### 5.5.11

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## Question

Find inverse of the following matrix, using elementary transformation

$$A = \begin{pmatrix} 2 & 0 & -1 \\ 5 & 1 & 0 \\ 0 & 1 & 3 \end{pmatrix}$$



### Solution

Construct the augmented matrix of A and I

$$\begin{pmatrix}
2 & 0 & -1 & 1 & 0 & 0 \\
5 & 1 & 0 & 0 & 1 & 0 \\
0 & 1 & 3 & 0 & 0 & 1
\end{pmatrix}
\xrightarrow{R_1 \leftarrow \frac{1}{2}R_1}
\begin{pmatrix}
1 & 0 & -\frac{1}{2} & \frac{1}{2} & 0 & 0 \\
5 & 1 & 0 & 0 & 1 & 0 \\
0 & 1 & 3 & 0 & 0 & 1
\end{pmatrix}$$
(1)

$$\frac{R_2 \leftarrow R_2 - 5R_1}{\phantom{-}} \begin{pmatrix}
1 & 0 & -\frac{1}{2} & \frac{1}{2} & 0 & 0 \\
0 & 1 & \frac{5}{2} & -\frac{5}{2} & 1 & 0 \\
0 & 1 & 3 & 0 & 0 & 1
\end{pmatrix} \tag{2}$$

#### solution

$$\xrightarrow{R_3 \leftarrow R_3 - R_2} \begin{pmatrix} 1 & 0 & -\frac{1}{2} & \frac{1}{2} & 0 & 0 \\ 0 & 1 & \frac{5}{2} & -\frac{5}{2} & 1 & 0 \\ 0 & 0 & \frac{1}{2} & \frac{5}{2} & -1 & 1 \end{pmatrix}$$
 (3)

$$\xrightarrow{R_3 \leftarrow 2R_3} \left( \begin{array}{ccc|c} 1 & 0 & -\frac{1}{2} & \frac{1}{2} & 0 & 0 \\ 0 & 1 & \frac{5}{2} & -\frac{5}{2} & 1 & 0 \\ 0 & 0 & 1 & 5 & -2 & 2 \end{array} \right) \tag{4}$$

### Solutions

$$\frac{R_2 \leftarrow R_2 - \frac{5}{2}R_3}{\longrightarrow} \begin{pmatrix}
1 & 0 & -\frac{1}{2} & \frac{1}{2} & 0 & 0 \\
0 & 1 & 0 & -15 & 6 & -5 \\
0 & 0 & 1 & 5 & -2 & 2
\end{pmatrix} \tag{5}$$

$$\frac{R_1 \leftarrow R_1 + \frac{1}{2}R_3}{\longrightarrow} \begin{pmatrix}
1 & 0 & 0 & 3 & -1 & 1 \\
0 & 1 & 0 & -15 & 6 & -5 \\
0 & 0 & 1 & 5 & -2 & 2
\end{pmatrix}$$
(6)

### Solutions

$$A^{-1} = \begin{pmatrix} 3 & -1 & 1 \\ -15 & 6 & -5 \\ 5 & -2 & 2 \end{pmatrix} \tag{7}$$

# Python Code

```
import numpy as np
# Define the matrix A
 A = np.array([[2, 0, -1]],
               [5, 1, 0],
               [0, 1, 3]]
st # Calculate the inverse of A
A_inv = np.linalg.inv(A)
print( Inverse of the matrix A is: )
print(A inv)
```

### C Code

```
#include <stdio.h>
void invert_matrix(double A[3][3], double inv[3][3]) {
    int i, j, k;
    double aug[3][6];
    // Build augmented matrix [A | I]
    for (i = 0; i < 3; ++i) {
        for (j = 0; j < 3; ++j) {
            aug[i][j] = A[i][j];
            aug[i][j+3] = (i == j) ? 1.0 : 0.0;
```

### C Code

```
// Forward elimination
  for (i = 0; i < 3; ++i) {
      double f = aug[i][i];
      for (j = 0; j < 6; ++j)
          aug[i][i] /= f;
      for (k = 0; k < 3; ++k) {
          if(k != i) {
              double f2 = aug[k][i];
              for (j = 0; j < 6; ++j)
                  aug[k][j] -= f2 * aug[i][j];
  // Extract inverse
  for (i = 0; i < 3; ++i)
      for(j = 0; j < 3; ++j)
          inv[i][j] = aug[i][j+3];
```

## Python and C Code

```
import ctypes
 import numpy as np
# Load shared library
 lib = ctypes.CDLL('./code.so')
# Prepare arguments
A = np.array([[2, 0, -1]],
               [5, 1, 0].
                [0, 1, 3]], dtype=np.float64)
 A_inv = np.zeros((3, 3), dtype=np.float64)
 # Set up argtypes for the C function
 lib.invert_matrix.argtypes = [ctypes.POINTER(ctypes.
    c_double * 3 * 3), ctypes.POINTER(ctypes.c_double *
     3 * 3)1
```

# Python and C Code

```
# Create ctypes pointers
A_ct = (ctypes.c_double * 3 * 3)(*A.flatten())
A_inv_ct = (ctypes.c_double * 3 * 3)()

# Call C function
lib.invert_matrix(ctypes.byref(A_ct), ctypes.byref(A_inv_ct))

# Convert result back to numpy
A_inv_result = np.array(A_inv_ct).reshape((3, 3))
print( Inverse matrix from C:\n , A_inv_result)
```