

# DSA Pattern Course 2025 – Day 4: Two Pointer Pattern Mastery (C++)

★ Today's Goal: Three Medium-Level Problems → One Pass Pattern



## 1. Sort Two Colors (Only 0s and 1s)

(Custom problem → Three Colors Problem ko samajhne ka base)



### Problem Statement

Ek array `nums` diya hai jisme **sirf 0s aur 1s hain.**

List ko **in-place** sort karna hai:

All 0s → left All 1s → right

### Approach 1: Brute Force (Two-Pass Counting)

#### ✓ Step 1: Count

- `c0` → number of 0s
- `c1` → number of 1s

#### ✓ Step 2: Overwrite

- First `c0` times write `0`
- Then `c1` times write `1`

#### Complexity

- Time:  $O(N) + O(N) = O(N)$
- Space: `O(1)` (only counters)
- ◆ Best brute force → but not one pass.

Interviewer: “One pass me solve karoo!”

# Approach 2: Optimal One Pass (Two Pointers)

## Pointer Meaning:

Pointer	Start	Invariant
i (Left)	0	i se pehle sab 0s
j (Right)	n-1	j ke baad sab 1s

Only i pointer traversal karega (`while(i <= j)`)

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## Logic (while i <= j)

### Case 1: nums[i] == 0

✓ Already correct

👉 Move `i++`

---

### Case 2: nums[i] == 1

✗ Wrong place → should be on right

👉 Swap `nums[i]` with `nums[j]`

👉 Move `j--`

❗ Don't increment `i`

(kyunki j se aaya element ab i par check hona chahiye)

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## Code (C++)

```
void sortTwoColors(vector<int>& nums) { int i = 0; // left pointer → 0s region
int j = nums.size() - 1; // right pointer → 1s region // Process until both pointers meet
while (i <= j) { // If nums[i] is 0 → already at correct place if (nums[i] == 0) { i++; } // If nums[i] is 1 → send it to right side else { swap(nums[i], nums[j]); j--; // decrease right boundary // i ko yahan increase nahi karte // kyunki swapped value ko dobara check karna zaroori hai } } }
```



Embed anything (PDFs, Google Docs, Google Maps, Spotify...)

## ■ 2 . LeetCode 75 - Sort Colors (Brute Force: Counting Method)

Most clean & most accepted brute force.

### 🧠 Intuition (Hinglish + Simple)

Array me sirf 3 values hoti hain → 0, 1, 2

Toh brute force ka best tareeka hai:

1 Count karo kitne 0, kitne 1, kitne 2

2 Rewrite kar do array ko is order me:

0 → 1 → 2

Bas. Sorting bhi nahi chahiye.

Extra space bhi nahi lagta.

Logic bhi crystal clear.

### 🧩 Step-by-Step Breakdown

#### Step 1: Count Frequency

- Har element ek loop me traverse hogा
- Values:
  - Agar 0 → zero++
  - Agar 1 → one++
  - Agar 2 → two++

#### Step 2: Rewrite Array

- Index = 0 se start
- Pehle saare zero values (0)
- Fir saare one values (1)
- Fir saare two values (2)
- Every assignment uses

```
nums[index++] = x;
```

# index++ (Important for beginners)

`index++` ka matlab:

- 👉 Pehle current index use hota hai
- 👉 Fir index **1 se increase** ho jaata hai

Example:

- index = 0 → use hua → index = 1
- index = 1 → use hua → index = 2
- index = 2 → use hua → index = 3

Yeh ensure karta hai ki **har naya element next position par hi jaaye.**

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## Brute Force Code (C++)

```
void sortColors(vector<int>& nums) { int zero = 0, one = 0, two = 0; // Step 1:  
Counting frequency for(int x : nums){ if(x == 0) zero++; else if(x == 1) one++;  
else two++; } // Step 2: Rewrite array int index = 0; while(zero--){ nums[index]  
++ = 0; } while(one--){ nums[index++] = 1; } while(two--){ nums[index++] = 2;  
} }
```



