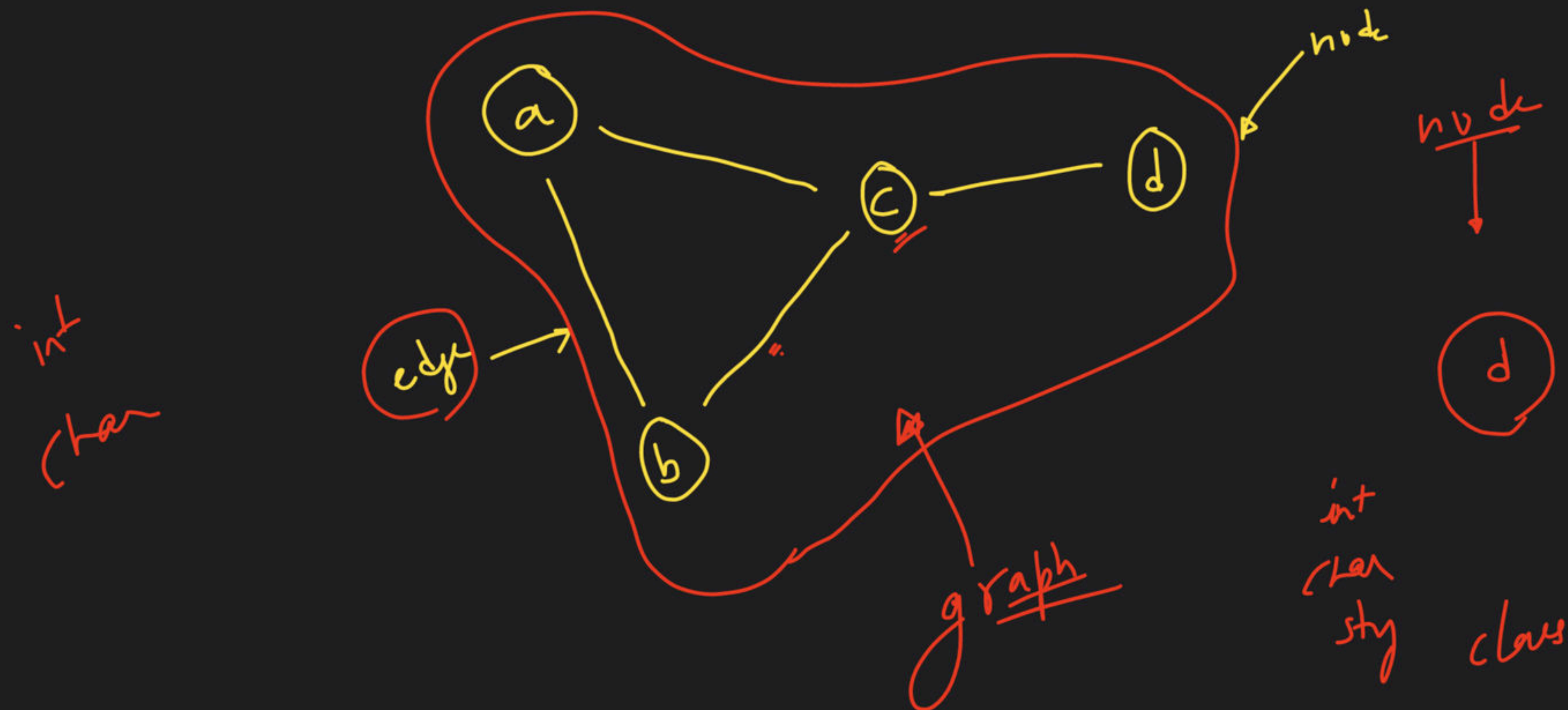
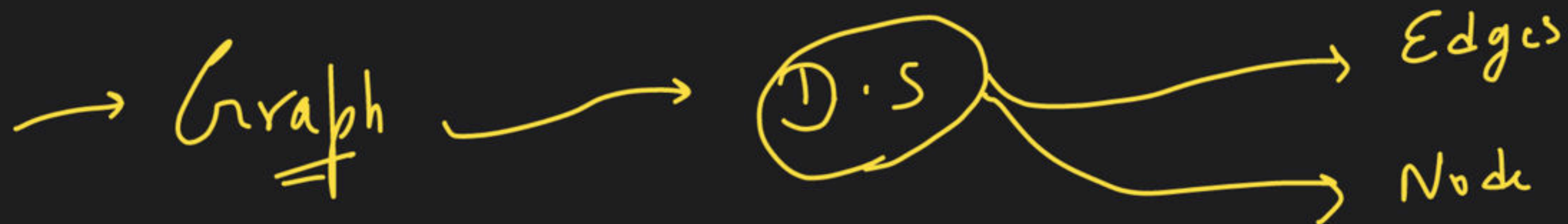




