)

(1998 - 8Marks)

H: Assertion & Reason Type Questions

1) Let $f(x) = 2 + \cos x$ for all real x. **STATEMENT - 1**: For each real t, there exists

a point c in $[t, t + \pi]$ such that f'(c) = 0because

STATEMENT - 2: $f(t) = f(t + 2\pi)$ for each real t. (2007 - 3Marks)

- a) Statement-1 is True, Statement-2 is True;
 Statement-2 is a correct explanation for Statement-1
- b) Statement-1 is True, Statement-2 is True; Statement-2 is NOT a correct explanation for Statement-1
- c) Statement-1 is True, Statement-2 is False
- d) Statement-1 is False, Statement-2 is True
- 2) Let f and g be real valued functions defined on interval (-1,1) such that g''(x) is continuous, $g(0) \neq 0.g'(0) = 0, g''(0) \neq 0$, and $f(x) = g(x) \sin x$

STATEMENT-1:

 $\lim_{x\to 0} [g(x)\cot x - g(0)\csc x] = f''(0)$ and **STATEMENT-2**: f'(0) = g(0) (2008)

- a) Statement-1 is True, Statement-2 is True;
 Statement-2 is a correct explanation for Statement-1
- b) Statement-1 is True, Statement-2 is True; Statement-2 is **NOT** a correct explanation for Statement-1
- c) Statement-1 is True, Statement-2 is False
- d) Statement-1 is False, Statement-2 is True

I:INTEGER VALUE CORRECT TYPE

- 1) If the function $f(x) = x^3 + e^{\frac{x}{2}}$ and $g(x) = f^{-1}(x)$, then the value of g'(1) is (2009)
- 2) Let

$$f(\theta) = \sin\left(\tan^{-1}\left(\frac{\sin\theta}{\sqrt{\cos 2\theta}}\right)\right), where -\frac{\pi}{4} < \theta < \frac{\pi}{4}$$
(17)

. Then the value of $\frac{d}{d(\tan\theta)}(f(\theta))$ is (2011)