## Dry Run (Clear & Simple)

Input:

```
[2, 0, 2, 1, 1, 0]
```

Step 1 → Count

```
zero = 2 one = 2 two = 2
```

Step 2 → Rewrite

```
nums[0] = 0 nums[1] = 0 nums[2] = 1 nums[3] = 1 nums[4] = 2 nums[5] = 2
```

Final Output:

[0, 0, 1, 1, 2, 2]

## ⌚ Time Complexity (Detailed + Interview Explanation)

### ✓ Step 1: Counting

- Hum array ko 1 bar traverse karte hain → length = n

Cost: O(n)

### ✓ Step 2: Rewrite

- Rewrite me total operations = **zero** + **one** + **two**
- Yeh values milke **n** hi hoti hain

Cost: O(n)

### ⌚ Total Time Complexity

$O(n) + O(n) = O(n)$

### Why it's efficient?

- No nested loops
- No sorting algorithm
- Two linear passes only

Interview me confidently bolo:

👉 “Brute force but still linear-time.”



## Space Complexity (Deep Explanation)

### Variables used:

zero → stores count of 0s  
one → stores count of 1s  
two → stores count of 2s  
ind ex → pointing to current write position

Bas 4 integer variables.

No extra array, no vector, nothing else.

## Constant space

Input array ke size par depend nahi hota.

## Why O(1)?

- Hum sirf counts store karte hain
  - Rewrite bhi **usi same array me** hota hai (in-place)
- 

 Final Summary (Easy to Recall)

Step	Work
Count	Find 0s, 1s, 2s
Rewrite	Fill array: $0 \rightarrow 1 \rightarrow 2$
TC	$O(n)$
SC	$O(1)$
Why good?	Fast, clean, interview-suitable brute force

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 2. LeetCode 75 – Sort Colors (Optimal:  
Two Pointer / Dutch National Flag  
Algorithm)

Most important + most asked + zero confusion version.

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 Intuition (Hinglish + Crystal Clear)

Array me sirf **0, 1, 2** hota hai.

Hume array ko *in-place* sort karna hai.

Goal:

0s left → 1s middle → 2s right

Toh hum 3 pointer use karte:

1) low

→ Jaha next 0 rakhna hai

## 2) mid

→ Current element jise check karna hai

## 3) high

→ Jaha next 2 rakhna hai

---



# Core Idea (Very Important)

Rules based on `nums[mid]`:

**Case 1 → `nums[mid] == 0`**

👉 Swap(`nums[low], nums[mid]`)

👉 `low++, mid++`

Because 0 belongs to left.

---

**Case 2 → `nums[mid] == 1`**

👉 `mid++`

Because 1 already at correct middle region.

---

**Case 3 → `nums[mid] == 2`**

👉 Swap(`nums[mid], nums[high]`)

👉 `high--`

BUT `mid++ nahi`,

kyunki swap ke baad jo element aya hai mid par, usko fir se check karna padta hai.

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# Why Two Pointer Works Perfectly?

- 0s ko left bhejo
- 2s ko right bhejo
- 1s automatically center me aa jaate

Ek hi pass me sorting complete.

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# Optimal Code (C++)

```
void sortColors(vector<int>& nums) { int low = 0, mid = 0, high = nums.size() - 1; while(mid <= high) { if(nums[mid] == 0) { swap(nums[low], nums[mid]); low++; mid++; } else if(nums[mid] == 1) { mid++; } else { // nums[mid] == 2 swap(nums[mid], nums[high]); high--; } } }
```

## Dry Run (Step-by-Step Clear Walkthrough)

Input:

```
[2, 0, 2, 1, 1, 0]
```

Start:

```
low=0, mid=0, high=5
```

**Step 1:**

mid=0 → 2

Swap(mid, high)

Array → [0, 0, 2, 1, 1, 2]

high=4

(mid same: 0)

**Step 2:**

mid=0 → 0

Swap(low, mid)

Array → [0, 0, 2, 1, 1, 2]

low=1, mid=1

**Step 3:**

mid=1 → 0

Swap(low, mid)

Array → [0, 0, 2, 1, 1, 2]

low=2, mid=2

---

#### Step 4:

mid=2 → 2

Swap(mid, high)

Array → [0, 0, 1, 1, 2, 2]

high=3

---

#### Step 5:

mid=2 → 1

mid = 3

---

#### Step 6:

mid=3 → 1

mid = 4 > high → STOP

Final Output:

[0, 0, 1, 1, 2, 2]

## ⌚ Time Complexity (Detail + Interview-Perfect)

### Single while loop

```
mid moves from 0 → n-1 (maximum once) low moves forward only high moves backward only
```

👉 No element is processed more than **once**.

