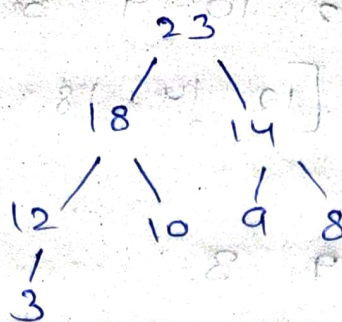


Heap Sort for max heap:

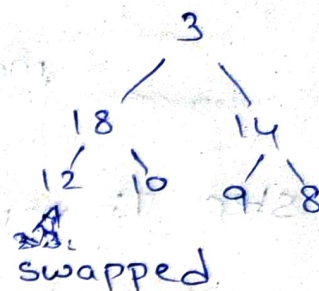
| | | | | | | | | | |
|----|----|----|----|----|---|---|---|---|---|
| 2 | 3 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| 23 | 18 | 14 | 12 | 10 | 9 | 8 | 3 | | |



step 1:- Extract Max(23), replace (swap) with 3 then.

| | | | | | | | |
|---|----|----|----|----|---|---|----|
| 3 | 18 | 14 | 12 | 10 | 9 | 8 | 23 |
|---|----|----|----|----|---|---|----|

Min heap.



step 2:- Now, again max heap for 18(max)

swap with the 3 and 3 is swapped with the 12(max).

| | | | | | | | |
|---|----|----|----|----|---|---|----|
| 3 | 18 | 14 | 12 | 10 | 9 | 8 | 23 |
| | | | | | | | |

$i = 1 \times 2 = 2, 3$
 $3 = 18, 14$

| | | | | | | | |
|----|---|----|----|----|---|---|----|
| 18 | 3 | 14 | 12 | 10 | 9 | 8 | 23 |
| | | | | | | | |

$i = 2 \times 2 = 4, 5$
 $3 = 12, 10$

| | | | | | | | |
|----|----|----|---|----|---|---|----|
| 18 | 12 | 14 | 3 | 10 | 9 | 8 | 23 |
|----|----|----|---|----|---|---|----|

step 3:- The array is max heap, remove (extract) the top (or) first (large) 18 and swap the last node index 8 to first index node.

| | | | | | | | |
|---|----|----|---|----|---|----|----|
| 8 | 12 | 14 | 3 | 10 | 9 | 18 | 23 |
|---|----|----|---|----|---|----|----|

Now, min heap.

| | | | | | | | |
|---|----|----|---|----|---|----|----|
| 8 | 12 | 14 | 3 | 10 | 9 | 18 | 23 |
| | | | | | | | |

$i = 1 \times 2 = 2, 3$

| | | | | | | | |
|----|----|---|---|----|---|----|----|
| 14 | 12 | 8 | 3 | 10 | 9 | 18 | 23 |
| | | | | | | | |

$i = 3 \times 2$

| | | | | | | | |
|----|----|---|---|----|---|----|----|
| 14 | 12 | 9 | 3 | 10 | 8 | 18 | 23 |
|----|----|---|---|----|---|----|----|

step 4:- remove 14 from array and swap 8 to first node

| | | | | | | | |
|---|----|---|---|----|----|----|----|
| 8 | 12 | 9 | 3 | 10 | 14 | 18 | 23 |
|---|----|---|---|----|----|----|----|

Max heap ->

| | | | | | | | |
|----|---|---|---|----|----|----|----|
| 12 | 8 | 9 | 3 | 10 | 14 | 18 | 23 |
| | | | | | | | |

| | | | | | | | |
|----|----|---|---|---|----|----|----|
| 12 | 10 | 9 | 3 | 8 | 14 | 18 | 23 |
|----|----|---|---|---|----|----|----|

Step 5: min heap \rightarrow extract '12' and swap with '8'.

~~8~~ ~~12~~ ~~8~~ 12 10 9 3 8 [14 18 23]

8 10 9 3 [12 14 18 23]

max heap \rightarrow

10 8 9 3.

Step 6: min heap \rightarrow extract '10' and swap '3'.

3 8 9 [10 12 14 18 23]

max heap \rightarrow

9 8 3 [10 12 14 18 23]

Step 7: min heap \rightarrow extract 9 and swap 3.

3 8 [10 12 14 18 23]

max heap \rightarrow

8 3 [10 12 14 18 23]

Step 8: min heap \rightarrow extract 8 & swap with 3.

3 [8 10 12 14 18 23]

max heap \rightarrow 3, [8 10 12 14 18 23]

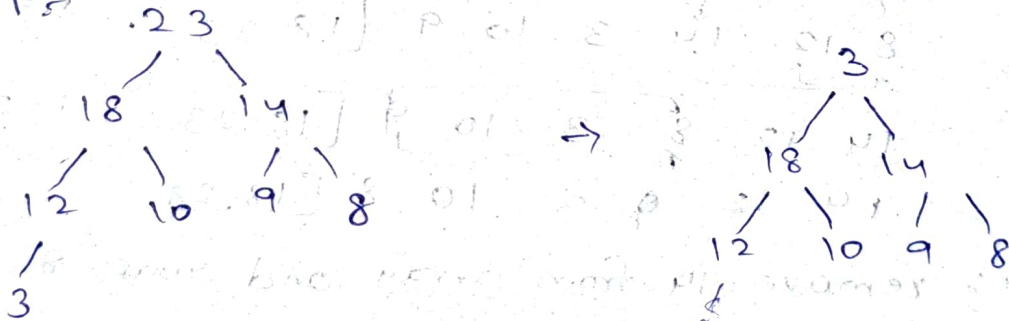
min heap \rightarrow extract 3.