# Graphs Class - 1

Special class



edge:-

directed

undirected

a →



Edge link

a-b a-d d-b b-c  
b-a d-a b-d c-b



a → b  
b → c  
b → d

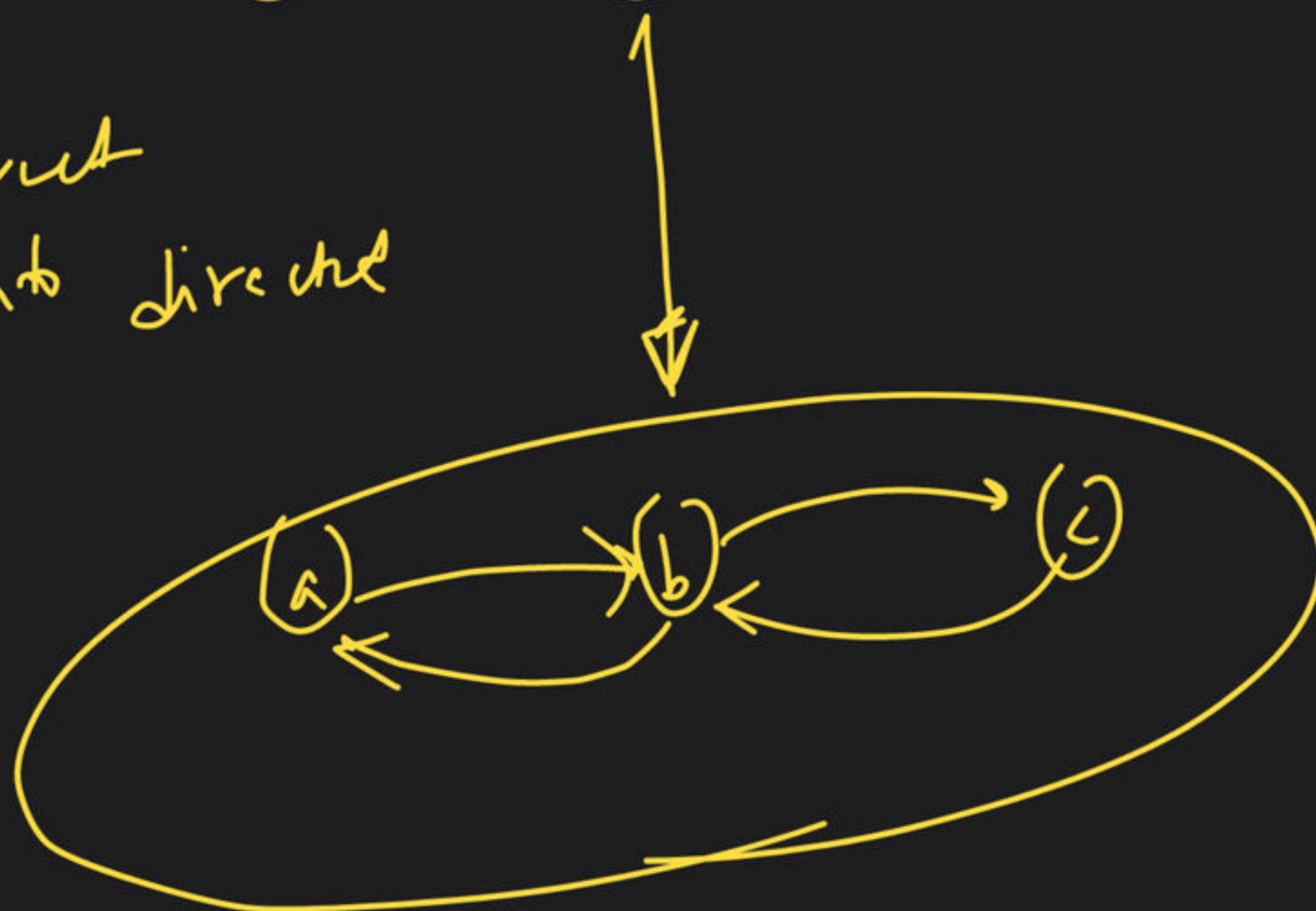
Edge list



undirected

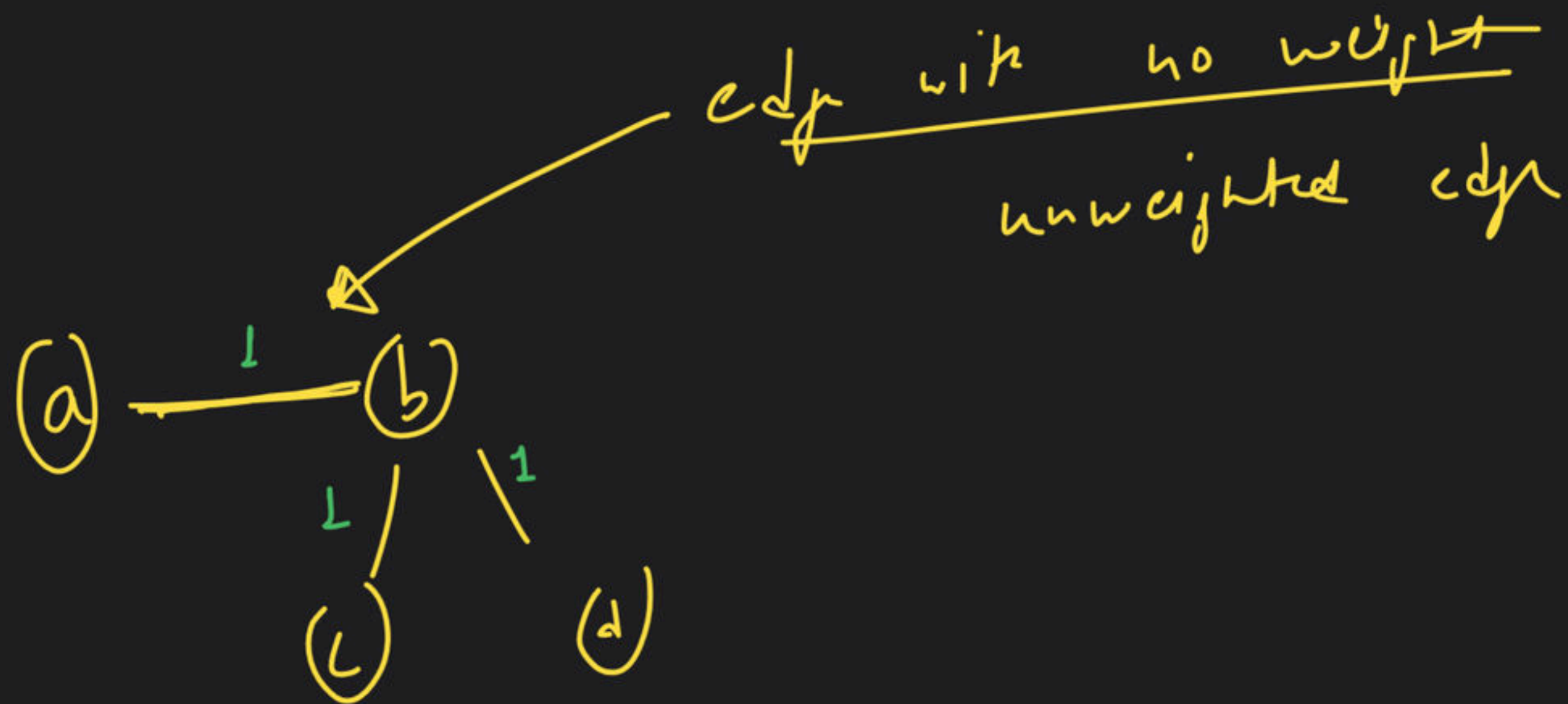


convert  
into directed

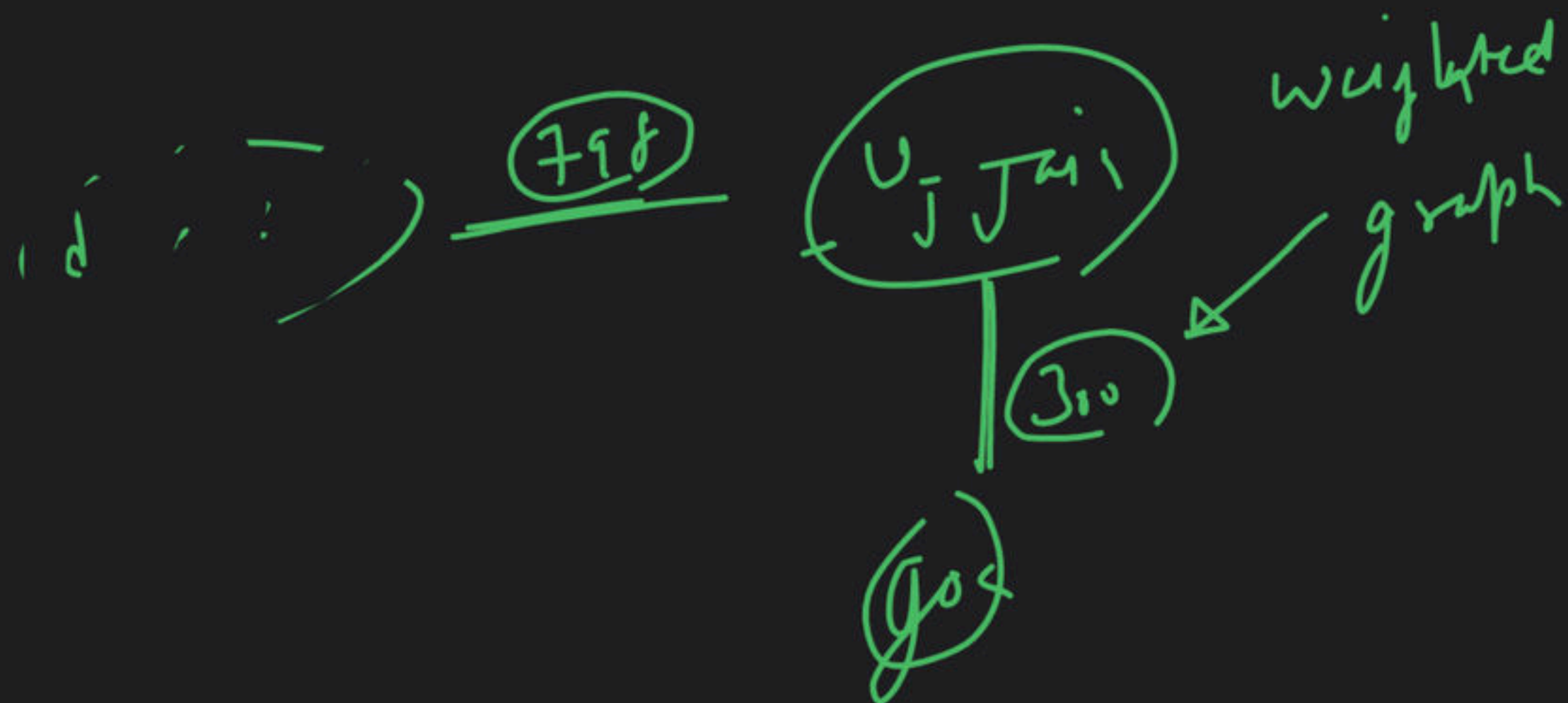


Practical  
applications

↳ google map  
↳ facebook map

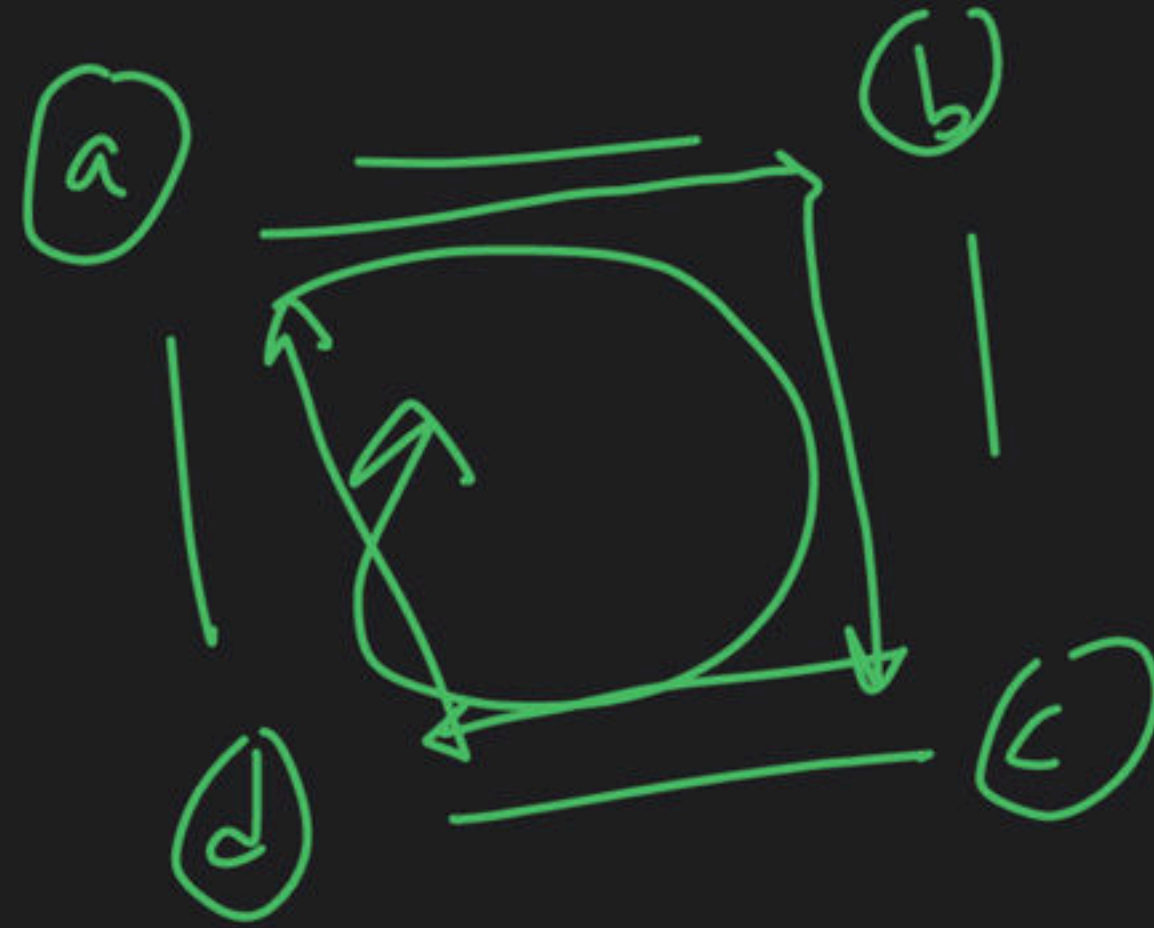


weight

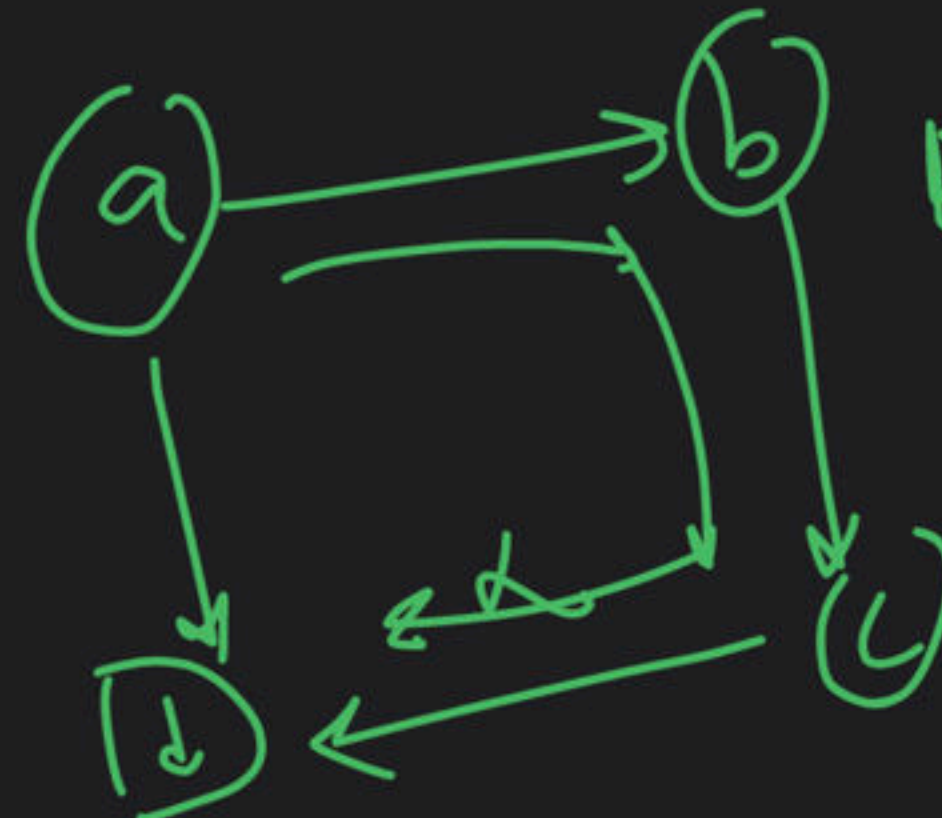




→ Cycle



Cyclic graph



Acyclic



degree



$$\text{degree}(a) = 3$$

$$\text{degree}(b) = 2$$

$$\text{degree}(d) = 2$$

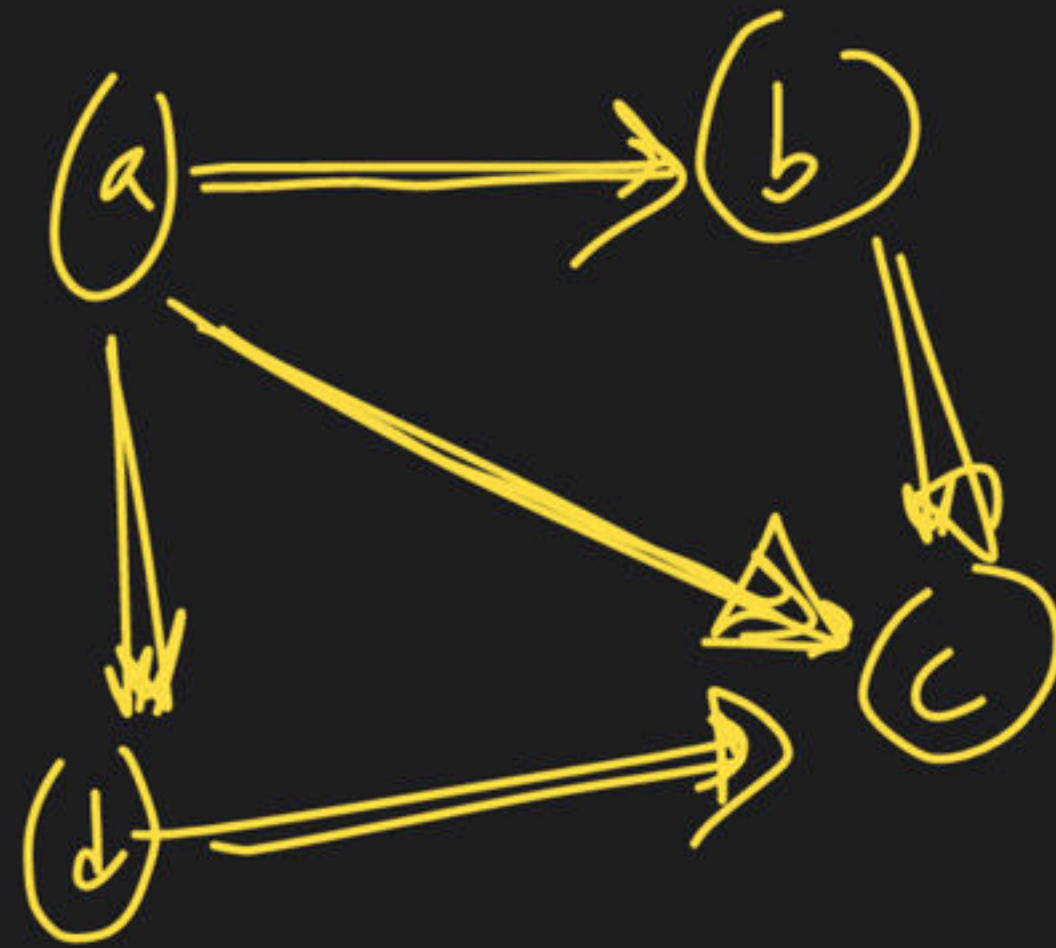
$$\text{degree}(c) = 3$$



Directed  
graph

Indegree

Outdegree



$$\text{Indegree}(a) = 0$$

