7.4.11

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Question

If the chord y = mx + 1 of the circle $x^2 + y^2 = 1$ subtends an angle of measure 45 at the major segment of the circle then the value of m is

$$0 \ 2 \pm \sqrt{2}$$

2
$$-2 \pm \sqrt{2}$$

$$0 -1 \pm \sqrt{2}$$

1 $2 \pm \sqrt{2}$ **2** $-2 \pm \sqrt{2}$ **3** $-1 \pm \sqrt{2}$ **4** none of these

Solution

The given line subtends an angle 45 at the major segment of the circle. Therefore, it will subtend $2\times45=90$ at the centre of the circle.

The line y = mx + 1 can be expressed as:

This line always passes through $\begin{pmatrix} 0 \\ 1 \end{pmatrix}$, which lies on the circle $x^2 + y^2 = 1$

(since $0^2+1^2=1$). Therefore one point of intersection is $\begin{pmatrix} 0\\1 \end{pmatrix}$.

Let the other point of intersection be **P**. **P** will be a ± 90 rotation of $\begin{pmatrix} 0 \\ 1 \end{pmatrix}$ about the origin.

Solution

The rotation matrix is:

$$\begin{pmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{pmatrix}. \tag{2}$$

Therefore:

$$\mathbf{P} = \begin{pmatrix} 0 \\ 1 \end{pmatrix} \begin{pmatrix} \cos(\pm 90) & \sin(\pm 90) \\ -\sin(\pm 90) & \cos(\pm 90) \end{pmatrix}$$
(3)

$$\mathbf{P} = \begin{pmatrix} 1 \\ 0 \end{pmatrix} \text{ or } \begin{pmatrix} -1 \\ 0 \end{pmatrix} \tag{4}$$

Solution

If
$$\mathbf{P} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}, m = \frac{0-1}{1-0} = -1$$
 (5)

If
$$\mathbf{P} = \begin{pmatrix} -1\\0 \end{pmatrix}$$
, $m = \frac{0-1}{-1-0} = 1$ (6)

$$m = \pm 1 \tag{7}$$

Therefore, **d)** is the correct answer.

Python, C, Python+C Codes

codes permalink

Plot