empty [3 8 10 12 14 18 23]

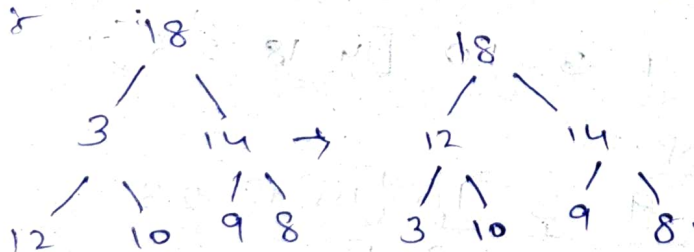
The ascending and perfect heap sort:

| | | | | | | | |
|---|---|---|----|----|----|----|----|
| 3 | 8 | 9 | 10 | 12 | 14 | 18 | 23 |
|---|---|---|----|----|----|----|----|

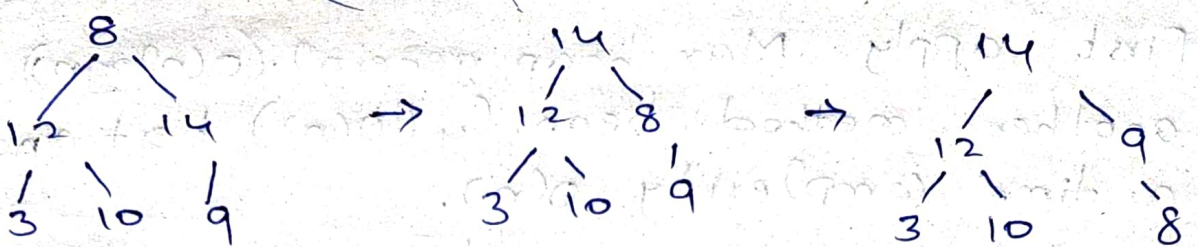
Step 1:



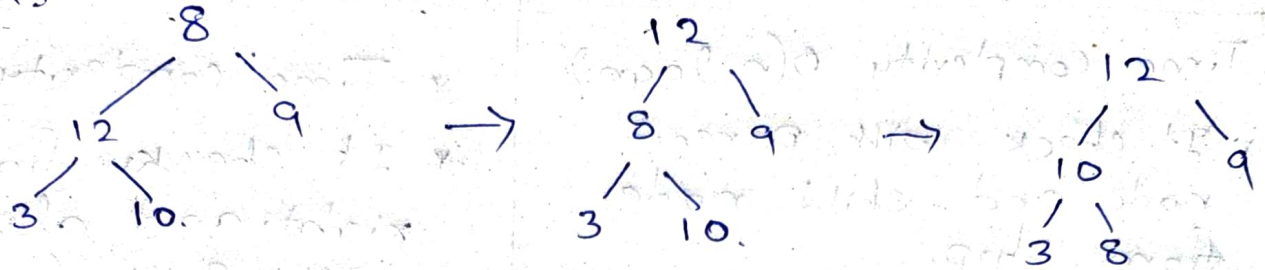
Step 2:



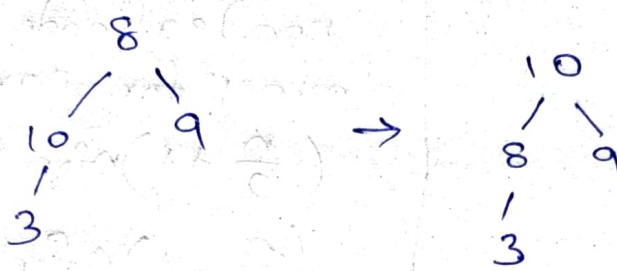
Step 3:-



Step 4:-



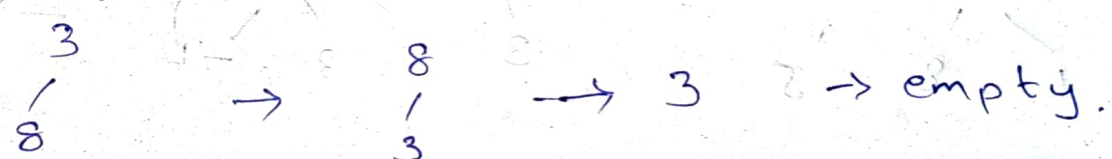
Step 5:-



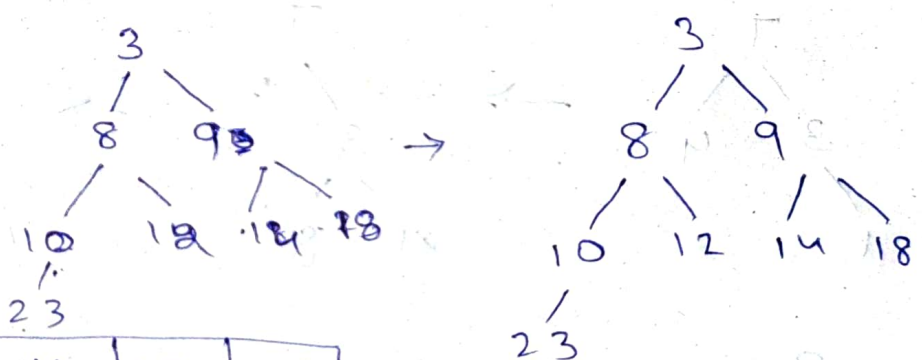
Step 6:-



Step 7:-



The min heap is



| | | | | | | | |
|---|---|---|----|----|----|----|----|
| 3 | 8 | 9 | 10 | 12 | 14 | 18 | 23 |
|---|---|---|----|----|----|----|----|