### Final Time Complexity

O(n)

Better than brute force?

→ Same time complexity, but **1 pass** instead of 2.



# Space Complexity

Hum sirf use kar rahe:

```
low, mid, high → 3 variables
```

Koi extra array nahi.

Sorting **in-place** hoti hai.

## Space Complexity

```
O(1)
```

## ★ Why TWO POINTER is Optimal?

- One-pass algorithm
- In-place (no extra space)
- No frequency counting
- No sorting
- Fastest + cleanest
- Interviewer always expects this solution



## Final Summary (Easy to Revise)

Pointer	Meaning
low	yaha next 0 jaayega
mid	current element
high	yaha next 2 jaayega

Case	Action
nums[mid] == 0	swap(low, mid), low++, mid++
nums[mid] == 1	mid++
nums[mid] == 2	swap(mid, high), high--

Result	Value
TC	$O(n)$
SC	$O(1)$
Passes	Single pass

## ■ 3. LeetCode #19 – Remove N-th Node From End of Linked List

### ★ Brute Force Solution (2-Pass Approach)

- ✓ Easiest
  - ✓ High clarity
  - ✓ No confusion
  - ✓ Interview-approved brute force
- 

### 🧠 Problem in Simple Hinglish

Ek linked list di hui hai.

Hume **end se N-th node** ko delete karna hai.

Example:

List = `1 → 2 → 3 → 4 → 5`, n = 2

→ End se 2nd = 4, so result = `1 → 2 → 3 → 5`

---

### 🚀 Brute Force Intuition (Super Clear)

Linked list me **piche se count nahi kar sakte**,

isiliye hum kya karte?

### 🔥 Step 1:

Pehle **total length L nikal lo**.

## 🔥 Step 2:

Agar length L pata hai...

Toh **end se n-th** node ka matlab hota hai:

```
Start se (L - n + 1)-th node delete karna
```

But delete karne ke liye hume **previous node** chahiye.

Yani hume reach karna hoga:

```
(L - n)-th node
```

## 🔥 Step 3:

Simply uska next skip kar do:

```
prev->next = prev->next->next
```

## ✳️ Edge Case (Important)

Agar tumhe **head** remove karna hai, that means:

```
n == length
```

→ Directly return `head->next`.

## 💻 Brute Force Code (C++) – Cleanest

```
ListNode* removeNthFromEnd(ListNode* head, int n) { // Step 1: Find total length of list
    int length = 0;
    ListNode* temp = head;
    while(temp != nullptr) {
        length++;
        temp = temp->next;
    }
    // Edge case: remove head if(n == length) {
    //     return head->next;
    // }
    // Step 2: Reach (length - n)-th node (previous node)
    temp = head;
    for(int i = 1; i < length - n; i++) {
        temp = temp->next;
    }
    // Step 3: Delete next node
    temp->next = temp->next->next;
    return head;
}
```



# Dry Run (Ultra Clear)

Input:

```
head = 1 → 2 → 3 → 4 → 5 n = 2
```

## ✓ Step 1: Find Length

```
length = 5
```

## ✓ Step 2: Which node to delete?

Delete =  $(5 - 2 + 1) = 4\text{th node}$  → value = 4

Previous node index =  $5 - 2 = 3$  → value = 3

## ✓ Step 3: Delete

```
3 → next = 4 → next 3 → next = 5
```

Final list:

```
1 → 2 → 3 → 5
```



## Time Complexity (Deep but Simple)

**Pass 1 → Length count**

$O(n)$

**Pass 2 → Delete position find**

$O(n)$

**Total:**

```
 $O(n) + O(n) = O(2n) = O(n)$ 
```

Linear time brute force.