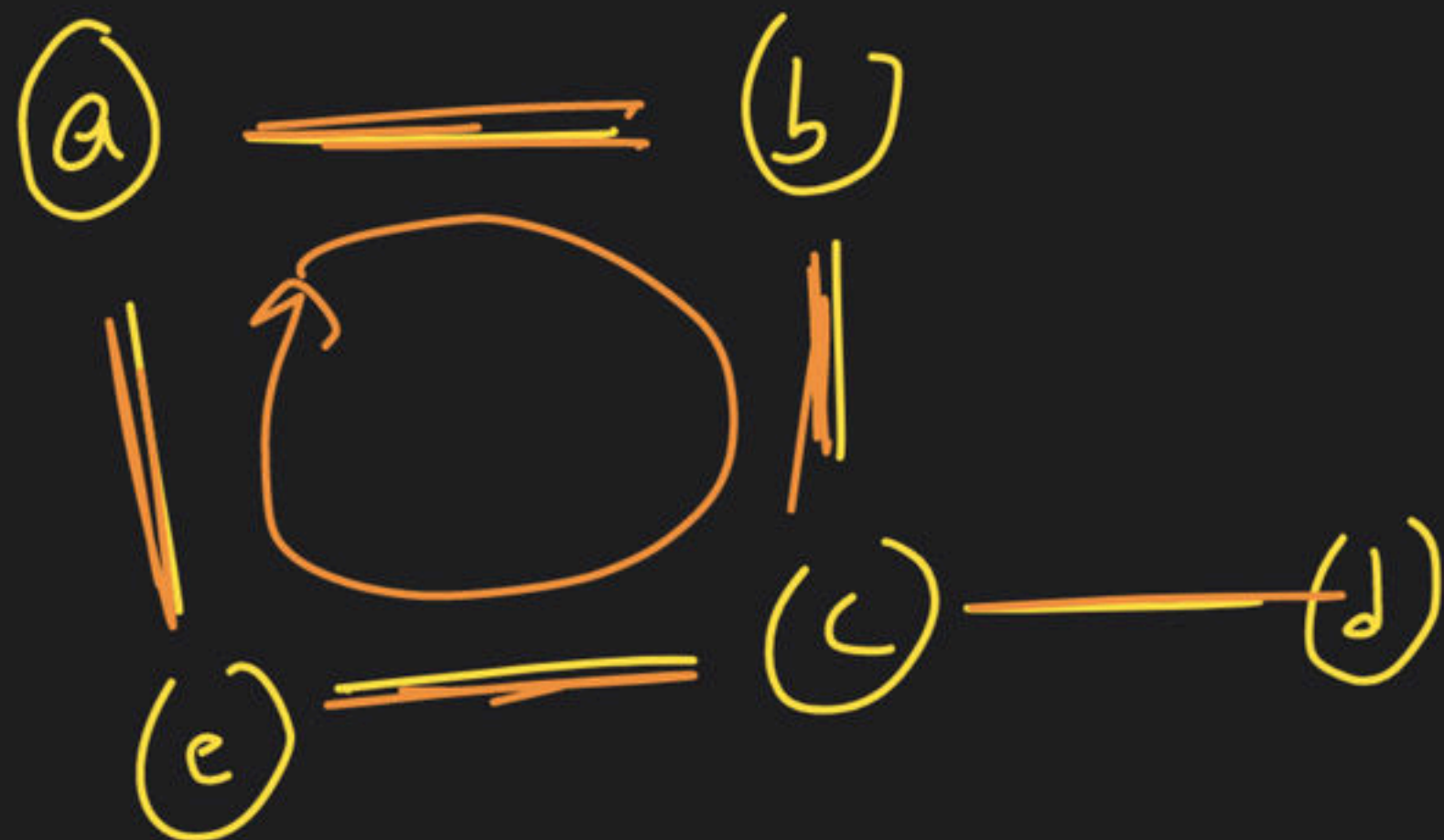
$$\text{Outdegree}(c) = 3$$

$$\text{Indegree}(c) = 3$$

$$\text{Outdegree}(c) = 0$$

Path:-

a - b - c - c - c



→ path

graph

→ edge

→ node

→ undirected

→ directed

→ weighted

→ unweighted

→ degree

→ in degree

→ out degree

→ cycle / Acyclic

a - b - c - d





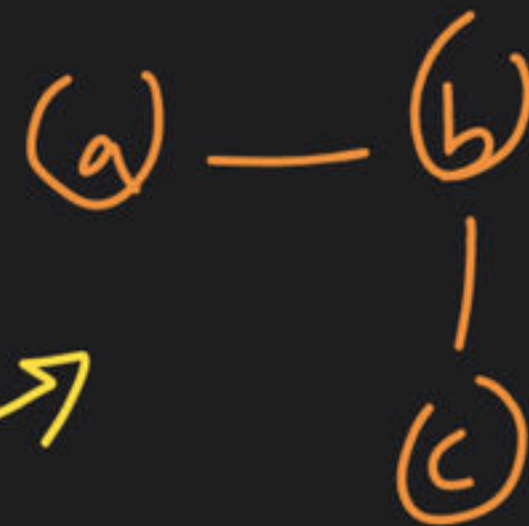
Component



Connected  
graph

disconnected  
graph

Component



Component



Component



graph





2 min  
3 sec



① clone a graph

②



Graph

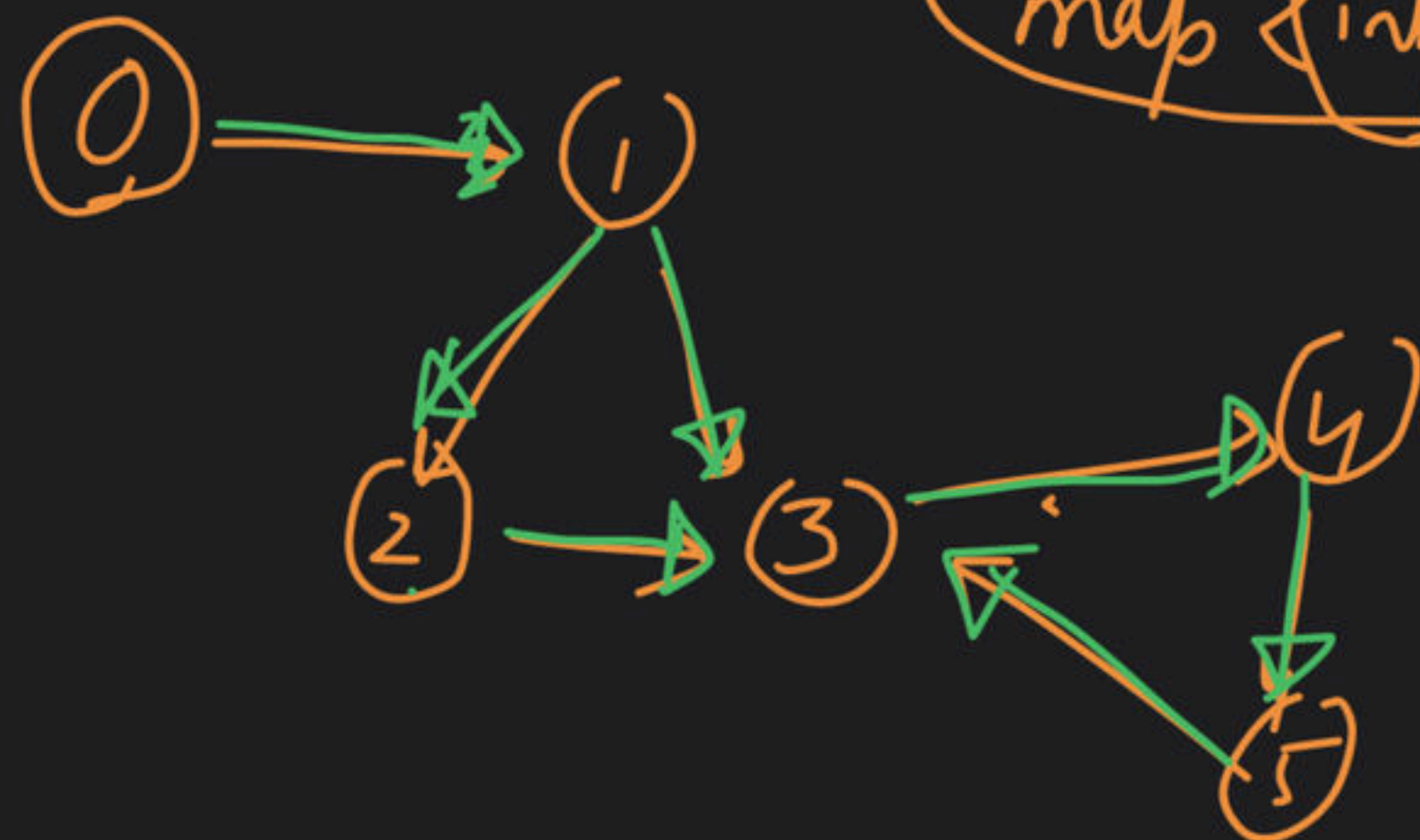
creation

Adjacency matrix

Adjacency List

map <int, list<int>>

Adj List





direction

$g.addEdge(0, 1, 0)$   
 $g.addEdge(1, 2, 0)$   
 $g.addEdge(1, 3, 0)$   
 $g.addEdge(2, 3, 0)$

