## 1-1.2-17

## EE24BTECH11064 - Harshil Rathan

## **Question:**

Three vertices of a parallelogram ABCD are  $\mathbf{A} = (3, -1, 2)$ ,  $\mathbf{B} = (1, -2, 4)$  and  $\mathbf{C} = (-1, 1, 2)$ . Find the coordinates of the fourth vertex. Solution:

Vertices	Given
A	$\left(3,-1,2\right)$
В	$\left(1,-2,4\right)$
С	(-1,1,2)
D	(x, y, z)

$$\mathbf{M} = \frac{\mathbf{A} + \mathbf{C}}{2} \tag{0.1}$$

$$\mathbf{P} = \frac{\mathbf{B} + \mathbf{D}}{2} \tag{0.2}$$

$$\mathbf{M} = \mathbf{P} \tag{0.3}$$

$$\mathbf{M} = \frac{\begin{pmatrix} 3 \\ -1 \\ 2 \end{pmatrix} + \begin{pmatrix} -1 \\ 1 \\ 2 \end{pmatrix}}{2} \tag{0.4}$$

$$\mathbf{M} = \begin{pmatrix} 1 \\ 0 \\ 2 \end{pmatrix} \tag{0.5}$$

$$\mathbf{P} = \frac{\begin{pmatrix} 1 \\ -2 \\ 4 \end{pmatrix} + \begin{pmatrix} x \\ y \\ z \end{pmatrix}}{2} \tag{0.6}$$

$$\mathbf{P} = \begin{pmatrix} \frac{1+x}{2} \\ \frac{y-2}{2} \\ \frac{z+4}{2} \end{pmatrix} \tag{0.7}$$

Since,

$$\mathbf{M} = \mathbf{P} \tag{0.8}$$

On comparing both sides,

$$x = 1, y = 2, z = 0 (0.9)$$

## Parallelogram ABCD

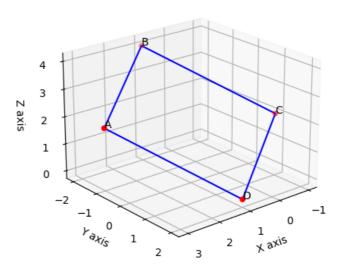


Fig. 0.1: Plot of Parallelogram ABCD