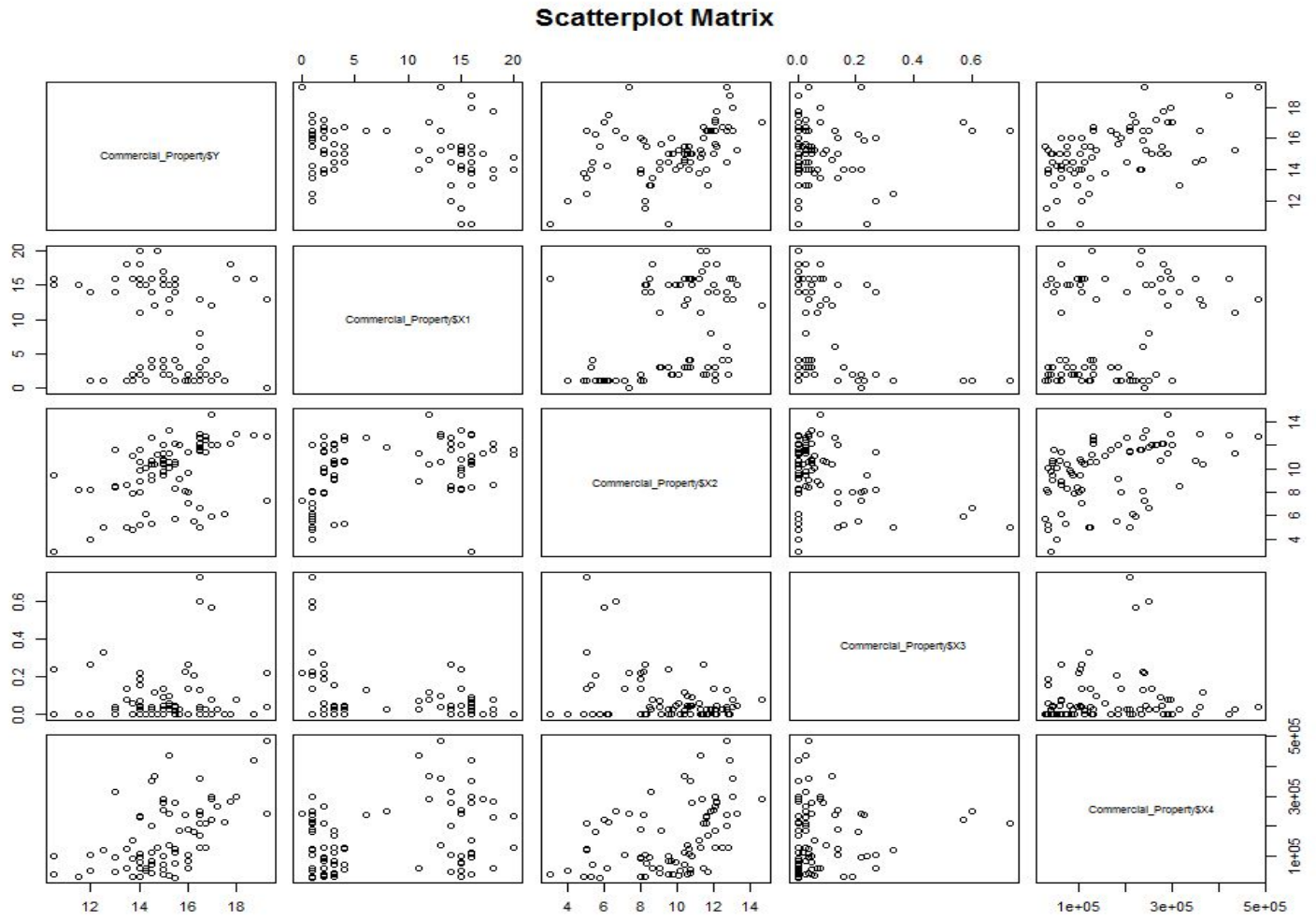


1.



Y and X1 are clearly non linear.

Y and X2 are linear.

Y and X3 are clearly non linear.

Y and X4 are linear.

