## EE24BTECH11063 - Y.Harsha Vardhan Reddy

## **Question:**

Construct a right triangle ABC with AB=6cm, BC =8cm and  $\angle B = 90^{\circ}$ . Draw BD, the perpendicular from B on AC. Draw the circle through B, C and D and construct the tangents from A to this circle.

**Solution:** Given, a=8cm and c=8cm.

Variable	Description
а	length of side-BC
b	length of side-CA
C	length of side-AB
A	co-ordinates of vertex-1
В	co-ordinates of vertex-2
С	co-ordinates of vertex-3
D	co-ordinates of perpendicular from B on AC

TABLE 0: Variables Used

Let us place B at origin, A along x-axis and C along the y-axis i.e,

$$B = \begin{pmatrix} 0 \\ 0 \end{pmatrix} \tag{0.1}$$

$$A = \begin{pmatrix} 6 \\ 0 \end{pmatrix} \tag{0.2}$$

$$C = \begin{pmatrix} 0 \\ 8 \end{pmatrix} \tag{0.3}$$

Now let us find the co-ordinates of D, Equation of AC is given by,

$$4x + 3y = 8 ag{0.4}$$

$$P = \begin{pmatrix} 0 \\ 0 \end{pmatrix}, n = \begin{pmatrix} 4 \\ 3 \end{pmatrix}, c = 8 \tag{0.5}$$

(0.6)

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the desired foot of perpendicular is given by,

$$\begin{pmatrix} 3 & -4 \\ 4 & 3 \end{pmatrix} Q = \begin{pmatrix} 0 \\ 8 \end{pmatrix} \tag{0.7}$$

By solving system of equations we get,

$$D = \begin{pmatrix} 3.84 \\ 2.88 \end{pmatrix} \tag{0.8}$$

By using the co-ordinates of B, C, D circle can be drawn and it's equation is given by,

$$(x-0)^2 + (y-4)^2 = 16 (0.9)$$

$$x^2 + y^2 - 8y = 0 ag{0.10}$$

Now let us find the equation of tangent from A to circle Let, Q be the conic matrix of the circle. Then Q is given by,

$$Q = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & -4 \\ 0 & -4 & 0 \end{pmatrix} \tag{0.11}$$

The direction vector of tangent from P(x1, y1) is given by,

$$\begin{pmatrix} x1 & y1 & 1 \end{pmatrix} Q \begin{pmatrix} x \\ y \\ 1 \end{pmatrix} = 0 \tag{0.12}$$

$$x1 = 6, y1 = 0 (0.13)$$

$$\begin{pmatrix} 6 & 0 & 1 \end{pmatrix} \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & -4 \\ 0 & -4 & 0 \end{pmatrix} \begin{pmatrix} x \\ y \\ 1 \end{pmatrix} = 0 \tag{0.14}$$

$$3x - 2y = 0 ag{0.15}$$

The tangent passes through A(6,0) and is given by,

$$3x - 2y = c \tag{0.16}$$

By substituting A in line we get the equation of tangent to be

$$3x - 2y = 18\tag{0.17}$$

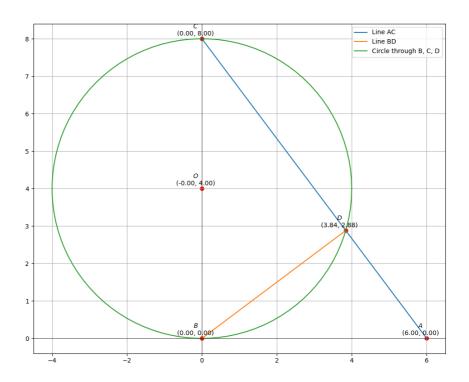


Fig. 0.1