$u=1$   
 $v=2$

$u=0$   
 $v=1$

$u=1$   
 $v=3$

$u=2$   
 $v=3$

$adj[u].push\_back(v)$   
 $adj[v].push\_back(u)$

adj List

0: {1}

1: {0, 2, 3}

2: {1, 3}

3: {1, 2}

```
for (auto _i = adjList)
```

```
{ // i → < 0 : {1} >
```

```
cout << i.first;
```

```
for (auto neighbour : i.second)
```

```
{  
    cout << neighbour;  
}  
}
```

print

adj List

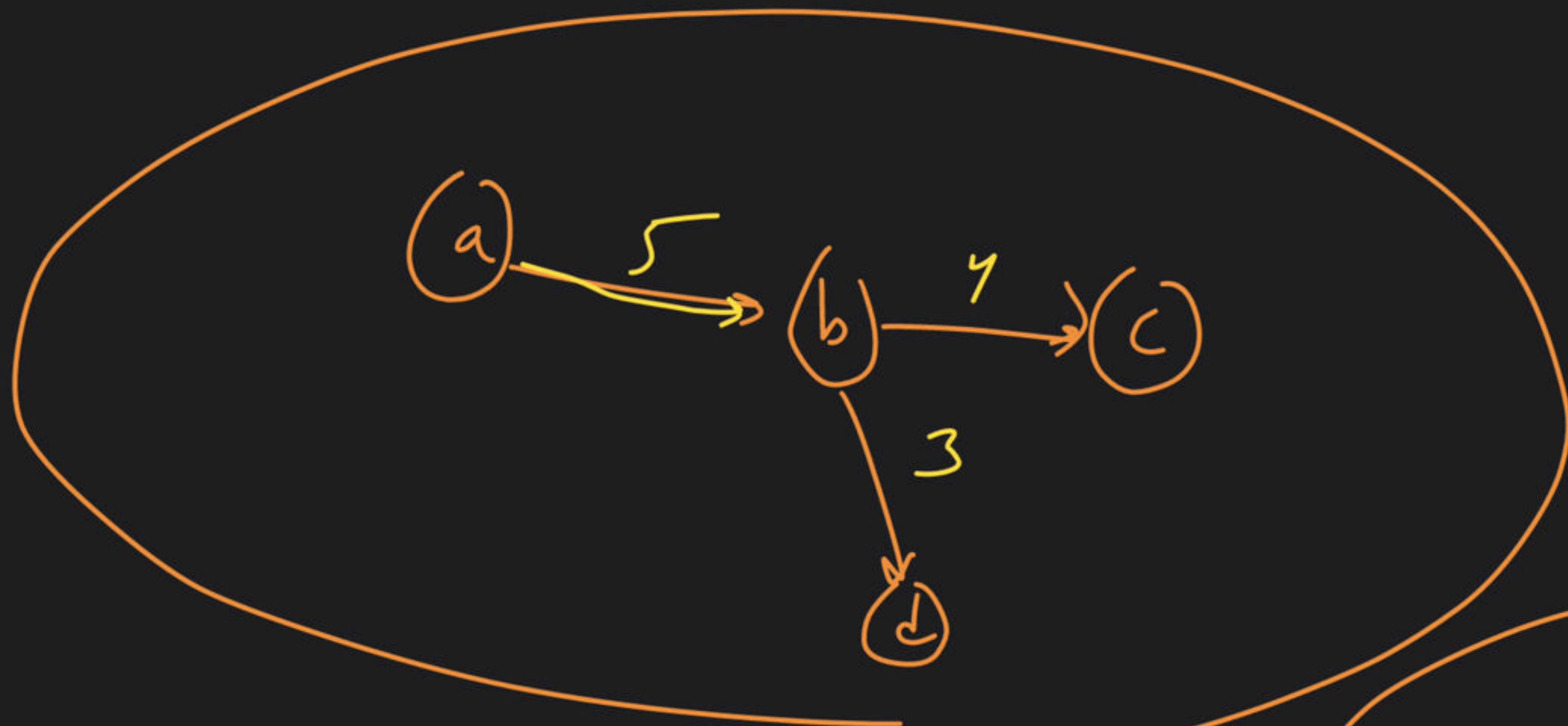
0 : {1}

1 : {2, 3}

2 : {3}

3 : { }



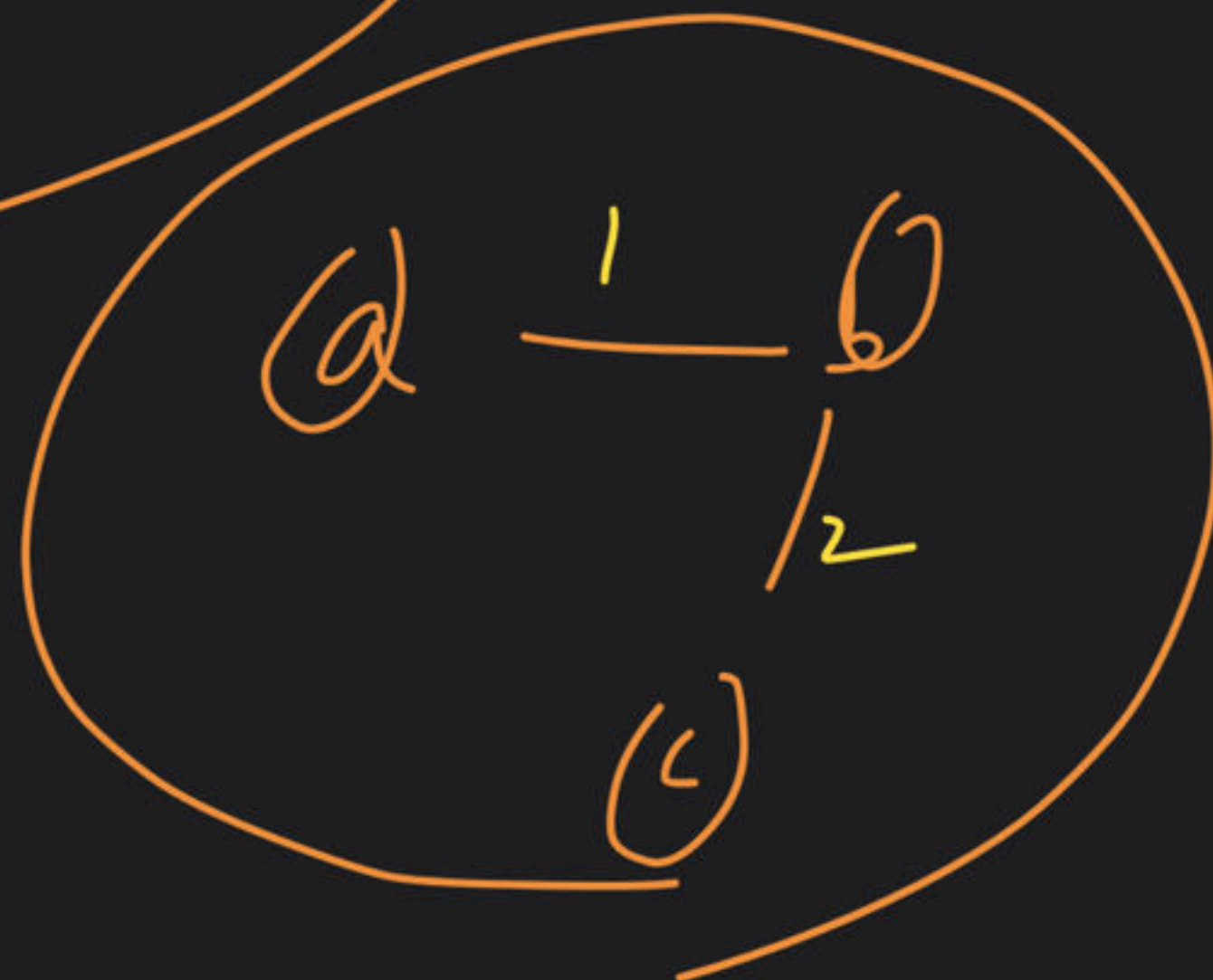


Rawat  
↓  
weighted

a  $\xrightarrow{5}$  b

b  $\xrightarrow{4}$  c

b  $\xrightarrow{3}$  d





map < (int) , (list < int) > >

↑  
val

↑  
neighbors

~~A~~