2.Yhat= 1.220 - 1.420X1+2.820X2+6.193X3+7.924X4

```
> fit<-lm(Commercial_Property$Y~Commercial_Property$X1+Commercial_Property$X2+Comm  
ercial_Property$X3+Commercial_Property$X4,data=Commercial_Property)  
> summary(fit)
```

call:

```
lm(formula = Commercial_Property$Y ~ Commercial_Property$X1 +  
    Commercial_Property$X2 + Commercial_Property$X3 + Commercial_Property$X4,  
    data = Commercial_Property)
```

Residuals:

Min	1Q	Median	3Q	Max
-3.1872	-0.5911	-0.0910	0.5579	2.9441

Coefficients:

	Estimate	Std. Error	t value	Pr(> t)	
(Intercept)	1.220e+01	5.780e-01	21.110	< 2e-16	***
Commercial_Property\$X1	-1.420e-01	2.134e-02	-6.655	3.89e-09	***
Commercial_Property\$X2	2.820e-01	6.317e-02	4.464	2.75e-05	***
Commercial_Property\$X3	6.193e-01	1.087e+00	0.570	0.57	
Commercial_Property\$X4	7.924e-06	1.385e-06	5.722	1.98e-07	***

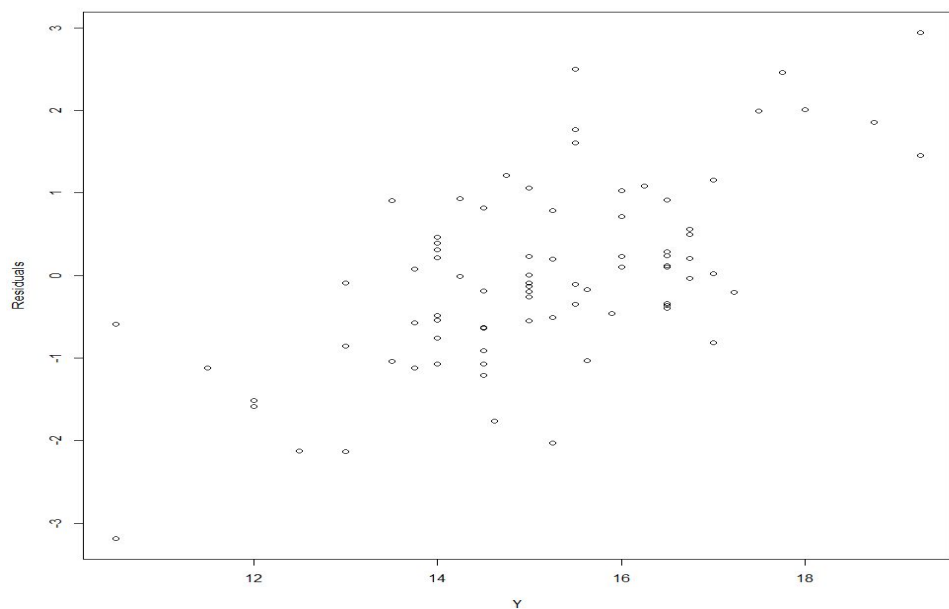
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 1.137 on 76 degrees of freedom

Multiple R-squared: 0.5847, Adjusted R-squared: 0.5629

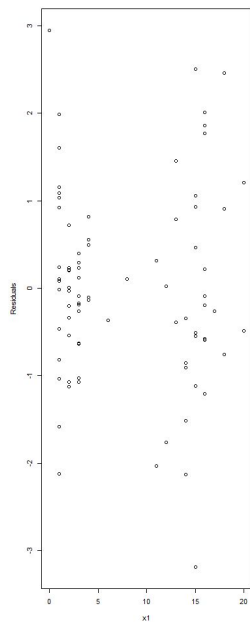
F-statistic: 26.76 on 4 and 76 DF, p-value: 7.272e-14

Residuals vs Y

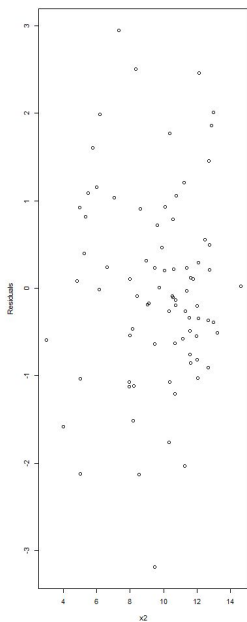


3.