# Space Complexity

Sirf 2-3 pointers and integers:

```
temp, length
```

**Total space:**

```
O(1)
```

Constant space, no extra list.

---

## ★ Why This is Pure BRUTE FORCE?

- ✓ Linked list ko **do baar traverse** karna
- ✓ Simple logic: pehle length, phir delete
- ✓ Easy to implement
- ✓ Beginner-friendly
- ✓ Interview me jab woh bole:

“Brute force solution batao” → yahi bolna

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## ● Final Revision Table

Task	Meaning
Step 1	Length count
Step 2	(L - n)-th node tak jao
Step 3	next skip karke delete karo
TC	<b>O(n)</b>
SC	<b>O(1)</b>
Style	2-pass

### 3. LeetCode #19 – Remove N-th Node From End of List

#### ★ Optimal Solution — Two Pointer (One-Pass Method)

- ✓ Fastest
  - ✓ Most elegant
  - ✓ Most asked in FAANG rounds
  - ✓ Single traversal only
- 

#### 🧠 Intuition (Super Clear Hinglish)

Hume end se N-th node delete karni hai.

But hum list ko **piche se** traverse nahi kar sakte.

Toh hum kya karte?

#### 🔥 Two Pointer Trick:

- **fast pointer** ko **n steps aage** chala do
- **slow pointer** ko head par hi rakho
- Ab dono ko **same speed** se move karo
- Jab fast end (NULL) par pahunch jaaye →  
**slow exactly delete hone wali node ke pehle** hogा

Yahi magic hai two-pointer technique ka.

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#### 🎯 Why It Works? (Very Visual)

Suppose list ka end se N=2 delete karna hai.

fast pointer ko:

```
fast → n steps ahead
```

So gap = **n nodes** between fast & slow.

Then:

- Dono ko ek sath move karo
- Jab fast end tak pahunchta hai:
  - slow → (end se n)-th node ke just pehle hota hai

Yani perfect delete position mil jaati hai.

## Edge Case: Delete head

Agar fast initially n step aage le jaane se fast NULL ho jaaye →

- Means humko **head delete** karna hai.

Solution:

```
return head->next;
```



## Optimal Two-Pointer Code (C++)

```
ListNode* removeNthFromEnd(ListNode* head, int n) { ListNode* fast = head; ListNode* slow = head; // Step 1: Move fast pointer n steps ahead for(int i = 0; i < n; i++) { fast = fast->next; } // If fast is NULL, delete head if(fast == NULL) { return head->next; } // Step 2: Move both pointers together while(fast->next != NULL) { fast = fast->next; slow = slow->next; } // Step 3: Delete slow->next slow->next = slow->next->next; return head; }
```



## Dry Run (Crystal Clear & Intuitive)

List:

```
1 → 2 → 3 → 4 → 5 n = 2
```

### Step 1 → Move fast n steps

fast moves 2 steps:

```
fast at 3 slow at 1
```

### Step 2 → Move both

Move until fast->next becomes NULL:

Movement	fast	slow
1	4	2
2	5	3
3	NULL (stop)	3

Now slow is at **3** → this is **previous node** of the node to delete.

### Step 3 → Delete

```
slow->next = 4 slow->next = slow->next->next
```

Final list:

```
1 → 2 → 3 → 5
```

Perfect.

## ⌚ Time Complexity (Best Possible)

Step 1: Move fast n steps → O(n)

Step 2: Move until end → O(n)

BUT both are **just consecutive steps in ONE traversal**, not two full traversals.

★ Final TC:

```
O(n)
```

Single pass algorithm.

## 💾 Space Complexity

Sirf do pointers:

```
fast, slow
```

O(1)

## ★ Why This is the Optimal Solution?

- Only **one traversal**
- Uses **two pointers**, perfect for linked list
- No need to count length
- Handles all cases cleanly
- Fastest and shortest code
- Interviewers LOVE this approach

## ✓ Final Revision Sheet

Step	Explanation
1	fast ko n steps aage bhejo
2	fast-null → delete head
3	fast & slow ko ek sath chalao
4	slow bilkul delete ke pehle hogा