

# 2020-January Session-07-01-2020-shift-1

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- 1)  $\lim_{x \rightarrow 2} \frac{3^x + \frac{27}{3^x} - 12}{\frac{1}{3^2} - \frac{3}{3^x}}$  is equal to.
- 2) If variance of first  $n$  natural numbers is 10 and variance of first  $m$  even natural numbers is 16,  $m + n$  is equal to
- 3) If the sum of the coefficients of all even powers of  $x$  in the product  $(1 + x + x^2 + x^3 \cdots + x^{2n})(1 - x + x^2 - x^3 \cdots + x^{2n})$  is 61, then  $n$  is equal to
- 4) Let  $S$  be the set of points where the function,  $f(x) = |2 - |x - 3||$ ,  $x \in \mathbb{R}$ , is not differentiable. Then, the value of  $\sum_{x \in S} f(f(x))$  is equal to

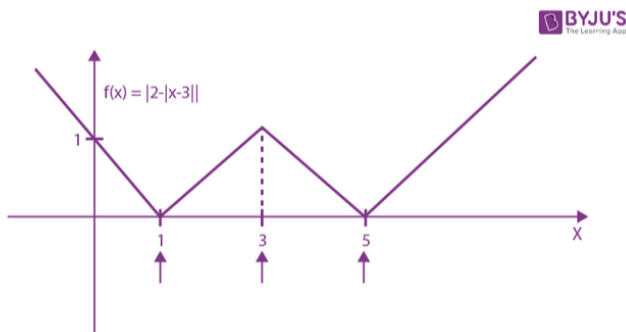


Fig. 4.

- 5) Let  $A(1, 0)$ ,  $B(6, 2)$ ,  $C(\frac{3}{2}, 6)$  be the vertices of a triangle  $ABC$ . If  $P$  is a point inside the triangle  $ABC$  such that the triangle  $APC$ ,  $APB$  and  $BPC$  have equal areas, then the length of the line segment  $PQ$ , where  $Q$  is the point  $(\frac{-7}{6}, \frac{-1}{3})$ , is