map < (int) , list < pair < int, int > > &g

↑  
val

0 : { {1, 5} , {2, 12} , {3, 20} }

↑  
val

↑  
neighbors

↑  
data

↑  
int

graph

↳ adj List

n/w

→ T.C →

→ S.C →

Graph

Traversal

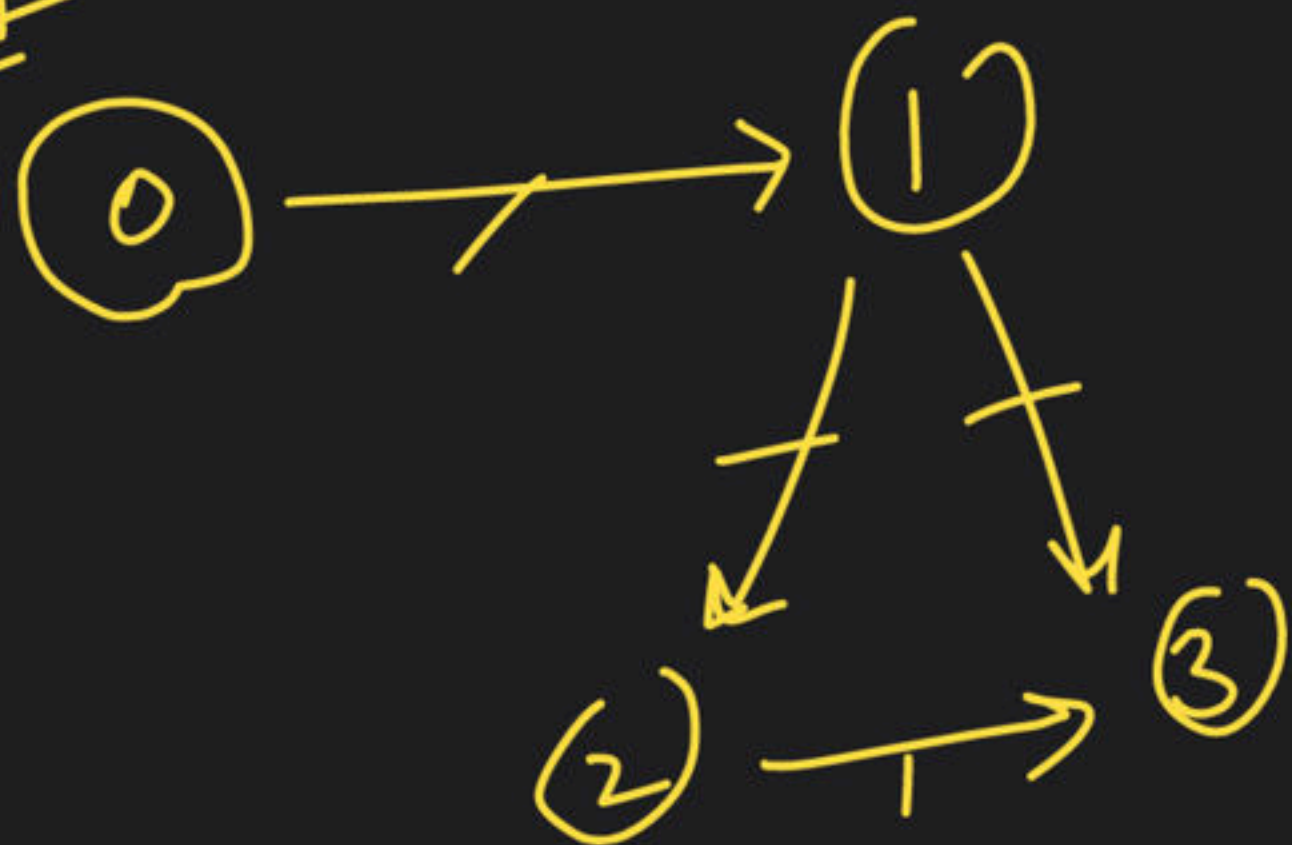
BFS

DFS

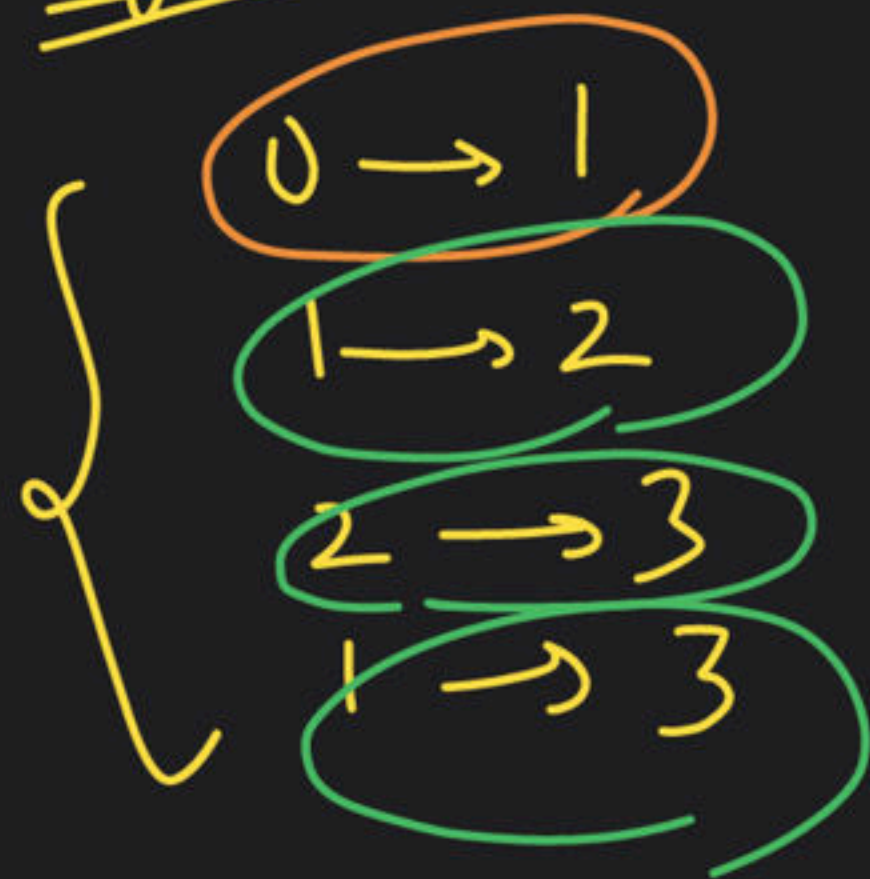




graph



edge list



Adjacency matrix

$n \times n$   
↓  
no. of nodes = 4

	0	1	2	3
0	0	1	0	0
1	0	0	1	1
2	0	0	0	1
3	0	0	0	0



T.C  $\rightarrow O(n^2)$

void

solve

(vector <pair <int, int>> edgelist)

{  
int n = edgelist.size

vector <vector <int>> adj(n, vector<int>(n, 0));

for

(auto i : edgelist)

{

int u = i.first;

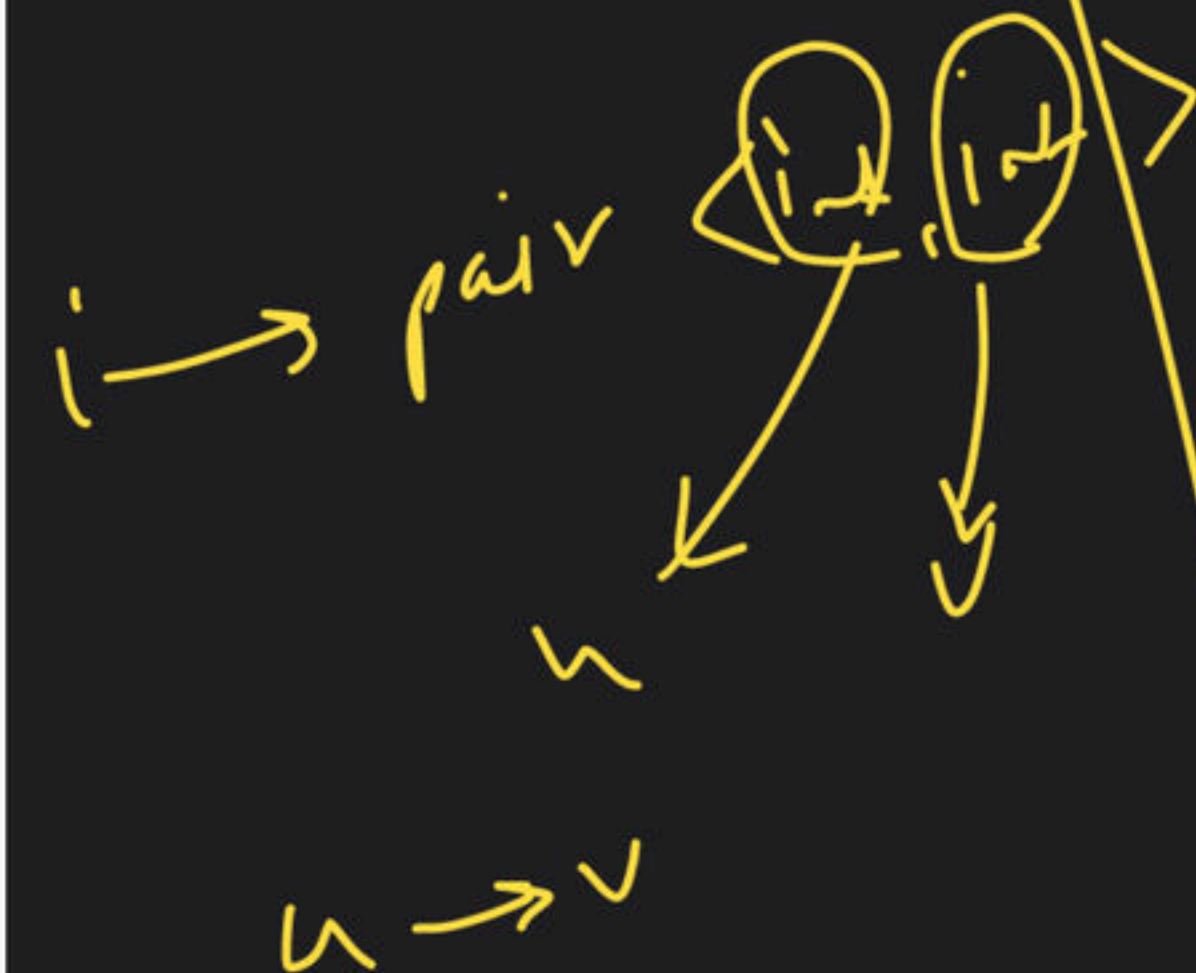
int v = i.second;

adj[u][v] = 1;

