

Market Direction Prediction using Statistical Models & Machine learning Models

Introduction:

This study attempts to predict Stock Market Index Direction based on 8 Predictor variables.

Objective of the study is to compare the Predictive Power of the Statistical Model Vs Machine Learning Models, on Financial Time series data.

S&P 500 Index data for 5 years was taken and for each date, the daily return and the returns for previous days (Lag1...Lag5) were computed. The direction of the market (Up, Down) along with Trading volume were recorded.

The data set was preprocessed and was split in 2 sets.

- a) Training data set – 1000 observations
- b) Test data set- 250 observations

The Models were built on training data set and tested on test data set.

For each Model, a confusion matrix was created and misclassification error rate was computed so as compare the Models.

The Statistical Models chosen:

- Logistic Model
- LDA Model
- QDA Model
- Naïve Bayes Model

The Machine learning Models used:

- SVM
- Random Forest
- Neural network

data.frame': 1250 obs. of 9 variables:

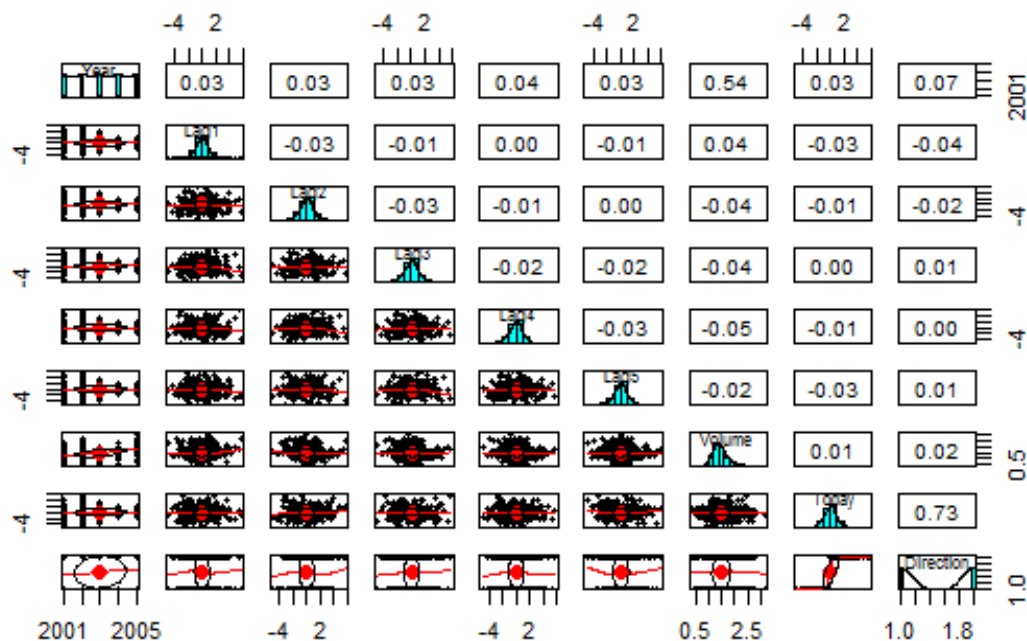
```
$ Year : num 2001 2001 2001 2001 2001 ...
$ Lag1 : num 0.381 0.959 1.032 -0.623 0.614 ...
$ Lag2 : num -0.192 0.381 0.959 1.032 -0.623 ...
$ Lag3 : num -2.624 -0.192 0.381 0.959 1.032 ...
$ Lag4 : num -1.055 -2.624 -0.192 0.381 0.959 ...
$ Lag5 : num 5.01 -1.055 -2.624 -0.192 0.381 ...
$ Volume: num 1.19 1.3 1.41 1.28 1.21 ...
$ Today : num 0.959 1.032 -0.623 0.614 0.213 ...
$ Direction: Factor w/ 2 levels "Down","Up": 2 2 1 2 2 2 1 2 2 2 ...
```

Summary(Data Set)

| | | | |
|--------------------|--------------------|--------------------|--------------------|
| Lag1 | Lag2 | Lag3 | |
| Min. :-4.922000 | Min. :-4.922000 | Min. :-4.922000 | |
| 1st Qu.: -0.639500 | 1st Qu.: -0.639500 | 1st Qu.: -0.640000 | |
| Median : 0.039000 | Median : 0.039000 | Median : 0.038500 | |
| Mean : 0.003834 | Mean : 0.003919 | Mean : 0.001716 | |
| 3rd Qu.: 0.596750 | 3rd Qu.: 0.596750 | 3rd Qu.: 0.596750 | |
| Max. : 5.733000 | Max. : 5.733000 | Max. : 5.733000 | |
| | | | |
| Lag4 | Lag5 | Volume | Today |
| Min. :-4.922000 | Min. :-4.92200 | Min. :0.3561 | Min. :-4.922000 |
| 1st Qu.: -0.640000 | 1st Qu.: -0.64000 | 1st Qu.:1.2574 | 1st Qu.: -0.639500 |
| Median : 0.038500 | Median : 0.03850 | Median : 1.4229 | Median : 0.038500 |
| Mean : 0.001636 | Mean : 0.00561 | Mean :1.4783 | Mean : 0.003138 |
| 3rd Qu.: 0.596750 | 3rd Qu.: 0.59700 | 3rd Qu.:1.6417 | 3rd Qu.: 0.596750 |
| Max. : 5.733000 | Max. : 5.73300 | Max. :3.1525 | Max. : 5.733000 |

