## EE24BTECH11064 - Harshil Rathan

## **Question:**

Find the area of the region enclosed by the line  $y = \sqrt{3}x$ , semi-circle  $y = \sqrt{4 - x^2}$  and X axis in first quadrant.

## **Solution:**

The parameters of the conic are

Equations
$y = \sqrt{3}x$
$y = \sqrt{4 - x^2}$

TABLE 0: Given Equations

Conic	Parameters
V	$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$
и	0
f	-4
h	0
m	$\begin{pmatrix} 1 \\ \frac{1}{\sqrt{3}} \end{pmatrix}$

$$L: x_i = h + \kappa_i m \tag{0.1}$$

Where,

$$\kappa_i = \frac{1}{m^{\top} V m} (-m^{\top} (V h + u)) \pm \sqrt{[m^{\top} (V h + u)]^2 - g(h)(m^{\top} V m)}$$
(0.2)

For the line  $y = \sqrt{3}x$ , the parameters are

$$h = \begin{pmatrix} 0 \\ 0 \end{pmatrix}, m = \begin{pmatrix} 1 \\ \frac{1}{\sqrt{3}} \end{pmatrix} \tag{0.3}$$

Substituting the above parameters in (0.2)

$$\kappa_i = \sqrt{3}, -\sqrt{3} \tag{0.4}$$

We consider only +ve value of  $\kappa_i$ , yilelding the points of intersection

$$x = \begin{pmatrix} \sqrt{3} \\ 1 \end{pmatrix} \tag{0.5}$$

Angle between given line and X axis is,

$$\theta = 30^{\circ} \tag{0.6}$$

$$\frac{\theta}{360}\pi r^2 = \frac{\pi}{3} \tag{0.7}$$

Area of sector is  $\frac{\pi}{3}$ .

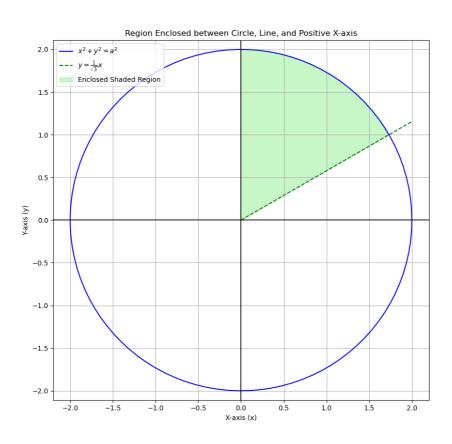


Fig. 0.1