}

}

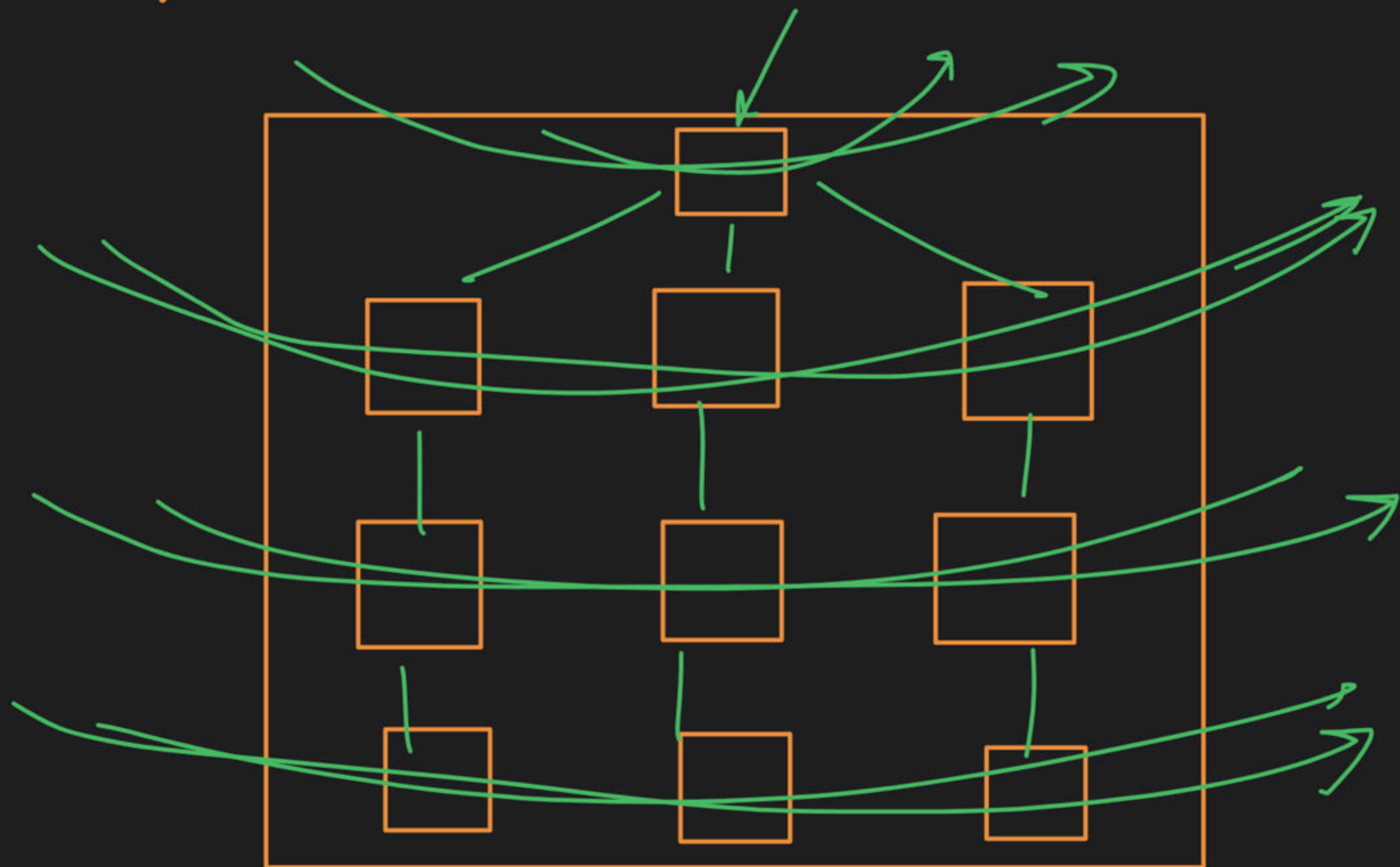
S.C  $\rightarrow O(n^2)$





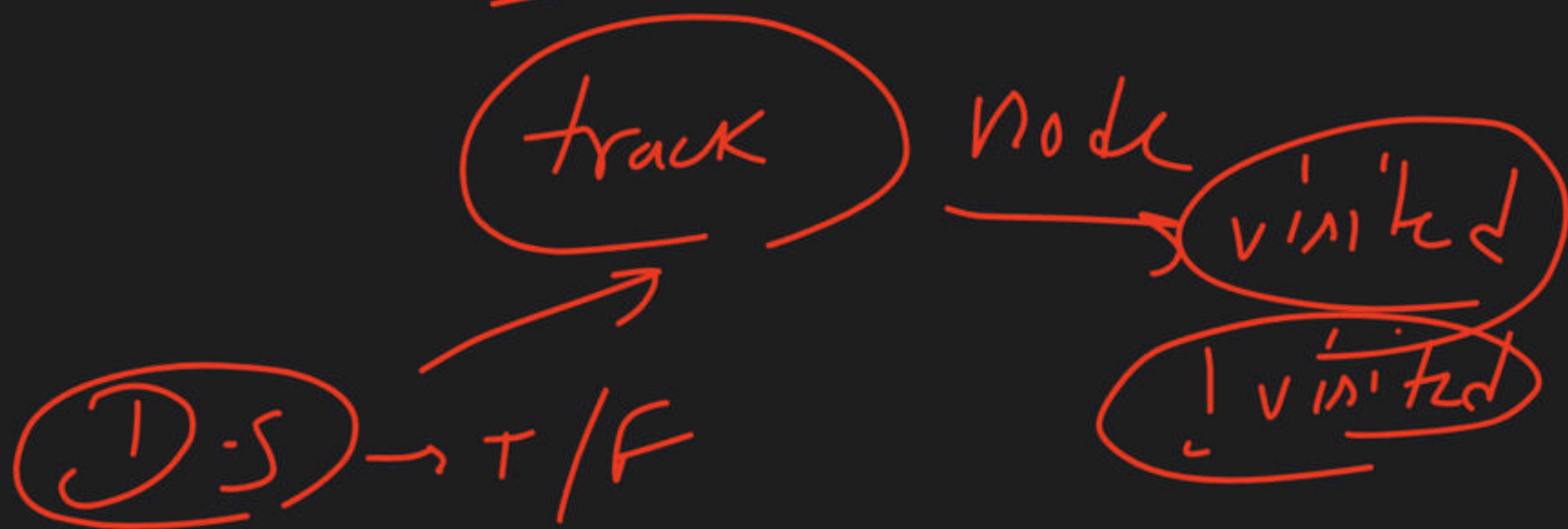
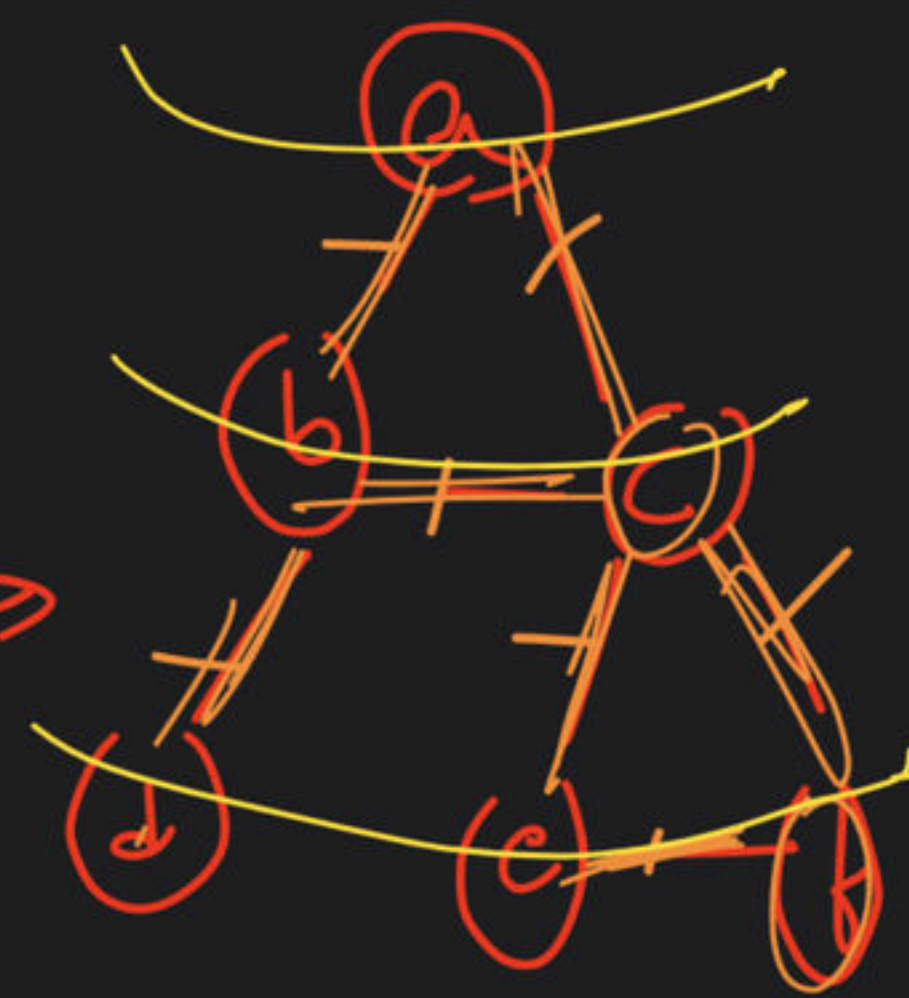
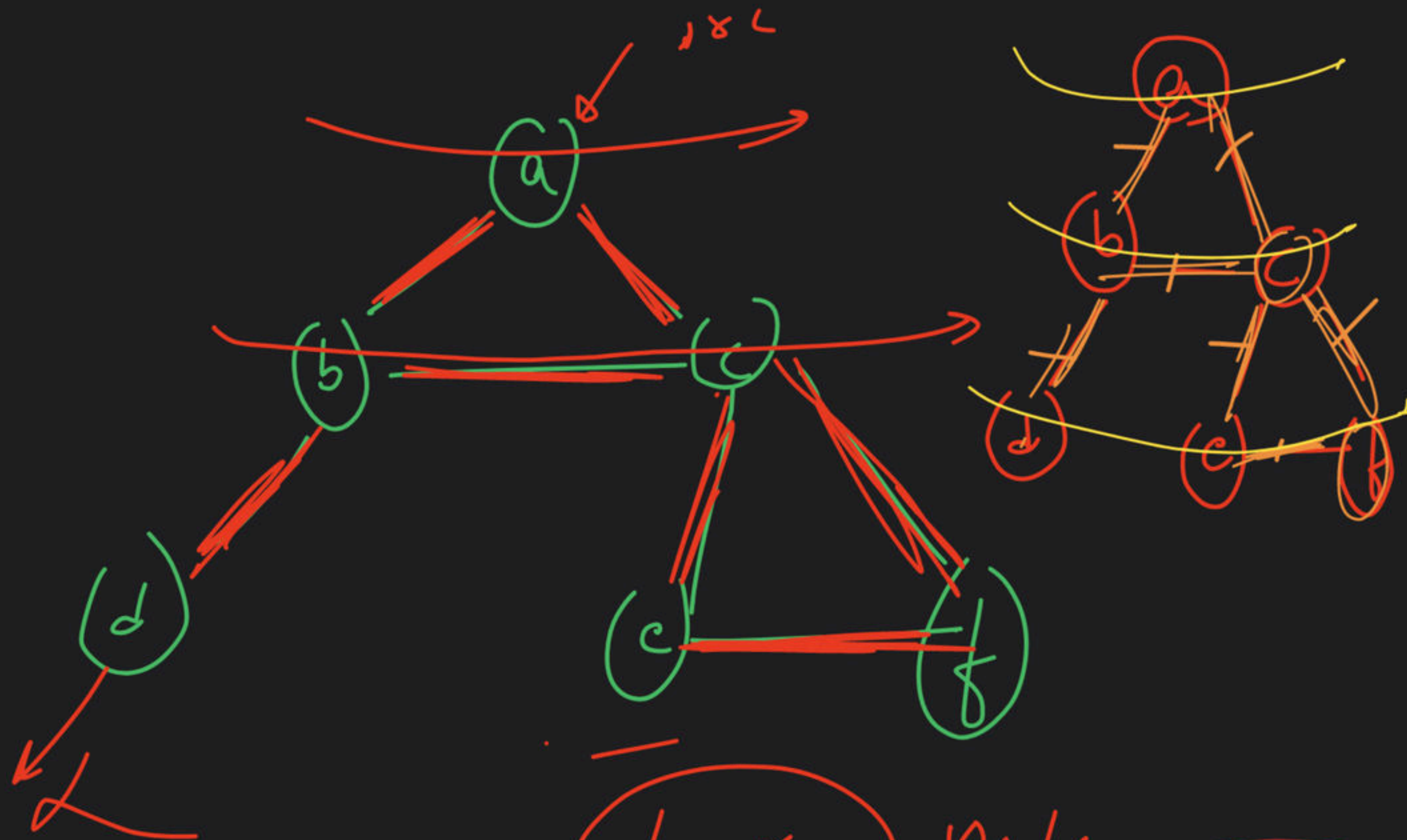
BFS:- Breadth first Search

Queue





a  
b c  
d e f





q.front



node = q.front()

node a

q.pop()

print

child

check

T → prn

copy  
↓  
mark new

initial

1st c → 'a'  
q.push(c)  
vis[a] = T

Adj List //

a → {b, c}  
b → {a, c, d}  
c → {a, b, e, f}  
d → {b}  
e → {c, f}  
f → {c, e}

visited //

a → ~~T~~  
b → ~~T~~  
c → ~~T~~  
d → ~~T~~  
e → ~~T~~  
f → ~~T~~

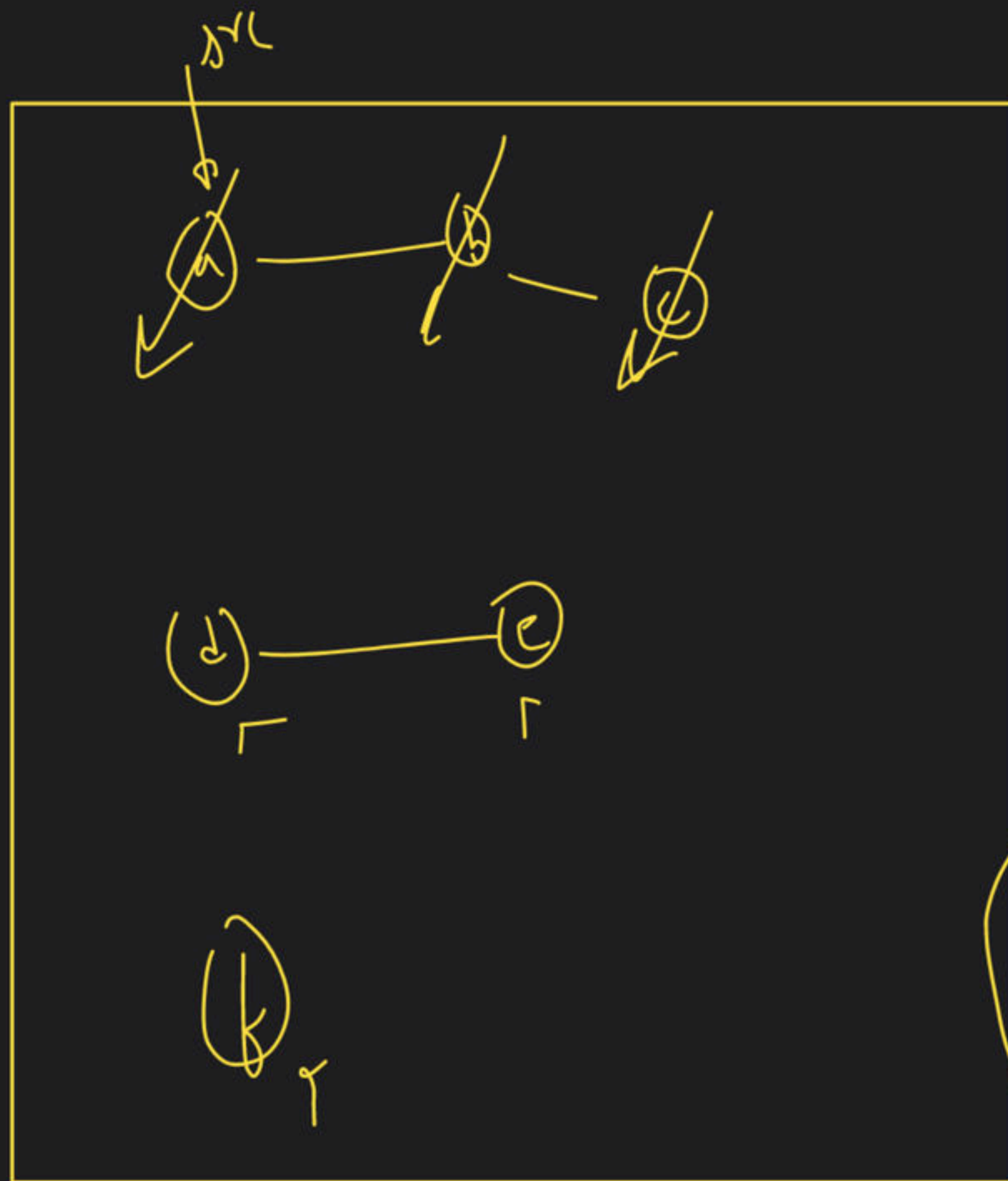
o/p

a  
b  
c  
d  
e  
f

edges-List //

a → b	c → c
b → a	c → c
a → c	c → f
c → a	f → c
b → c	c → f
c → b	f → c
b → d	
d → b	



