

# 9-9.5-9

EE24BTECH11063 - Y.Harsha Vardhan Reddy

## Question:

Using integration, find the area of the region bounded by the parabola  $y^2 = 4x$  and the circle  $4x^2 + 4y^2 = 9$ .

**Solution:** The parameters of the conics are

Variable	Description
$V_1, u_1, f_1$	Parameters of Parabola
$V_2, u_2, f_2$	Parameters of circle
$P_1, P_2$	Points of intersection
$A$	Area between the conics

TABLE 0: Variables Used

$$V_1 = \begin{pmatrix} 0 & 0 \\ 0 & 1 \end{pmatrix}, u_1 = \begin{pmatrix} -2 \\ 0 \end{pmatrix}, f_1 = 0 \quad (0.1)$$

$$V_2 = \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}, u_2 = \begin{pmatrix} 0 \\ 0 \end{pmatrix}, f_2 = -\frac{9}{4} \quad (0.2)$$

The intersection of two conics with parameters  $V_i, u_i, f_i, i = 1, 2$  is defined as

$$x^T (V_1 + \mu V_2) x + 2(u_1 + \mu u_2)^T x + (f_1 + \mu f_2) = 0 \quad (0.3)$$

Solving this the points of intersection are

$$\left( \frac{1}{2\sqrt{2}}, \frac{1}{2\sqrt{2}} \right), \left( -\frac{1}{2\sqrt{2}}, -\frac{1}{2\sqrt{2}} \right) \quad (0.4)$$

Area between the curves is,

$$2 \int_0^{\sqrt{2}} \left( \sqrt{\frac{9}{4} - y^2} - \frac{y^2}{4} \right) dy \quad (0.5)$$

By solving the integration, we get area is equal to 3.06 sq.units

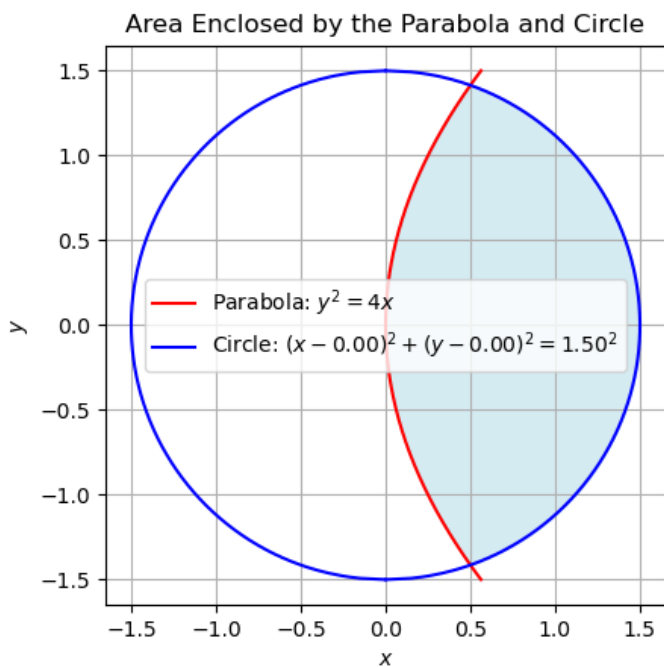


Fig. 0.1