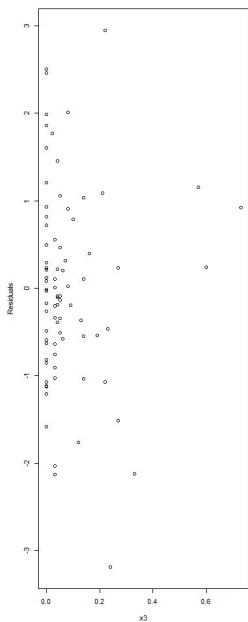
Residuals vs X1



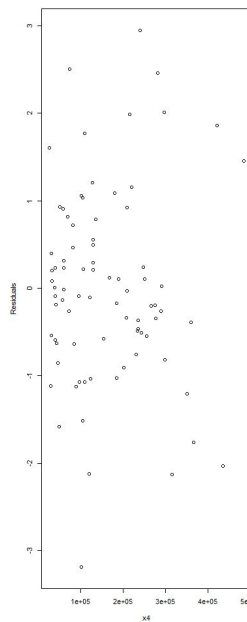
Residuals vs X2

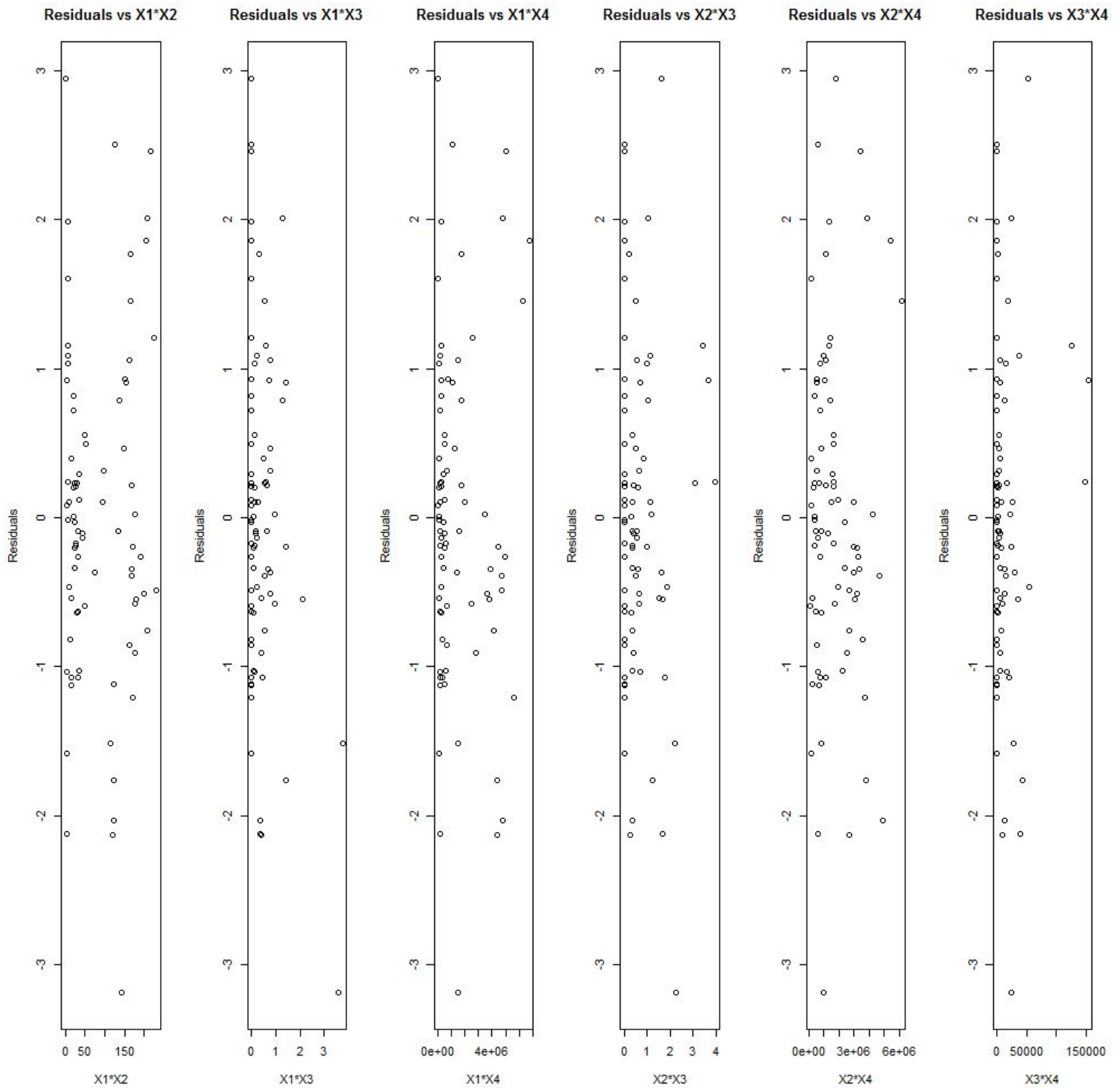


Residuals vs X3



Residuals vs X4





The residuals look like i.i.d. normally distributed, i.e., the pattern is unsystematic random around zero

4. Yes, it is significant

```
> anova(fit)
Analysis of Variance Table

Response: Commercial_Property$Y
              Df Sum Sq Mean Sq F value    Pr(>F)
Commercial_Property$X1  1 14.819   14.819 11.4649  0.001125 **
Commercial_Property$X2  1 72.802   72.802 56.3262 9.699e-11 ***
Commercial_Property$X3  1  8.381    8.381  6.4846  0.012904 *
Commercial_Property$X4  1 42.325   42.325 32.7464 1.976e-07 ***
Residuals              76 98.231    1.293
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

5. Rsq: 58.47%
Adj Rsq: 56.29%

```
> pred.commerc
      fit      lwr      upr
1 14.53567 13.97132 15.10003
2 13.51381 12.89591 14.13170
6. 3 11.09105 10.09034 12.09176

> pred.commerp
      fit      lwr      upr
1 14.53567 12.202099 16.86925
2 13.51381 11.166710 15.86090
3 11.09105  8.615475 13.56663
```

7. $\hat{Y} = 1.237 - 1.442X_1 + 2.672X_2 + 8.178X_4$

```
call:
lm(formula = Commercial_Property$Y ~ Commercial_Property$X1 +