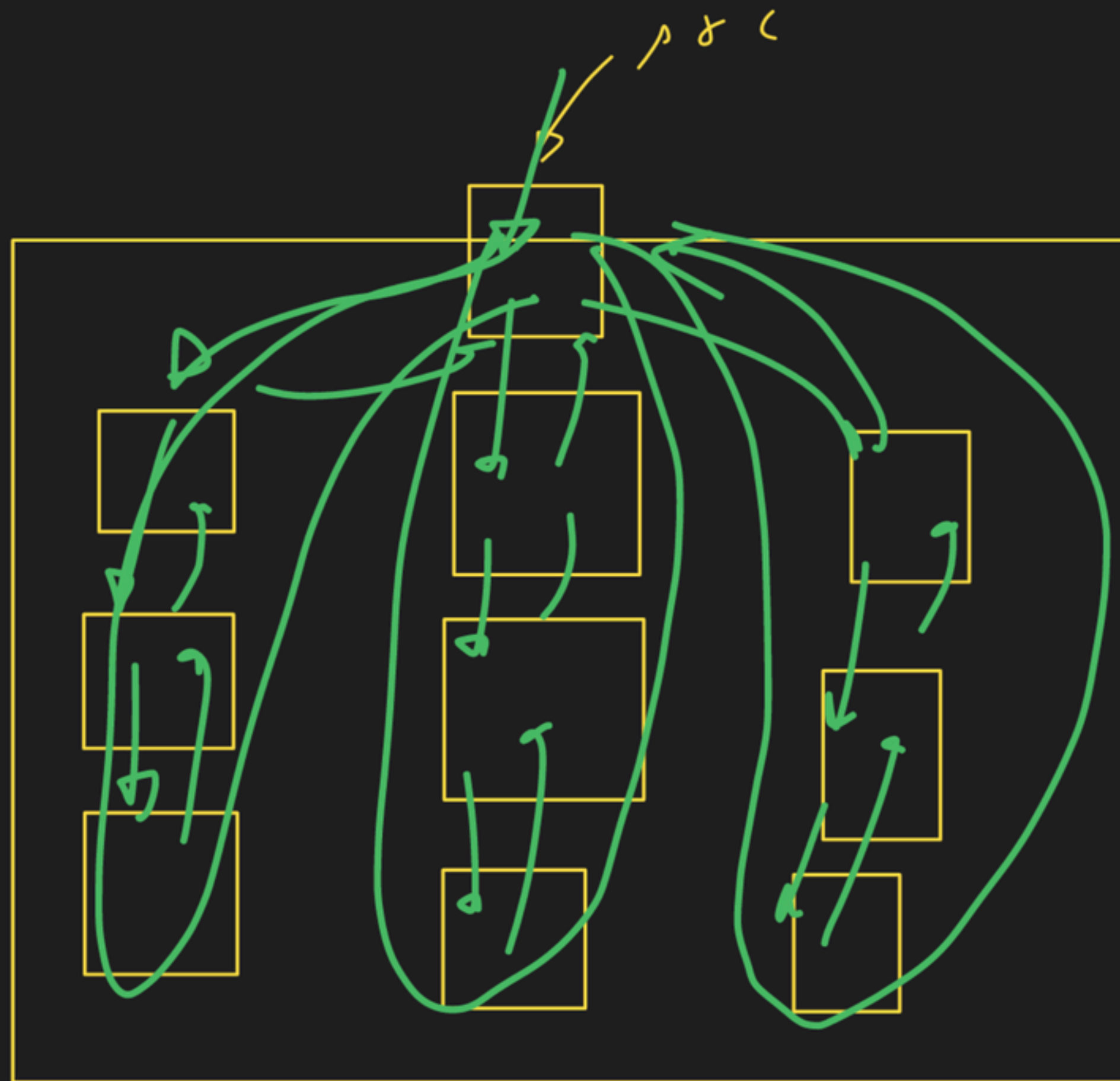


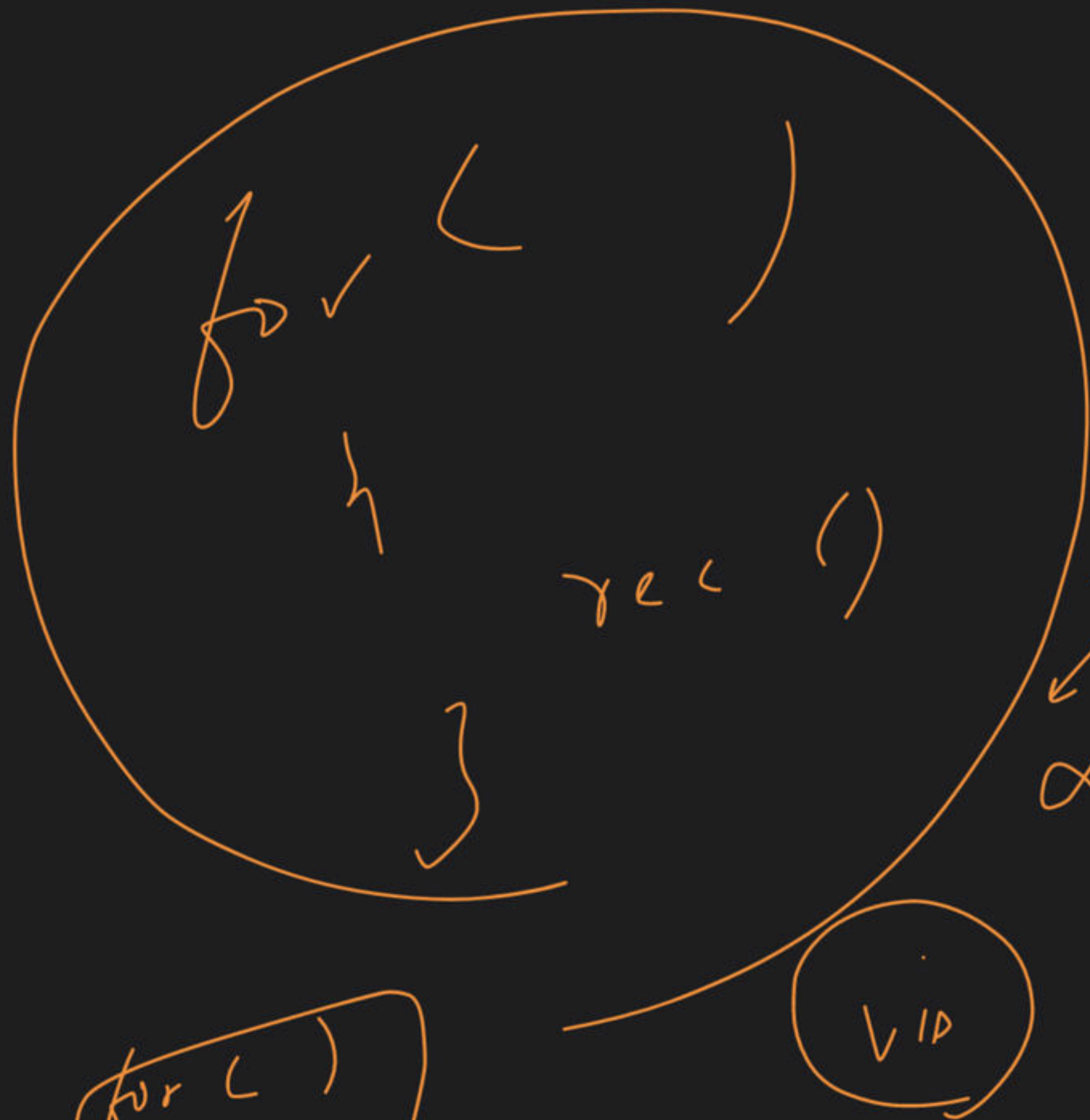
$I.C \rightarrow$   
 $S.C \rightarrow$



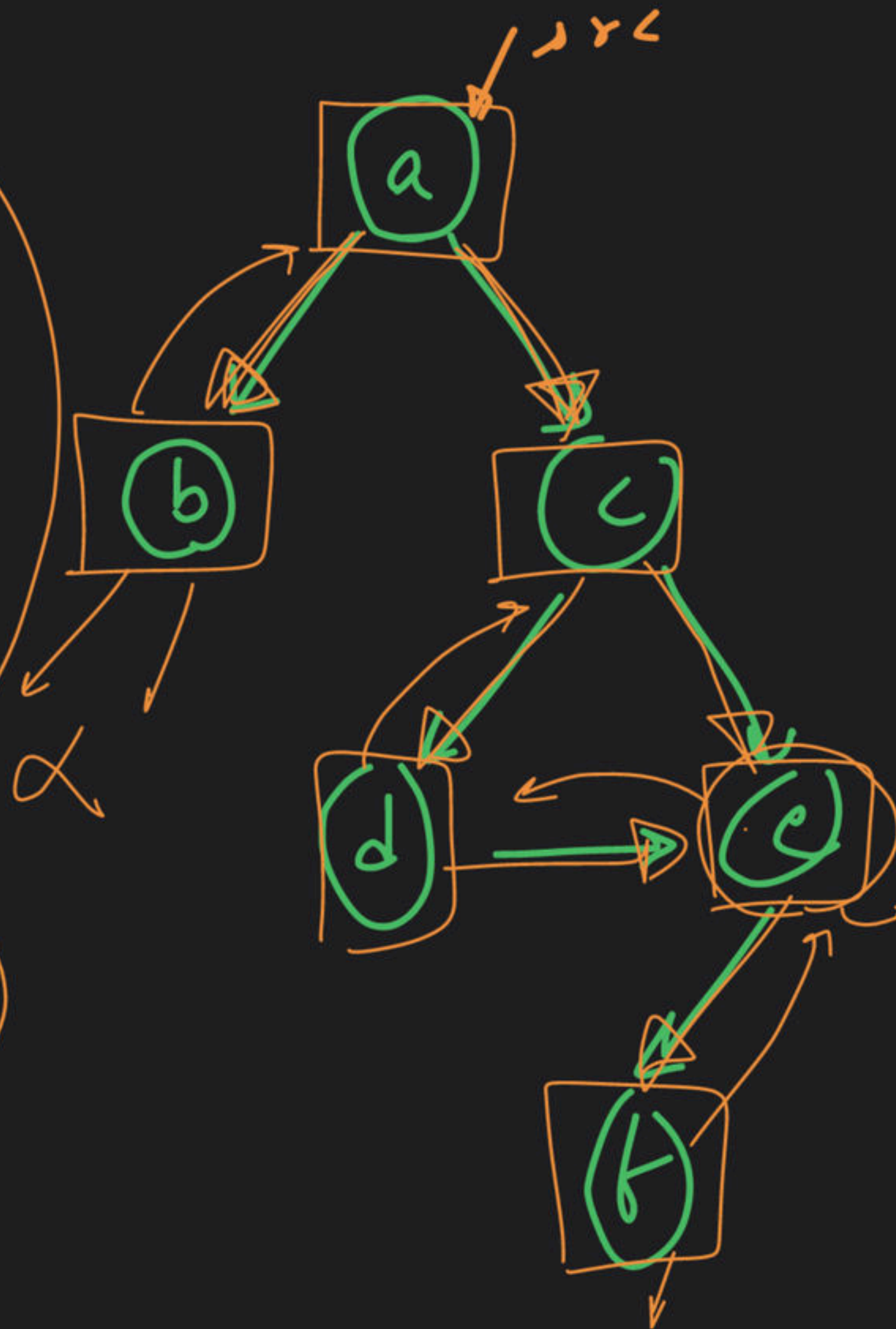


→ DFS



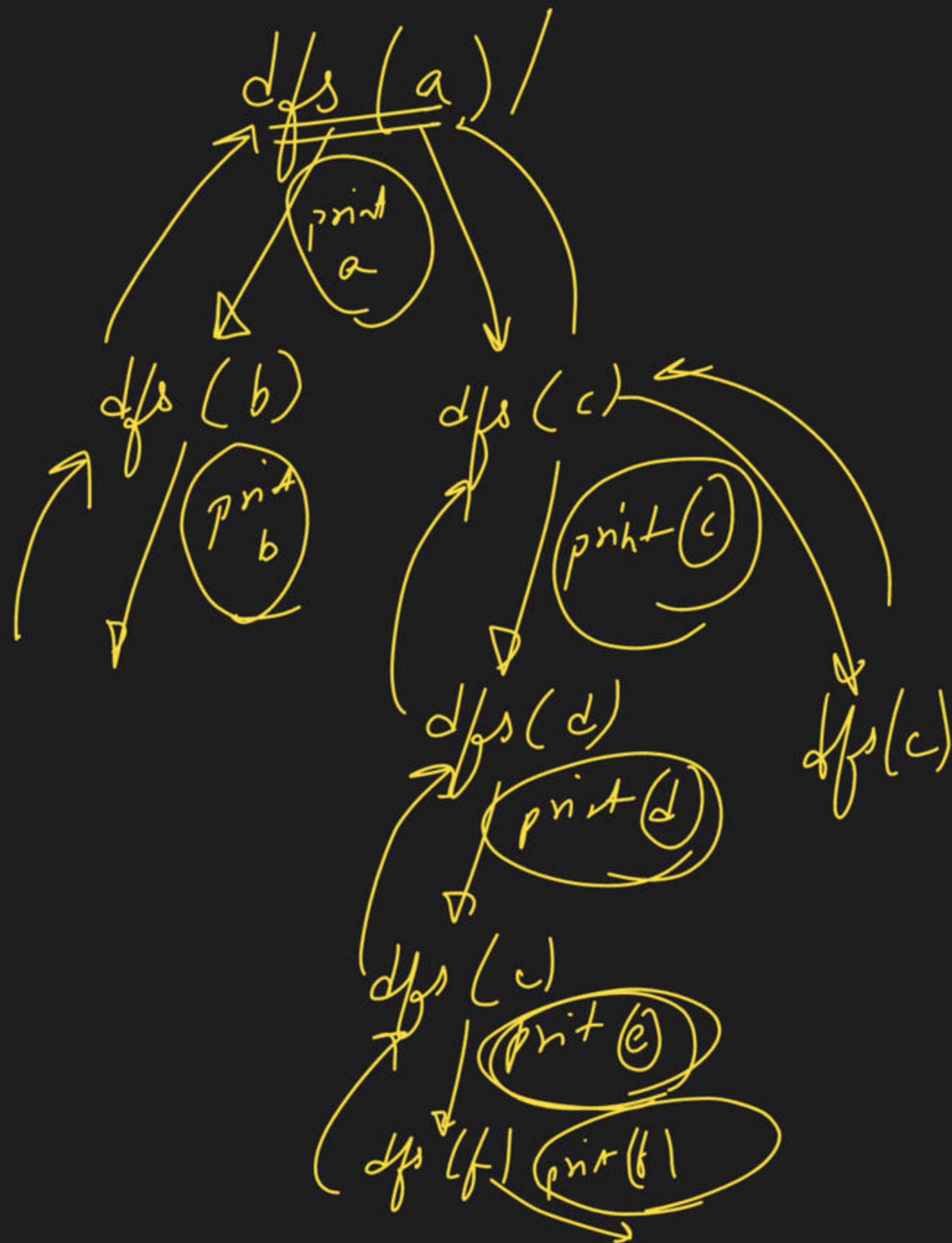


for ( L )  
{  
    ans + = rec ( )  
}



- a
- b
- c
- d
- e
- f





$a \rightarrow \{b, c\}$