Direction :Down:602 , Up :648

Distribution & Correlation:



Statistical Models Classification Performance

1) Logistic Model:

Confusion Matrix

| Model | Actual | |
|-------|--------|-----|
| | Down | Up |
| Down | 2 | 1 |
| Up | 109 | 140 |

Misclassification rate: 0.4365079

2) Linear Discriminant Analyses Model:

Confusion Matrix

| Model | Actual | |
|-------|--------|-----|
| | Down | Up |
| Down | 2 | 12 |
| Up | 108 | 130 |

Misclassification rate: 0.47619

3) Quadratic Discriminant Analyses Model:

Confusion Matrix

| Model | Actual | |
|-------|--------|----|
| | Down | Up |
| Down | 43 | 51 |
| Up | 68 | 90 |

Misclassification rate: 0.4722222

4) Naive Bayes Model:

Confusion Matrix

| Model | Actual | |
|-------|--------|----|
| | Down | Up |
| Down | 36 | 45 |
| Up | 75 | 96 |

Misclassification rate: 0.4761905

Machine Learning Models:

1) Support Vector Machine (SVM):

Parameters:

SVM-Type: C-classification
SVM-Kernel: radial
cost: 1
gamma: 0.1428571
Number of Support Vectors: 946
Number of Classes: 2
Levels: Down Up

Confusion Matrix

| Model | Actual | |
|-------|--------|-----|
| | Down | Up |
| Down | 1 | 0 |
| Up | 110 | 141 |

Misclassification rate: 0.4365079

2) Random Forest:

[summary\(rfmodel\)](#)

Type of random forest: classification

Number of trees: 500

No. of variables tried at each split: 2

OOB estimate of error rate: 49.4%

[rfmodel\\$importance](#)

MeanDecreaseGini

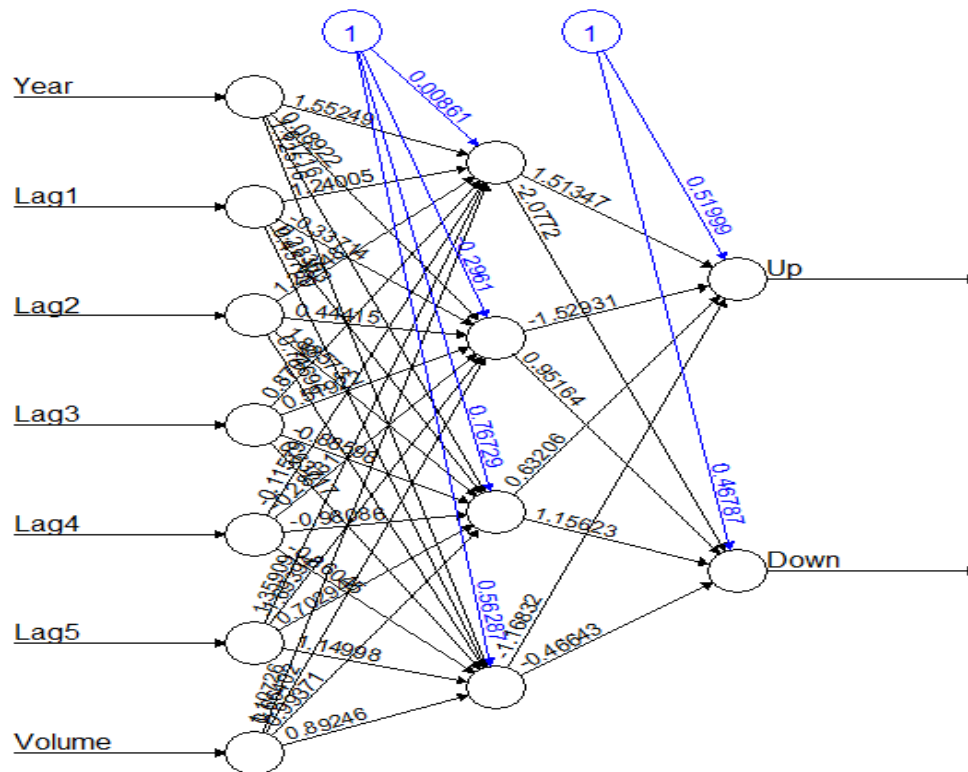
| | |
|--------|----------|
| Year | 22.85293 |
| Lag1 | 83.01989 |
| Lag2 | 77.37586 |
| Lag3 | 77.67590 |
| Lag4 | 77.00136 |
| Lag5 | 78.16711 |
| Volume | 82.25598 |

Confusion Matrix

| Model | Actual | |
|-------|--------|----|
| | Down | Up |
| Down | 64 | 38 |
| Up | 67 | 83 |

Misclassification rate(Test): 0.4166

3) Neural Net Model:



Error: 249.435872 Steps: 35

Confusion Matrix

| Model | Actual | |
|-------|--------|-----|
| | Down | Up |
| Down | 109 | 137 |
| Up | 2 | 4 |

Misclassification rate(Test): 0.5515

Conclusion:

The results are intriguing. The best performing Models among Statistical Models is the Logistic Model with lowest misclassification error rate.

Among machine Learning Models Learning Models, Random Forest is the best predictor with lowest Misclassification error.

Machine Learning Algorithm Prediction completely depends on the data, sample size and latent construct.

The Research Team,

ALBEDO ENERGY

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