    Commercial_Property$X2 + Commercial_Property$X4, data = Commercial_Property)

Residuals:
    Min       1Q   Median       3Q      Max
-3.0620 -0.6437 -0.1013  0.5672  2.9583

Coefficients:
              Estimate Std. Error t value Pr(>|t|)
(Intercept)   1.237e+01  4.928e-01  25.100 < 2e-16 ***
Commercial_Property$X1 -1.442e-01  2.092e-02  -6.891 1.33e-09 ***
Commercial_Property$X2  2.672e-01  5.729e-02   4.663 1.29e-05 ***
Commercial_Property$X4  8.178e-06  1.305e-06   6.265 1.97e-08 ***
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 1.132 on 77 degrees of freedom
Multiple R-squared:  0.583,    Adjusted R-squared:  0.5667
F-statistic: 35.88 on 3 and 77 DF, p-value: 1.295e-14
```

```
> anova(fit)
Analysis of Variance Table

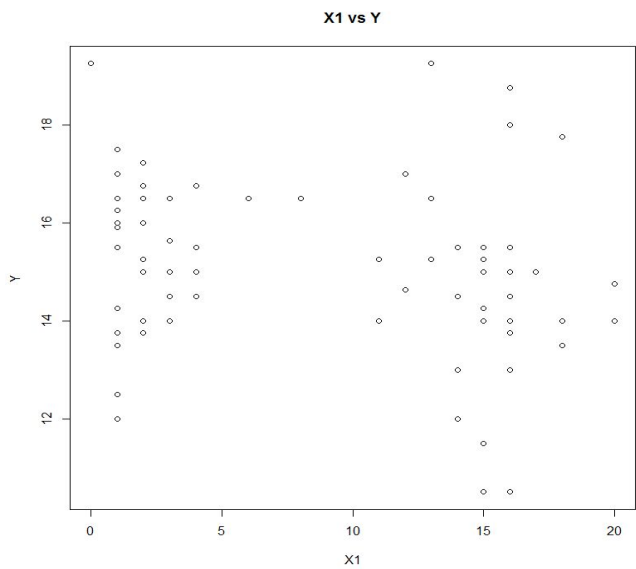
Response: Commercial_Property$Y
              Df Sum Sq Mean Sq F value    Pr(>F)
Commercial_Property$X1  1 14.819   14.819 11.4649  0.001125 **
Commercial_Property$X2  1 72.802   72.802 56.3262 9.699e-11 ***
Commercial_Property$X3  1  8.381    8.381  6.4846  0.012904 *
Commercial_Property$X4  1 42.325   42.325 32.7464 1.976e-07 ***
Residuals              76 98.231    1.293
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