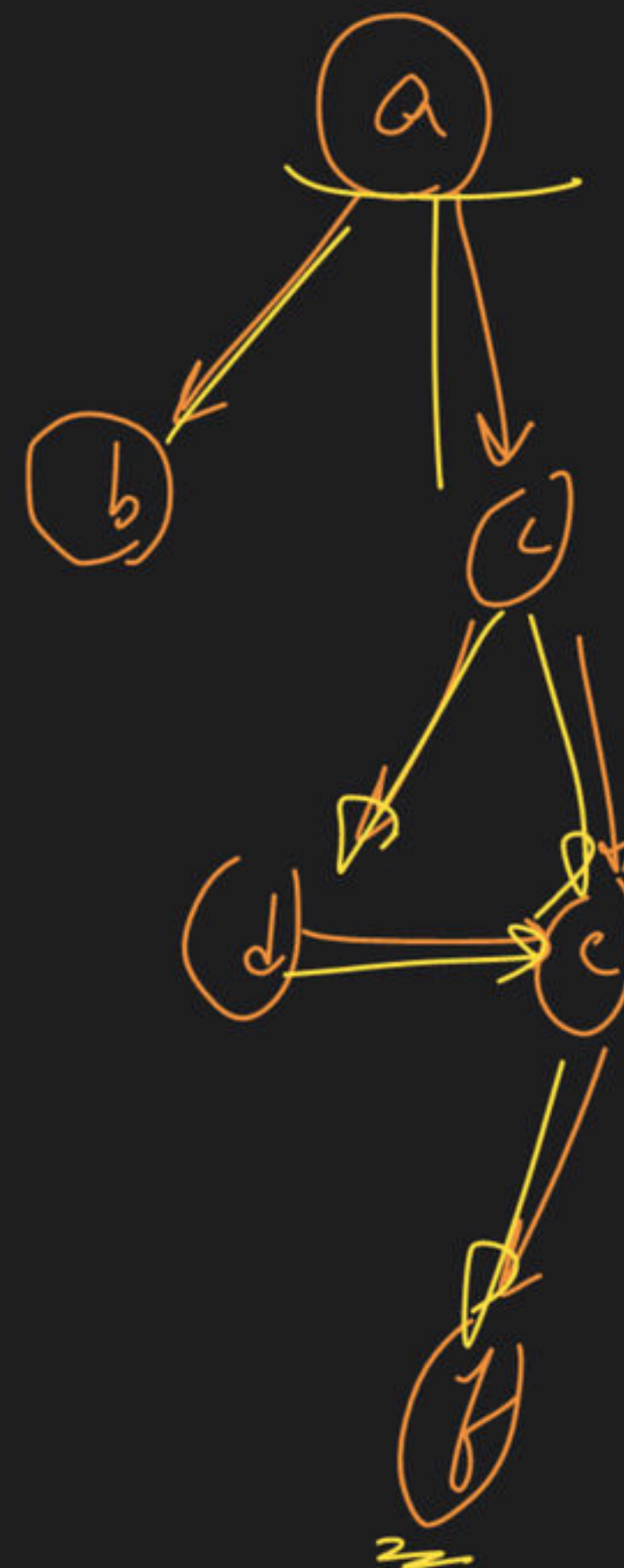
$b \rightarrow \{ \}$

$c \rightarrow \{d, e\}$

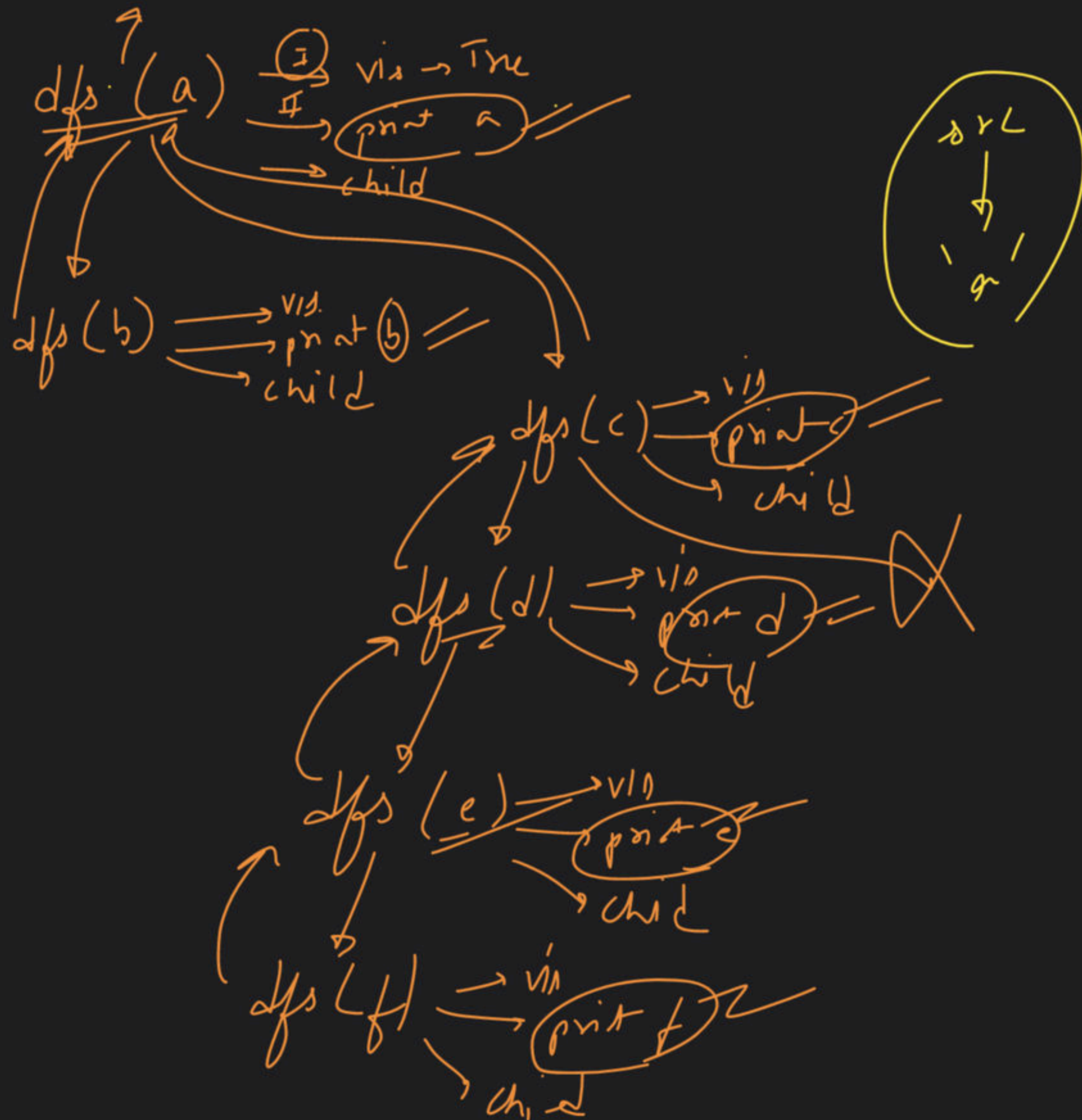
$d \rightarrow \{e\}$

$e \rightarrow \{f\}$

$f \rightarrow \{ \}$







AdjList

a: {b, c}

b: { }

c: {d, e}

d: { }

e: { }

f: { }

init

a → T

b → T

c → T

d → T

e → 1

f → T