EE24BTECH11063 - Y.Harsha Vardhan Reddy

Question:

Find the area of the smaller region bounded by the ellipse $\frac{x^2}{9} + \frac{y^2}{4} = 1$ and the line $\frac{x}{3} + \frac{y}{2} = 1$. **Solution:** The parameters of given conic,

Variable	Description
V, u, f	Parameters of conic
h, m	Parameters of line
c	length of side-AB
P_{1}, P_{2}	Points of intersection

TABLE 0: Variables Used

$$V = \begin{pmatrix} \frac{1}{9} & 0\\ 0 & \frac{1}{4} \end{pmatrix} \tag{0.1}$$

$$u = \begin{pmatrix} 0 \\ 0 \end{pmatrix} \tag{0.2}$$

$$f = 0 \tag{0.3}$$

for the line,

$$h = \begin{pmatrix} 0\\2 \end{pmatrix} \tag{0.4}$$

$$m = \begin{pmatrix} 3 \\ -2 \end{pmatrix} \tag{0.5}$$

By Solving we get points of intersection as

$$\begin{pmatrix} 3 \\ 0 \end{pmatrix}, \begin{pmatrix} 0 \\ 2 \end{pmatrix} \tag{0.6}$$

Area can be evaluated as

$$\int_{0}^{3} (f(x) - g(x)) dx$$
 (0.7)

$$\int_0^3 \left(2\sqrt{1 - \frac{x^2}{9}} - \left(-\frac{2}{3}x + 2 \right) \right) dx \tag{0.8}$$

By simplifying area enclosed comes to be 1.71 sq.units

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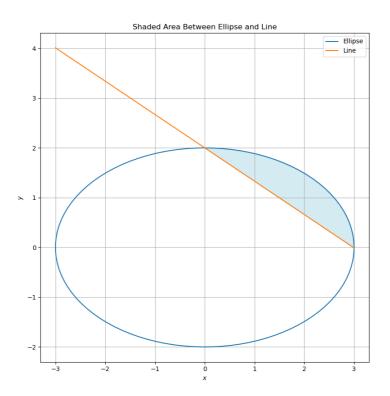


Fig. 0.1