> anova(fit1)
Analysis of Variance Table

Response: Commercial_Property$Y
              Df Sum Sq Mean Sq F value    Pr(>F)
Commercial_Property$X1  1 14.819   14.819 11.566   0.001067 **
Commercial_Property$X2  1 72.802   72.802 56.825   7.841e-11 ***
Commercial_Property$X4  1 50.287   50.287 39.251   1.973e-08 ***
Residuals              77 98.650    1.281
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

Removing X3 makes the model better

8.Yes there is a curvature



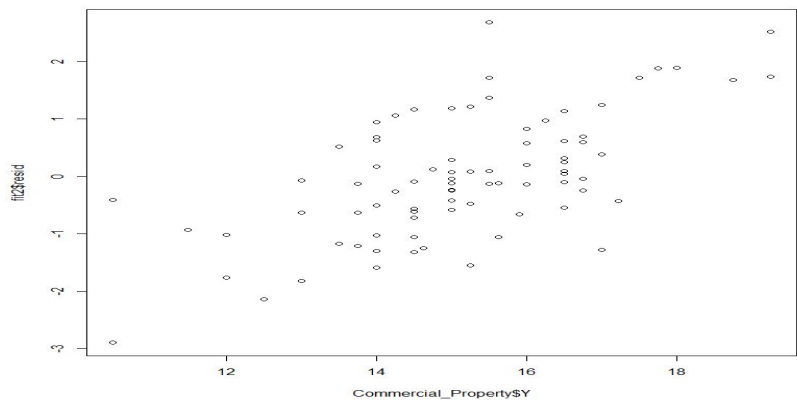
9.Yhat= 1.249 - 4.043X1 + 3.14X2 + 8.046X4 + 1.415X1^2

```
lm(formula = Commercial_Property$Y ~ Commercial_Property$X1 +
  Commercial_Property$X2 + Commercial_Property$X4 + I(Commercial_Property$X
1^2),
  data = Commercial_Property)

Residuals:
    Min       1Q   Median       3Q      Max
-2.89596 -0.62547 -0.08907  0.62793  2.68309

Coefficients:
              Estimate Std. Error t value Pr(>|t|)
(Intercept)    1.249e+01  4.805e-01  26.000  < 2e-16 ***
Commercial_Property$X1  -4.043e-01  1.089e-01  -3.712  0.00039 ***
Commercial_Property$X2   3.140e-01  5.880e-02   5.340  9.33e-07 ***
Commercial_Property$X4   8.046e-06  1.267e-06   6.351  1.42e-08 ***
I(Commercial_Property$X1^2)  1.415e-02  5.821e-03   2.431  0.01743 *
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 1.097 on 76 degrees of freedom
Multiple R-squared:  0.6131,    Adjusted R-squared:  0.5927
F-statistic: 30.1 on 4 and 76 DF, p-value: 5.203e-15
```



Yes, as the new addition of quadratic term makes the model better.

10. Clearly X_1^2 is significant

```
> anova(fit1)
Analysis of Variance Table

Response: Commercial_Property$Y
          Df Sum Sq Mean Sq F value    Pr(>F)
Commercial_Property$X1  1 14.819   14.819   11.566 0.001067 **
Commercial_Property$X2  1 72.802   72.802   56.825 7.841e-11 ***
Commercial_Property$X4  1 50.287   50.287   39.251 1.973e-08 ***
Residuals              77 98.650    1.281
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

> anova(fit2)
Analysis of Variance Table

Response: Commercial_Property$Y
          Df Sum Sq Mean Sq F value    Pr(>F)
Commercial_Property$X1  1 14.819   14.819  12.3036 0.0007627 ***
Commercial_Property$X2  1 72.802   72.802  60.4463 2.968e-11 ***
Commercial_Property$X4  1 50.287   50.287  41.7522 8.907e-09 ***
I(Commercial_Property$X1^2) 1  7.115    7.115   5.9078 0.0174321 *
Residuals              76 91.535    1.204
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```