

# Control Systems

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For a particular amplifier connected in a feedback loop in which the output voltage is sampled, measurement of the output resistance before and after the loop is connected shows a change by a factor of 100. Is the resistance with feedback higher or lower? What is the value of the loop gain  $GH$ ? If  $R_{of}$  is  $100\ \Omega$ , what is  $R_o$  without feedback.

1. Find the loop gain  $GH$ .

**Solution:** We know that,

$$R_o = R_{of}(1 + GH) \quad (1.1)$$

Output resistance before and after the loop is connected changes by a factor 100. So,

$$GH = 99 \quad (1.2)$$

Open loop gain  $GH$  is 99.

Given,

$$R_{of} = 100 \quad (1.3)$$

$$R_o = 100(1 + 99) \quad (1.4)$$

$$R_o = 10000 \quad (1.5)$$

Output resistance without feedback is  $10\text{k}\Omega$   
Output resistance without feedback is greater than with feedback.

2. The following code generates the values

codes/ee18btech11042.py

3. Design a circuit. **Solution:**

Feedback Gain

$$H = \frac{R_1}{R_1 + R_2} = \frac{1}{40} \quad (3.1)$$

From fig ??, Open Loop input resistance

$$R_{in} = R_s + R_{id} + (R_1 // R_2) \quad (3.2)$$

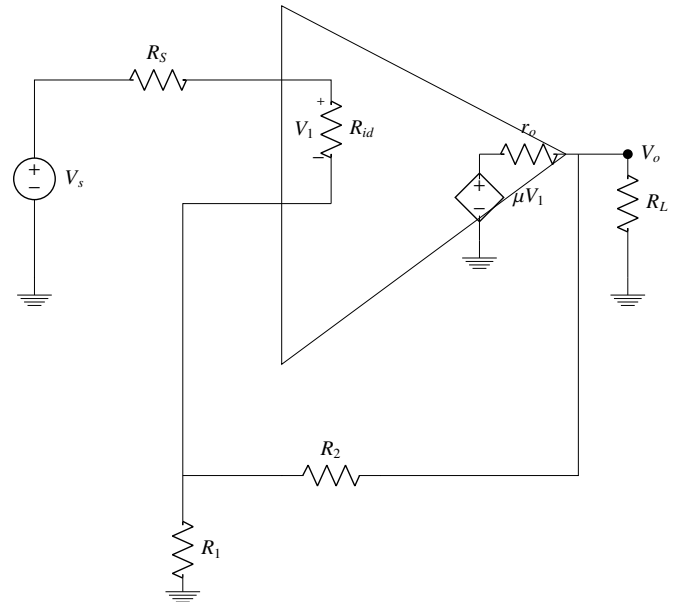


Fig. 3.1: Amplifier Circuit

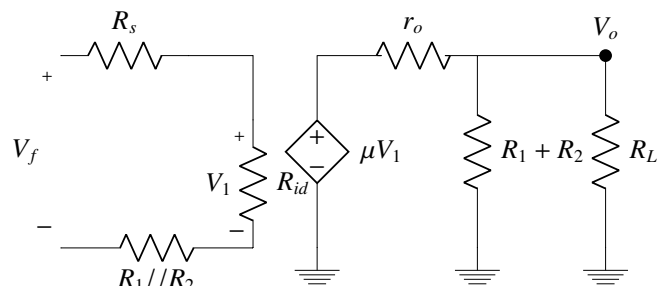


Fig. 3.2: H circuit

Open loop output resistance

$$R_o = r_o // R_L // (R_1 + R_2) \quad (3.3)$$

Open Loop gain

$$G = \mu \frac{R_{id}}{R_s + R_{id} + (R_1 // R_2)} \frac{R_L // R_1 + R_2}{(r_o + (R_L // R_1 + R_2))} \quad (3.4)$$

Closed Loop Gain  $\frac{G}{1+GH}$  is 39.6

4. Verify through spice.

The following file provides how to simulate the spice file.

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Parameter	Value
$R_s$	$13.33K$
$R_{id}$	$692$
$R_1$	$1K$
$R_2$	$39K$
$r_o$	$40K$
$R_L$	$20K$
$\mu$	$17.82K$
$G$	$3.96K$
$H$	$\frac{1}{40}$

TABLE 3: parameter values

```
spice/ee18btech11042/readme
```

The following is .net list file for spice simulation

```
spice/ee18btech11042/ee18btech11042.net
```

Given,

$$V_s(t) = \sin(2000\pi t) \quad (4.1)$$

We got output as

$$V_o(t) = 40\sin(2000\pi t) \quad (4.2)$$

Overall gain  $\frac{V_o(t)}{V_m(t)}$  is 40 same as thereotical value. The following code creates the python

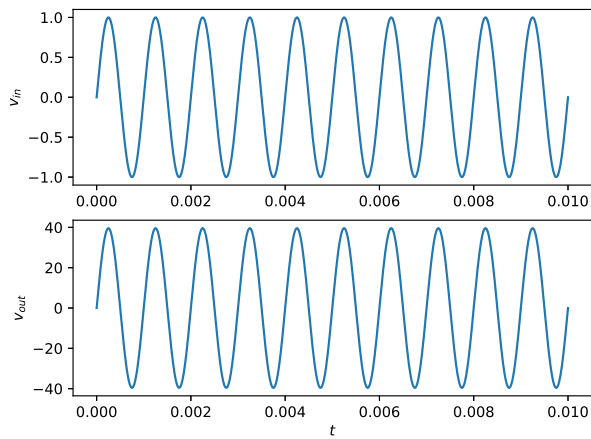


Fig. 4.1: Time response of system

plots.

```
spice/ee18btech11042/ee18btech11042_spice.py
```