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## Shift-2

EE24BTECH11063 - Y.Harsha Vardhan Reddy

### INTEGER TYPE

- 1)  $\lim_{x \rightarrow 0} \frac{ax - (e^{4x} - 1)}{ax(e^{4x} - 1)}$  exists and is equal to  $b$ , then the value of  $a - 2b$  is
- 2) A line is a common tangent to the circle  $(x - 3)^2 + y^2 = 9$  and the parabola  $y^2 = 4x$ . If the two points of contact  $(a, b)$  and  $(c, d)$  are distinct and lie in the first quadrant, then  $2(a + c)$  is equal to
- 3) The value of  $\int_{-2}^2 |3x^2 - 3x - 6| dx$  is
- 4) If the remainder when  $x$  is divided by 4 is 3, then the remainder when  $(2020 + x)^{2022}$  is divided by 8 is
- 5) A line  $L$  passing through origin is perpendicular to the lines

$$L_1 : \mathbf{r} = (3 + t)\hat{i} + (-1 + 2t)\hat{j} + (4 + 2t)\hat{k}$$

$$L_2 : \mathbf{r} = (3 + 2s)\hat{i} + (3 + 2s)\hat{j} + (2 + s)\hat{k}$$

If the co-ordinates of the point in the first octant on  $L_2$  at the distance of  $\sqrt{17}$  from the point of intersection of  $L$  and  $L_1$  are  $(a, b, c)$ , then  $18(a + b + c)$  is equal to

- 6) A function  $f$  is defined on  $[-3, 3]$  as

$$f(x) = \begin{cases} \min\{|x|, 2 - x^2\}, & -2 \leq x \leq 2 \\ [x], & 2 < |x| \leq 3 \end{cases}$$

where  $[x]$  denotes the greatest integer  $\leq x$ . The number of points, where  $f$  is not differentiable in  $(-3, 3)$  is

- 7) If the curves  $x = y^4$  and  $xy = k$  cut at right angles, then  $(4k)^6$  is equal to
- 8) The total number of two digit numbers 'n', such that  $3^n + 7^n$  is a multiple of 10, is
- 9)  $\vec{a} = \hat{i} + \alpha\hat{j} + 3\hat{k}$  and  $\vec{b} = 3\hat{i} - \alpha\hat{j} + \hat{k}$ . If the area of the parallelogram whose adjacent sides are represented by the vector  $\vec{a}$  and  $\vec{b}$  is  $8\sqrt{3}$  square units, then  $\vec{a} \cdot \vec{b}$  is equal to
- 10) If the curve  $y = y(x)$  represented by the solution of the differential equation  $(2xy^2 - y)dx + xdy = 0$ , passes through the intersection of the lines,  $2x - 3y = 1$  and  $3x + 2y = 8$ , then  $|y(1)|$  is equal to